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Discussions

Analysis of three-dimensional slope stability combined with rainfall and earthquake

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Abstract

In the current context of global climate change, geohazards such as earthquakes and extreme rainfall pose a serious threat to regional stability. We investigate a three-dimensional slope dynamic model under earthquake action, derive the calculation of seepage force and the normal stress expression of slip surface under seepage and earthquake, and propose a rigorous overall analysis method to solve the safety factor of slopes subjected to combined with rainfall and earthquake. The accuracy and reliability of the method is verified by two classical examples. Finally, the effects of soil permeability coefficient, porosity and saturation on slope stability under rainfall in a project located in the Three Gorges Reservoir Area are analyzed. The safety evolution of the slope combined with both rainfall and earthquake is also studied. The results indicate that porosity has a greater impact on the safety factor under rainfall conditions, while the influence of permeability coefficient and saturation is relatively small. With the increase of horizontal seismic coefficient, the safety factor of the slope decreases

https://doi.org/10.5194/nhess-2023-181
Preprint. Discussion started: 13 November 2023

Natural Hazards and Earth System Sciences
Open Access
Discussions

significantly. The influence of earthquake on slope stability is significantly greater than that of rainfall. The corresponding safety factor when the vertical seismic action is vertically downward is smaller than that when it is vertically upward. When considering both horizontal and vertical seismic effects, slope stability is lower.

Keywords

Three-dimensional slopes; Rainfall; Earthquake; Stability analysis

1 Introduction

Landslides often occur due to the combined effects of rainfall and earthquake. Seepage causes an increase in pore water pressure, leading to a decrease in effective stress and shear strength of the soil. The weight of the soil also increases, while seismic inertial forces act unfavorably by accelerating the loss of effective stress. Therefore, these two external forces seriously weaken slope stability. When these two hazards coincide, it often results in computational instability of previously stable slopes. Further research is necessary to investigate the stability of slopes under the combined influence of rainfall and earthquake (David, 2000; Iverson, 2000; Sassa et al., 2010).

At present, the main research methods for slope stability include the limit equilibrium method (Bishop, 1955; Morgenstern and Price, 1965; Spencer, 1967), limit analysis (Farzaneh et al.,2008; Michalowski, 1995; Qin and Chian, 2018; Zhou et al., 2017), Finite Element Method (Griffiths and Lane, 1999; Ishii et al., 2012) et al. There have been numerous studies and findings regarding the stability assessment of three-dimensional slopes. However, most of these methods are based on extended three-

https://doi.org/10.5194/nhess-2023-181
Preprint. Discussion started: 13 November 2023

Natural Hazards and Earth System Sciences
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Discussions

dimensional equilibrium analysis techniques (Hungr, 1987; Zhang, 1988; Chen, 2001; Cheng and Yip, 2007), which rarely strictly adhere to the six equilibrium conditions. Additionally, these approaches often introduce a significant number of assumptions that limit their practical engineering applications. The strict three-dimensional limit equilibrium method proposed by Zheng (2007) is an overall analysis approach based on the natural form of slip surface stress distribution and approximation through shard interpolation. Sun et al. (2016, 2017) combined Morgenstern-Price and Bell global analysis method to analyze the stability of reservoir bank slope, applying this method to the Three Gorges reservoir area. Rahardjo et al. (2010) studied the effect of groundwater table position, rainfall intensities, and soil properties in affecting slope stability using the numerical analyses. Zhou and Qin (2022) proposed a finite element upper bound method for assessing the stability of soil slopes subjected to reservoir water decline and rainfall.

As a common geological hazard in seismic zones, earthquake-triggered landslides have been extensively investigated by numerous scholars (Sepúlveda et al., 2005; Chang et al., 2012; Jibson and Harp, 2016; Marc et al., 2017; Salinas-Jasso et al., 2019). At present, the stability analysis method of 3D slope is not mature, and the research on the dynamic stability of 3D slope is even more scarce. The quasi-static method (Liu et al., 2001) introduces coefficients (k_v and k_h) that reflect dynamic action, thereby transforming a dynamic problem into a static one for easier resolution. This approach avoids the complexities associated with dynamic analysis and has become widely used

https://doi.org/10.5194/nhess-2023-181
Preprint. Discussion started: 13 November 2023

Natural Hazards and Earth System Sciences
Open Access
Discussions

in engineering. Horizontal seismic effects are often a significant consideration in slope stability analysis, however, some research (Chopra, 1966; Lew, 1991; Ling et al., 1999; Shukha and Baker, 2008) confirms that the vertical component of seismic forces should also be given great attention. Wang and Xu (2005) employed the dynamic finite element method to investigate the seismic response characteristics of various components in a three-dimensional high slope, yet failed to determine the safety factor. Guo et al. (2011) obtained the time history curve of slope safety factor during earthquake using vector sum method in two-dimensional situations, but did not extend their findings to three-dimensional situations. Cao et al. (2019) studied the seismic response and dynamic failure mode of the slope subjected to earthquake and rainfall by two model tests, and few studies we have found combining effect of rainfall and earthquake.

Most studies only consider the role of a single factor in seepage or earthquake, neglecting the slope stability analysis under combined working conditions. Therefore, analyzing the change law of safety factors for slopes during seepage and seismic action is of great practical value in guiding slope support design and evaluating slope stability. In this paper, a 3D rigorous slice-free method considering seepage and seismic forces to solve the safety factor of bank slopes is proposed. The proposed method strictly satisfies the force balance and moment balance in three directions, without introducing other redundant assumptions.

https://doi.org/10.5194/nhess-2023-181
Preprint. Discussion started: 13 November 2023

Natural Hazards and Earth System Sciences
Open Access
EGU
Discussions

2 Rise of phreatic surface and calculation of seepage force with rainfall infiltration in the soil column

A differential soil slice is taken from the slip surface to the slope surface in the landslide body is shown in Fig. 1. $z(t)$ is the rise of phreatic surface after rainfall infiltration, which refers to Conte and Troncone (2017), the height of the soil slice below the phreatic line on *BE* and *CF* side are respectively z_1 and z_2. It is assumed that rainfall is consistent with groundwater movement and that the slope surface is well drained and free of standing water. Regardless of rainfall intensity, runoff will form if it is greater than the infiltration capacity. The height of rise of the phreatic surface within the slope after the rainfall is

$$z(t)=\frac{z_r}{n\left(1-S_r\right)}\exp\left[-\frac{k}{ds\cos\alpha}i\cos\delta\left(t-t_0\right)\right] \tag{1}$$

where z_r is the volume of water (per unit area) that infiltrates the slope, n is porosity, k is permeability coefficient, S_r is saturation, i is the hydraulic gradient, δ is the angle between the slope surface and the horizontal plane, α is the angle between the sliding surface *BC* of the differential soil slice and the horizontal plane, ds is the length of the sliding surface *BC* of the differential soil slice, t is time, and t_0 is the initial moment.

