

## 1 The characteristics of the 2022 Tonga volcanic tsunami in the Pacific Ocean

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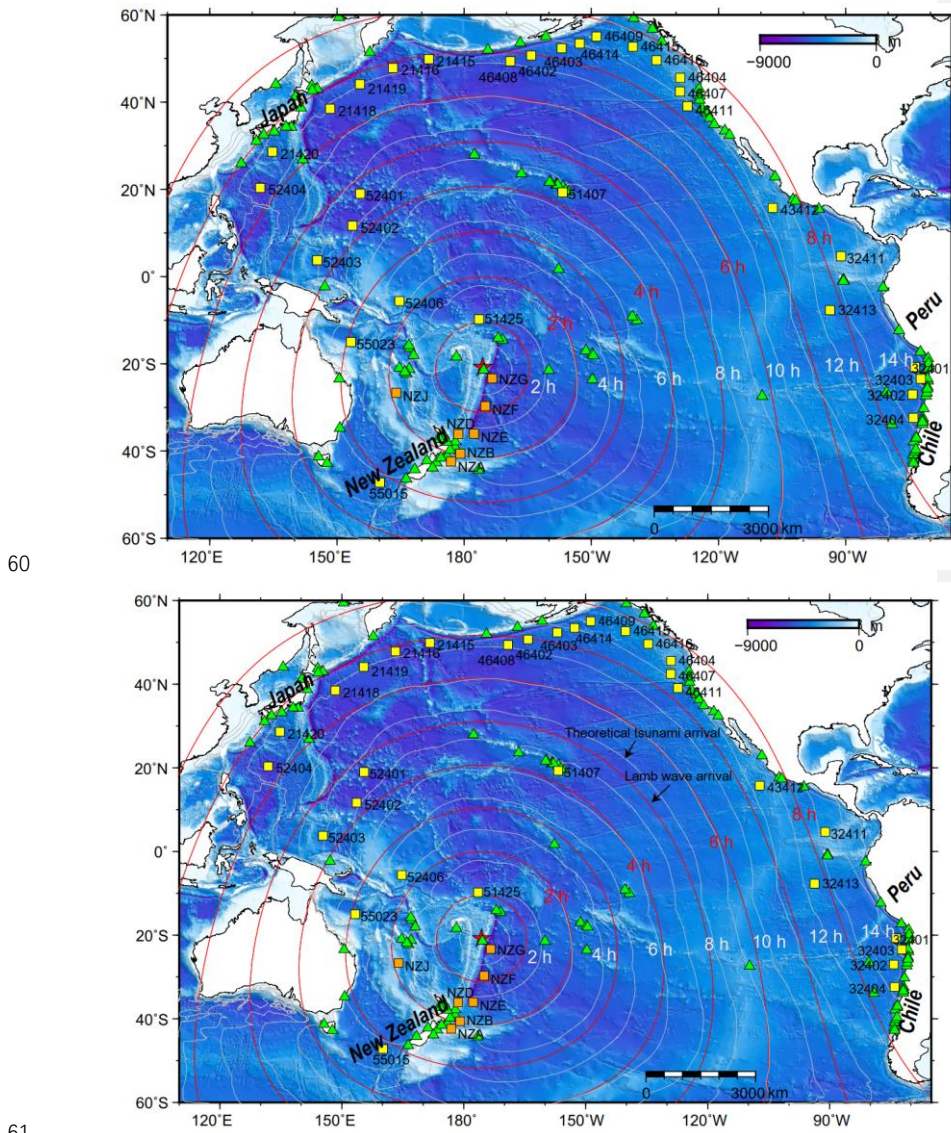
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8 **Abstract.** On 15th January 2022, an exceptional eruption of Hunga Tonga–Hunga Ha’apai volcano  
9 generated atmospheric and tsunami waves that were widely observed at oceans globally, gaining a  
10 remarkable attention to scientists in related fields. The tsunamigenic mechanism of this rare event  
11 remains an enigmatic due to its complexity and lacking of direct underwater observations. Here, to  
12 explore the tsunamigenic mechanisms of this volcanic tsunami event and its hydrodynamic processes in  
13 the Pacific Ocean, we conduct tsunami waveform and spectral analyses of the waveform recordings at  
14 116 coastal gauges and 38 deep-ocean buoys across the Pacific Ocean. Combined with the constraints of  
15 some representative barometers, we obtain the plausible tsunamigenic origins during the volcano activity.  
16 We identify four distinct tsunami wave components generated by air-sea coupling and seafloor crustal  
17 deformation. Those tsunami components are differentiated by their different propagating speeds or period  
18 bands. The first-arriving tsunami component with ~80–100 min period was from shock waves spreading  
19 at a velocity of ~1000 m/s in the vicinity of the eruption. The second component with extraordinary  
20 tsunami amplitude in deep sea was from Lamb waves. The Lamb wave with ~30–40 min period radically  
21 propagated outward from the eruption site with spatially decreasing propagation velocities from ~340  
22 m/s to ~315m/s. The third component with ~10–30 min period was probably from some atmospheric  
23 gravity wave modes propagating faster than 200 m/s but slower than Lamb waves. The last component  
24 with ~3–5 min period originated from partial caldera collapse with dimension of ~0.8–1.8 km.  
25 Surprisingly, the 2022 Tonga volcanic tsunami produced long oscillation in the Pacific Ocean which is  
26 comparable with those of the 2011 Tohoku tsunami. We point out that the long oscillation is not only  
27 associated with the resonance effect with the atmospheric acoustic-gravity waves, but more importantly  
28 the interactions with local bathymetry. This rare event also calls for more attention to the tsunami hazards  
29 produced by atypical tsunamigenic source, e.g., volcanic eruption.

30 **1. Introduction**

31 On 15 January 2022 at 04:14:45 (UTC), a submarine volcano erupted violently at the uninhabited Hunga  
32 Tonga-Hunga Ha'apai (HTHH) island at 20.546°S 175.390°W (USGS, 2022). The volcano is located ~67  
33 km north of Nuku'alofa, the capital of Tonga (NASA, 2022) (Figure 1). The blasts launched plumes of  
34 ash, steam, and gas ~58 km high into stratosphere (Yuen et al., 2022) which not only blanketed nearby  
35 islands in ash (Duncombe, 2022; NASA, 2022), but caused various atmospheric acoustic-gravity wave  
36 modes (AGWs) of various scales, e.g., Lamb waves from atmospheric surface pressure disturbance  
37 associated with the eruption (Liu and Higuera, 2022; Adam, 2022; Kubota et al., 2022; Matoza et al.,  
38 2022). Tsunami with conspicuous sea level changes were detected by coastal tide gauges and Deep-ocean  
39 Assessment and Reporting of Tsunamis (DART) buoy stations in the Pacific (Figure 1), the Atlantic, and  
40 Indian Oceans as well as the Caribbean and Mediterranean seas (Carvajal et al., 2022; Kubota et al., 2022;  
41 Ramírez-Herrera et al., 2022), while the large waves were mainly concentrated in the Pacific Ocean, like  
42 coastlines of New Zealand, Japan, California, and Chile (Carvajal et al., 2022). The event caused at least  
43 3 fatalities in Tonga. Two people drowned in northern Peru when ~2 m destructive tsunami waves  
44 inundated an island in the Lambayeque region, Chile (Edmonds, 2022).

45 Satellite images revealed that the elevation of HTHH island has gone through dramatic change before  
46 and after the mid-January 2022 eruption. Previously, after the 2015 eruption, the two existing Hunga  
47 Tonga and Hunga Ha'apai Islands were linked together. The volcanic island rose 1.8 km from the seafloor  
48 where it stretched ~20 km across and topped a underwater caldera ~5 km in diameter (Garvin et al., 2018;  
49 NASA, 2022). After the violent explosion on 15 January 2022, the newly formed island during 2015 was  
50 completely gone, with only small tips left in far southwestern and northeastern HTHH island (NASA,  
51 2022). HTHH volcano lies along the northern part of Tonga–Kermadec arc, where the Pacific Plate  
52 subducts under the Indo-Australian Plate (Billen et al., 2003). The convergence rate (15–24 cm/year)  
53 between the Tonga–Kermadec subduction system and the Pacific plate is among the fastest recorded plate  
54 velocity on Earth, forming the second deepest trench around the globe (Satake, 2010; Bevis et al., 1995).  
55 The fast convergence rate contributes to the frequent earthquakes, tsunamis and volcanic eruptions in  
56 this region historically (Bevis et al., 1995). The 2022 HTHH volcano is part of a submarine-volcano  
57 chain that extends all the way from New Zealand to Fiji (Plank et al., 2020). HTHH volcano had many  
58 notable eruptions before 2022 since its first historically recorded eruption in 1912, i.e., in 1937, 1988,



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61  
62 **Figure 1. The spatial distribution of the eruption site (red star), DART stations (squares), tide**  
63 **gauges (triangles) and the calculated tsunami arrival times. White contours indicate the modelled**  
64 **arrival times of conventional tsunami. Red contours indicate the estimated arrival times of Lamb**  
65 **waves (see how we derive these contours in section 3.1).**

66 The 2022 HTHH eruption is the first volcanic event which generates worldwide tsunami signatures since  
67 the 1883 Krakatau event (Matoza et al., 2022; Self and Rampino, 1981; Nomanbhoy and Satake, 1995).

68 The tsunamigenic mechanism of this rare volcanic eruption-induced tsunami is still poorly understood  
69 due to its complex nature and the deficiencies of near-field seafloor surveys. Various tsunami generation  
70 mechanisms have been proposed so far based on the observations of ground-based and spaceborne  
71 geophysical instrumentations (Kubota et al., 2022; Matoza et al., 2022; Carvajal et al., 2022). The  
72 mechanisms are closely associated with the air-sea coupling with atmospheric waves. Atmospheric  
73 waves propagating in the atmospheric fluid with different speeds are generated by different physical  
74 mechanisms (E. E. Gossard and W. H. Hooke, 1975). Nonlinearities in the process may lead to the  
75 formation of shock-wave and period lengthening. The balance between gravity and buoyancy causes  
76 gravity waves. The acoustic wave propagate by atmospheric fluid compression and rarefaction. (Matoza  
77 et al., 2022). The most-mentioned mechanism of the tsunami is the fast-traveling atmospheric Lamb wave  
78 generated by the atmospheric pressure rise of ~2 hPa during the eruption. The Lamb wave circled the  
79 Earth for several times with travelling speed close to that of the sound wave in the lower atmosphere,  
80 leading to globally observed sea level fluctuations (Adam, 2022; Duncombe, 2022; Kubota et al., 2022;  
81 Matoza et al., 2022) (Figure 1). The second mechanism is suggested to be a variety of other acoustic-  
82 gravity wave modes (Adam, 2022; Matoza et al., 2022; Themens et al., 2022; Zhang et al., 2022). The  
83 third mechanism may be related to the seafloor crustal deformation induced by one or more volcanic  
84 activities in the vicinity of the eruption site (e.g., pyroclastic flows, partial collapse of the caldera)  
85 (Carvajal et al., 2022), which are more responsible for the near-field tsunamis with theoretical tsunami  
86 speeds.

