A new skill score for ensemble flood maps: assessing spatial spread-skill with remote sensing observations.

Helen Hooker[1], Sarah L. Dance[1,2,3], David C. Mason[4], John Bevington[5], and Kay Shelton[5]

[1]Department of Meteorology, University of Reading, UK
[2]Department of Mathematics and Statistics, University of Reading, UK
[3]National Centre for Earth Observation (NCEO), Reading, UK
[4]Department of Geography and Environmental Science, University of Reading, UK
[5]Jeremy Benn Associates Limited (JBA Consulting), UK

Correspondence: Helen Hooker (h.hooker@pgr.reading.ac.uk)

Abstract. An ensemble of forecast flood inundation maps has the potential to represent the uncertainty in the flood forecast and provide a location specific, ~~probabilistic,~~ likelihood of flooding. ~~This gives valuable information to~~ Ensemble flood map forecasts provide probabilistic information to flood forecasters, flood risk managers and insurers and will ultimately benefit people living in flood prone areas. Spatial verification of the ensemble flood map forecast against remotely observed flooding is important to understand both the skill of the ensemble forecast and the uncertainty represented in the variation or spread of the individual ensemble member flood maps. ~~Previously~~ In atmospheric sciences, a scale-selective approach has been used to evaluate a convective precipitation ensemble forecast. This determines a skilful scale (agreement scale) of ensemble performance by locally computing a skill metric across a range of length scales. By extending this approach through a new application we evaluate the spatial predictability and the spatial spread-skill of an ensemble flood forecast across a domain of interest. The spatial spread-skill method computes an agreement scale at every grid cell ~~at grid level~~ between each unique pair of ensemble flood maps (ensemble spatial spread) and between each ensemble flood map with a SAR-derived flood map (ensemble spatial skill). ~~By comparing these we can determine the spatial spread-skill performance~~ These two are compared to produce the final spatial spread-skill performance. These methods are applied to ~~an example~~ the August 2017 flood event on the Brahmaputra River in the Assam region of India~~, August 2017~~. Both the spatial-skill and spread-skill relationship vary with location and ~~can be~~ are related to physical characteristics of the flooding event. ~~Routine~~ Validation and mapping of the spatial ~~predictability~~ spread-skill relationship in ~~an~~ operational system monitoring would allow better quantification of ~~model~~ forecast systematic biases and uncertainties. This would be particularly useful for ungauged catchments and would enable targeted model improvements to be made across different parts of the forecast chain.

1 Introduction

Forecast flood maps indicating the extent and depth of a ~~predicted~~ fluvial flood within an actionable lead time, are a ~~vital~~ useful tool for flood risk managers and emergency response teams prior to and during a flood event. Typically, forecast flood maps are presented as deterministic forecasts ~~predicting~~ showing precisely where flooding will occur. This can lead to inci-

dents of false alarms or missed warnings and subsequent recriminations causing mistrust in the system (Arnal et al., 2020; Savage et al., 2016). A timely prediction of exactly where and when fluvial flooding caused by intense or prolonged rainfall will occur is virtually impossible due to the chaotic nature of the atmosphere (Lorenz, 1969), which ultimately determines where heavy precipitation will fall. The ensemble forecasting approach aims to address the sensitive nature of the atmosphere to its initial conditions and through multiple model runs these initial condition uncertainties can be quantified (Leutbecher and Palmer, 2008). This The ensemble forecast results in a probabilistic weather forecast that indicates the predictability of the atmosphere at a given space and time. State-of-the-art operational ensemble flood forecasting systems link together a chain of forecast models to produce probabilistic streamflow and flood inundation forecasts at national and global scales (Cloke and Pappenberger, 2009; Emerton et al., 2016; Wu et al., 2020). Ensemble Numerical Weather Prediction (NWP) models provide meteorological inputs into land-surface, hydrological and hydraulic models, cascading the atmospheric uncertainty through to the flood forecast. Throughout this chain of models multiple sources of uncertainties exist (Beven, 2016; Matthews et al., 2022; Pappenberger et al., 2005; Zappa et al., 2011). As discussed by Boelee et al. (2019) , these uncertainties include those detail the uncertainties arising from meteorological inputs, measurements and observations, initial conditions, unresolved physics within the models and parameter estimates. A probabilistic flood inundation forecast should present a meaningful prediction of the likelihood of flooding so that there is confidence in the forecast, given the uncertainties represented in the system (Alfonso et al., 2016).

The accuracy of the location of flooding, predicted in advance, is defined as spatial predictability. The spatial predictability of ensemble forecasts of flood inundation could be verified by comparing with a remote observation of the flood from satellite or unmanned aerial vehicle (UAV) based sensors. Satellite-based optical and Synthetic Aperture Radar (SAR) sensors are well known for their flood detection capability (e.g. Horritt et al., 2001; Mason et al., 2012). SAR sensors are active, which enables them to scan the Earth through weather and clouds, and at night. The SAR backscatter intensity detected depends on the roughness of the surface, with unobstructed flooded areas and other surface water bodies appearing relatively smooth and returning low backscatter values. Dasgupta et al. (2018a) detail some of the challenges along with approaches to solutions of flood detection using SAR, examples of these challenges include: roughening of the water surface by heavy rain and strong wind, emergent or partially submerged vegetation and flood detection in urban areas. Accurate flood detection in urban areas particularly due to surface water flooding has become increasingly important (Speight and Krupska, 2021) and recent techniques have led to improved flood detection (Mason et al., 2018, 2021a, b). Optical instruments rely on solar energy and cannot penetrate cloud, making them less useful during a flooding situation. Recent studies have investigated the flood detection benefits from combining both optical and SAR imagery (Konapala et al., 2021; Tavus et al., 2020). Improvements in the spatial-temporal resolution of SAR images and their open source availability mean that they are an increasingly valuable tool for hydraulic and hydrodynamic model improvements through calibration, validation and data assimilation (e.g. García-Pintado et al., 2015; Hostache et al., 2018; Cooper et al., 2018, 2019; Di Mauro et al., 2021; Dasgupta et al., 2018b, 2021a, b). The Global Flood Monitoring (GFM) product (EU Science Hub, 2021; GFM, 2021; Hostache, R., 2021) of the Copernicus Emergency Management Service (CEMS) (Copernicus Programme, 2021) produces SAR-derived flood inundation maps for every Sentinel-1

image detecting flooding. Three flood detection algorithms provide uncertainty estimation and population affected estimates within 8 hours of the image acquisition. The European Space Agency (ESA) Copernicus Programme have recently included the ICEYE constellation of small satellites into the fleet of missions contributing to Europe's Copernicus environmental monitoring programme (ESA, 2021). ICEYE captures very high resolution (spot mode ground range resolution = 1 m) SAR images which brings the potential for increased accuracy of flood detection, particularly in urban areas.

To evaluate the accuracy of an ensemble forecast, a number of verification measures have been ~~applied previously~~ proposed. Anderson et al. (2019) developed a joint verification framework for end-to-end assessment of the England and Wales Flood Forecasting Centre (FFC) ensemble flood forecasting system. Anderson et al. (2019) describe verification metrics such as the continuous rank probability score (CRPS), rank histograms, Brier Skill Score (BSS) and the relative operative characteristics (ROC) diagrams that are commonly applied to assess the main ensemble attributes desirable in both precipitation and streamflow ensemble forecasts (e.g. Renner et al., 2009). These metrics refer to flooding events as part of a time series evaluated against a reference benchmark, such as climatology, to produce an average skill score. ~~These differ from the ensemble spatial verification approaches applied at a specific time point considered here.~~ In contrast, here we consider ensemble *spatial* verification at a single time point. The verification of ensemble forecasts usually involves comparing the RMSE of the ensemble mean against an observed quantity to assess the *skill* of the forecast with the ensemble standard deviation used as a measure of *spread*. A perfect ensemble should encompass forecast uncertainties such that the ensemble spread ~~equals~~ is correlated to the RMSE of the forecast (Hopson, 2014). This *spread-skill* relationship was assessed by Buizza (1997) to investigate the predictability limits of the European Centre for Medium-Range Weather Forecasts (ECMWF) Ensemble Prediction System (EPS). This approach to ensemble verification is based on point values and makes the assumption that the ensemble mean is the forecast state with the highest probability and that the forecast distribution is Gaussian. Significant flooding events are, in their nature, a rare occurrence and in certain circumstances a few ensemble members can indicate a low probability of an extreme flood. Also, in particular atmospheric scenarios the ensemble forecast may result in a multi-modal forecast where two clusters of ensemble members are each equally likely (Galmiche et al., 2021). For example, both clusters may indicate flooding events but at different magnitudes. In both of these instances the individual ensemble member details are important and evaluation of the ensemble mean alone would not be meaningful. When mapping the flood extent prediction, the ensemble mean field alone does not retain the spatial detail of the individual member forecasts.

~~The spatial predictability of the full ensemble must be evaluated against observations of flooding to determine the spatial spread-skill of the ensemble forecast.~~ The spatial spread-skill of the ensemble forecast is determined by evaluating the full ensemble against observations of flooding. For a flood map ensemble to be considered spatially well-spread, the spread or variation between ensemble members should equal the spatial predictability, or skill of the ensemble members (Dey et al. (2014), see Section 2). Presently, to the best of our knowledge, quantitative evaluation methods assessing the spatial spread-skill of ensemble forecast flood maps do not exist. ~~In numerical weather prediction previous work by~~ However, previous work in numerical weather prediction by Ben Bouallègue and Theis (2014) investigated the application of spatial techniques to ensemble

precipitation forecasts using a neighbourhood, or fuzzy approach that allowed comparisons at larger scales than grid level. A location dependent approach to the spatial spread-skill evaluation of a convective precipitation ensemble forecast was developed by Dey et al. (2016). This method compares every ensemble member across a range of scales on a spatial field against an observation field to assess whether the ensemble forecast is spatially over-, under- or well-spread on average across a domain of interest (Chen et al., 2018). In a recent study, a scale-selective approach was developed and applied to evaluate a deterministic flood map forecast where comparisons were made against conventional binary performance measures (Hooker et al., 2022a). ~~This paper~~ The work described here extends and applies this scale-selective approach to assess the spatial predictability and the spatial spread-skill of an ensemble flood map forecast.