https://doi.org/10.5194/nhess-2023-181
Preprint. Discussion started: 13 November 2023

Natural Hazards and Earth System Sciences
Open Access
Discussions

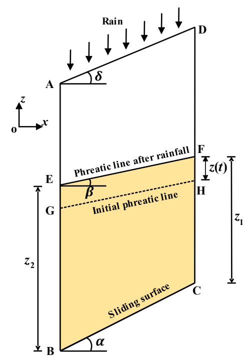

Fig. 1 Relationship between rainfall and groundwater level

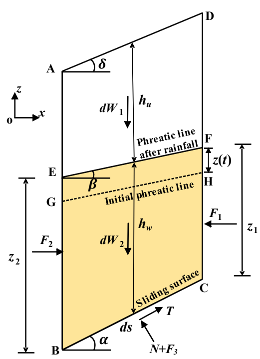

Fig. 2 Calculation sketch of forces acting on the differential soil slice

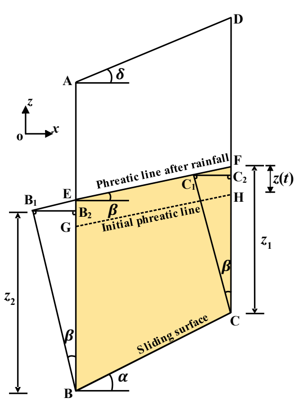

Fig. 3 Calculation sketch of hydraulic head

The load on the soil slice is shown in Fig. 2. dW_1 and dW_2 are the gravity of the differential soil slice above and below the phreatic line. The resultant hydrostatic force of the boundary *AB*, *CD*, and *BC* are F_1, F_2, and F_3 respectively. *N* is the contact pressure (effective pressure) between the soil particles, and *T* is the sliding resistance force. β is the angle between the phreatic line and the horizontal plane, h_u and h_w are the height of the soil slice above and below the phreatic line respectively.

According to the flow properties of the phreatic line perpendicular to the equipotential line, the surrounding hydrostatic pressures F_1, F_2, and F_3 on the boundary *CF*, *BE*, and *BC* can be determined. As shown in Fig. 3, BB_1 and CC_1 are perpendicular to the phreatic line, then make B_1B_2 perpendicular to *AB*, and C_1C_2 perpendicular to *CD*. According to the geometric relationship, the hydrostatic pressure resultant forces at the boundary *CF* and *BE* are

$$F_1 = \frac{1}{2}\gamma_w z_1{}^2 cos^2\beta, F_2 = \frac{1}{2}\gamma_w z_2{}^2 cos^2\beta \tag{2}$$

γ_w is the unit weight of the water. Let $h_w = \frac{1}{2}(z_1 + z_2)$, the hydrostatic pressure resultant force on the slip surface *BC* is

$$F_3 = \frac{1}{2}\gamma_w (z_1 + z_2) ds cos^2\beta = \gamma_w h_w ds cos^2\beta \tag{3}$$

The components of F_3 in the horizontal and vertical directions are

$$U_x = \gamma_w h_w ds cos^2\beta \cos\alpha, \quad U_y = \gamma_w h_w ds cos^2\beta \sin\alpha \tag{4}$$

The gravity of water in differential soil slice is

$$dW_{2w} = \gamma_w h_w ds \cos\alpha \tag{5}$$

The permeability pressure is a pair of balancing forces with the water weight in a

https://doi.org/10.5194/nhess-2023-181
Preprint. Discussion started: 13 November 2023

differential soil slice and the hydrostatic pressure around it (Zheng et al., 2004). Therefore, the weight of water in the differential soil slice and the surrounding hydrostatic pressure can be replaced by a seepage force. The force diagram in Fig. 2 can be replaced by Fig. 4. $dW_2^{'}$ represents the effective unit weight of the soil below the phreatic line and dW_D is the seepage force.

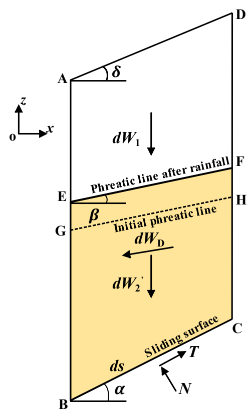

Fig. 4 Simplified force diagram on a differential soil slice

The horizontal and vertical component of the seepage force dW_3 are

$$dW_{Dx} = F_1 - F_2 + U_x = \gamma_w h_w cos^2 \beta (z_1 - z_2 + dssin\alpha) \tag{6}$$

$$dW_{Dy} = dW_{2w} - U_y = \gamma_w h_w dscos\alpha sin^2 \beta \tag{7}$$

According to geometric relation

$$z_1 - z_2 + dssin\alpha = dscos\alpha \tan \beta \tag{8}$$

Therefore, the seepage force is

$$dW_D = \gamma_w h_w dscos\alpha \sin \beta \tag{9}$$

The direction of seepage force is consistent with water flow.

https://doi.org/10.5194/nhess-2023-181
Preprint. Discussion started: 13 November 2023

Natural Hazards and Earth System Sciences
Discussions

3 A global analysis method for slope stability under seepage and earthquake

3.1 Overall system of equilibrium equations

As shown in Fig. 5, taking the whole sliding body Ω as the research object, and S is a potential slip surface.

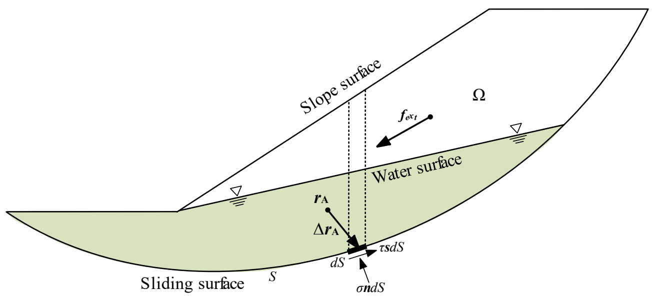

Fig. 5 A 2D schematic plot for force system in/on the sliding body

dS is a differential element on the sliding surface S .The normal force on a differential element dS at point $\boldsymbol{r}$ is $\sigma \boldsymbol{n} dS$, the resultant shear force is $\tau \boldsymbol{s} dS$, $\boldsymbol{n}$ (specified pointing to the inside of the slide Ω) is the unit normal vector at position vector $\boldsymbol{r}$, and $\boldsymbol{s}$ (specified opposite to the sliding direction) is the unit tangent vector, so the reaction on dS is:

$$d\boldsymbol{f} = \left(\sigma \boldsymbol{n} + \tau \boldsymbol{s}\right) dS \tag{10}$$

$$d\boldsymbol{m}_A = \Delta \boldsymbol{r}_A \times d\boldsymbol{f} \tag{11}$$

Here, $\Delta \boldsymbol{r}_A = \boldsymbol{r} - \boldsymbol{r}_A$, $\boldsymbol{r}$ is the position vector of dS , $\boldsymbol{r}_A$ is the position vector for any given reference point *A*, "$\times$" represents vector multiplication.