87 To investigate the possible tsunamigenic mechanisms and detailed hydrodynamic behaviors of this rare  
88 volcanic tsunami event, in this study, we collect, process and analyze the sea level measurements from  
89 116 tide gauge and 38 DART buoys in the Pacific Ocean (shown in Figures 1 and 2). We first do statistical  
90 analysis of the tsunami waveforms to estimate the propagating speed of the Lamb wave and to understand  
91 the tsunami wave characteristics in the Pacific Ocean through demonstrating the tsunami wave properties,  
92 i.e., arrival times, wave heights and durations. We then conduct wavelet analysis for representative DART  
93 buoys and tide gauges respectively to explore tsunamigenic mechanisms of the event and to better  
94 understand its hydrodynamic processes in the Pacific Ocean. Aided by wavelet analysis of corresponding  
95 barometers near the selected DART buoys and comparison with tsunami records of the 2011 Tohoku  
96 tsunami, we are able to piece together all the analysis and demonstrate that the 2022 HTHH tsunami was

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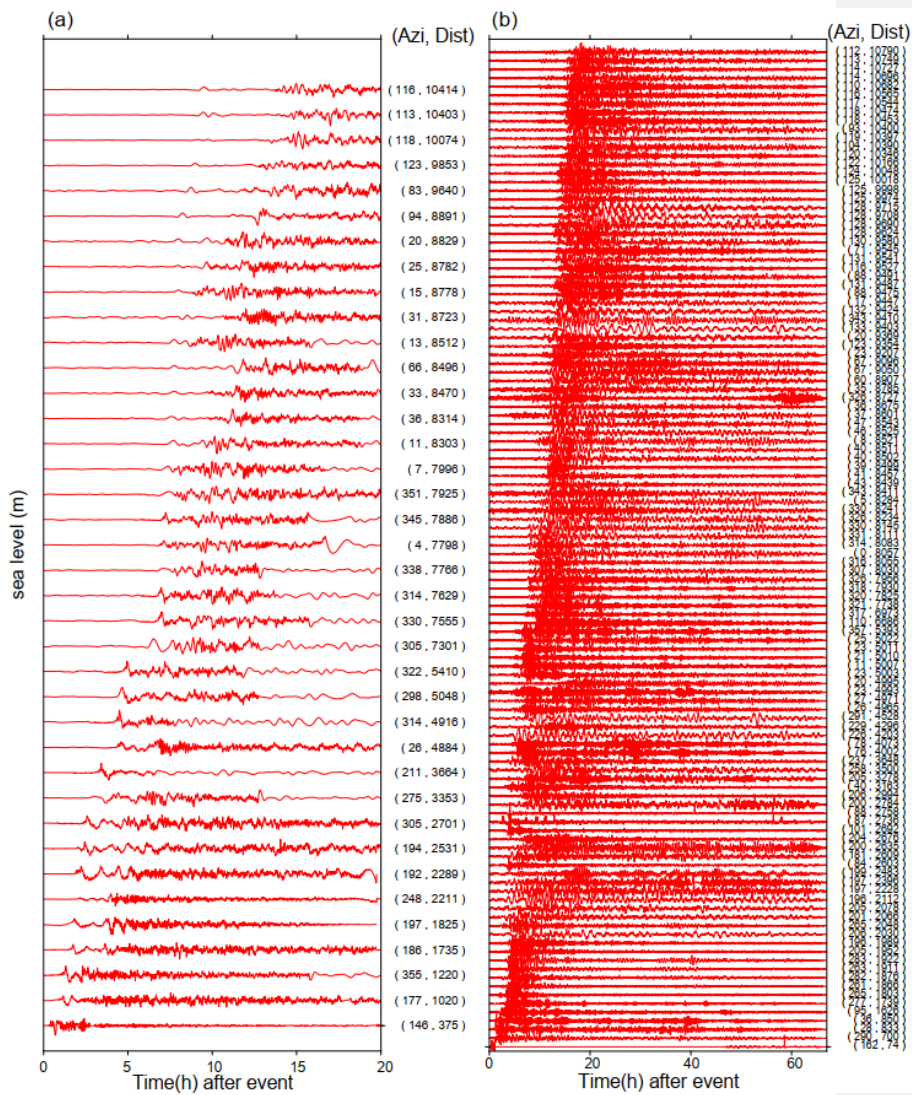
97 generated by air-sea coupling with a wide range of atmospheric waves with different propagating  
98 velocities and period bands, and seafloor crustal deformation associated with the volcanic eruption. We  
99 demonstrate as well that the tsunami was amplified at the far-field Pacific coastlines where the local  
100 bathymetric effects play a dominant role in tsunami scale.

## 101 2. Data and Methods

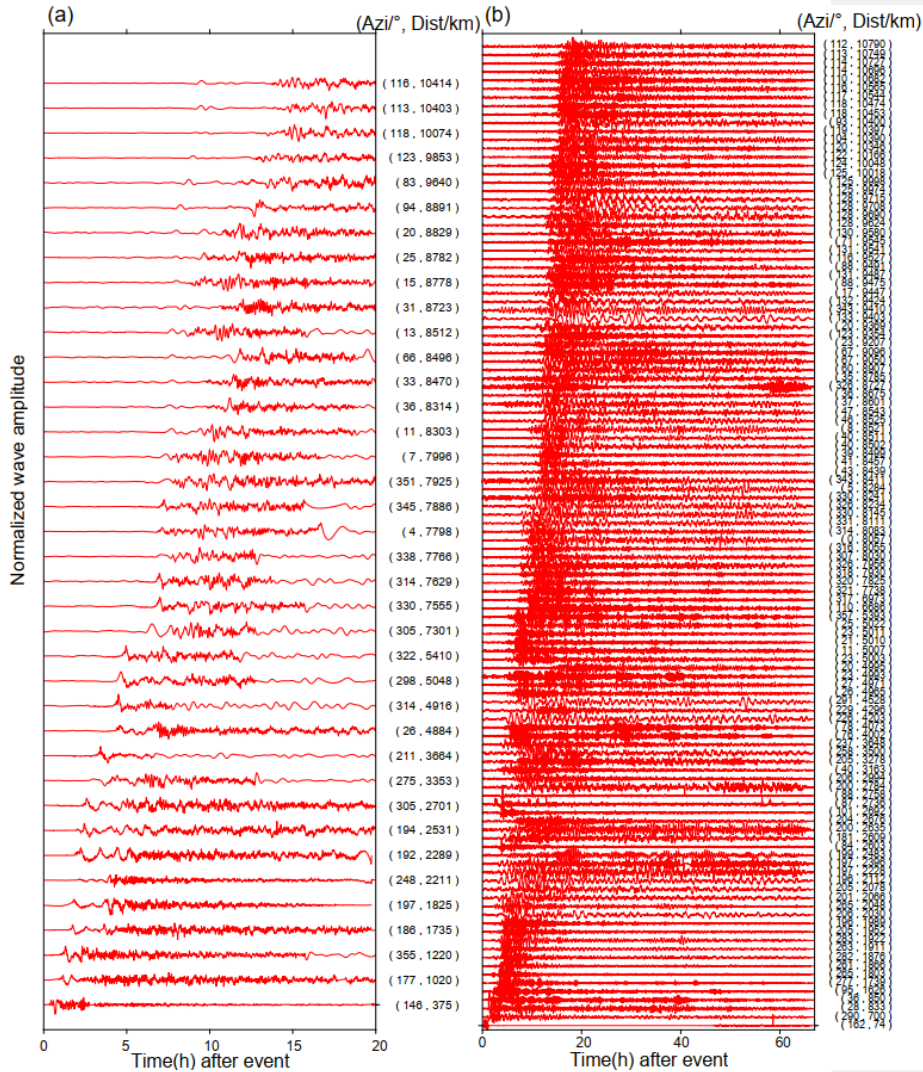
### 102 2.1 Data

103 We collected high-quality sea level records across the Pacific Ocean at 38 DART buoys (in which 31  
104 stations from <https://nctr.pmel.noaa.gov/Dart/>, 7 stations from <https://tilde.geonet.org.nz/dashboard/>) and  
105 116 tide gages from IOC (The Intergovernmental Oceanographic Commission, [http://www.ioc-](http://www.ioc-sealevelmonitoring.org)  
106 [sealevelmonitoring.org](http://www.ioc-sealevelmonitoring.org)) (Figure 1). The epicentral distances of tide gauges and DART buoys range  
107 between 74–10790 km and 375–10414 km, respectively. The sampling rates of DART buoys are  
108 changing over time. Passing of tsunami event generally can trigger the DART system to enter its high  
109 frequency sampling mode (15 seconds or 1 min) from normal frequency mode (15 min)  
110 ([www.ndbc.noaa.gov/dart](http://www.ndbc.noaa.gov/dart)). In contrast, sampling rates of normal tide gauges at coasts are uniform with  
111 sampling interval of 1 min. The sampling interval of both DART and tide gauges is preprocessed to 15  
112 seconds. Firstly, we eliminate abnormal spikes and fill gaps by linear interpolation. Secondly, we applied  
113 a fourth-order Butterworth-Highpass filter with a cut-off frequency of  $3.5 \times 10^{-5}$  Hz (~ 8 hours) to remove  
114 the tidal components (Figure 2) (Heidarzadeh and Satake, 2013). After the two steps, quality control step  
115 is conducted to select high-quality data, in which we delete waveforms with spoiled data or massive data  
116 loss due to equipment failure, or with the maximum tsunami heights [of tide gauges](#) less than 0.2 m, then  
117 the selected data will be ready for further statistics and spectral analysis. We also collect and analyze the  
118 atmospheric pressure disturbance data recorded by some representative barometers. The sampling rates  
119 of the barometers is generally uniform with a sampling rate of 1 min except for some stations in New  
120 Zealand with interval of 10 min. Considering the sample rate, we employ a fourth-order Butterworth-  
121 Bandpass filter with period ranging between 2–150 min for wavelet analysis of the barometers with 1  
122 min sample rate, while we apply the fourth-order Butterworth-Bandpass filter with range of 30–150 min  
123 to long-period waveform display based on two reasons. (1) The barometer data we use for the analysis  
124 include some in New Zealand with 10 min sample rate; (2) Filtering out the short-period waves helps

125 highlight long-period tsunami wave components.  
 126 The tsunami waveforms recorded by DART buoys which are installed offshore in the deep water are  
 127 expected to contain certain characteristics of the tsunami source (Wang et al., 2020, 2021). The  
 128 waveforms recorded by tide gauge distributed along coastlines are significantly influenced by local  
 129 bathymetry/topography which are used for investigating bathymetric effect on tsunami behaviors  
 130 (Rabinovich et al., 2017, 2006; Rabinovich, 2009). Therefore, we use the DART data for source-related  
 131 analysis and choose some tide gauge data to investigate the tsunami behaviors at the Pacific coastlines.



132



133

134 **Figure 2. Detided tsunami waveforms at (a) DART buoys and (b) tide gauges. Waveforms in both**  
 135 **subplots are shown in ascending distance. Azi stands for azimuth.**

136 **2.2 Tsunami Modelling**

137 We use a numerical tsunami modelling package JAGURS (Baba et al. 2015) to simulate the tsunami  
 138 propagation of the 2022 HTHH event and obtain the theoretical tsunami arrival time based on the shallow  
 139 water wave speed (white contours in Figure 1). The code solves linear Boussinesq-type equations in a  
 140 spherical coordinate system using a finite difference approximation with the leapfrog method. We specify

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141 a unit Gaussian-shaped vertical sea surface displacement at the volcanic base as the source of  
142 conventional tsunamis. For a unit source  $i$  with center at longitude  $\varphi_i$  and latitude  $\theta_i$ , the  
143 displacement distribution  $Zi(\varphi, \theta)$  can be expressed as:

$$144 \quad Zi(\varphi, \theta) = \exp\left[-\frac{(\varphi-\varphi_i)^2+(\theta-\theta_i)^2}{2\sigma}\right] \quad (1)$$

145 Where we set characteristic length  $\sigma$  as 5 km (NASA, 2022). The bathymetric data is resampled from the  
146 GEBCO 2019 with 15 arc-sec resolution (The General Bathymetric Chart of the Oceans, downloaded  
147 from <https://www.gebco.net>).