In this paper we aim to address the following questions:

- How can we summarise the spatial predictability information in ensemble flood map forecasts?

- How can we evaluate the spatial spread-skill of an ensemble flood map forecast?

- How does the spatial spread-skill vary with location and how can this be presented?

In Section 2 we present a new approach to the evaluation of spatial predictability and the spatial spread-skill of an ensemble flood map forecast by comparing against a remotely observed flooding extent. We illustrate the features of the methods through an example case study of an extreme flooding event of the Brahmaputra River which impacted India and Bangladesh in August 2017; with a focus on the Assam region of India. The flood event details are described in Section 3.1. The international ensemble version of the JBA Consulting Flood Foresight system provides forecast flood maps for the study and is described in Section 3.2. Observations of the flood are derived from satellite based Synthetic Aperture Radar (SAR) sensors and the method is explained in Section 3.3. The results including our new Spatial spread-skill (SSS) map are discussed in Section 4. Our results show that individual ensemble member spatial predictions of flooding are meaningful and that the full ensemble spatial detail should be evaluated. We conclude in Section 5 that the spatial spread-skill of the ensemble forecast varies with location across the domain and can be linked to physical characteristics of the flooding event.

2 Ensemble flood map spatial predictability evaluation methods

In this Section we present new methods for evaluating and visualising the spatial-spread skill of an ensemble flood map forecast. Hooker et al. (2022a) described and applied a new scale-selective approach to evaluate the spatial skill of a *deterministic* flood map forecast ~~in terms of a skilful scale at which the forecast captures the~~ relative to an observed SAR-derived flood map. Here, we apply this ~~verification~~ same measure to evaluate different aspects of an *ensemble* forecast. The scale-selective Fraction Skill Score (FSS) method is outlined in Section 2.1. Agreement scale maps indicating forecast accuracy are defined for location-specific comparisons between ~~two fields~~ forecast and observed flood maps in Section 2.2. These are used to assess the spatial relationship between each unique pair of ensemble member flood maps (member-member) and between every ensemble

member flood map and the observed SAR-derived flood map (member-SAR, Section 2.3). Visualisation methods of the spatial
spread-skill relationship including our new *Spatial Spread-Skill (SSS)* map are presented in Section 2.4.

2.1 Fraction Skill Score

The FSS is a scale-selective verification measure that can determine the skilful scale of a modelled flood map, when compared
against a remotely sensed observation of flooding (Hooker et al., 2022a). We will call these flood maps the *model array* and
the *observed array* respectively. For an ensemble forecast, the model array could be an individual ensemble member, or a
summarised flood estimate derived from a combination of ensemble members such as a combined ensemble or the ensemble
median (see Section 3.4). Both the model and observed arrays are converted into binary fields using a situation dependent
threshold. For this ensemble application of the FSS we evaluate the flooding extent and each grid cell in the domain is labelled
as inundated (1) or dry (0). All grid cells are numbered according to their spatial locations (i,j), $i = 1 \dots N_x$ and $j = 1 \dots N_y$
where N_x is the number of columns and N_y is the number of rows. Surrounding each grid cell, a square of length n creates an
$n \times n$ neighbourhood. The fraction of $1s$ (inundated cells) in the square neighbourhood area is calculated for every grid cell.
This creates two arrays of fractions across the domain for both the observed O_{nij} and modelled M_{nij} data. The mean squared
error (MSE) for the fraction arrays is calculated for the domain and a given neighborhood size, n:

~~Hooker et al. (2022a) describe the calculation of the FSS. "Both arrays are converted into binary fields using a threshold~~
~~approach that is predetermined for the situation. For a flood map verification of spatial skill, the simplest example is applied~~
~~here and assigns each grid cell as unflooded (0) or flooded (1) for the entire domain. Alternative threshold approaches for flood~~
~~depth maps could include applying thresholds to water depth percentiles. Given a domain of interest, each of the grid cells are~~
~~numbered according to their spatial coordinates~~ (i,j), $i = 1 \dots N_x$ and $j = 1 \dots N_y$ ~~where N_x is the number of columns in the~~
~~domain and N_y is the number of rows. For each grid cell a square of length n forms an $n \times n$ neighbourhood surrounding the~~
~~grid cell. The fraction of $1s$ in the square neighbourhood is calculated for each grid cell. This creates two fields of fractions~~
~~over the domain for both the forecast M_{nij} and observed O_{nij} data. The fraction fields are compared against one another to~~
~~calculate the mean squared error (MSE) for the neighbourhood~~

$$MSE_n = \frac{1}{N_x N_y} \sum_{i=1}^{N_x} \sum_{j=1}^{N_y} [O_{nij} - M_{nij}]^2. \tag{1}$$

~~Based~~ Depending on the fractions calculated for the model and observed fields a ~~worst~~ maximum possible MSE is calculated
as:

$$MSE_{n(ref)} = \frac{1}{N_x N_y} \sum_{i=1}^{N_x} \sum_{j=1}^{N_y} [O_{nij}^2 + M_{nij}^2]. \tag{2}$$

Finally, the FSS is ~~given by~~

$$FSS_n = 1 - \frac{MSE_n}{MSE_{n(ref)}}. \tag{3}$$

In general, the FSS is calculated for each length of neighbourhood n. For a given neighbourhood size an FSS of 1 is said to have perfect skill and 0 means no skill. The FSS will increase as n increases up to an asymptote (see Fig. 3 from Roberts and Lean (2008)). If there is no model bias across the whole domain of interest (observed and forecast flooded areas are the same) then the asymptotic fraction skill score (AFSS) at $n = 2N - 1$, where N is the number of points along the longest side of the domain, will equal 1. Plotting FSS against spatial scale can indicate a range of scales where the model is deemed to be the most useful. This usefulness is a trade-off between being too smooth (larger n) or too fine, where the forecast skill is lost and the computation time lengthy. A target FSS score (FSS_T) is defined as

The FSS is initially calculated for the smallest neighbourhood size ($n = 3$) before increasingly larger neighbourhood sizes ($n = 5$, $n = 7...$) are considered. The FSS ranges between 0 (no skill) and 1 (perfect skill). Increasing the neighbourhood size typically leads to an improved FSS as the fractions are calculated over a larger area. Plotting FSS against the neighbourhood size can indicate a range of scales where the model is deemed to be the most skilful. A target FSS score (FSS_T) can be determined from the fraction of observed flooding across the whole domain (f_0)

$$FSS_T \geq 0.5 + \frac{f_o}{2}. \tag{4}$$

where f_0 is the fraction of flood observed across the whole domain of interest and can be thought of as being equidistant between the skill of a random forecast and perfect skill. FSS_T will vary depending on the magnitude of the observed flood, relative to the domain area. This allows the comparison of the FSS_T scale across different domain sizes and floods of different magnitudes.

The point where the FSS_n exceeds FSS_T can be viewed as being equidistant between the skill of a random forecast and perfect skill (Roberts and Lean, 2008). The magnitude of the observed flood, relative to the domain area, determines the value of FSS_T. This allows the comparison of the skilful scale (neighbourhood size) where FSS_T is reached across different domain sizes and floods of different magnitudes.

2.2 Location dependent agreement scales

The FSS (Section 2.1) gives a domain average measure of forecast performance and a minimum scale at which the forecast is deemed skilful. To enable the spatial spread-skill of the full ensemble to be evaluated, we first define a measure of similarity in terms of location specific agreement scales. Here, two data fields are compared f_{1ij} and f_{2ij}, these could both be ensemble member flood maps or an ensemble member flood map and an observed flood map. These are non-thresholded fields and the agreement scale method can be applied to both binary flood extent maps as well as flood depth fields. Following Hooker et al. (2022a) "the aim is to find a minimum neighbourhood size (or scale) for every grid point such that there is an agreement between f_{1ij} and f_{2ij}. This is known as the agreement scale $S_{ij}^{A(f_1 f_2)}$. The relationship between the agreement scale and the neighbourhood size described previously in section 2.1 is given by $S_{ij}^{A(f_1 f_2)} = (n-1)/2$.

Firstly, all grid points are compared by calculating the relative MSE D_{ij}^S at the grid scale, $S = 0$ ($n = 1$),

$$D_{ij}^S = \frac{(f_{1ij}^S - f_{2ij}^S)^2}{(f_{1ij}^S)^2 + (f_{2ij}^S)^2}. \tag{5}$$

If $f_{1ij} = 0$ and $f_{2ij} = 0$ (both dry) then $D_{ij}^S = 0$ (correct at grid level). Note that D_{ij}^S varies from zero to 1. The fields are considered to be in agreement at the scale being tested if:

190 $\quad D_{ij}^S \le D_{crit,ij}^{S_{ij}} \quad$ where $\quad D_{crit,ij}^S = \alpha + (1 - \alpha)\dfrac{S}{S_{lim}}$ $\hspace{2cm}$ (6)

and S_{lim} is a predetermined, fixed maximum scale. The parameter value α is chosen to indicate the acceptable bias at grid level such that $0 \le \alpha \le 1$. Here we set $\alpha = 0$ (no background bias). If $D_{ij}^S \ge D_{crit,ij}^S$ then the next neighbourhood size up is considered ($S = 1$, a 3 by 3 square). The process continues with increasingly larger neighbourhoods until the agreement scale

$$S_{ij}^{A(f_1f_2)} \quad \text{or} \quad S_{lim} \quad \text{at} \quad D_{ij}^S \le D_{crit,ij}^{S_{ij}} \tag{7}$$

195 is reached for every cell in the domain of interest. The agreement scale at each grid cell is then mapped onto the domain of interest."