$\boldsymbol{f}_{ext}$ is the resultant external force vector, including external loads such as gravity, seepage force, seismic force et al.; $\boldsymbol{m}_{\mathrm{ext}}$ denotes the moment $\boldsymbol{f}_{ext}$ concerning $\boldsymbol{r}_A$. To

https://doi.org/10.5194/nhess-2023-181
Preprint. Discussion started: 13 November 2023

Natural Hazards and Earth System Sciences
Discussions

integrate over the entire sliding surface dS :

$$\iint_s d\boldsymbol{f} + \boldsymbol{f}_{ext} = \boldsymbol{0} \tag{12}$$

$$\iint_s d\boldsymbol{m}_A + \boldsymbol{m}_{ext} = \boldsymbol{0} \tag{13}$$

According to Mohr-Coulomb criterion,

$$\tau = \frac{1}{F_s}\left[c' + f'\left(\sigma - u\right)\right] = \frac{1}{F_s}\left(c_w + f'\sigma\right) \tag{14}$$

Here, F_s is the safety factor, c' and f' are the effective stress shear strength parameters , u is the pore pressure; c_w is defined as

$$c_w \equiv c' - f'u \tag{15}$$

Order,

$$\boldsymbol{n}' = \begin{pmatrix} \boldsymbol{n} \\ \Delta\boldsymbol{r}_A \times \boldsymbol{n} \end{pmatrix}, \quad \boldsymbol{s}' = \begin{pmatrix} \boldsymbol{s} \\ \Delta\boldsymbol{r}_A \times \boldsymbol{s} \end{pmatrix}, \quad \boldsymbol{f}_m = \begin{pmatrix} \boldsymbol{f}_{ext} \\ \boldsymbol{m}_{ext} \end{pmatrix} \tag{16}$$

Substituting equations (10), (11), and (14) into equations (12) and (13), and merging into a more compact form:

$$F_s\left(\iint_s \boldsymbol{n}'\sigma dS + \boldsymbol{f}_m\right) + \iint_s \left(c_w + f'\sigma\right)\boldsymbol{s}'dS = 0 \tag{17}$$

3.2 Normal stress expression of slip surface under seepage force and seismic force

As shown with the dash line in Fig. 5, a vertical differential cylinder is now taken from the homogeneous sliding body from the slip surface to the slope surface. The load on the differential cylinder is shown in Fig. 6. $-\boldsymbol{k}dw_1$ is the weight of the soil above phreatic surface, and $-\boldsymbol{k}dw_2'$ refer to the floating weight of the soil below the phreatic surface. $\boldsymbol{p}dw_3$ and $\boldsymbol{e}dw_4$ denote the seepage force and seismic force. $d\boldsymbol{h}$ refers to the action force of the soil around the differential cylinder.

https://doi.org/10.5194/nhess-2023-181
Preprint. Discussion started: 13 November 2023

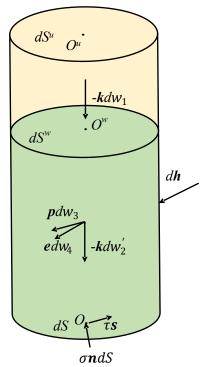

Fig. 6 Sketch of force acting on a vertical differential cylinder in a sliding body

Here, $\boldsymbol{k}$ = unit vector of z-axis; $\boldsymbol{p}$ = unit vector pointing to the direction of the seepage force; $\boldsymbol{e}$ = unit vector pointing to the direction of the seismic force; θ = angle between dS and the horizontal plane; ξ = angle between the phreatic surface dS^w and the horizontal plane in the differential cylinder.

The force equilibrium condition for a differential cylinder is

$$\sigma \boldsymbol{n} dS + \tau \boldsymbol{s} dS - \boldsymbol{k} dw_1 - \boldsymbol{k} dw_2^{'} + \boldsymbol{p} dw_3 + \boldsymbol{e} dw_4 + d\boldsymbol{h} = \boldsymbol{0} \tag{18}$$

Both sides of the Eq. (18) are simultaneously multiplied by $\boldsymbol{n}$ to obtain

$$\sigma = n_3 \left(\frac{dw_1}{dS} + \frac{dw_1^{'}}{dS} \right) - n_p \frac{dw_3}{dS} - n_e \frac{dw_4}{dS} - \frac{\boldsymbol{n} \cdot d\boldsymbol{h}}{dS} \tag{19}$$

Here, n_3 = component of $\boldsymbol{n}$ in the positive direction of z-axis, n_p = projection of $\boldsymbol{p}$ in $\boldsymbol{n}$ direction, n_e = projection of $\boldsymbol{e}$ in $\boldsymbol{n}$ direction.

Known,

https://doi.org/10.5194/nhess-2023-181
Preprint. Discussion started: 13 November 2023

Natural Hazards and Earth System Sciences
Open Access
Discussions

$$\begin{cases} dw_1 = \bar{\gamma} H_u dS \cos\theta \\ dw_2' = \overline{\gamma'} H_w dS \cos\theta \\ dw_3 = \gamma_w H_w dS \cos\theta \sin\xi \\ dw_4 = k_c \left(\bar{\gamma} H_u + \bar{\gamma}_{sat} H_w \right) dS \cos\theta \\ n_p = \boldsymbol{n} \cdot \boldsymbol{p} \\ n_e = \boldsymbol{n} \cdot \boldsymbol{e} \end{cases} \tag{20}$$

where, $\bar{\gamma}$ = average value of the unit weight of the soil above the phreatic surface; γ' = average value for the unit floating weight of the soil below the phreatic surface; $\bar{\gamma}_{sat}$ = average value of the unit saturated weight of below the phreatic surface; γ_w = unit weight of water; H_u = height of soil above the phreatic surface; H_w = height of the soil below the phreatic surface; k_c = seismic force coefficient.