### 148 **2.3 Spectral Analysis of Tsunami Waves**

149 To investigate the temporal changes of the dominant wave periods, we conduct continuous wavelet  
150 transformation (frequency-time) analyses for some representative DART buoys, tide gauges and  
151 barometers, in which wavelet Morlet mother function is implemented (Kristeková et al., 2006). The first  
152 32-hour time series of DART buoys and barometers after the eruption (at 04:14:45 on 15 January 2022)  
153 are used for source-related wavelet analysis. The first 48-hour time series of tide gauges after the eruption  
154 are employed for hydrodynamics-related wavelet analysis at coastlines. We adopt the Averaged-Root-  
155 Mean-Square (ARMS) method as a measure of absolute average tsunami amplitude with a moving time  
156 window of 20 min to calculate the tsunami duration (Heidarzadeh and Satake, 2014). We define the time  
157 durations as the time period where ARMS levels of tsunami waves are above those prior to the tsunami  
158 arrivals.

## 159 **3. Results**

### 160 **3.1 The decreasing propagation velocities of the Lamb Wave**

161 Although many types of atmospheric waves were generated by the 2022 HTHH eruption, the most  
162 prominent signature was the Lamb waves which were globally observed by ground-based and spaceborne  
163 geophysical instrumentations (Kulichkov et al., 2022; Liu et al., 2022; Lin et al., 2022; Matoza et al.,  
164 2022; Themens et al., 2022; Adam, 2022; Kubota et al., 2022). Interestingly, we notice that a wide range  
165 of the velocities from 280 m/s to 340 m/s were proposed through observations and Lamb wave modelling  
166 (e.g., Kubota et al., 2022; Lin et al., 2022; Matoza et al., 2022; Themens et al., 2022). The travelling  
167 velocity of Lamb waves in real atmosphere is affected by temperature distributions, winds and dissipation



168 (Otsuka, 2022). To investigate whether the propagation speeds of the lamb wave change in space and  
169 time, we analyze the waveforms recorded by the DART buoys in the Pacific Ocean. DART buoy with  
170 pressure sensor deployed at the ocean's bottom records the sea level change that is transferred from  
171 pressure records in Pascals, instead of direct water height. For the 2022 HTHH tsunami event, the  
172 pressure fluctuation at DART buoy is a superposition of the pressure changes caused by tsunami and the  
173 Lamb wave (Kubota et al., 2022). The Pacific DART buoys recorded the most discernible air-sea  
174 coupling pulse in deep ocean with Lamb waves that arrived earlier than the theoretical tsunamis (Figure  
175 1). The tsunami waveforms recorded by tide gauges did not clearly detect the tsunami signals associated  
176 with the lamb-Lamb waves, therefore not sufficient for further analysis (Figure 2). Thus, we estimate the  
177 speed of Lamb waves using the waveforms recorded by the Pacific DART buoys. The Lamb wave  
178 arrivals are limited within arrival time range from possible velocities of 280–340 m/s. The time points at  
179 which the tsunami amplitudes first exceed 1 e-4 m above sea level are defined as Lamb wave arrivals.  
180 By carefully fitting the arrivals with different constant velocities, we illustrate the velocities of Lamb  
181 wave were generally uniform, but slightly decrease with the increase of propagation distance (Figure 3).  
182 The Lamb waves initially propagated radially at speed of ~340 m/s before slowing to ~325 m/s after  
183 reaching ~3400 km, and further decreasing to ~315 m/s at 7400 km. In an isothermal troposphere  
184 assumption, the phase velocity of the Lamb wave ( $C_L$ ) can be estimated with the following equation  
185 (Gossard and Hooke, 1975):

$$186 \quad C_L = \sqrt{\frac{\gamma R T}{M}} \quad (2)$$

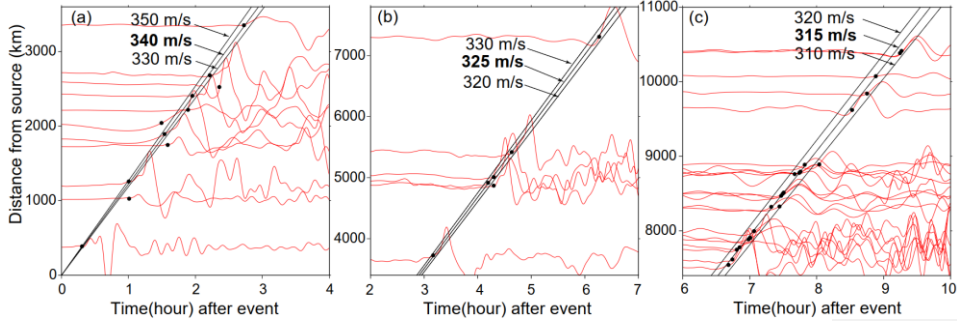
187 Where  $\gamma = 1.4$  (air specific heat ratio corresponding to atmospheric temperature),  $R = 8314.36 \text{ J kmol}^{-1}$   
188  $\text{K}^{-1}$  (the universal gas constant),  $M = 28.966 \text{ kg kmol}^{-1}$  (molecular mass for dry air) are constant for the  
189 air,  $T$  is the absolute temperature in kelvin. Thus, Lamb wave velocity is mainly affected by the air  
190 temperature, meaning the travelling velocity of lamb waves might decrease when propagating from  
191 regions with high temperature towards those with low temperatures, e.g., the north pole. By assuming a  
192 set of possible temperatures in January (Table 1), we calculated the velocities  $C_L$  could range between  
193 312–343 m/s when temperatures vary between -30–20 °C. Therefore, the decreased velocity of the Lamb  
194 waves could be a consequence of cooling of the air temperature.

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196 **Figure 3. Fitting the arrival times of normalized Lamb waveforms with different velocities. Black**  
197 **dots mark the arrival times of the Lamb waves. Black lines represent velocities.**

198 **Table 1. Estimated Lamb wave velocities in an isothermal troposphere assumption**

Celsius temperature (°C)	thermodynamic temperature (K)	$C_L$ (m/s)
20	293.15	343.14
10	283.15	337.23
0	273.15	331.21
-10	263.15	325.19
-20	253.15	318.86
-30	243.15	312.49

199 **3.2 Tsunami features observed by DART buoys and Tide gauges**

200 The statistics of tsunami heights and arrival times recorded at 38 DART buoys and 116 tide gauges across  
201 the Pacific Ocean are used to interpret the tsunami characteristics. The comparison of the statistical  
202 characters between DART and tide gauge observations yields some useful information of the  
203 hydrodynamic process of tsunami propagation and help identify tsunami wave components with different  
204 traveling velocities.

205 The average value of the maximum tsunami wave height (trough-to-crest) for the 116 tide gauge stations  
206 is ~1.2 m. Figure 4a shows tide gauges with large tsunami heights exceeding 2 m are mainly distributed  
207 in coastlines with complex geometries (Figure S1a), such as gauges at New Zealand, Japan, and north  
208 and south America. For example, the largest tsunami height among tide gauges is 3.6 m at a bay-shaped  
209 coastal area Chañaral in Chile (Figure S1b). In sharp contrast to tide gauges, the maximum tsunami  
210 heights of most Pacific DART buoys are less than 0.2 m. The largest tsunami height in the DART buoys  
211 is only ~0.4 m recorded at the nearest one, 375 km from the volcano (Figure 4b). The comparison between  
212 DART buoys and tide gauges indicate that the direct contribution of air-sea coupling to the tsunami

213 heights is probably in the level of tens of centimeters (Kubota et al., 2022). The meter-scale tsunami  
214 heights at the coastlines suggest the bathymetric effect could play a major role during tsunami  
215 propagation. In respect to the arrival of maximum tsunami waves, the time lags between Lamb waves  
216 and the maximum heights of tide gauges mainly range between ~0–10 h (Figure 4c). The delayed times  
217 of ~10 h are observed in New Zealand, Hawaii, and west coast of America (Figure 4c), suggesting the  
218 interaction between tsunami waves and local topography/bathymetry delays the arrival of the maximum  
219 waves (e.g., Hu et al., 2022). For example, the delayed maximum tsunami height can be attributed to the  
220 edge waves (Satake et al., 2020) and resonance effect (Wang et al., 2021), from tsunami interplays with  
221 bays/harbors, islands, and continental shelves of various sizes. The significant regional dependence of  
222 the coastal tsunami heights and the time lags of the maximum tsunami waves can be attributed to the  
223 complexity of local bathymetry, such as continental shelves with different slopes, and harbor/bay with  
224 different shapes and sizes (Satake et al., 2020). On the other hand, since the DART records are less  
225 influenced by bathymetric variation in space, the first waves in DART buoys are supposed to be the  
226 maximum tsunami waves as observed in the 2011 Tohoku tsunami event (Heidarzadeh and Satake, 2013).  
227 However, we observe the inconsistency between the arrivals of the Lamb waves and the maximum  
228 tsunami heights (Figure 4d). The time lags of the maximum waves of DART buoys present a coarsely  
229 increasing tendency with the increasing distance from the volcano, which indicates the contribution of  
230 other tsunami generation mechanism propagating with a uniform but lower speed than Lamb wave.

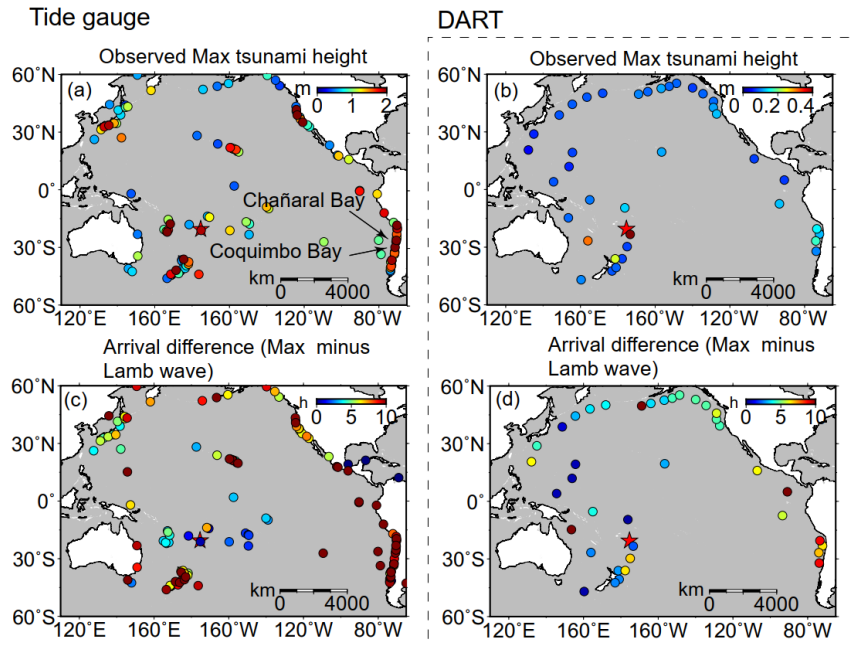
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 232 **Figure 4. The spatiotemporal signatures of the 2022 HTHH tsunami across the Pacific Ocean. (a)**  
 233 **Observed the maximum tsunami height (trough-to-crest height) of tide gauges. (c) Arrival**  
 234 **differences between the maximum tsunami height of tide gauges and Lamb waves. (b) and (d)**  
 235 **are the same as (a) and (c) but for DART buoys.**

### 236 3.3 Tsunami components identified from wavelet analysis

237 The statistical analysis of tsunami waveforms at tide gauges and DART buoys suggest the tsunami waves  
 238 likely contain several components with different source origins. To further identify these tsunami  
 239 components, we conduct wavelet analysis for tsunami waveforms recorded by representative DART  
 240 buoys and air pressure waveforms recorded by selected barometers. We demonstrate the analysis result  
 241 through the frequency-time (f-t) plot of wavelet which shows how energy and period vary at frequency  
 242 and time bands (Figure 5 and Figure 6). Tsunami components have clear signatures in all f-t plots as the  
 243 energy levels are quite large when they arrive. Figure 5 shows the wavelet analysis of six DART buoys  
 244 located in the vicinity of the eruption site (<3664 km). Figure 6 show the wavelet analysis of ten DART  
 245 buoys located in the Pacific rim which are far away from the source location. We observe three interesting  
 246 phenomena: 1) most of the tsunami wave energy is concentrated in four major period bands, i.e., 3-5  
 247 min, ~10-30 min, ~30-40 min, and ~80-100 min ~~80-100 min, 10-30 min, 30-40 min, and 3-5 min;~~ 2)

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248 The significant tsunami component with period band of 3-5 mins are recorded by stations between the  
249 eruption site and the north tip of the New Zealand. The stations with 3-5 mins wave periods are mainly  
250 located in the vicinity of the volcano site; 3) There exists one exceptional tsunami component with longer  
251 wave period of ~80-100 min, mainly recorded in the Tonga, the New Zealand and Hawaii, in the near  
252 source region which travels even faster than the Lamb waves.