A categorical scale map for an individual ensemble member or a combination of members such as the ensemble median can be created by combining the agreement scale map with a conventional contingency map (see Hooker et al. (2022a) for further details). Categorical scale maps may be used as a basis for comparison between ensemble members and observations, as we illustrate with our case study in Section 4.3.

The FSS (Section 2.1) gives a domain average measure of forecast performance and a minimum spatial scale at which the forecast is deemed skilful. To enable the spatial spread-skill of the full ensemble to be evaluated at specific locations, we first

205 define an agreement scale (see Hooker et al. (2022a) for full methodology). The agreement scale is calculated and mapped for every grid cell in the domain and shows a measure of similarity between two arrays of data. In contrast to the FSS method the arrays are not required to be thresholded. The agreement scale method can be applied to both binary flood extent maps as well as flood depth fields. These could both be ensemble member flood maps or an ensemble member flood map and an observed flood map. Two data arrays are compared f_{1ij} and f_{2ij} and the aim is to find a minimum neighbourhood size (or spatial scale)

210 for every grid cell such that there is a predetermined acceptable minimum level of agreement between f_{1ij} and f_{2ij}. This is known as the agreement scale $S_{ij}^{A(f_1f_2)}$. (Note that the relationship between the agreement scale and the neighbourhood size described previously in section 2.1 is given by $S_{ij}^{A(f_1f_2)} = (n-1)/2$.)

A relative MSE D_{ij}^S is calculated for all grid cells, initially at grid level, $S = 0$ ($n = 1$),

$$D_{ij}^S = \frac{(f_{1ij}^S - f_{2ij}^S)^2}{(f_{1ij}^S)^2 + (f_{2ij}^S)^2}. \tag{8}$$

If $f_{1ij} = 0$ and $f_{2ij} = 0$ (both dry) then $D_{ij}^S = 0$ (correct at grid level). The value of D_{ij}^S ranges between zero and 1. The arrays are deemed to be in agreement at the scale being tested if:

$$D_{ij}^S \leq D_{crit,ij}^{S_{ij}} \quad \text{where} \quad D_{crit,ij}^S = \alpha + (1-\alpha)\frac{S}{S_{lim}} \tag{9}$$

The parameter value α indicates an acceptable bias at grid level such that $0 \leq \alpha \leq 1$ and S_{lim} is a fixed maximum scale that is predetermined. We set the criterion for no background bias, $\alpha = 0$. If $D_{ij}^S \geq D_{crit,ij}^S$ then the next neighbourhood size up is considered ($S = 1$, $n = 3$, a 3 by 3 square) where f_{1ij}^1 and f_{2ij}^1 are the average value of each neighbourhood surrounding the grid cell at position (i, j) for each array. The process continues by comparing increasingly larger neighbourhoods (e.g. $S = 2$, $n = 5$, a 5 by 5 square) until the agreement criterion

$$S_{ij}^{A(f_1 f_2)} \quad \text{or} \quad S_{lim} \quad \text{at} \quad D_{ij}^S \leq D_{crit,ij}^{S_{ij}} \tag{10}$$

is met for every cell in the domain. The agreement scale at which the agreement criterion is met will usually vary from grid cell to grid cell and these values ($S = 0$, $S = 1$, $S = 2$ and so on up to S_{lim}), each specific to each grid cell location can be mapped onto the domain of interest to provide a location specific measure of agreement between the two data arrays that are compared.

A categorical scale map shows a measure of spatial accuracy between two data arrays (Hooker et al., 2022a). Validation of forecast flood maps against remotely observed flooding extent is typically carried out by labelling each grid cell using a contingency table with categories: correctly predicted flooded, under-prediction (miss), over-prediction (false alarm) and correctly predicted unflooded. Mapping these categories creates a conventional contingency map, which combined with an agreement scale map creates a categorical scale map. Categorical scale maps may be used as a basis for comparison between ensemble members and observations, as we illustrate with our case study in Section 4.3.

2.3 Ensemble spatial spread-skill evaluation

We assume that each ensemble forecast flood map represents an equally likely future scenario and the evaluation of the full ensemble is needed to quantify the uncertainty and to evaluate the spatial spread-skill relationship. The ensemble flood map spatial characteristics vary with location and in order to preserve the location dependent information, we utilise a method developed to evaluate a convective ensemble precipitation forecast (Dey et al., 2016). Here, we outline the method and describe a new application to evaluate an ensemble forecast flood map. (see Dey et al. (2016) for additional details of the method).

A neighbourhood approach (Section 2.2) is used to assess the spatial agreement scale $S_{ij}^{A(f_1 f_2)}$ or measure of similarity at each grid cell location (i, j) between each unique pair of ensemble flood maps. For an ensemble of M members, there are

$$M_p = \frac{M(M-1)}{2}, \tag{11}$$

unique pairs (e.g., 1275 pairs for a 51 member ensemble). ~~Between each flood map and the SAR-derived flood map there are 51 pairs.~~ For an ensemble, the skillful scale can be renamed as a *believable scale*, which is the scale where ensemble members become sufficiently similar to observations such that they are a useful prediction. Every paired ensemble agreement scale field is averaged at each grid cell to produce a mean field, following from equation (7)

$$S_{ij}^{A(\overline{mm})} = \frac{1}{M_p} \sum_{f_1=1}^{M-1} \sum_{f_2=f_1+1}^{M} S_{ij}^{A(f_1 f_2)} \tag{12}$$

indicating the location specific believable scales of the forecast flood map ensemble. Maps of $S_{ij}^{A(\overline{mm})}$ summarise the spatial spread of the full ensemble.~~predictability and can be linked to physical processes.~~ Each of the agreement scale fields between the ensemble members and the observations are also averaged at each grid cell to give

$$S_{ij}^{A(\overline{mo})} = \frac{1}{M} \sum_{f=1}^{M} S_{ij}^{A(f_0)}. \tag{13}$$

A measure of the spatial spread-skill of the ensemble can be found by comparing the average agreement scale between the ensemble members $S_{ij}^{A(\overline{mm})}$ representing the ensemble *spread* with the average agreement scale between the ensemble members and the observed flood field $S_{ij}^{A(\overline{mo})}$ representing the ensemble *skill*. ~~Visualisation methods for evaluating the spatial spread-skill are presented in Section~~ 2.4.

2.4 Spatial spread-skill visualisation methods

To evaluate the spatial spread-skill relationship, $S_{ij}^{A(\overline{mm})}$ (representing the ensemble *spread*) must be compared in the same location as $S_{ij}^{A(\overline{mo})}$ (representing the ensemble *skill*). ~~A binned scatter plot compares groups of grid cells from two domains by averaging~~ Data arrays can be visually compared using a binned scatter plot that averages across a selected bin of cells at the same location ~~on each~~ within the domain. Dey et al. (2016) demonstrated for an idealised example that by plotting $S_{ij}^{A(\overline{mm})}$ against $S_{ij}^{A(\overline{mo})}$ as a binned scatter plot in order to preserve the spatial location of the comparison (Fig. 1), the ensemble can be classified as over-, under- or well-spread. The ensemble is deemed to be *well-spread* at a specific location in the domain of interest when the spread of the individual members represented at each grid cell by $S_{ij}^{A(\overline{mm})}$ equals the skill of the ensemble represented at each grid cell by $S_{ij}^{A(\overline{mo})}$, i.e. $S_{ij}^{A(\overline{mm})} - S_{ij}^{A(\overline{mo})} = 0$. The result would lie on a 1:1 line on the binned scatter plot. Where the spread between the ensemble members exceeds the skill of the ensemble forecast i.e. $S_{ij}^{A(\overline{mm})} > S_{ij}^{A(\overline{mo})}$ the ensemble is considered to be *over-spread* and the binned scatter plot will lie beneath the 1:1 line. The converse is true for an *under-spread* ensemble forecast where the agreement between members, the spread, is less than the agreement between the ensemble and the observations, the skill. Here, $S_{ij}^{A(\overline{mm})} < S_{ij}^{A(\overline{mo})}$ and the binned scatter plot would lie above the 1:1 line.

To summarise the spread-skill relationship ~~for our example flood case~~ we develop this visualisation further by plotting a hexagonal binned 2D histogram plot ~~(see hexbin plot, Section 4.3, Fig.~~ 8) (an example hexbin plot is presented in Section 4.3). The domain is divided into a (pre-determined) number of hexagons. ~~Hexagons reduce the sampling bias compared with a square grid due to the edge effects of the grid shape. This is related to the low perimeter-to-area ratio of the shape of the~~

~~hexagon, a circle has the lowest ratio but cannot tessellate to form a continuous grid. Hexagons are closest to a circular shape and can tessellate to form an evenly spaced grid.~~ Hexagons minimize the perimeter to area ratio and therefore minimize the edge effects. The hexbin histogram plot colour shade represents the number of data points within each bin. ~~This adds additional~~
280 ~~information to the standard binned scatter plot.~~
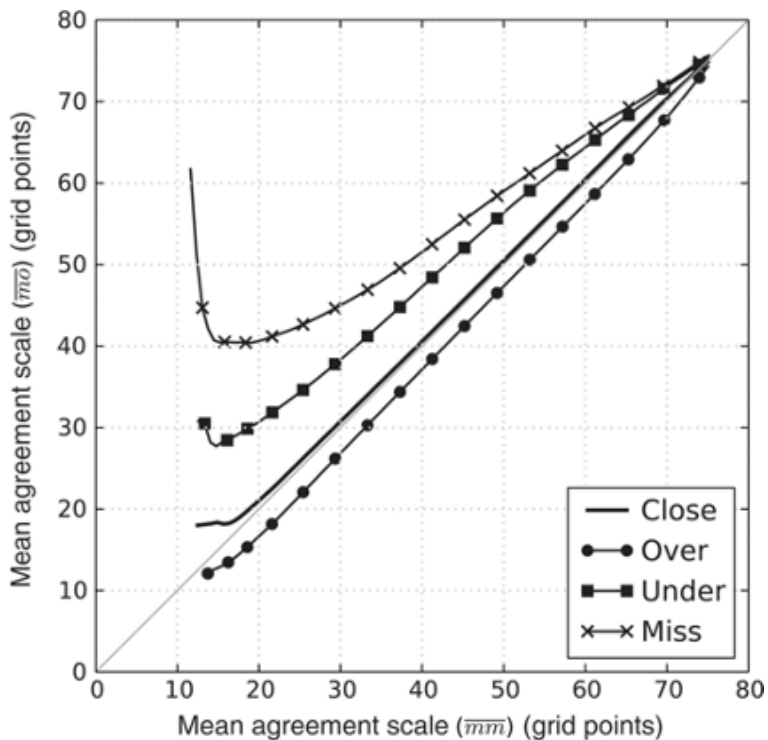
Figure 1. Figure reproduced with permission from Dey et al. (2016) showing results from an idealised experiment indicating the spatial spread-skill relationship between an ensemble forecast and the observation.