Substitute Eq. (20) into Eq. (19) and sort it out

$$\sigma = (\gamma H_u + \gamma' H_w)\cos^2\theta - n_p \gamma_w H_w \cos\theta \sin\xi - n_e k_c \left(\gamma H_u + \gamma_{sat} H_w \right) \cos\theta - \frac{\boldsymbol{n} \cdot d\boldsymbol{h}}{dS} \tag{21}$$

Order

$$\begin{aligned} &\sigma_0 = \left(\gamma H_u + \gamma' H_w \right)\cos^2\theta - n_p \gamma_w H_w \cos\theta \sin\xi - n_e k_c \left(\gamma H_u + \gamma_{sat} H_w \right)\cos\theta, \\ &h_n = -\frac{\boldsymbol{n} \cdot d\boldsymbol{h}}{dS} \end{aligned} \tag{22}$$

Therefore

$$\sigma = \sigma_0 + h_n \tag{23}$$

Here, σ_0 = contribution of volume force to the normal stress. h_n = contribution of the force of surrounding soil to the normal stress of sliding surface.

The normal stress distribution of the slip surface can be approximated in the following (Zheng, 2009):

$$\sigma = \sigma_0 + f(x, y; \boldsymbol{a}) \tag{24}$$

where $f(x, y; \boldsymbol{a})$ = function in the horizontal coordinates (x, y) with a parametric

https://doi.org/10.5194/nhess-2023-181
Preprint. Discussion started: 13 November 2023

Natural Hazards and Earth System Sciences
Discussions

vector $\boldsymbol{a}$ consisting of five unknowns. $f(x,y;\boldsymbol{a})$ is constructed by piecewise triangular linear interpolation:

$$f(x,y;\boldsymbol{a}) = \boldsymbol{la} \tag{25}$$

where $\boldsymbol{l}$ is the interpolation function, $\boldsymbol{l} = (l_1, l_2, ..., l_5)$, and it satisfies $\sum_{i=1}^{5} l_i = 1$.

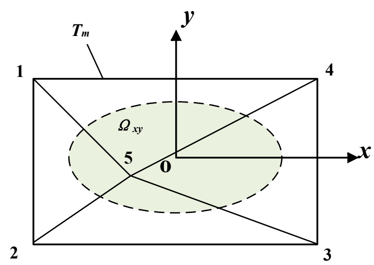

Fig. 7 A triangular mesh for interpolation of normal stress on slip surface

As shown in Fig. 7, Ω_{xy} is the projection of the sliding body on the *xoy* plane, the area characterized by the dashed line. T_m is a triangular network containing 5 nodes. $l_i(x,y)(i=1,2,...,5)$ is the interpolation function for these 5 nodes, which can be formed as in finite elements with the help of the area coordinates of the 4 triangles on T_m.

Substitute Eq. (24) into Eq. (17), a system of nonlinear equations with F_s and $\boldsymbol{a}$ as unknowns is obtained:

$$F_s\boldsymbol{Ba} + \boldsymbol{Da} + F_s\boldsymbol{b} + \boldsymbol{d} = 0 \tag{26}$$

Where $\boldsymbol{B}$ and $\boldsymbol{D}$ are both matrices of order 6×5, and $\boldsymbol{b}$ and $\boldsymbol{d}$ are both vectors of order six, whose expressions are respectively

https://doi.org/10.5194/nhess-2023-181
Preprint. Discussion started: 13 November 2023

$$\begin{cases} \boldsymbol{B} = \iint_s \boldsymbol{n}' \boldsymbol{l} dS \\ \boldsymbol{D} = \iint_s f' \boldsymbol{s}' \boldsymbol{l} dS \\ \boldsymbol{b} = \boldsymbol{f}_m + \iint_s \sigma_0 \boldsymbol{n}' dS \\ \boldsymbol{d} = \iint_s \left(c_w + f' \sigma_0 \right) \boldsymbol{s}' dS \end{cases} \tag{27}$$

We can solve Eq. (26) by either Newton's method or eigenvalue method.

In Eq. (26), all terms except the resultant external force (moment) $\boldsymbol{f}_m$ are area integrals. The volume integrals on the sliding body involved in the problem are transformed into boundary integrals that can skip the column partitions. Hence, it is not required to divide the sliding body into columns anymore, only the surface of the sliding body needs to be partitioned, as detailed in Zheng (2007).

4 Verification examples

In order to verify the accuracy of the proposed method, two examples are analyzed in this section. Different working conditions were set up for Example 2 and the results are compared with those calculated by the software.

4.1 Example 1: translational sliding

Wedge stability in rock mechanics is a typical 3D limit equilibrium analysis problem. Examples of wedge include two cases of geometric symmetry and asymmetry. Example 1 is an asymmetric wedge. Fig. 8 shows the three-dimensional model and geometric parameters of the wedge plane sliding. The sliding surface is composed of two structural planes, ABC and OAB, and the left and right structural planes of the wedge adopt the same shear strength: $c' = 50\text{kPa}$ and $\varphi' = 30^\circ$. The unit weight of the wedge is 26 kN/m^3. For simple wedges, the 3D limit equilibrium method has analytical

https://doi.org/10.5194/nhess-2023-181
Preprint. Discussion started: 13 November 2023

solutions, but these methods all include an assumption that the shear force on the bottom slip plane is parallel to the intersecting prism. If the sliding direction of the wedge sliding body is assumed to be parallel to the intersection line AB of the two structural planes, the wedge sliding body is statically determinate, and the safety factor has an exact value of 1.640 (Hoek and Bray, 1977) for this example. The safety factor calculated based on the method in this paper is 1.652. It demonstrates that the proposed method can reasonably evaluate the stability of rocky slopes containing different structural surfaces.

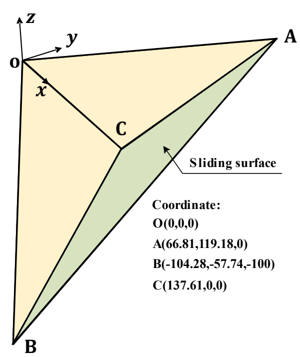

Fig. 8 Model and geometric parameters of the wedge

4.2 Example 2: ellipsoidal sliding

In order to verify the feasibility of the proposed method for calculating the slope stability under seepage and earthquake, a classical ellipsoid example is selected for the stability analysis, which is derived from the study of Zhang (1988). Zhang's (1988) paper in 1988 provides a three-dimensional slope ellipsoid slip surface example, and the simplified three-dimensional limit equilibrium method (only three force equilibrium and one moment equilibrium are satisfied) is used for the stability analysis. Zhang's

https://doi.org/10.5194/nhess-2023-181
Preprint. Discussion started: 13 November 2023