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253 To further explore the source mechanism of these tsunami components, we take advantage of the  
254 published information related to different propagating velocities of atmospheric gravity waves (Kubota  
255 et al., 2022) and add four kinds of propagating velocities as criteria to differentiate the tsunami arrivals  
256 from different sources (Figure 5 and Figure 6). The first reference speed is 1000 m/s related to the  
257 radically propagating atmospheric shock waves near the source region (Matoza et al., 2022; Themens et  
258 al., 2022). The second one is the velocities of Lamb wave ranging between 315-340 m/s derived from  
259 the aforementioned analysis in section 3.1 (Figure 3). The third one is 200 m/s corresponding to the lower  
260 limit of atmospheric gravity wave modes other than Lamb waves which were also excited by the volcanic  
261 eruptions (Kubota et al., 2022). The last is the arrival time of conventional tsunami given by tsunami  
262 modelling (Figure 1). The theoretical velocity of conventional tsunami is significantly nonuniform  
263 spatially as compared with those of the atmospheric waves. The conventional tsunami propagation speed  
264 is determined by the water depth along the propagation route. The velocity of non-dispersion shallow-  
265 water waves ( $C_H$ ) in the ocean is given by:

$$266 \quad C_H = \sqrt{g \cdot H} \quad (3)$$

267 Where  $g$  is gravity acceleration ( $9.81 \text{ m/s}^2$ ),  $H$  is the water depth. The propagation velocities of tsunami  
268 are ~296-328 m/s in the deepest trenches on earth (i.e., ~11 km in Mariana Trench and ~9 km in Tonga  
269 Trench). The velocities decrease quickly to only ~44 m/s at ~200 m depth along the edge of continental  
270 shelf. With the average depth of ~4-5 km, the average velocities in the Pacific Ocean range between  
271 ~198-221 m/s. Thus, theoretical tsunami velocities present significant slowness and variability. We  
272 delineate the arrival times of the four reference speeds in Figures 5 and 6. For each panel of the figures,  
273 from left to right, the solid vertical white lines mark velocity of 1000 m/s. The solid vertical red lines  
274 mark the arrival of Lamb waves. The dashed vertical white lines mark lower limit of gravity waves'  
275 velocity of 200 m/s. The dashed vertical black lines represent the calculated theoretical tsunami arrivals.  
276 Horizontal white dashed lines mark two reference periods of 10 min and 30 min.

277 One particularly remarkable phenomenon is that the wave component with period of ~80–100 min  
278 propagated at a very fast speed of ~1000 m/s in the vicinity of the HTHH site, i.e., New Zealand and  
279 Hawaii (e.g., stations 52406, NZJ, NZE, 51425 in Figure 5, and 51407 in Fig. 6). We infer that the  
280 tsunami component within ~80–100 min period band was likely produced by the atmospheric shock  
281 waves during the initial stage of the volcanic eruption and spatially only cover the near-source region.  
282 To verify this observation, we select 16 representative barometers located in the near-source region and  
283 far-field area for wavelet analysis (see the locations in Figure 5 and Figure 6). Figure 7 shows the  
284 waveforms of atmospheric pressure at selected locations and Figure 8 provides the frequency-time (f-t)  
285 plot of wavelet analysis of some representative barometers. Interestingly, we are able to discern the air  
286 pressure pulses prior to Lamb waves at barometers in New Zealand (the two columns on the left in Figure  
287 7), although such signals are not detectable in waveforms recorded by barometers far from the source  
288 (the two columns on the right in Figure 7). The spatial distribution of such unusual pressure changes  
289 suggest that the fast travelling shock waves were only limited in the near-source region, as reflected in  
290 the travelling ionospheric disturbances (Matoza et al., 2022; Themens et al., 2022). Additionally, we also  
291 see that the long period signals of ~80–100 min appear in DART buoys far away from the eruption site.  
292 Such signals may be related with the long-period gravity waves (Matoza et al., 2022).

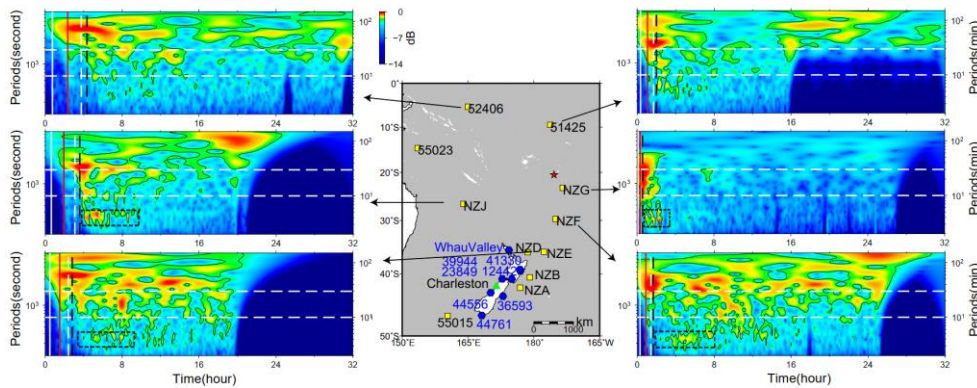
293 The tsunami components at period band of ~30–40 min can be readily associated with Lamb waves  
294 because the arrival times of tsunami waves and Lamb waves have excellent match, as shown in the  
295 tsunami data recorded by DART buoys (e.g., NZJ and 51425 in Figure 5; 51407, 32401 and 32413 in  
296 Figure 6) and pressure data by barometers (Figure 8).

297 For the tsunami components with the period band of ~10–30 min, although the arrivals of ~10–30 min  
298 tsunami components cover some theoretical tsunami arrival times, they do not consistently match. The  
299 tsunami components occurring within the time period between Lamb waves and the lower gravity waves'  
300 velocities has a good agreement with the velocity range of several atmospheric gravity wave modes  
301 (Matoza et al., 2022; Themens et al., 2022; Kubota et al., 2022). Similarly, the air pressure data also show  
302 energy peaks at ~10–30 min period band, which is consistent with the tsunami data (Figure 8). Such  
303 consistency further verifies the contribution of atmospheric gravity waves to the volcanic tsunami.

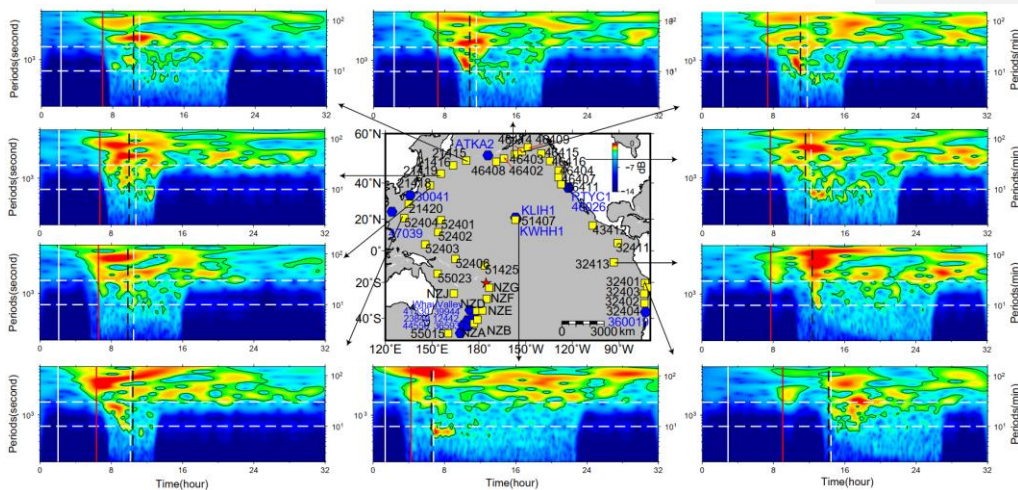
304 The tsunami components with the shortest period of ~3–5 min (stations NZE, NZF, NZG and NZJ;  
305 marked with black dashed squares in Figure 5) are only observed at DART records near the eruption

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306 location. Meanwhile, the arrival times of these components agree well with the modelled arrivals of  
 307 conventional tsunamis. Thus, we believe the observed shortest period band should originate from the  
 308 seafloor crustal deformation. We further infer that this component could be generated by the partial  
 309 underwater caldera collapse and/or subaerial/submarine landslide failures associated with 2022 HTHH  
 310 volcanic eruption.

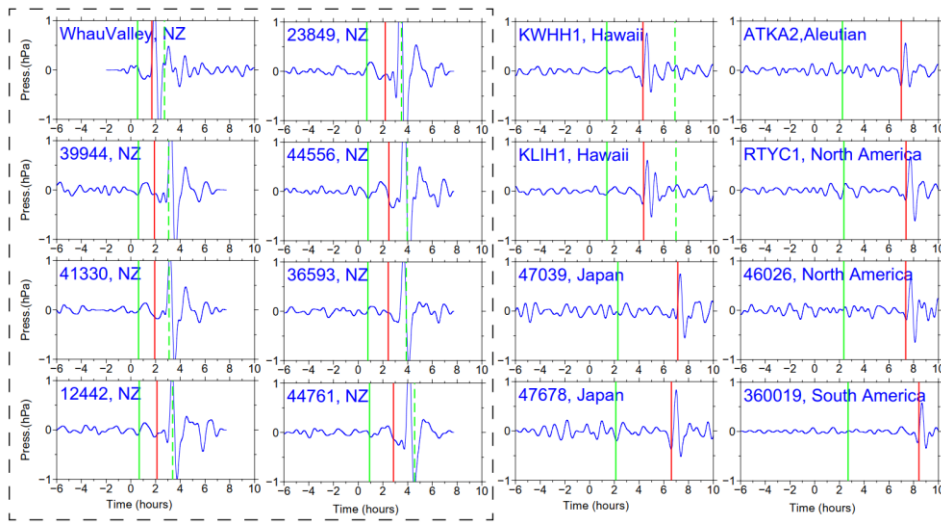


311  
 312 **Figure 5. Wavelet analysis of representative DART buoys in the vicinity of the HTHH volcano. In**  
 313 **each sub-plot, the solid vertical white lines mark the arrival time with travelling velocity of 1000**  
 314 **m/s. The solid vertical red lines mark the arrivals of Lamb waves. The dashed vertical white lines**  
 315 **mark lower limit of AGWs' velocity of 200 m/s (Kubota et al., 2022). The dashed vertical black**  
 316 **lines represent the theoretical tsunami arrivals. The dashed horizontal white lines mark two**  
 317 **reference wave periods of 10 min and 30 min. The blue hexagons represent the locations of**  
 318 **barometers. Green triangle makes the location of the tide gauges at Charleston.**