2.4.1 ~~Spatial Spread-Skill (SSS) map~~

Whilst the hexbin plot is useful for gaining an understanding of the general spread-skill relationship of the ensemble flood map forecast, it does not tell us specifically where in the domain the ensemble spatial predictability is better or worse so that it can
285 be linked to physical processes and to improve ~~model performance~~ aspects of the flood forecasting modelling chain. Our new *Spatial Spread-Skill* (SSS) map plots $S_{ij}^{A(\overline{mm})} - S_{ij}^{A(\overline{mo})}$ at every grid cell location so that the spread-skill is mapped across the domain and can be linked directly to different sub-catchments and surface features such as tributaries, embankments, bridges and importantly the underlying topography or DTM, which influence the derivation of the ensemble flood maps. Regions on the SSS map where the ensemble is over-spread are positive with negative areas indicating where the ensemble is under-spread,

290   zero values show a well-spread ensemble. Note that this does not necessarily mean that the entire ensemble is in agreement with observations at grid level, but that the agreement scales between $S_{ij}^{A(\overline{mm})}$ and $S_{ij}^{A(\overline{mo})}$ are equal. (An example SSS map is presented in Section 4.3).

3   Ensemble forecasting flood event case study

In this section we describe an example flooding event used to demonstrate the application of our new spatial spread-skill
295   evaluation approach. We evaluate a 1-day flood inundation 51 ensemble member forecast from the Flood Foresight system (Section 3.2) for the domain area against a satellite SAR-derived flood map (Section 3.3).

3.1   Brahmaputra flood, Assam India, August 2017

The origin of the Brahmaputra River (also known as the Yarlung Tsangpo in Tibetan, the Siang/Dihang River in Arunachali, Luit in Assamese, and the Jamuna River in Bangladesh) lies in the Himalayan Kailas Range of southwestern Tibet, China.
300   Draining an area of 543,000 km^2, the Brahmaputra flows for 2000 km across the Tibetan Plateau and a further 1000 km parallel to the Himalayan foothills through the Assam Valley, India before entering Bangladesh where the Brahmaputra joins the Ganges River (Palash et al., 2020). The Brahmaputra baseflow originates from the upstream glacial snow melt, however the streamflow rates are dominated by the summer monsoon precipitation. The basin receives up to 95% of its annual rainfall during the pre-monsoon and monsoon season, which usually runs from April to September and causes annual flooding of the
305   Brahmaputra. The Assam region typically records on average 2300 mm of annual rainfall and up to 5000 mm in the Himalayan foothills (Dhar and Nandargi, 2000, 2003).

For this example case we focus on the third wave of flooding that occurred during the monsoon season in August 2017, peaking around the 12$^{\text{th}}$. Figure 2 shows the location of the Brahmaputra and of a chosen domain centred upon some of the
310   worst flooding that occurred. This area includes a confluence zone where the Subansiri River meets the Brahmaputra. The monsoon flooding impacted an estimated 40 million people across India and Bangladesh. ~~Locally in the Assam region, the flooding in August affected 3.3 million people and 3186 villages. Over 14,000 people were evacuated to one of 678 relief camps that were also needed to home the 183,584 people relocated.~~ Locally in the Assam region, the flooding in August affected over 3.3 million people and approximately 3200 villages, river embankments were damaged in 11 districts. Over 14,000 people were
315   evacuated to one of around 700 relief camps that were also needed to house over 180,000 people relocated (Floodlist, 2017). The local Assam State Disaster Management Authority (ASDMA, 2017) flood early warning system issued a low warning alert (disasters that can be managed at the district level) on the 10$^{\text{th}}$ August for the district.

In 2017, the southwest monsoon season rainfalls were predicted to be *normal* by the South Asian Climate Outlook Forum
320   (WMO, 2017). However, the pre-monsoon season began early in the year with heavy thunderstorms affecting the region from March onwards. In the Assam region, June and July were 60% wetter than the previous three years and during August more
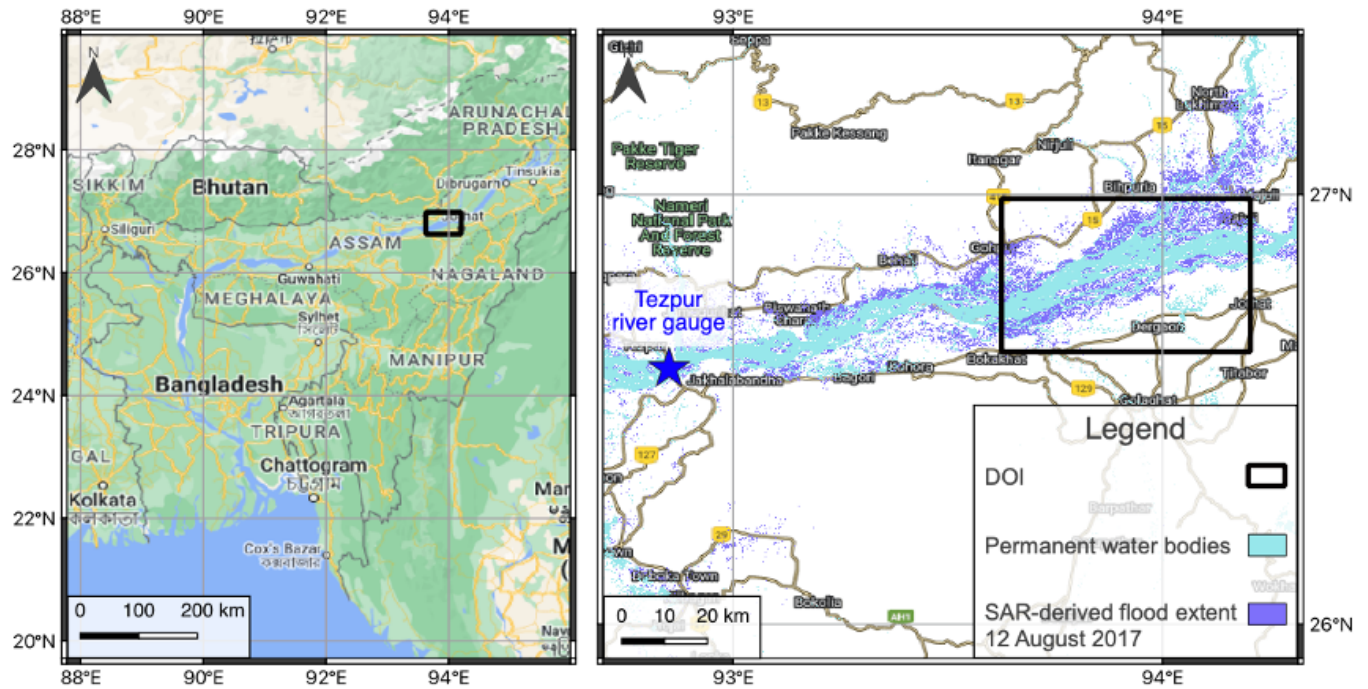
Figure 2. Left panel: domain location on the Brahmaputra River in the Assam region of India. Domain size is 57.5 km by 39.3 km. Right panel: Sentinel-1 SAR-derived flood map for the domain of interest. Base map from ©Google Maps.

locally intense rainfall was recorded compared with historical observations (Palash et al., 2020). In higher latitude areas, 30 km to the north of the domain at North Lakhimpur, 215.8 mm rainfall was recorded in the three days prior to the flood peak (Floodlist, 2017; Hossain et al., 2021). ~~A flooding situation is declared in India when water levels (WL) rise above a pre-de-~~
325 ~~termined danger level (DL). If the WL increases beyond +1 m of the DL then a severe flood situation is triggered.~~ An above normal flood situation is declared in India where the river water level exceeds the Warning Level, a severe flood occurs where the water level exceeds the Danger Level, and an extreme flood occurs where the previous Highest Flood Level is exceeded (Central Water Commission, 2023). The peak ~~WL~~ water level recorded ~~at~~ downstream at Tezpur (~~DL~~ Danger Level 65.23 m) on August 14th was 66.12 m (Fig. 2). ~~There are reports of regional variations in maximum WL recorded with upland regions to the~~
330 ~~north of the Assam valley exceeding record levels. Flooding was exacerbated due to embankment breaches and deforestation has contributed to worsening flooding.~~ There are regional variations in maximum water levels reported, with upland regions to the north of the Assam valley recording water levels that exceed the previous Highest Flood Level indicating an extreme flood occurred (Floodlist, 2017).