Natural Hazards and Earth System Sciences
Discussions
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(1988) solution for the 3D limit equilibrium of a symmetric ellipsoid can be regarded as a rigorous solution since the ellipsoid has a symmetric sliding surface and the other two moment equilibrium conditions are automatically satisfied by the symmetric bar-column method. Zhang's (1988) solution has also been used by many scholars to check the correctness of their own procedures. The example is a homogeneous slope, the potential sliding surface is a part of a simple ellipsoid, the sliding surface is symmetric about the *xoz* plane, and the equation of the sliding surface is

$$\left(\frac{x\text{-}36.6}{24.4}\right)^2+\left(\frac{y}{66.9}\right)^2+\left(\frac{z\text{-}27.4}{24.4}\right)^2=1 \tag{26}$$

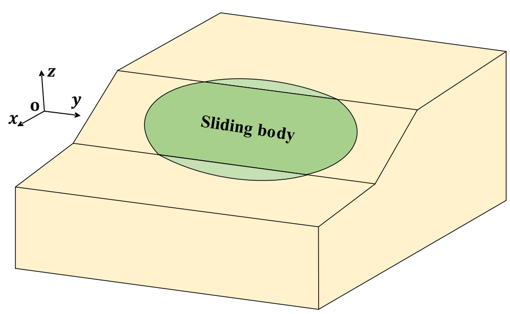

Fig. 9 Model of ellipsoid example

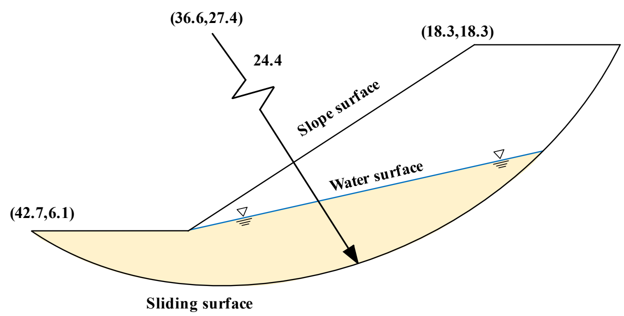

Fig. 10 Geometric parameters and middle profile with groundwater

The ellipsoid model is shown in Fig. 9. The external load of the slope is only

https://doi.org/10.5194/nhess-2023-181
Preprint. Discussion started: 13 November 2023

considered the effect of gravity, the unit gravity is 19.2kN/m3, and the effective shear strength parameter: $c^{'} = 29.3\text{kPa}$ and $\varphi^{'} = 20^{\circ}$. Four working conditions are considered in this section, case-1: no groundwater is considered as in the computational model of Zhang (1988); case-2: groundwater is set up as shown in Fig. 10; case-3: earthquake action in the horizontal direction is considered; case-4: both groundwater and horizontal earthquake action are considered. The earthquake acceleration is 0.05g and the horizontal earthquake direction is taken as along the x-axis positive direction.

Case-1: The safety factor calculated using our proposed method is 2.054, whereas Zhang (1988) obtained a result of 2.122 using the limit equilibrium method. Additionally, we perform a 2D stability analysis of the intermediate cross-section of the model using Rocscience's Slide software, and obtain a safety factor of 2.084. Comparing the results mentioned above, it becomes evident that our proposed method for slope stability analysis is feasible, and its calculation results are consistent with the results obtained by using the traditional limit equilibrium method and two-dimensional stability analysis.

Case-2: Only the effect of groundwater seepage is considered, and the groundwater not only induces hydrodynamic effects, but also softens the geotechnical materials, leading to a significant decrease in the strength of the soil. In this working condition, the calculated safety factor is 1.183, which is close to 1.057 calculated by Rocscience's Slide.

Case-3: We only consider the effect of horizontal earthquake on slope stability. In

https://doi.org/10.5194/nhess-2023-181
Preprint. Discussion started: 13 November 2023

order to compare the results with the 2D stability calculations, we choose the horizontal seismic action direction to be in the *xoz* plane. The results calculated by the 3D procedure and the 2D software are 1.855 and 1.861, respectively. Compared with the case-2, the effect of seepage on the slope stability is greater than that of seismic action.

Case-4: We considered both seepage and horizontal seismic effects. In this case, the results calculated by 3D program and 2D software are 1.047 and 0.934 respectively.

Based on the above calculation results, we can conclude that the proposed method shows reliability in calculating the slope stability under seepage and seismic actions. The calculation results under different working conditions reinforce this conclusion.

5 A True 3D Slope

This section investigates slope stability evolution under the influence of rainfall and earthquake by taking an actual slope in the Three Gorges reservoir as a case study.

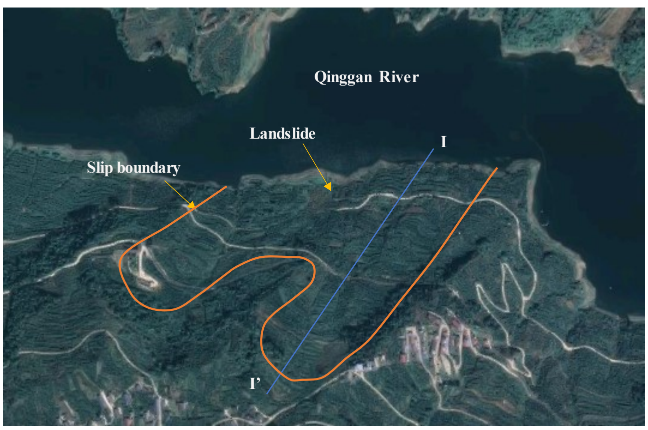

Fig. 11 Geographical location map of Woshaxi slope (© Google Maps)

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Preprint. Discussion started: 13 November 2023

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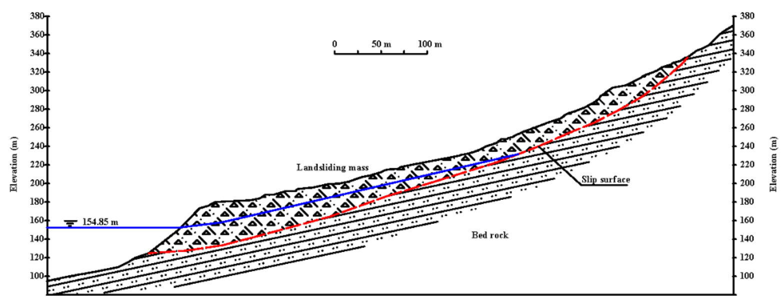

Fig. 12 Geological section map of Woshaxi slope

The geographical location of the Woshaxi landslide is depicted in Fig. 11, while the cross-section of the landslide (I-I') is illustrated in Fig. 12. Situated on the right bank of Qinggan River, a tributary of Yangtze River, and approximately 1.5km away from Qianjiangping landslide on its left bank. The landslide has been affected by water level fluctuations ranging between 145-175m that have submerged its frontal edge by up to 20-50m. The Woshaxi landslide exhibits a high-to-low gradient from southwest to northeast, with its rear edge situated at an elevation of 405m and the front edge below 140m. This geological event boasts an average thickness of approximately 15m and a volume of 4.2×10^6 m^3, while its primary sliding direction is oriented at 40°.