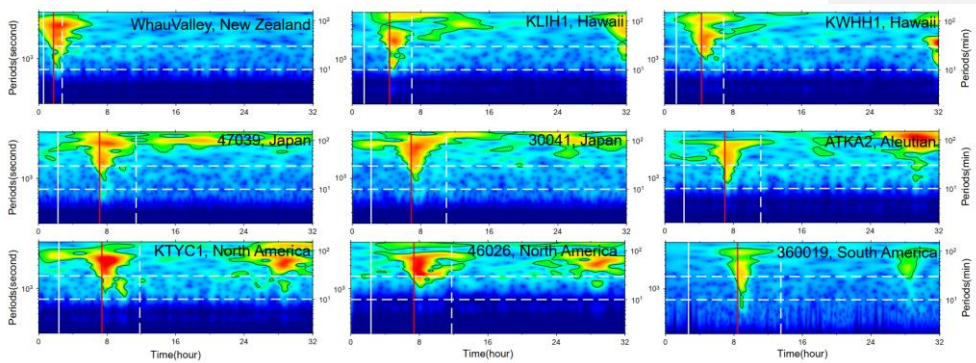


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320 **Figure 6. Wavelet analysis of representative DART buoys far away from the HTHH volcano. In**  
 321 **each sub-plot, the solid vertical white lines mark the arrival time with travelling velocity of 1000**  
 322 **m/s. The solid vertical red lines mark the arrivals of Lamb waves. The dashed vertical white lines**  
 323 **mark lower limit of AGWs' velocity of 200 m/s. The dashed vertical black lines represent the**  
 324 **theoretical tsunami arrivals. The dashed horizontal white lines mark two reference wave periods**  
 325 **of 10 min and 30 min. The blue hexagons represent the locations of barometers.**



326  
 327 **Figure 7. Shockwave-related atmospheric pressure waveforms of selected barometers in the Pacific**  
 328 **Ocean. All traces have been filtered between 30 min and 150 min. In each sub-plot, the solid vertical**  
 329 **green lines mark the arrival time with travelling velocity of 1000 m/s. The solid vertical red lines**  
 330 **mark the arrivals of Lamb waves. The dashed vertical green lines mark lower limit of AGWs'**  
 331 **velocity of 200 m/s.**



332  
 333 **Figure 8. Wavelet analysis of some representative barometers. In each sub-plot, the solid vertical**  
 334 **white lines mark the arrival time with travelling velocity of 1000 m/s. The solid vertical red lines**  
 335 **mark the arrivals of Lamb waves. The dashed vertical white lines mark lower limit of AGWs'**



336 velocity 200 m/s. The dashed horizontal white lines mark three reference periods of 10 min and 30  
337 min.

## 338 4. Discussion

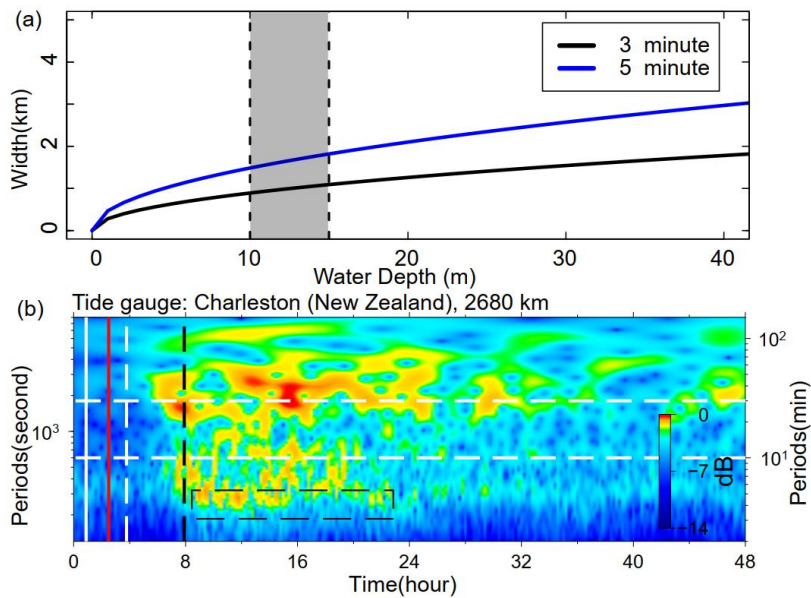
### 339 4.1 Tsunami from Caldera Collapse and Its Long-distance Traveling Capability

340 The tsunami wave energy distributed in different period bands is identified with reference arrival times.  
341 The tsunami component with 3–5 min period is most likely generated by seafloor crustal deformation in  
342 the volcanic site, but specific mechanism is not determined. A variety of possible scenarios associated  
343 with the eruption could be responsible for the near-field tsunami waves, such as volcanic earthquakes,  
344 pyroclastic flows entering the sea, underwater caldera flank collapse, and subaerial/submarine failures  
345 (Self and Rampino, 1981; Pelinovsky et al., 2005). To further investigate the source mechanism, we  
346 apply a simplified model (Rabinovich, 1997) to estimate the probable dimension of tsunami source:

$$347 L = \frac{T\sqrt{gH}}{2} \quad (4)$$

348 Where  $L$  is the typical dimension (length or width) of the tsunami source,  $H$  is average water depth in the  
349 source area,  $g$  is the gravity acceleration, and  $T$  is primary tsunami period. By comparing with the post-  
350 2015 morphology of the HTHH caldera which was obtained through drone photogrammetry and  
351 multibeam sounder surveys, Stern et al. (2022) estimate that much of the newly-formed Hunga Tonga  
352 Island and the 2014/2015 cone were destroyed by the 2022 eruption, and the vertical deformation of  
353 Hunga Ha'apai Island is ~10–15 m (Stern et al., 2022). With no more quantitative constraint of the  
354 seafloor deformation, we tentatively assume  $H$  as 10–15 m, then the possible dimension of seafloor  
355 crustal deformation responsible for the small-scale tsunami could be in the scale of 0.8–1.8 km (Figure  
356 9a). The estimated size is very likely from partial caldera collapse that usually has limited scale in  
357 volcanic site (Ramalho et al., 2015; Omira et al., 2022). If it is the case, the partial flank collapse could  
358 be located between Hunga Tonga and Hunga Ha'apai Islands.

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359

360 **Figure 9. Mechanism of tsunami component with 3–5min period. (a) The source dimension**  
 361 **estimated by equation 4. (b) Wavelet analysis of tide gauge at Charleston, New Zealand, 2680 km**  
 362 **away from the eruption site. The solid vertical white line marks the arrival time with travelling**  
 363 **velocity of 1000 m/s. The solid vertical red line marks the arrival of Lamb wave. The dashed**  
 364 **vertical white line marks lower limit of AGWs' velocity 200 m/s. The dashed vertical black line**  
 365 **marks the theoretical tsunami arrivals.**

366 An interesting phenomenon is that the tsunami component with 3–5 min period can still be observed in  
 367 a bay-shaped coastal area at Charleston in New Zealand (see the location in Figure 5) which is 2680 km  
 368 away from the eruption site and maintains a high energy level lasting up to 14 h (Figure 9b). The long-  
 369 traveling capability could be associated with the  $\sim 10000$  m deep water depth of the Tonga Trench that  
 370 keeps the source signals from substantial attenuation. In deep open ocean, the wavelength of a tsunami  
 371 can reach two hundred kilometers, but the height of the tsunami may be only a few centimeters. Tsunami  
 372 waves in the deep ocean can travel thousands of kilometers at high speeds, meanwhile losing very little  
 373 energy in the process. The long oscillation can be attributed to the multiple reflections of the incoming  
 374 waves trapped in the shallow-water bay at Charleston.

375 Generally, devastating tsunamis with long-distance travelling capability are mostly generated by  
 376 megathrust earthquakes (Titov et al., 2005). Caldera collapses or submarine landslides with limited scale  
 377 normally only generate local tsunamis, e.g., the 1998 PNG (Papua New Guinea) tsunami event (Kawata

378 et al., 1999) and the 1930 Cabo Girão tsunami event (Ramalho et al., 2015). Therefore, it's exceptional  
379 that the tsunami component from scale-limited failure could travel at-least 2680 km away from the  
380 eruption site. It demonstrates that tsunamis from small-scale tsunamigenic source have the capability to  
381 travel long distance and cause long oscillation at favored condition, e.g., deep trench, ocean ridge and  
382 bay-shaped coasts.

#### 383 4.2 The Possible Mechanisms of Long Tsunami Oscillation

384 An important tsunami behavior of the 2022 HTHH tsunami is the long-lasting oscillation ~ 3 days in the  
385 Pacific Ocean (Figure 10a), which is comparable to that of the 2011 Tohoku tsunami, ~4 days  
386 (Heidarzadeh and Satake, 2013). We demonstrate the duration time of the tsunami oscillation through  
387 ARMS (Averaged-Root-Mean-Square) approach that is a measure of absolute average tsunami amplitude  
388 in a time period. The long-lasting tsunami energy can be observed at many regions, such as the coasts of  
389 New Zealand, Japan, Aleutian, Chile, Hawaii, and west coasts of America. Several mechanisms could  
390 account for the long-lasting tsunami, including (1) Lamb waves circling the Earth multiple times  
391 (Amores et al., 2022; Matoza et al., 2022), (2) resonance effect between ocean waves and atmospheric  
392 waves (Kubota et al., 2022), and (3) bathymetric effect. We discuss the contribution of each mechanism  
393 in the following section.

394 To investigate the contribution of Lamb wave to the long-lasting tsunami, we compare the air pressure  
395 disturbances recorded by selected barometers together with the tsunami waveforms of nearby tide gauges  
396 (Figure 10b). While the barometers present discernible wave pulses at each Lamb wave's arrival, only  
397 the first Lamb wave triggered clear tsunami signal and no detectable tsunami signatures correspond to  
398 the following passage, suggesting the Lamb waves do not directly contribute to the long oscillation.

399 Theoretically, the resonance effects between ocean waves and atmospheric waves could contribute to the  
400 long oscillation on coastlines based on the following reasons. First, part of the atmospheric gravity waves  
401 propagated at velocities close to averaged velocities of conventional tsunami in the Pacific Ocean (198–  
402 221 m/s) which resulted in the resonance with ocean waves (Kubota et al., 2022). Second, when Lamb  
403 wave speed approaches the tsunami speed, Proudman resonance gradually increase tsunami heights,  
404 wherein Proudman resonance optimally maximizes tsunami heights when they match well. In deep  
405 oceanic trenches, such as Mariana and Tonga-Kermadec trench (10000–11000 m), tsunami velocities  
406 range between ~314–330m/s which are comparable with those of the observed Lamb waves 315–340

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407 ~~m/s. Second, in deep oceanic trenches, such as Mariana and Tonga-Kermadec trench (10000–11000 m),~~  
408 ~~tsunami velocities range between ~314–330 m/s which are comparable with those of the observed Lamb~~  
409 ~~waves 315–340 m/s. When Lamb wave speed approaches the tsunami speed, Proudman resonance~~  
410 ~~gradually increase tsunami heights, wherein Proudman resonance optimally maximizes tsunami heights~~  
411 ~~when they match well (Tanioka et al., 2022; Lynett et al., 2022). Therefore, the resonance effect could~~  
412 ~~be a possible source of increased wave energy continuously supplied wave energy to the ocean, especially~~  
413 ~~in the deep trenches (Lynett et al., 2022; Tanioka et al., 2022).:-~~

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414 To examine the role of local bathymetry in the long-lasting tsunami, we choose a well-studied and well-  
415 recorded event: the 2011 Mw 9.0 Tohoku tsunami as a reference event and compare the tsunami records  
416 of these two events at the same coastal stations. Although the two tsunami events were generated by  
417 completely different mechanisms, i.e., large-scale seafloor deformation for the Mw 9.0 megathrust  
418 earthquake (Mori et al., 2011) and fast-moving atmospheric waves for the Mw 5.8 volcanic eruption  
419 (Matoza et al., 2022) (Titov et al., 2005), they both produced widespread transoceanic tsunamis which

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420 were well recorded in the Pacific DART buoys and tide gauges. In the near-field, the 2011 Tohoku  
421 earthquake produced runup up to 40 m at Miyako in the Iwate Prefecture, ~70 km from the source (Mori  
422 et al., 2011) (Tanioka et al., 2022), while the 2022 HTHH tsunami produced only ~13 m runup in the  
423 near field from eyewitness accounts in Kanokupolu, 60 km from the volcano (Lynett et al., 2022).  
424 However, in the far-field (>1000 km), we observe comparable tsunami wave heights in certain coastal  
425 regions. Based on the tsunami records at 21 tide gauges surrounding the Pacific Ocean, Heidarzadeh &  
426 Satake (2013) calculated the average value of the maximum tsunami heights (trough-to-crest) of the 2011  
427 Tohoku tsunami is 1.6 m with the largest height of 3.9 m at the Coquimbo Bay in Chile (Heidarzadeh  
428 and Satake, 2013). Coincidentally, the statistics of 116 tide gauges in this study also suggest the average  
429 tsunami heights of the 2022 HTHH tsunami is around the same order, ~1.2 m, among which, the largest  
430 height is 3.6 m at Chañaral Bay in Chile. Interestingly, in the coastal region of South America, the  
431 locations of the largest tsunami heights of both events are adjacent (Figure 4a), i.e., Coquimbo (the 2011  
432 Tohoku) and Chañaral (The 2022 HTHH).