3.2 Ensemble flood forecasting system

The Flood Foresight system (Fig. 3), developed and operationally run by JBA Consulting, is a fluvial flood inundation mapping system that can be implemented at any river basin around the world. Flood Foresight utilises a simulation library approach to generate real-time and forecast flood inundation and water depth maps. The simulation library approach saves valuable computing time and allows the application of Flood Foresight in near continuous real-time at national and international scales. A pre-computed library of flood maps for a river basin or country are created using JFlow®, (Bradbrook, 2006) and RFlow. JFlow uses a raster-based approach with a detailed underlying digital terrain model (DTM) and a ~~simplified form~~ diffusion wave approximation of the full 2D hydrodynamic shallow water flow equations. RFlow combines a 1D model based upon Normal Depth calculations, optimised for use on a Digital surface Model (DSM, NEXTmap (2016)) with rapid 2D flood spreading (created by spreading Normal Depth from upstream to downstream) and is calibrated against JFlow. These equations capture the main controls of the flood routing for shallow, topographically driven flow. Six flood maps at 30 m resolution are created for 20, 50, 100, 200, 500 and 1500 year return period flood events (corresponding to annual exceedance probabilities (AEPs) of 5%, 2.5%, 1%, 0.5% and 0.2% and 0.07% respectively). ~~These are interpolated to derive five intermediate maps between each adjacent pair of the JFlow maps and 5 maps below the lowest 20 year return period map, equally spaced in return period creating a total library of 36 flood maps.~~ Between each adjacent pair of modelled return period maps, five additional intermediate flood maps are created by linear interpolation. An additional five flood maps are also created beneath the lowest return period flood map. This gives, in total, a library of 36 flood maps. Note that the flood maps are undefended. Flood Foresight takes inputs of rainfall from numerical weather prediction (NWP) models, river gauge data (both historical and real-time) and forecast streamflow and uses these to select the most appropriate flood map for the location and forecasts daily flood maps out to ten days.

The global (non UK and Ireland) configuration of Flood Foresight uses ensemble streamflow forecast data from the Global Flood Awareness System (GloFAS) (Alfieri et al., 2013; GloFAS, 2021). GloFAS was jointly developed by the European Commission and the European Centre for Medium-Range Weather Forecasts (ECMWF) and is composed of an integrated hydro-meteorological forecasting chain that couples state-of-the-art weather forecasts with a land surface and hydrological model. With its continental scale set-up, GloFAS provides downstream countries with forecasts of upstream river conditions up to one month ahead as well as continental and global overviews for large world river basins. Meteorological forecast data are provided by the ECMWF Ensemble (IFS) model, the operational ensemble weather forecasting product of the ECMWF. The meteorological forecast data provide inputs to the land surface module, HTESSEL (Hydrological Tiled ECMWF Scheme for Surface Exchange over Land). HTESSEL simulates the land surface response to the meteorological data, based on simulated interactions with soil conditions, idealised vegetation cover and land cover. From these simulations, HTESSEL outputs forecast global surface and sub-surface flows per grid cell. These simulated flows are then used by a simplified version of the hydrological model LISFLOOD, a ~~one-dimensional~~1D routing model which simulates the movement of the surface and sub-surface flows. The runoff data produced is routed through a representation of the river network using a double kinematic
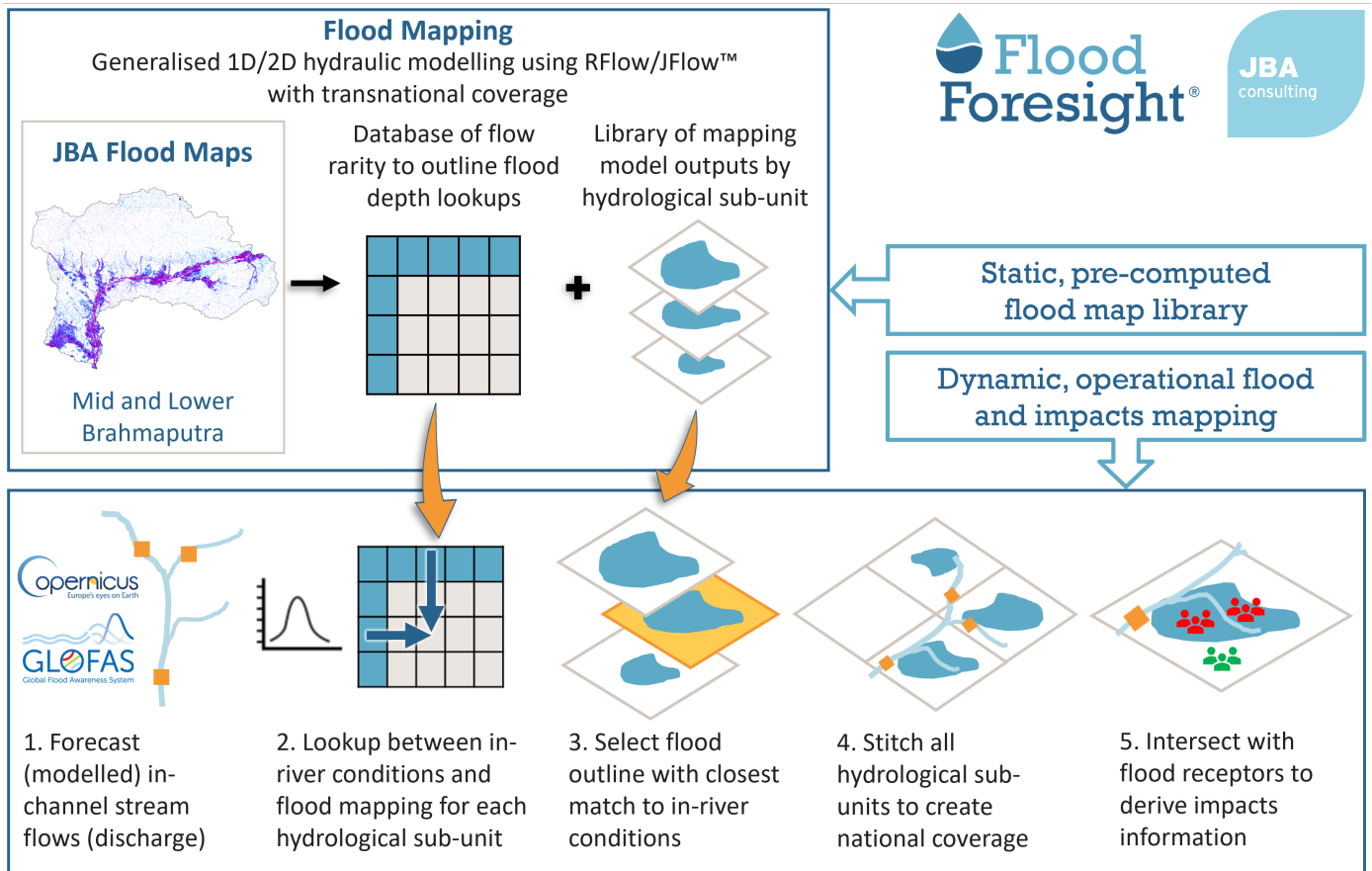
Figure 3. Flood Foresight ensemble forecast flood inundation and impact mapping work flow.

wave approach, which includes bankfull and over bankfull routing. The river network used is taken from the HydroSHEDS
370   dataset (Lehner and Grill, 2013).

  GloFAS outputs a gridded (approximately 10 km spatial resolution) ensemble forecast of river streamflow. Each of the Glo-
FAS grid cells are linked to sub-catchments in the Flood Foresight system. The simulation library flood maps are selected
when the forecast streamflow exceeds a return period threshold level. Each ensemble member flood map forecast is created by
375   aggregating the individual sub-catchment maps. In summary, the meteorological IFS 51 member ensemble input to the flood
forecasting chain allows atmospheric evolution uncertainties to be represented within the ensemble streamflow forecast and
the ensemble of inundation flood maps, thus creating a probabilistic flood map forecast, indicating the likelihood of flooding.

3.3 SAR-derived flood map

A Sentinel-1 (S1A) image was acquired in interferometric wide swath mode (swath width 250 km) around the time of the flood peak at ~~11:48~~ 17:18 (IST) on the 12th August 2017. ~~A pre-flood image (February 2017) from the same satellite sensor and track was used to derive the flood map~~ (Fig. 2). The ESA Grid Processing on Demand (GPOD) HASARD service (http://gpod.eo.esa.int/) ~~has been~~ was utilised to map the flooding. The flood mapping algorithm (Chini et al., 2017) uses an automated, statistical, hierarchical split-based approach to distinguish between two classes (background and flood) using a pre-flood and flood image. A pre-flood image (February 2017) from the same satellite sensor and track was used to derive the flood map (Fig. 2).Original SAR images (VV) ~~are~~ were pre-proccesed, which involved: precise orbit correction, radiometric calibration, thermal noise removal, terrain correction, speckle reduction and re-projection to the WGS84 coordinate system. The HASARD mapping algorithm removes permanent water bodies that are detected on the pre-flood image, such as the unflooded river water, lakes and reservoirs by applying a thresholding approach. Flooded areas beneath vegetation, bridges and near to buildings will not be detected using this method. Flood Foresight forecast flood maps include the river channel and exclude surface features such as vegetation and buildings. To smooth the HASARD flood maps and allow a fairer comparison we apply a morphological closing operation (without impacting the location of the flood extent) to flood fill vegetation and buildings. The wide and braided Brahmaputra River in the Assam region covers a significant area of the selected domain. So that the flood prediction accuracy alone can be evaluated, the pre-flood occurrence of surface water using the JRC Global Surface Water database (Pekel et al., 2016) has been removed from the Flood Foresight forecast inundation maps. The observed flood extent derived from satellite based SAR data at 20 m grid size is re-scaled to match the forecast flood map grid size (30 m) using ~~spline interpolation~~ average aggregation. The closest available (cloud free) optical image available was a Sentinel-2 image on the 17th August 2017, 5 days after the SAR image acquisition. During this time the flood waters had receded from their peak, which makes this unsuitable for comparison with the SAR-derived flood map. Since no other validation sources are available, for the purposes of this study we assume that the SAR-derived observation of flooding represents the true flooding extent. From October 2021, Sentinel-1 SAR images are processed by CEMS GFM (GFM, 2021) to derive flooding extent and provide an uncertainty estimate of the grid cell classification. This means uncertainty information in the SAR-derived flood map could be accounted for in future evaluation studies.