According to the Seismic Ground Motion Parameter Zonation Map of China, the peak ground motion acceleration in this region is 0.05g. To investigate slope stability evolution under seismic conditions, peak accelerations are calculated and analyzed at various levels. The most dangerous case is considered in the following calculations, where the direction of the horizontal seismic action coincides with the primary sliding direction. The precipitation pattern in this region is characterized by relatively concentrated temporal and spatial distribution. Most of the rainfall occurs between

https://doi.org/10.5194/nhess-2023-181
Preprint. Discussion started: 13 November 2023

Natural Hazards and Earth System Sciences
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April and October. To investigate the stability of three-dimensional slopes under the combined influence of rainfall and earthquake, this study considers the effects of three geotechnical parameters: permeability coefficient, porosity, and saturation. The proposed method is applied to calculate changes in slope stability resulting from average monthly rainfall and earthquake occurring between 2007-2009.

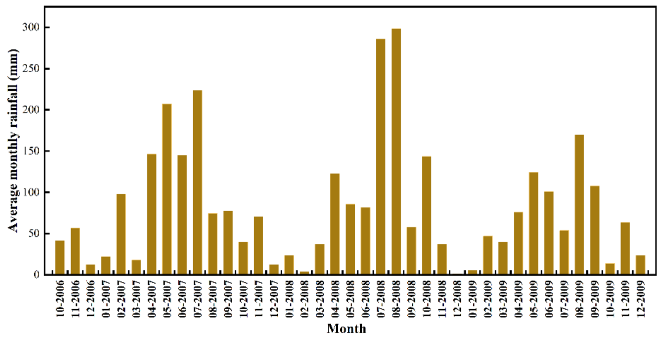


Fig. 13 Average monthly rainfall from 2007 to 2009

Fig. 13 shows the average monthly rainfall from 2007 to 2009. Table 1 lists the physical and mechanical parameters of the landslide body. It is assumed that the reservoir water level remains unchanged. To assess the effects of different geotechnical parameters and seismic action on the safety factor, four cases are considered: (i) rainfall only, (ii) rainfall and horizontal earthquake, (iii) rainfall and vertical earthquake, and (iv) rainfall and earthquake in both horizontal and vertical directions.

Table 1 Mechanical parameters of Woshaxi slope

Unit weight, γ (KN/m^3)		Shear strength, c' (kPa)		Friction angle, φ' (°)	
Saturated condition	Natural condition	Saturated condition	Natural condition	Saturated condition	Natural condition
22.4	20.8	18	22	10	20

https://doi.org/10.5194/nhess-2023-181
Preprint. Discussion started: 13 November 2023

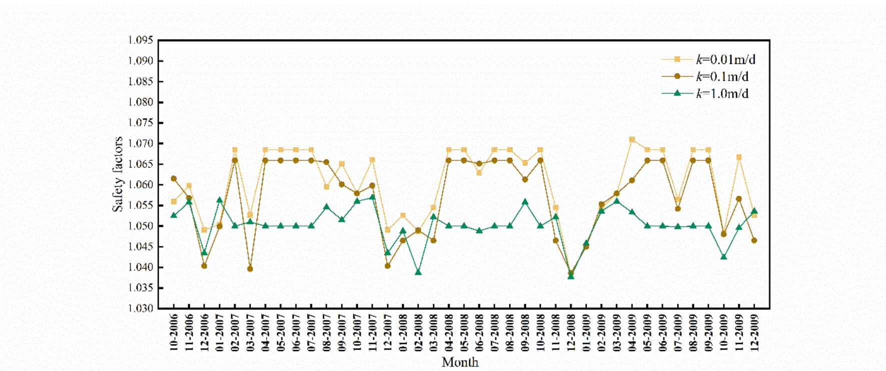
(i) Rainfall only

The three parameters, infiltration coefficient, porosity, and saturation, have different effects on the safety factor of slopes. The safety factor varies with the monthly rainfall. The analysis shows that an increase in rainfall does not necessarily lead to a lower safety factor. This is because the increase in rainfall leads to a higher phreatic surface, which causes changes in two aspects: an increase in hydrodynamic and an increase in pressure at the foot of the slope. When the pressure at the foot of the slope has more influence on the slope than the hydrodynamic, the safety factor will increase at this time, and conversely the stability of the slope will decrease. As shown in Fig. 14(a), the permeability coefficient k is 0.01, 0.1 and 1m/d, respectively. With other parameters unchanged, the trend of safety factor variation for Woshaxi landslide is consistent. The higher the permeability coefficient, the greater the soil's ability to allow water to pass through above the phreatic surface, the smaller the rise of the phreatic surface within the slope. This results in a smaller increase in pressure at the foot of the slope and a lower safety factor.

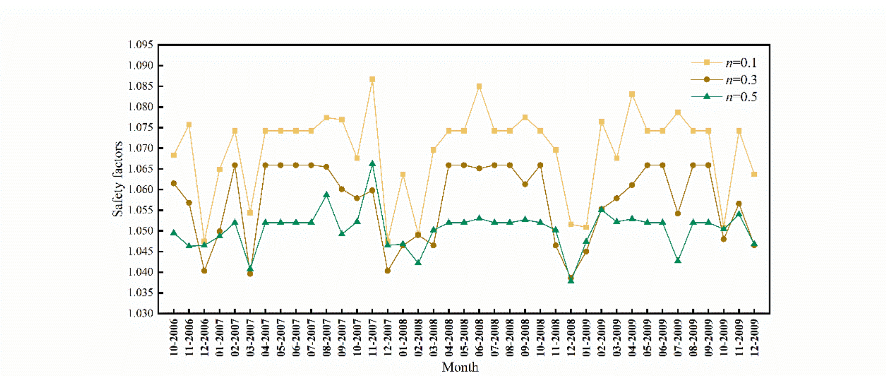
As shown in Fig. 14(b), the porosity n is 0.1, 0.3 and 0.5, respectively, and the safety coefficient of the Woshaxi landslide is consistent under the condition that other parameters remain unchanged. The higher the porosity, the greater the soil permeability above the phreatic surface, the smaller the rise of the phreatic surface within the slope, resulting in a smaller increase of pressure at the slope's foot and thus a lower safety factor.

https://doi.org/10.5194/nhess-2023-181
Preprint. Discussion started: 13 November 2023