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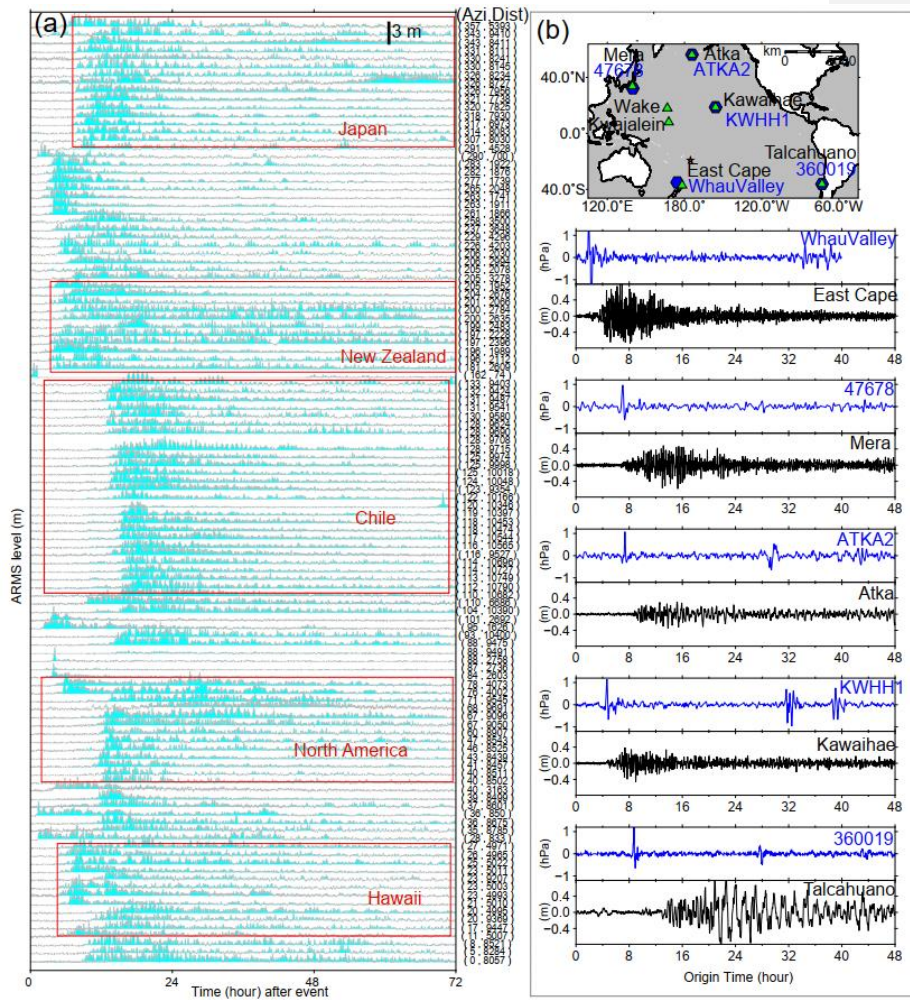
433 To further compare the far-field hydrodynamic processes between these two events quantitatively, we  
434 conduct wavelet analysis for four representative tide gauges distributed across the Pacific Ocean, i.e.  
435 coastal gauges at East Cape in New Zealand, Kwajalein Island, Wake Island, and Talcahuano in Chile

436 (see their locations in Figures 10b). The temporal changes of tsunami energy of both events can be seen  
437 in Figure 11. At each tide gauge, the tsunami energy of the 2011 HTHH (Figure 11a) and the 2022 Tohoku  
438 tsunamis (Figure 11b) for the first few hours after the arrivals is nonuniform with different significant  
439 peaks distributed within a wide period band of ~3–100 min. Then, the following long-lasting energy of  
440 the both at each station presents similar pattern and is concentrated at identical and fairly narrower period  
441 channel, i.e., ~20–30 min at East Cape in New Zealand, ~40–60 min at Kwajalein Island, ~10 min at  
442 Wake Island, and ~100 min at Talcahuaho in Chile, which reflects the local bathymetric effects of natural  
443 permanent oscillations (Hu et al., 2022; Satake et al., 2020). Specifically, many bathymetric effects can  
444 contribute to the long-lasting tsunami, such as multiple reflections across the basins, or the continental  
445 shelves, and the excited tsunami resonance in bays/harbors with variable shapes and sizes (Aranguiz et  
446 al., 2019; Satake et al., 2020). For example, tide gauges around New Zealand are primarily distributed in  
447 harbors/ports with major natural oscillation modes of ~20–30 min (De Lange and Healy, 1986; Lynett et  
448 al., 2022). The first oscillation mode of central Chile is centered around ~100 min (Aranguiz et al., 2019).  
449 Consequently, Figure 11 illustrates that the long-lasting tsunami energy of the two events is respectively  
450 distributed in 20–30 min period at East Cape in New Zealand and in ~100 min period at Talcahuaho in  
451 central Chile. The coupling of bathymetric oscillation mode with tsunami containing similar-period wave  
452 results in the excitement of tsunami resonance, which amplifies tsunami waves and prolongs the tsunami  
453 oscillation at the two stations (Heidarzadeh et al., 2019, 2021; Hu et al., 2022; Wang et al., 2022).

454 Simply put, ~~we do not have clear evidence that atmospheric acoustic-gravity waves from the 2022 HTHH~~  
455 ~~eruption directly contribute to the long-lasting tsunami, but the resonance effect associated with ocean~~  
456 ~~waves could a possible source of increased wave energy and amplification~~ ~~atmospheric acoustic gravity~~  
457 ~~waves from the 2022 HTHH eruption do not directly contribute to the long-lasting tsunami, but the~~  
458 ~~resonance effect associated with ocean waves theoretically could contribute to it.~~ However, the similarity  
459 of far-field hydrodynamic behaviors between the 2022 HTHH volcanic tsunami and the 2011 Tohoku  
460 seismogenic tsunami well demonstrates the both went through similar hydrodynamic processes after their  
461 arrivals. The consistency favors that the long-lasting tsunami of 2022 HTHH tsunami event can very  
462 likely be attributed by the interplays between local bathymetry and conventional tsunami left after each  
463 passage of atmospheric waves, which can well explain why the two completely distinct tsunami events  
464 possess a comparable duration time.

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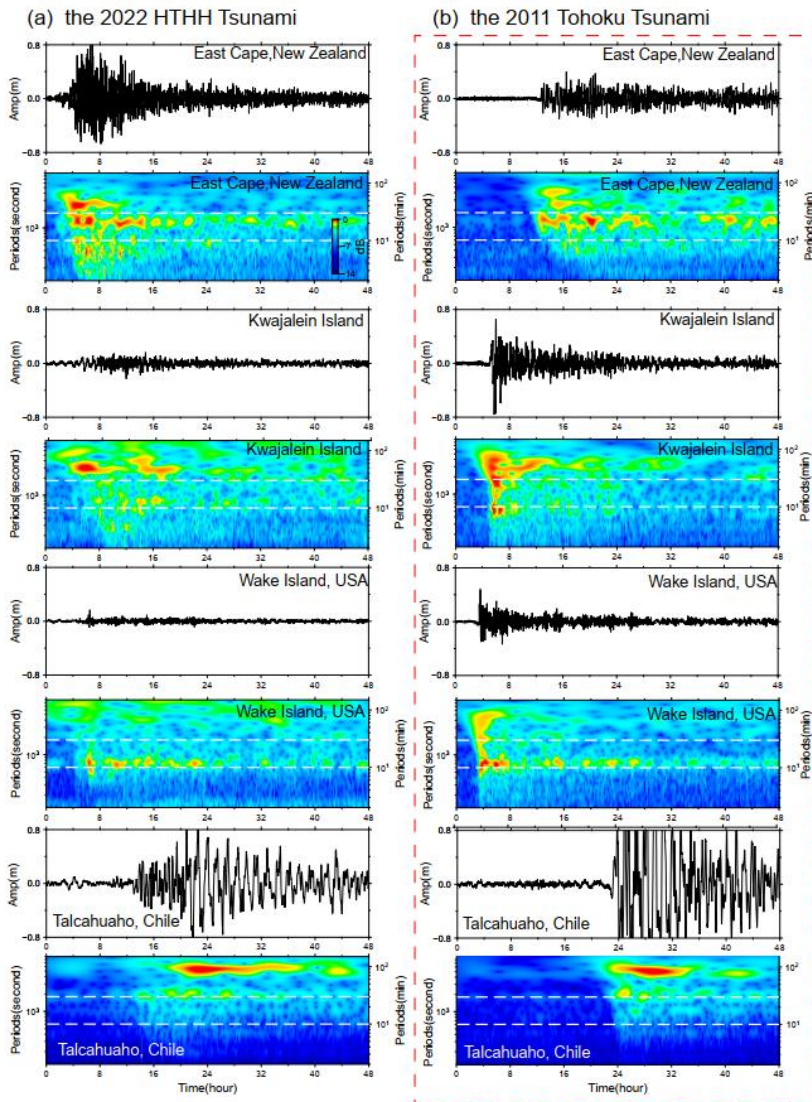
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465

466 **Figure 10. Tsunami duration. (a) Tsunami durations at Pacific 116 tide gauges through ARMS level**  
 467 **approach. (b) the location of barographs (blue curves) and nearby tide gauges (green curves), as**  
 468 **well as their waveforms.**

469



470  
 471 **Figure 11. Wavelet analysis of tsunami waveforms recorded by 4 tide gauges during (a) the 2022**  
 472 **HTHH tsunami event, and (b) the 2011 Tohoku tsunami event. Horizontal white dashed lines**  
 473 **respectively mark reference periods of 10 min and 30 min.**

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474 **4.3 Challenges for Tsunami Warning**

475 The generation mechanisms and hydrodynamic characteristics of the 2022 HTHH volcanic tsunami are  
 476 more complicated than pure seismogenic tsunami, which challenge the traditional tsunami warning

477 approach.

478 The first challenge is posed by the tsunami components with propagating velocities faster than the  
479 conventional tsunami. The Tonga volcanic tsunami event provides an excellent example which highlights  
480 that the tsunamigenic mechanisms are not limited to tectonic activities related with the sudden seafloor  
481 displacements, but also include a variety of atmospheric waves with distinct propagation velocities. The  
482 tsunami components in 2022 HTHH event generated by the air-sea coupling possess a wide range of  
483 velocities from 1000 m/s to 200 m/s. The Lamb waves recorded in both the 2022 HTHH event and the  
484 1833 Krakatoa volcanic event traveled along the Earth's surface globally for several times (Carvajal et  
485 al., 2022). The tsunami waves produced by Lamb waves, the wave components associated with resonance  
486 of the air-sea coupling and their superimposition increase the difficulty of tsunami warning.