3.4 Forecast data

Flood Foresight was set-up for the Brahmaputra basin in India and Bangladesh using the simulation library approach to flood mapping described in Section 3.2. The ~~Flood Foresight~~ forecast data for the Brahmaputra flood event contains a 51 member ensemble of flood maps indicating flooding extent, produced at a 1-day lead time. Vertically stacking each individual ensemble member flood map and adding vertically across every grid cell combines all ensemble members into a single flood map (all flooded grid cells are set to 1) showing where flooding is possible across all members (ens_{all}). A spatial median flood map is created (ens_{median}) where 26 members or more predict flooding at a particular grid cell location. Each of the ensemble

410   member flood maps for the domain (Fig. 2) are plotted in Figure 4 along with ens_{all}, ens_{median} and the SAR-derived flood map.
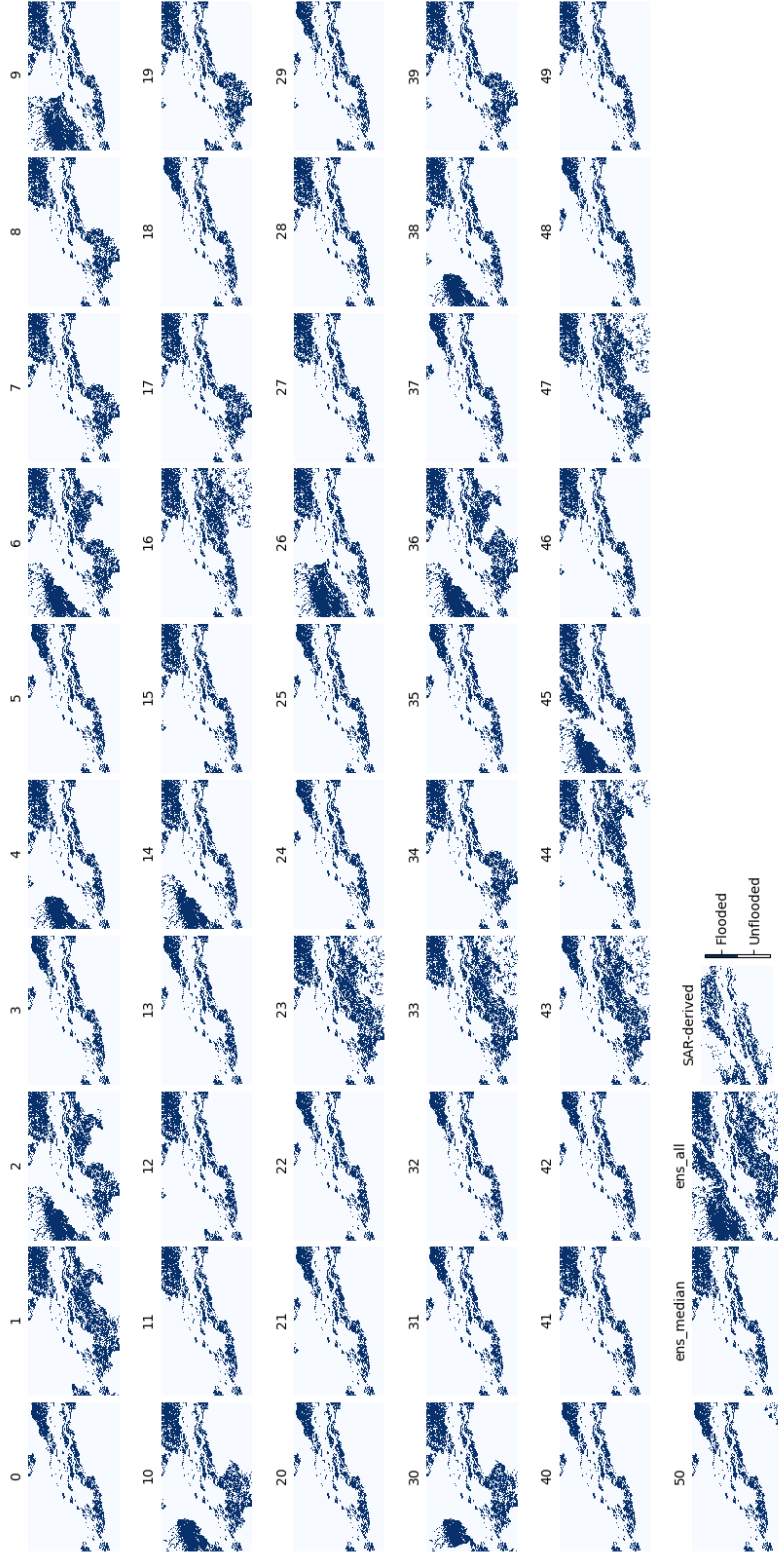
Figure 4. Brahmaputra River, Assam region, August 2017. 51 ensemble member forecast flood maps (labelled 0 to 50), ens_{median} and ens_{all} all at 1-day lead time and the Sentinel-1 SAR-derived flood map.

Figure 5 shows the amalgamated probabilistic ensemble forecast indicating the probability of flooding at each grid cell location. This was produced by vertically stacking each ensemble member flood map and adding vertically the number of flooded cells at each grid cell location across all ensemble members. The total is divided by 51 to calculate the probability.

415 Dark blue colours near to the central river channel indicate agreement between all ensemble members and 100% forecast probability of flooding, lighter colours to the north of the river indicate a low probability of flooding.
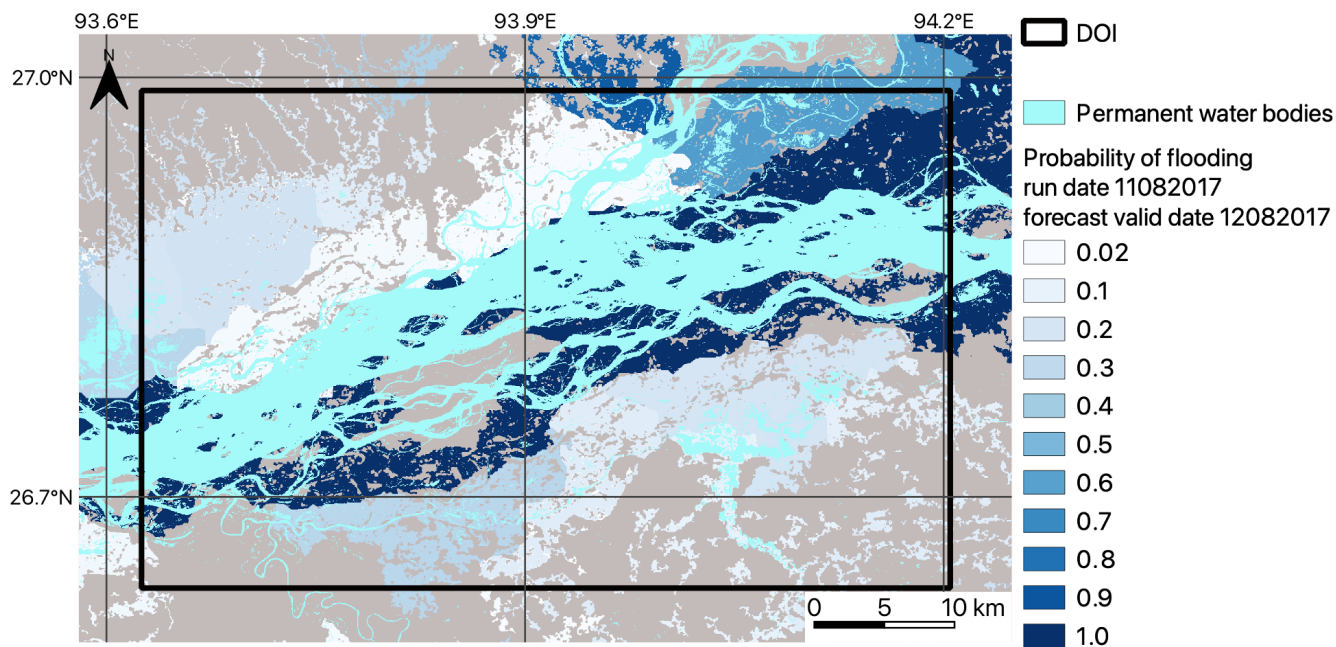
Figure 5. Brahmaputra River, Assam region, August 2017. Colour shading from white (low) to dark blue (high) indicate the forecast probability of flooding based on a 1-day lead time, 51 ensemble member flood map forecast for the Brahmaputra River in the Assam region, August 2017. ~~Dark grey areas are unflooded.~~ (Note map background is grey.)

4 Results and discussion

To demonstrate an application of our new spatial scale approach to both ensemble forecast flood map evaluation of forecast skill and the spatial spread-skill relationship, we apply the methods outlined in Section 2 to the flooding case described in Sec-

420 tion 3.1. First, in Section 4.1 we verify the full ensemble using a spatial scale approach to calculate a skilful scale of agreement between each ensemble member and the SAR-derived flood map (Fig. 2) along with the combined ensemble (ens_{all}) and the ensemble spatial median (ens_{median}). We evaluate the location specific spatial skill of the ensemble by calculating categorical scale maps (Section 4.2) for ens_{all}, ens_{median} and a best and worst case ensemble members determined by the skilful scale

calculated in Section 4.1. In Section 4.3 we evaluate the spatial predictability of the full ensemble and show this on our new

425 *Spatial Spread-Skill (SSS)* map, indicating regions where the ensemble is over-, under- or well-spread.