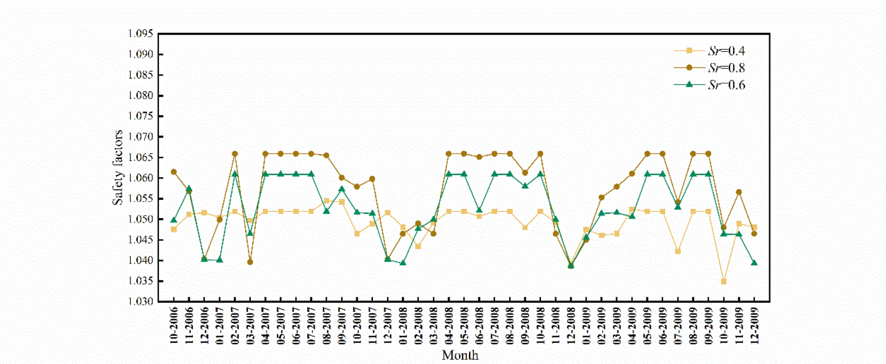
As shown in Fig. 14(c), the saturation S_r of the soil above the phreatic surface of the landslide is 0.4, 0.6 and 0.8, respectively, and the safety factor of the Woshaxi landslide is consistent under other parameters remained unchanged. The higher the saturation, the lower the permeability of soil above the phreatic surface, resulting in a greater rise of phreatic surface within the slope and an increased pressure at its foot, thereby leading to a higher safety factor. Overall, under rainfall conditions, soil porosity on the phreatic surface has a greater impact on safety factor than permeability coefficient and saturation.



(a) permeability coefficient



(b) porosity

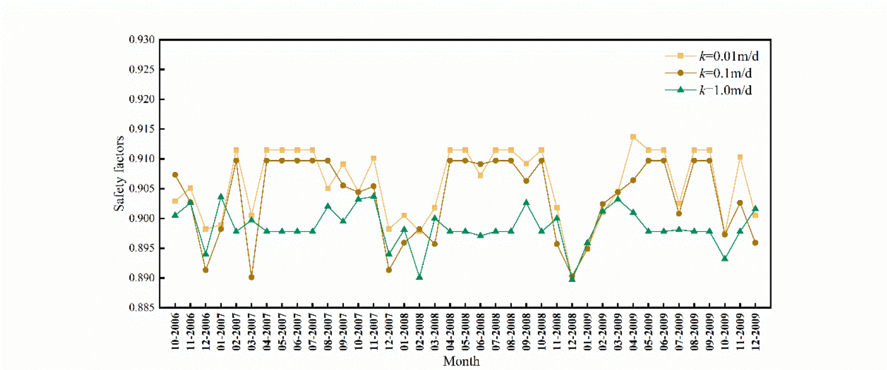


(c) saturation

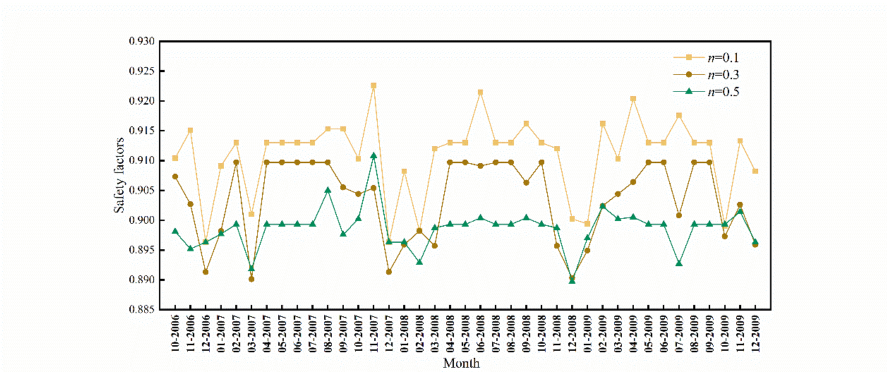
Fig. 14 Safety factors of the Woshaxi landslide under rainfall

(ii) Rainfall and horizontal earthquake

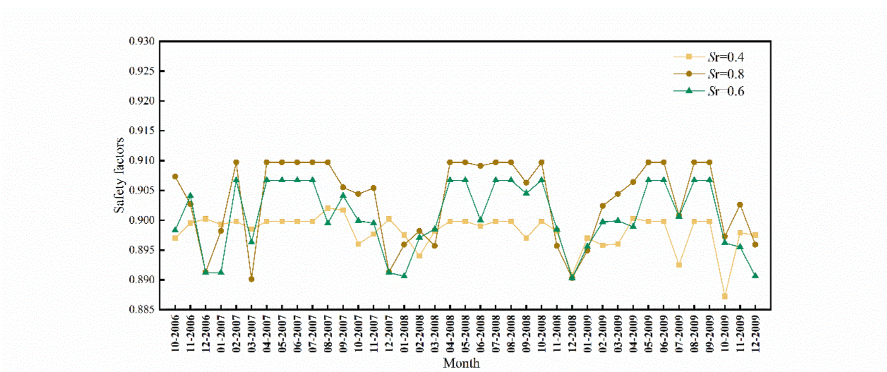
Fig. 15 shows the evolution of the stability of the Woshaxi landslide under the combined effect of rainfall and horizontal earthquake with different geotechnical parameters, and the horizontal earthquake coefficient k_h is taken as 0.05. Comparing with Fig. 14, it can be observed that after considering the effect of horizontal earthquake, the variation trend of the safety factor of the Woshaxi landslide calculated with different geotechnical parameters is consistent with that under the rainfall condition only, but the stability of the landslide is obviously decreased. Fig. 16 shows the evolution of the stability of the Woshaxi landslide with rainfall and different horizontal earthquake coefficients. With other parameters unchanged, the values of the horizontal earthquake coefficients are 0.05, 0.1 and 0.15 respectively. As the horizontal earthquake coefficient increases, the safety factor of the landslide decreases significantly. The seismic influence on slope stability is considerably greater than that of rainfall.