487 Another critical challenge is associated with the interplays between tsunami waves and local bathymetry.  
488 The tsunami waves left by each passage of the atmospheric waves can interact with local bathymetry at  
489 coastlines, such as continental shelves with different slopes, and harbor/bay with different shapes and  
490 sizes. The interaction can intensify the tsunami impact and excite a variety of natural oscillation periods.  
491 The 2022 HTHH tsunami with an extremely wide period range of ~2–100 min have a great potential to  
492 couple with the excited natural oscillations and form extensive tsunami resonance phenomena. The  
493 resonance effects result in long-lasting oscillation and delayed tsunami wave peaks. The uncertain  
494 arrivals of the maximum tsunami waves pose an extra challenge to tsunami warning.

#### 4955. **Conclusion**

496 In the study, we explore the tsunamigenic mechanisms and the hydrodynamic characteristics of the 2022  
497 HTHH volcanic tsunami event. Through extensive analysis of waveforms recorded by the DART buoys,  
498 tide gauges and barometers in the Pacific Ocean, we reach the main findings as follows:

499 (1) We identify four distinct tsunami wave components based on their distinct propagation velocities or  
500 period bands (~80–100 min, 10–30 min, 30–40 min, and 3–5 min). The generation mechanisms of these  
501 tsunami components range from air-sea coupling to seafloor crustal deformation during the volcanic  
502 eruption.

503 (2) The first-arriving tsunami component with 80–100 min period was most likely from shock wave  
504 spreading at a velocity of ~1000 m/s in the vicinity of the eruption. This tsunami component was not



505 clearly identified by currently available publication and it's not easy to be visually observed through time  
506 series of the waveforms. The physical mechanism is yet to be understood. The second tsunami component  
507 with 30–40 min period was from Lamb waves, and was the most discussed tsunami source of this event  
508 so far. A thorough analysis of DART measurements indicates that the Lamb waves traveled at the speed  
509 of ~340 m/s in the vicinity of the eruption and decreased to ~315 m/s when traveling away due to cooling  
510 of the air temperature. The third tsunami component was from some atmospheric gravity wave modes  
511 with propagation velocity faster than 200 m/s but slower than Lamb waves. The last tsunami component  
512 with the shortest periods 3-5 min was probably produced by partial caldera collapse with estimated  
513 dimension of ~0.8–1.8 km.

514 (3) ~~Although the resonance effect with the atmospheric acoustic-gravity waves theoretically could be a~~  
515 ~~source of increased wave energy, its direct contribution to the long-lasting oscillation is not demonstrated~~  
516 ~~yet. However, the comparison of hydrodynamical characteristics between the 2022 HTHH tsunami event~~  
517 ~~and the 2011 Tohoku tsunami event well demonstrated that the interactions between the ocean waves left~~  
518 ~~by atmospheric waves and local bathymetry contribute to the long-lasting Pacific oscillation of the 2022~~  
519 ~~tsunami event. The long-lasting Pacific oscillation of this tsunami event was not only associated with the~~  
520 ~~resonance effect with the atmospheric acoustic gravity waves, but more importantly the interactions with~~  
521 ~~local bathymetry. The velocities of tsunami waves in deep ocean (especially at Mariana and Tonga-~~  
522 ~~Kermadec trenches) close to those of acoustic Lamb waves and some gravity wave modes produced~~  
523 ~~resonance effects, which supplied energy to the ocean. The comparison of hydrodynamical characteristics~~  
524 ~~between the 2022 HTHH tsunami event and the 2011 Tohoku tsunami event suggests the volcanic~~  
525 ~~tsunami oscillation was prolonged by their interplays with local bathymetry.~~

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526 (4) The extraordinary features of this rare volcanic tsunami event challenge the current tsunami warning  
527 system which is mainly designed for seismogenic tsunamis. It is necessary to improve the awareness of  
528 people at risks about the potential tsunami hazards associated with volcanic eruptions. New approaches  
529 are expected to be developed for tsunami hazard assessments with these unusual sources: various  
530 atmospheric waves radiated by volcanic eruptions besides those traditionally recognized, e.g.  
531 earthquakes, landslides, caldera collapses and pyroclastic flows etc.

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538 The JAGURS tsunami simulation code is employed for tsunami modelling (Baba et al., 2015;  
539 <https://zenodo.org/record/6118212#.Yk98qdtBxPY>). Bathymetry data are obtained from GEBCO at  
540 <http://www.gebco.net>. The sea level records in deep ocean are available from the Deep Ocean Assessment  
541 and Reporting of Tsunamis (DART) buoy network in the Pacific (<https://nctr.pmel.noaa.gov/Dart/>), and  
542 GeoNet New Zealand DART network (<https://tilde.geonet.org.nz>). The sea level records of tide gauges  
543 are downloaded from UNESCO/ IOC (<http://www.ioc-sealevelmonitoring.org/>). Barometer data are  
544 provided by the following providers: Direcció'n Meteorol'gica de Chile  
545 (<https://climatologia.meteochile.gob.cl>), NOAA National Weather Service  
546 (<https://www.weather.gov/ilm/observations>), Japan Meteorological Agency (<https://www.jma.go.jp>),  
547 The UK Met Office Weather Observation (<https://www.metoffice.gov.uk/observations>), and Fiji  
548 Meteorological Service (<https://www.met.gov.fj>).

549 **Reference**

550 Adam, D.: Tonga volcano created puzzling atmospheric ripples, Nature,  
551 <https://doi.org/10.1038/d41586-022-00127-1>, 2022.  
552 Amores, A., Monserrat, S., Marcos, M., Argüeso, D., Villalonga, J., Jordà, G., and Gomis, D.:  
553 Numerical simulation of atmospheric Lamb waves generated by the 2022 Hunga-Tonga volcanic  
554 eruption, Geophys. Res. Lett., 49, e2022GL098240, <https://doi.org/10.1029/2022GL098240>, 2022.  
555 Aranguiz, R., Catalán, P. A., Cecioni, C., Bellotti, G., Henriquez, P., and González, J.: Tsunami  
556 Resonance and Spatial Pattern of Natural Oscillation Modes With Multiple Resonators, J. Geophys.  
557 Res. Ocean., 124, 7797–7816, <https://doi.org/10.1029/2019JC015206>, 2019.  
558 Baba, T., Takahashi, N., Kaneda, Y., Ando, K., Matsuoka, D., and Kato, T.: Parallel Implementation of  
559 Dispersive Tsunami Wave Modeling with a Nesting Algorithm for the 2011 Tohoku Tsunami, Pure

560 Appl. Geophys., 172, 3455–3472, <https://doi.org/10.1007/s00024-015-1049-2>, 2015.

561 Bevis, M., Taylor, F. W., Schutz, B. E., Recy, J., Isacks, B. L., Helu, S., Singh, R., Kendrick, E.,  
562 Stowell, J., Taylor, B., and Calmantli, S.: Geodetic observations of very rapid convergence and back-  
563 arc extension at the tonga arc, *Nature*, 374, 249–251, <https://doi.org/10.1038/374249a0>, 1995.

564 Billen, M. I., Gurnis, M., and Simons, M.: Multiscale dynamics of the Tonga–Kermadec subduction  
565 zone, *Geophys. J. Int.*, 153, 359–388, <https://doi.org/10.1046/j.1365-246X.2003.01915.x>, 2003, 2003.

566 Carvajal, M., Sepúlveda, I., Gubler, A., and Garreaud, R.: Worldwide Signature of the 2022 Tonga  
567 Volcanic Tsunami, *Geophys. Res. Lett.*, 49, e2022GL098153, <https://doi.org/10.1029/2022GL098153>,  
568 2022.

569 Duncombe, J.: The Surprising Reach of Tonga’s Giant Atmospheric Waves.pdf, *Eos (Washington*  
570 *DC)*, 103, <https://doi.org/10.1029/2022EO220050>, 2022.

571 E. E. Gossard and W. H. Hooke: *Waves in the Atmosphere: Atmospheric Infrasound and Gravity*  
572 *Waves—Their Generation and Propagation*, Elsevier, 1975.

573 Edmonds, M.: Hunga-Tonga-Hunga-Ha’apai in the south Pacific erupts violently, *Temblo*,  
574 <https://doi.org/10.32858/temblor.231>, 2022.

575 Garvin, J. B., Slayback, D. A., Ferrini, V., Frawley, J., Giguere, C., Asrar, G. R., and Andersen, K.:  
576 Monitoring and Modeling the Rapid Evolution of Earth’s Newest Volcanic Island: Hunga Tonga  
577 Hunga Ha’apai (Tonga) Using High Spatial Resolution Satellite Observations, *Geophys. Res. Lett.*, 45,  
578 3445–3452, <https://doi.org/10.1002/2017GL076621>, 2018.

579 Gossard, E. E. and Hooke, W. H.: *Waves in the Atmosphere*, Amsterdam: Elsevier, 1975.

580 Heidarzadeh, M. and Satake, K.: Waveform and Spectral Analyses of the 2011 Japan Tsunami Records  
581 on Tide Gauge and DART Stations Across the Pacific Ocean, *Pure Appl. Geophys.*, 170, 1275–1293,  
582 <https://doi.org/10.1007/s00024-012-0558-5>, 2013.

583 Heidarzadeh, M. and Satake, K.: Excitation of Basin-Wide Modes of the Pacific Ocean Following the  
584 March 2011 Tohoku Tsunami, *Pure Appl. Geophys.*, 171, 3405–3419, [https://doi.org/10.1007/s00024-](https://doi.org/10.1007/s00024-013-0731-5)  
585 [013-0731-5](https://doi.org/10.1007/s00024-013-0731-5), 2014.

586 Hu, G., Feng, W., Wang, Y., Li, L., He, X., Karakaş, Ç., and Tian, Y.: Source characteristics and  
587 exacerbated tsunami hazard of the 2020 Mw 6.9 Samos earthquake in eastern Aegean Sea, *J. Geophys.*  
588 *Res. Solid Earth*, 127, e2022JB023961, <https://doi.org/10.1029/2022JB023961>, 2022.

589 Kawata, Y., Benson, B. C., Borrero, J. C., Borrero, J. L., Davies, H. L., Lange, W. P. de, Imamura, F.,  
590 Letz, H., Nott, J., and Synolakis, C. E.: Tsunami in Papua New Guinea Was as Intense as First  
591 Thought, *Eos, Trans. Am. Geophys. Union*, 80, 9, <https://doi.org/10.1029/99EO00065>, 1999.

592 Kristeková, M., Kristek, J., Moczo, P., and Day, S. M.: Misfit Criteria for Quantitative Comparison of  
593 Seismograms, *Bull. Seismol. Soc. Am.*, 96, 1836–1850, <https://doi.org/10.1785/0120060012>, 2006.

594 Kubota, T., Saito, T., and Nishida, K.: Global fast-traveling tsunamis by atmospheric pressure waves  
595 on the 2022 Tonga eruption, *Science* (80-. ), <https://doi.org/10.1126/science.abo4364>, 2022.

596 Kulichkov, S. N., Chunchuzov, I. P., Popov, O. E., Gorchakov, G. I., Mishenin, A. A., Perepelkin, V.  
597 G., Bush, G. A., Skorokhod, A. I., Yu. A. Vinogradov, Semutnikova, E. G., Šepic, J., Medvedev, I. P.,  
598 Gushchin, R. A., Kopeikin, V. M., Belikov, I. B., Gubanova, D. P., and A. V. Karpov & A. V.  
599 Tikhonov: Acoustic-Gravity Lamb Waves from the Eruption of the Hunga-Tonga-Hunga-Hapai  
600 Volcano, Its Energy Release and Impact on Aerosol Concentrations and Tsunami, *Pure Appl.*  
601 *Geophys.*, <https://doi.org/10.1007/s00024-022-03046-4>, 2022.