4.1 Ensemble spatial scale evaluation

Here we investigate how a scale-selective approach can be useful for extracting meaningful information from a flood map ensemble forecast where multiple forecast flood maps represent equally likely flooding scenarios (Fig. 4). A minimum skilful

430 scale (where $FSS > FSS_T$) has been calculated for each individual member flood map, ens_{all} and ens_{median}. The results in Figure 6 show that individual ensemble member spatial skill varies considerably with FSS at grid level ranging from 0.35 to 0.59. One member ens_1, which would usually be disregarded as an outlier due to its low probability, outperformed all other members significantly with a skilful scale achieved at a neighbourhood size of $n = 3$. The combined ens_{all} showed more skill at grid level ($n = 1$) and smaller neighbourhood sizes compared with ens_{median}, both however exceeded FSS_T at $n = 41$,

435 or 600 m. At neighbourhood sizes greater than $n = 41$, ens_{median} outperformed ens_{all}. ~~An average agreement discrepancy distance of more than 600 m may appear large, however it is worth remembering the magnitude of this flood event in which the flood width exceeds tens of kilometers.~~ There is a cluster of members showing similar skill to ens_{median} and ens_{all} and a second cluster, with more ensemble variation but indicating lower skill than the first cluster. The ens_{median} and ens_{all} flood maps outperform the second cluster, however there are individual members with a higher spatial skill score compared to ens_{median}

440 and ens_{all}. These results show that all ensemble member flood maps, including outliers, should be considered individually as possible future flooding scenarios. Spatial variations across individual ensemble members (see Fig. 4 ens_1 compared to ens_{median}) indicate that it is not meaningful to consider only the ensemble median flood map to represent the information within the full ensemble.

445 ## 4.2 Ensemble spatial predictability

The scale-selective skill scores calculated for different aspects of the ensemble forecast give a domain-averaged score and skilful scale. To understand location specific spatial predictability of the ensemble forecast, categorical scale maps are calculated and presented in Figure 7. These show how the agreement scale (Section 2.2) varies with location for (a) ens_{all}, (b) ens_{median}, (c) ens_1, the 'best' performing ensemble member and (d) ens_{21}, the 'worst' performing ensemble member. The

450 ensemble summary map, ens_{all} (Fig. 7 (a)) captures most of the observed flooding (in grey) with small regions of under-prediction (red). However, as you might expect to see by including every potential flooding realisation there are significant regions of over-prediction (blue) or false alarm. The region of over-prediction to the south of the river is less evident in the ens_{median} categorical scale map (Fig. 7 (b)) which performs worse to the north by under-predicting flooding here. This flooding is captured well by ens_1 (Fig. 7 (c)) and in particular close to a confluence zone where the Subansiri River joins the

455 Brahmaputra (grid cell location (1100, 250)). This ties in with the high rainfall totals accumulated just to the north of this region associated with localised very heavy rainfall (Floodlist, 2017). A region of under-prediction at grid cell location (750,
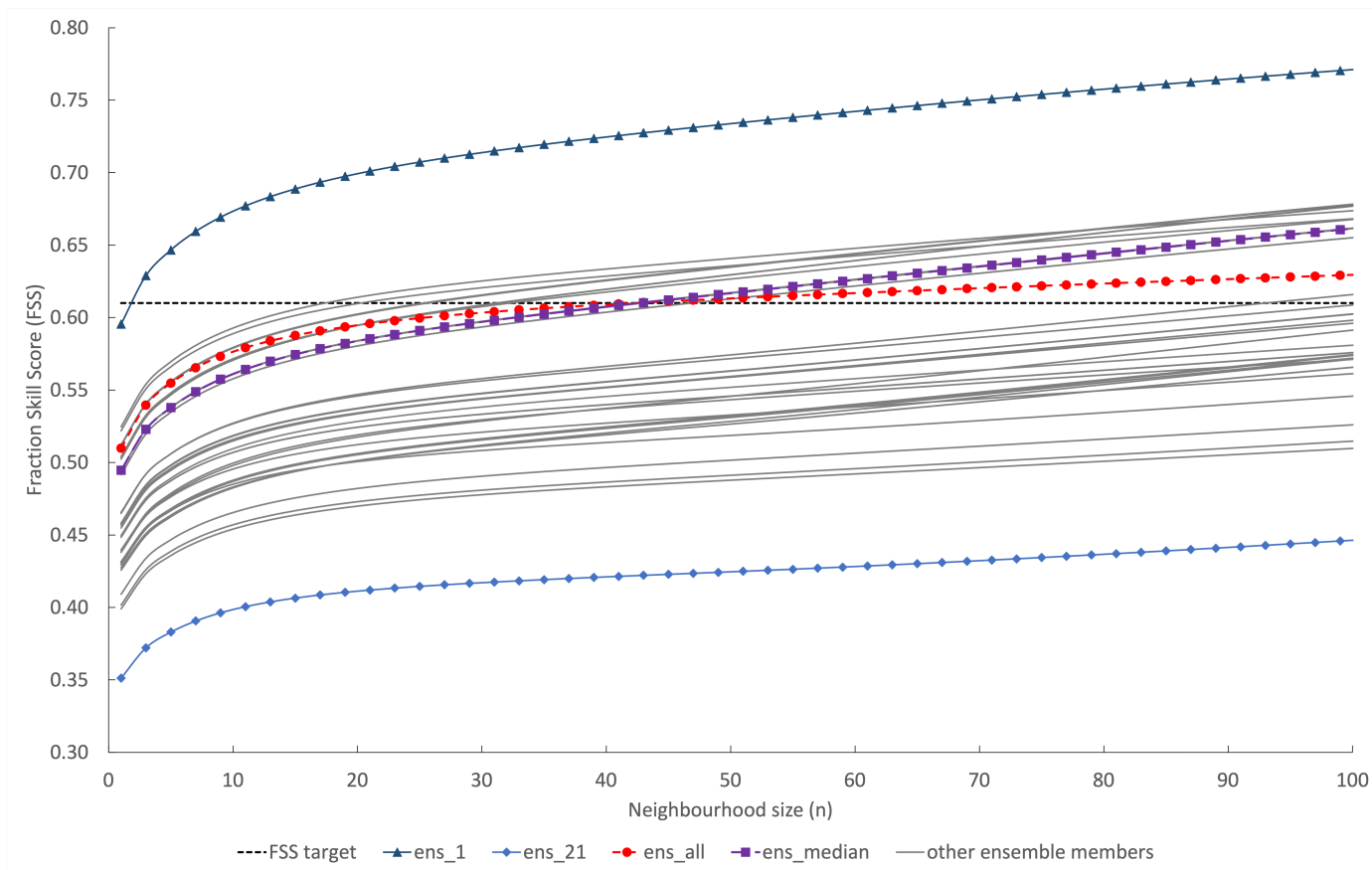
Figure 6. The spatial skill of each individual ensemble member forecast flood extent is evaluated along with the ens_{median} (a spatial median where 26 or more members predict flooding at a grid cell location) and ens_{all} (flooded grid cells from all ensemble members are combined). The FSS is calculated at increasing neighbourhood sizes to determine the scale at which the forecast becomes skilful at capturing the observed flood (FSS_T).

750) is missed by all members. A closer inspection of the DTM or surface features included/excluded in the hydraulic modelling, such as embankment heights, may indicate how this modelling could be improved. The 'worst' performing ensemble member ens_{21} (Fig. 7 (d)) accurately predicts flooding closer to the river channel, however under-prediction to the north along with over-prediction to the south show where the forecast was inaccurate. Categorical scale maps enable different ensemble flood map presentations to be evaluated so that the most useful presentation method can be determined for a particular flooding situation.
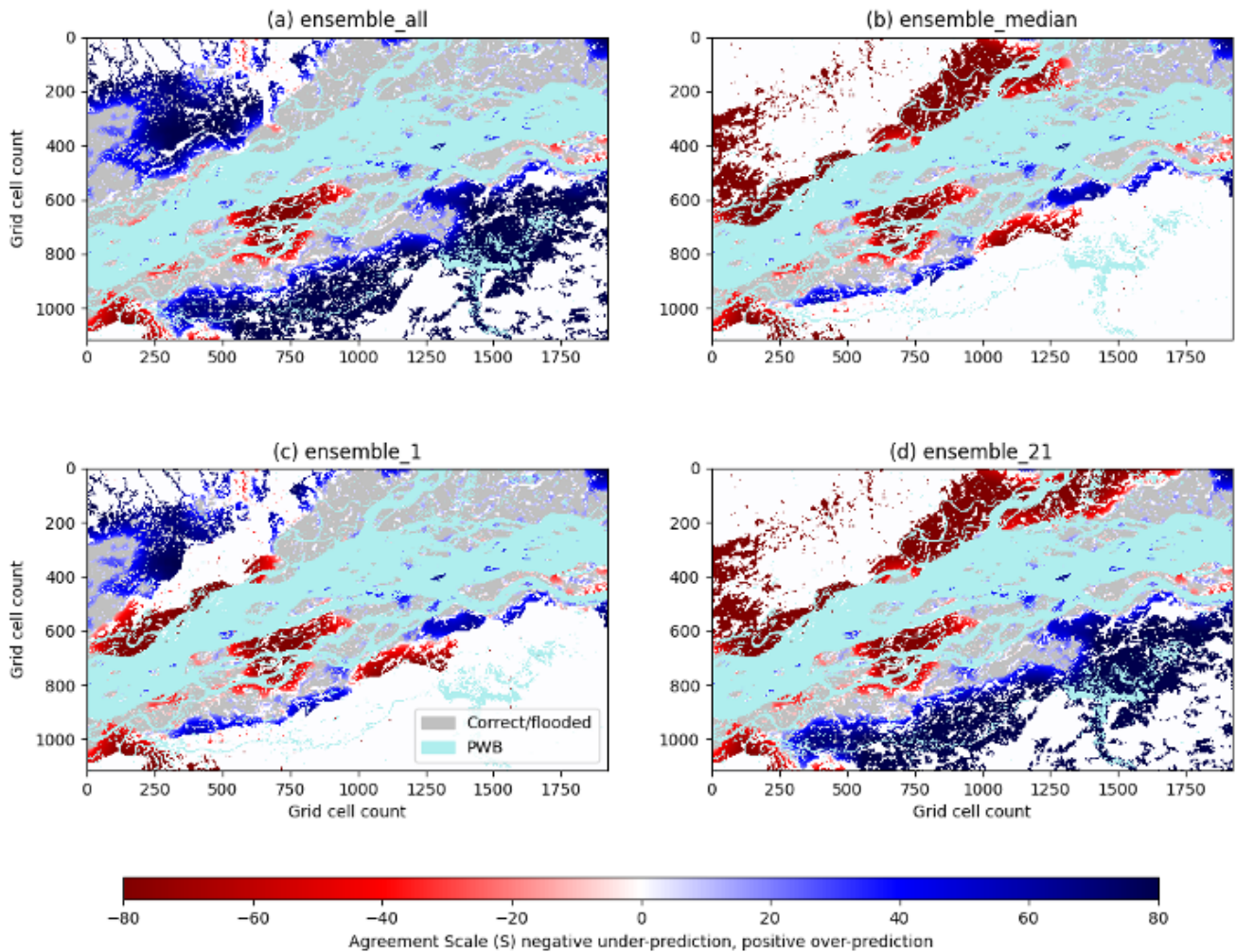
Figure 7. Brahmaputra River, Assam region, August 2017. Categorical scale maps for (a) ens_{all} (flooded grid cells from all ensemble members are combined), (b) ens_{median} (a spatial median where 26 or more members predict flooding at a grid cell location), (c) individual ensemble member 1 and (d) individual ensemble member 21. Red areas indicate where the forecast is under-predicted and blue regions represent over-prediction. The colour shade gives the scale of agreement between the forecast and the observed flooding with lighter shading indicating a smaller agreement scale. For georeferencing see Figure 5, each grid cell is 30 m x 30 m.