(a) permeability coefficient



(b) porosity



(c) saturation

Fig. 15 Safety factors of the Woshaxi landslide under rainfall and horizontal earthquake ($k_h = 0.05$)

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Preprint. Discussion started: 13 November 2023

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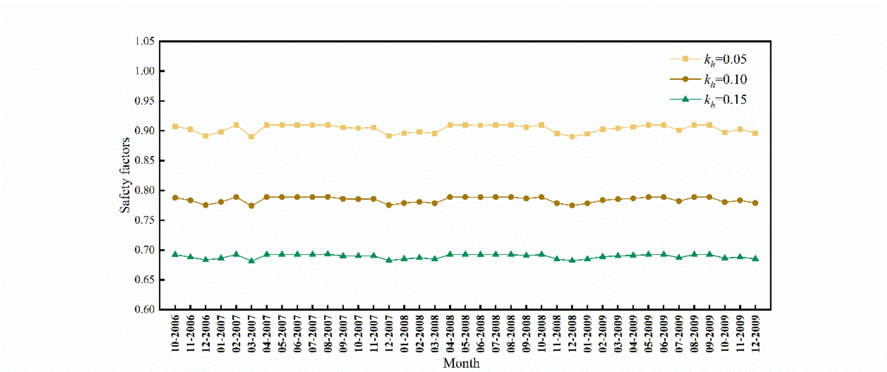
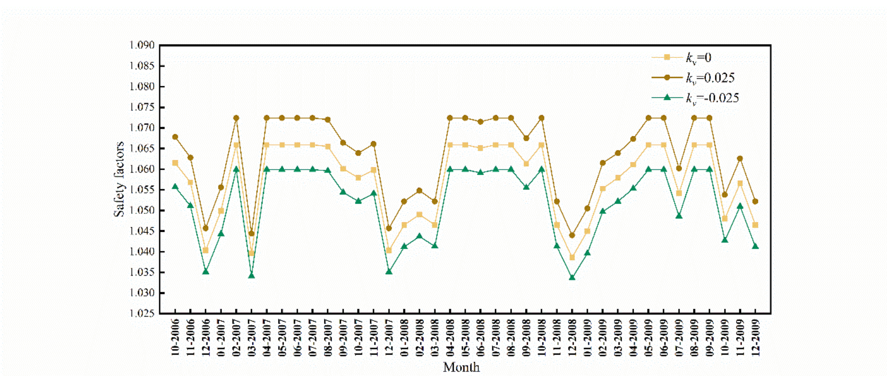


Fig. 16 Safety factors of the Woshaxi landslide under rainfall and horizontal earthquake (different horizontal seismic coefficient)

(iii) Rainfall and vertical earthquake

Fig. 17 shows the evolution of the stability of the Woshaxi landslide with rainfall and different vertical earthquake coefficients. With other parameters unchanged, the vertical earthquake coefficient k_v takes on values of 0.025, 0, and -0.025 respectively, and the negative sign indicates that the direction of vertical earthquake is vertically downward. It is obvious from Fig. 17 that the corresponding safety factor when the earthquake acts vertically downward is smaller than the corresponding safety factor when it is vertically upward.



https://doi.org/10.5194/nhess-2023-181
Preprint. Discussion started: 13 November 2023

Fig. 17 Safety factors of the Woshaxi landslide under rainfall and vertical earthquake

(iv) Rainfall and earthquake in both horizontal and vertical directions

Fig. 18 shows the evolution of the stability of the Woshaxi landslide with rainfall and different earthquake coefficients. Horizontal earthquake coefficient k_h is taken as 0.05, and the values of vertical earthquake coefficient are 0.025, 0, -0.025 respectively, and the negative sign indicates that the direction of vertical earthquake action is vertically downward. Under the condition that other parameters remain unchanged, the slope stability is lower when considering both horizontal and vertical upward earthquake compared to considering only horizontal earthquake. Therefore, it is essential to properly account for the effect of vertical earthquake in order to ensure maximum safety.

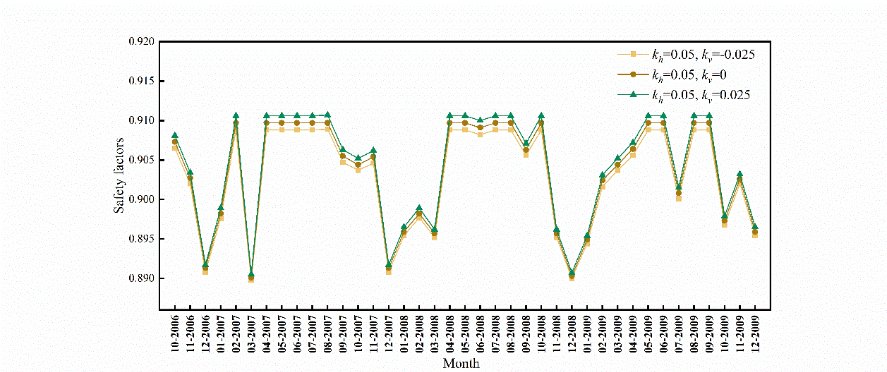


Fig. 18 Safety factors of the Woshaxi landslide under rainfall and earthquake (in both horizontal and vertical directions)

6 Conclusions

In this paper, the calculation of the seepage force is studied, the normal stress expression on the sliding surface of a slope under seepage force and seismic force are

https://doi.org/10.5194/nhess-2023-181
Preprint. Discussion started: 13 November 2023

also derived. Furthermore, a global analysis method that considers both seepage and seismic forces is proposed to determine the safety factor of slopes subjected to the combined effect of rainfall and earthquake. The reliability of the proposed method is also verified with two examples combining software calculations and previous results.

Taking a slope in the Three Gorges reservoir area as an example, this study investigates the influence of soil permeability coefficient, porosity and saturation on slope stability, and analyzes the safety evolution of this slope under combined effects of rainfall and earthquake. The results indicate that, under rainfall conditions, the porosity of the soil above the phreatic surface exerts a greater influence on safety factor than permeability coefficient and saturation. With an increase in the horizontal earthquake coefficient, the safety factor of the landslide is significantly reduced, and the impact of earthquake on slope stability surpasses that of rainfall. The safety factor corresponding to vertical downward earthquake action is smaller than that of vertical upward, and the stability of slope is lower when considering horizontal and vertical upward earthquake actions. Therefore, in order to ensure maximum safety, proper consideration should be given to vertical earthquake actions.

Considering the effect of seismic force and seepage force, the formula for calculating the stability of landslide under the combined effect of earthquake and rainfall is improved, and the stability coefficient of the landslide is calculated to be low and unstable. The research results provide scientific basis for slope stability analysis and prevention. Further, the proposed method can identify potential risk areas for

https://doi.org/10.5194/nhess-2023-181
Preprint. Discussion started: 13 November 2023

landslide hazards, and planners in the Three Gorges Reservoir area can better consider these risks and take measures to increase the seismic and flood resilience of reservoir infrastructure.

Data availability

The data used in this study are available from the first author upon request.

Author contribution

JW analyzed the data, conceived the paper, and wrote the paper; ZW conceived and co-wrote the paper; HL reviewed and improved the analysis and paper; and GS provided the data of the actual slope in the Three Gorges reservoir.

Competing interests

The contact author has declared that none of the authors has any competing interests.

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