602 De Lange, W. P. and Healy, T. R.: New Zealand tsunamis 1840–1982, *New Zeal. J. Geol. Geophys.*,  
603 29, 115–134, <https://doi.org/10.1080/00288306.1986.10427527>, 1986.

604 Lin, J., Rajesh, P. K., Lin, C. C. H., Chou, M., Liu, J.-Y., Yue, J., Hsiao, T.-Y., Tsai, H.-F., Chao, H.-  
605 M., and Kung, M.-M.: Rapid Conjugate Appearance of the Giant Ionospheric Lamb Wave Signatures  
606 in the Northern Hemisphere After Hunga- Tonga Volcano Eruptions, *Geophys. Res. Lett.*, 49,  
607 e2022GL098222, <https://doi.org/10.1029/2022GL098222>, 2022.

608 Liu, P. L.-F. and Higuera, P.: Water waves generated by moving atmospheric pressure : Theoretical  
609 analyses with applications to the 2022 Tonga event, *arXiv Prepr.*,  
610 <https://doi.org/10.48550/arXiv.2205.05856>, 2022.

611 Liu, X., Xu, J., Yue, J., and Kogure, M.: Strong Gravity Waves Associated With Tonga Volcano  
612 Eruption Revealed by SABER Observations, *Geophys. Res. Lett.*, 49, e2022GL098339,  
613 <https://doi.org/10.1029/2022GL098339>, 2022.

614 Lynett, P., McCann, M., Zhou, Z., Renteria, W., Borrero, J., Greer, D., Fa’anunu, ‘Ofa, Bosserelle, C.,  
615 Jaffe, B., Selle, S. La, Ritchie, A., Snyder, A., Nasr, B., Bott, J., Graehl, N., Synolakis, C., Ebrahimi,  
616 B., and Cinar, E.: The Tsunamis Generated by the Hunga Tonga- Hunga Ha ’ apai Volcano on January  
617 15 , 2022, *ResearchSquare*, <https://doi.org/10.21203/rs.3.rs-1377508/v1>, 2022.

618 Matoza, R. S., Matoza, R. S., Fee, D., Assink, J. D., Iezzi, A. M., Green, D. N., Kim, K., Lecocq, T.,  
619 Krishnamoorthy, S., Lalande, J., Nishida, K., and Gee, K. L.: Atmospheric waves and global  
620 seismoacoustic observations of the January 2022 Hunga eruption ,Tonga, *Science* (80-. ),  
621 <https://doi.org/10.1126/science.abo7063>, 2022.

622 Mori, N., Takahashi, T., Yasuda, T., and Yanagisawa, H.: Survey of 2011 Tohoku earthquake tsunami  
623 inundation and run-up, *Geophys. Res. Lett.*, 38, L00G14, <https://doi.org/10.1029/2011GL049210>,  
624 2011.

625 NASA: National Aeronautics and Space Administration,“Dramatic changes at Hunga Tonga-Hunga  
626 Ha’apai,” 2022.

627 Nomanbhoy, N. and Satake, K.: Generation mechanism of tsunamis from the 1883 Krakatau Eruption,  
628 *Geophys. Res. Lett.*, 22, 509–512, <https://doi.org/10.1029/94GL03219>, 1995.

629 Omira, R., Baptista, M. A., Quartau, R., Ramalho, R. S., Kim, J., Ramalho, I., and Rodrigues, A.: How  
630 hazardous are tsunamis triggered by small-scale mass-wasting events on volcanic islands ? New  
631 insights from Madeira–NE Atlantic, *Earth Planet. Sci. Lett.*, 578, 117333,  
632 <https://doi.org/10.1016/j.epsl.2021.117333>, 2022.

633 Otsuka, S.: Visualizing Lamb Waves From a Volcanic Eruption Using Meteorological Satellite  
634 Himawari-8, *Geophys. Res. Lett.*, 49, e2022GL098324, <https://doi.org/10.1029/2022GL098324>, 2022.

635 Pelinovsky, E., Choi, B. H., Stromkov, A., Didenkulova, I., and Kim, H.: Analysis of Tide-Gauge  
636 Records of the 1883 Krakatau Tsunami. In: Satake, K. (eds) *Tsunamis, Adv. Nat. Technol. Hazards*  
637 *Res.*, 23, Springer, Dordrech, [https://doi.org/10.1007/1-4020-3331-1\\_4](https://doi.org/10.1007/1-4020-3331-1_4), 2005.

638 Plank, S., Marchese, F., Genzano, N., Nolde, M., and Martinis, S.: The short life of the volcanic island  
639 New Late’iki (Tonga) analyzed by multi-sensor remote sensing data, *Sci. Rep.*, 10, 22293,  
640 <https://doi.org/10.1038/s41598-020-79261-7>, 2020.

641 Rabinovich, A. B.: Spectral analysis of tsunami waves: Separation of source and topography effects, *J.*  
642 *Geophys. Res. Ocean.*, 102, 12663–12676, <https://doi.org/10.1029/97JC00479>, 1997.

643 Rabinovich, A. B.: Seiches and harbor oscillations. in: *Handbook of coastal and ocean engineering*, pp.  
644 193–236, 2009.

645 Rabinovich, A. B., Thomson, Æ. R. E., and Stephenson, F. E.: The Sumatra tsunami of 26 December  
646 2004 as observed in the North Pacific and North Atlantic oceans, *Surv. Geophys.*, 27, 647–677,

647 <https://doi.org/10.1007/s10712-006-9000-9>, 2006.

648 Rabinovich, A. B., Titov, V. V., Moore, C. W., and Eble, M. C.: The 2004 Sumatra Tsunami in the  
649 Southeastern Pacific Ocean: New Global Insight From Observations and Modeling, *J. Geophys. Res.*  
650 *Ocean.*, 122, 7992–8019, <https://doi.org/https://doi.org/10.1002/2017JC013078>, 2017.

651 Ramalho, R. S., Winckler, G., Madeira, J., Helffrich, G. R., Hipólito, A., Quartau, R., Adena, K., and  
652 Schaefer, J. M.: Hazard potential of volcanic flank collapses raised by new megatsunami evidence, *Sci.*  
653 *Adv.*, 1, e1500456, <https://doi.org/10.1126/sciadv.1500456>, 2015.

654 Ramírez-Herrera, M. T., Coca, O., and Vargas-Espinosa, V.: Tsunami Effects on the Coast of Mexico  
655 by the Hunga Tonga-Hunga Ha’apai Volcano, *Pure Appl. Geophys.*, [https://doi.org/10.1007/s00024-](https://doi.org/10.1007/s00024-022-03017-9)  
656 [022-03017-9](https://doi.org/10.1007/s00024-022-03017-9), 2022.

657 Satake, K.: Earthquakes: Double trouble at Tonga, *Nature*, 466, 931–932,  
658 <https://doi.org/10.1038/466931a>, 2010.

659 Satake, K., Heidarzadeh, M., Quiroz, M., and Cienfuegos, R.: History and features of trans-oceanic  
660 tsunamis and implications for paleo-tsunami studies, *Earth-Science Rev.*, 202, 103112,  
661 <https://doi.org/10.1016/j.earscirev.2020.103112>, 2020.

662 Self, S. and Rampino, M. R.: K-1981Self\_Nature\_The 1883 eruption of Krakatau, *Nature*, 294, 699–  
663 704, <https://doi.org/10.1038/294699a0>, 1981.

664 Stern, S., Cronin, S., Ribo, M., Barker, S., Brenna, M., Smith, I. E. M., Ford, M., Kula, T., and  
665 Vaiomounga, R.: Post-2015 caldera morphology of the Hunga Tonga-Hunga Ha ’apai caldera ,  
666 Tonga , through drone photogrammetry and summit area bathymetry, *EGU Gen. Assem.* 2022,  
667 <https://doi.org/10.5194/egusphere-egu22-13586>, 2022.

668 Tanioka, Y., Yamanaka, Y., and Nakagaki, T.: Characteristics of the deep sea tsunami excited offshore  
669 Japan due to the air wave from the 2022 Tonga eruption, *Earth, Planets Sp.*, 74, 61,  
670 <https://doi.org/10.1186/s40623-022-01614-5>, 2022.

671 Themens, D. R., Watson, C., Žagar, N., Vasylykevych, S., Elvidge, S., McCaffrey, A., Prikryl, P., Reid,  
672 B., Wood, A., and Jayachandran, P. T.: Global Propagation of Ionospheric Disturbances Associated  
673 With the 2022 Tonga Volcanic Eruption, *Geophys. Res. Lett.*, 49, e2022GL098158,  
674 <https://doi.org/10.1029/2022GL098158>, 2022.

675 Titov, V., Rabinovich, A. B., Mofjeld, H. O., Thomson, R. E., and Gonza, F. I.: The Global Reach of

676 the 26 December 2004 Sumatra Tsunami, *Science* (80-. ), 309, 2045–2049,  
677 <https://doi.org/10.1126/science.1114576>, 2005.

678 USGS: M 5.8 Volcanic Eruption - 68 km NNW of Nuku'alofa, Tonga, U.S. Geol. Surv., 2022.

679 Wang, Y., Heidarzadeh, M., Satake, K., Mulia, I. E., and Yamada, M.: A Tsunami Warning System  
680 Based on Offshore Bottom Pressure Gauges and Data Assimilation for Crete Island in the Eastern  
681 Mediterranean Basin, *J. Geophys. Res. Solid Earth*, 125, e2020JB020293,  
682 <https://doi.org/10.1029/2020JB020293>, 2020.

683 Wang, Y., Zamora, N., Quiroz, M., Satake, K., and Cienfuegos, R.: Tsunami Resonance  
684 Characterization in Japan Due to Trans-Pacific Sources: Response on the Bay and Continental Shelf, *J.*  
685 *Geophys. Res. Ocean.*, 126, 1–16, <https://doi.org/10.1029/2020JC017037>, 2021.

686 Wang, Y., Heidarzadeh, M., Satake, K., and Hu, G.: Characteristics of two tsunamis generated by  
687 successive Mw 7.4 and Mw 8.1 earthquakes in Kermadec Islands on March 4,2021, *Nat. Hazards Earth*  
688 *Syst. Sci.*, 22, 1–10, <https://doi.org/10.5194/nhess-2021-369>, 2022.

689 Yuen, D. A., Scruggs, M. A., Spera, F. J., Yingcai Zheng, Hao Hu, McNutt, S. R., Glenn Thompson,  
690 Mandli, K., Keller, B. R., Wei, S. S., Peng, Z., Zhou, Z., Mulargia, F., and Tanioka1, Y.: Under the  
691 Surface: Pressure-Induced Planetary-Scale Waves, Volcanic Lightning, and Gaseous Clouds Caused by  
692 the Submarine Eruption of Hunga Tonga-Hunga Ha'apai Volcano Provide an Excellent Research  
693 Opportunity, *Earthq. Res. Adv.*, <https://doi.org/10.1016/j.eqrea.2022.100134>, 2022.

694 Zhang, S., Vierinen, J., Aa, E., Goncharenko, L. P., Erickson, P. J., Rideout, W., Coster, A. J., and  
695 Spicher, A.: 2022 Tonga Volcanic Eruption Induced Global Propagation of Ionospheric Disturbances  
696 via Lamb Waves, *Front. Astron. Sp. Sci.*, 9, 1–10, <https://doi.org/10.3389/fspas.2022.871275>, 2022.

697