4.3 Ensemble spatial spread-skill

To evaluate the location specific skill of the full ensemble, one option would be to calculate 51 categorical scale maps from
465 each individual member flood map (Fig. 4). This approach maintains the spatial detail held within each of the ensemble member flood maps, although does require multiple visual comparisons to be made by the flood forecaster or modeller, which takes

time and effort. Making comparisons across the different ensemble member flood maps in Figure 4 provides a demonstration of these forecasting difficulties. Further, the categorical scale maps do not evaluate the ensemble spatial spread. To address this, we ~~present a new~~ develop a summary ensemble Spatial Spread-Skill (SSS) map (Fig. 9) showing the spread-skill of the full

470   ensemble forecast and keeping the location specific detail. All ensemble members are included in this analysis which evaluates both the spatial skill and the ensemble spatial spread of the forecast against the remotely observed flooding extent.

    Figure 8 shows how the average-ensemble/ensemble-agreement scale in (a) ~~i.e.~~ $S_{ij}^{A(\overline{mm})}$ calculated at each grid cell (representing ensemble *spread*) compares with the average ensemble/observed scale in (b) ~~i.e.~~ $S_{ij}^{A(\overline{mo})}$ (representing ensemble *skill*)

475   along with the hexbin scatter plot in (c) which compares (a) and (b) to indicate the spatial spread-skill of the forecast. The hexagonal tessellation is used so that the distances along the hexbin diagonal are on the same scale as those along the ~~abscissa and ordinate~~ x and y-axis. For a perfect ensemble forecast the average agreement scale between ensemble members should match the agreement scale between the ensemble forecast and observed flood map, i.e. they should align along the 1:1 line. The SSS map plots the difference between the ensemble/ensemble and the ensemble/observed average agreement scales at

480   each grid cell (Fig. 9) and indicates where the spatial spread-skill is over-, under-, or well-spread. Three numbered areas (Fig 8(a)) identify three different ensemble spread-skill relationships. Area 1 shows that the agreement between ensemble members is close, but that they disagree with the observed flooding extent. This is displayed in orange shades as an under-spread or miss region on the SSS map, Figure 9. This is the region close to the confluence area described in Section 4.2. Recall that in this region, most ensemble members did not predict the flooding that occurred with the exception of one ensemble member (ens_1).

485   In area 2 on Figure 8, both (a) and (b) are in agreement at grid level, which indicates the ensemble is well-spread; these are shown in white on Figure 9. Away from the miss and well-spread regions in Figure 8, the overall visual impression is that the ensemble spread-skill lies below the 1:1 line and is over-spread, indicated by area 3. This corresponds to purple shading on the SSS map (Fig. 9). Overall Figure 8 tells us that the spread-skill relationship for this example case study is not uniform across the domain but is in fact location specific. ~~The SSS map displays where the spatial spread-skill is over-, under-, or~~

490   ~~well-spread.~~ Using the spatial spread-skill relationship shown on the ensemble SSS map ~~From this~~ we can infer how well the ensemble forecasting system encompasses the multiple sources of uncertainty and how meaningful the probabilistic ensemble ~~predictability~~ forecast of flood inundation actually is. This is a ~~important~~ useful evaluation tool for ~~all catchments and becomes essential for~~ validating flood forecasts in un-gauged or partially gauged rivers. A simulation library approach, like the Flood Foresight maps used here, relies on the accuracy of the return period thresholds set, the (ensemble) forecast streamflow and the

495   accuracy of the flood inundation map for a given streamflow. The forecast evaluation approaches presented here enable these system attributes to be evaluated even where observed streamflow is limited or erroneous. The SSS map summarises the whole ensemble, which makes it useful for forecasters attempting to convey uncertainty information to decision makers, highlighting regions where there is high/low confidence in the forecast.
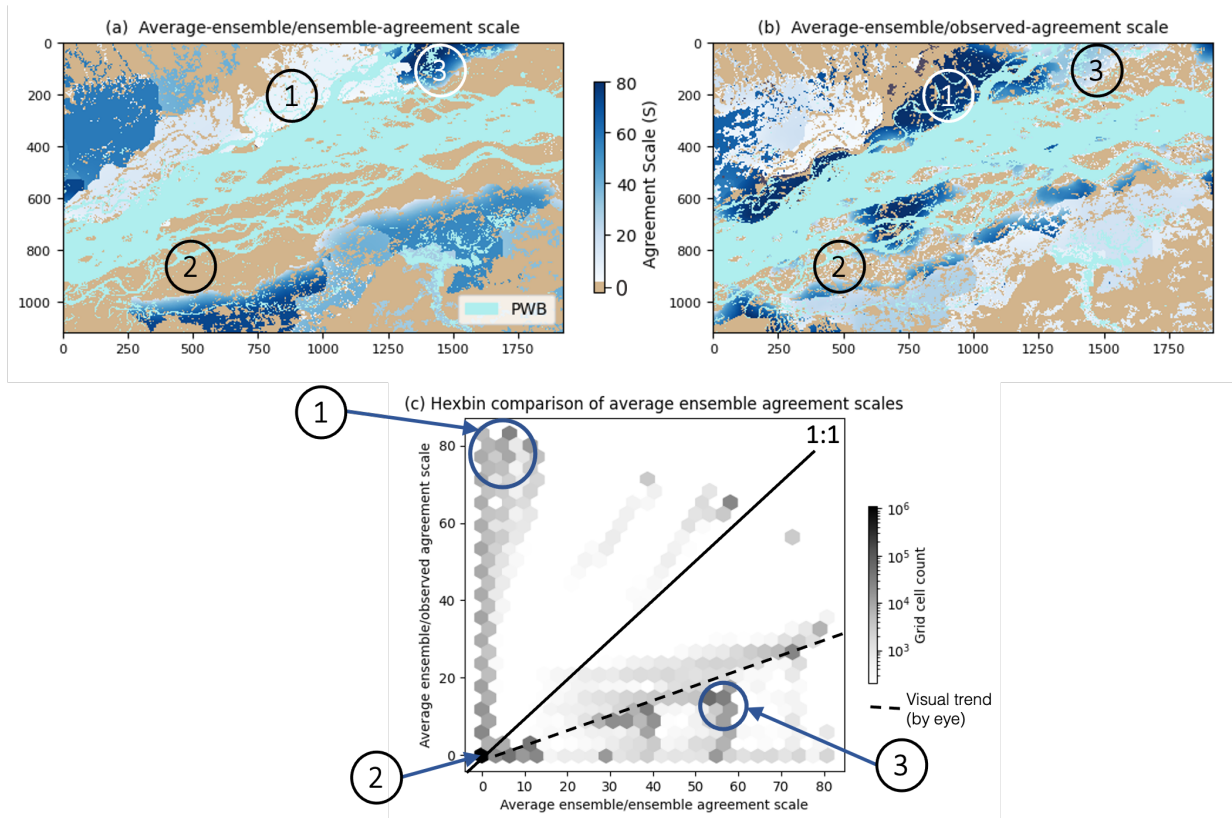
Figure 8. ~~The average agreement scale map of each unique pair of forecast ensemble flood maps is plotted in (a) and between each ensemble member compared against the observed SAR-derived flood map in (b). A binned histogram scatter plot compares (a) and (b) to indicate the spatial spread-skill of the forecast ensemble. For a perfect ensemble forecast the average agreement scale between ensemble members should match the agreement scale between the ensemble forecast and observed flood map, i.e. they should align along the 1:1 line. The main trend from the whole domain is indicated with a dashed black line which shows that generally the forecast ensemble is over-spread (e.g. area 3), however there are variations in the spatial spread-skill across the domain with regions that are under-spread and misses (e.g. area 1) along with regions where all members show accurate spatial predictability of the observed flooded/unflooded grid cells (e.g. area 2) and the ensemble is considered well-spread.~~ Brahmaputra River, Assam region, August 2017. (a) The average agreement scale map of each unique pair of forecast ensemble flood maps and (b) between each ensemble member compared against the observed SAR-derived flood map. (c) A binned histogram scatter plot compares (a) and (b) to indicate the spatial spread-skill of the forecast ensemble. Areas labelled (1, 2 and 3) are discussed in Section 4.3. For georeferencing of (a) and (b) see Figure 5. Note PWB means permanent water bodies.
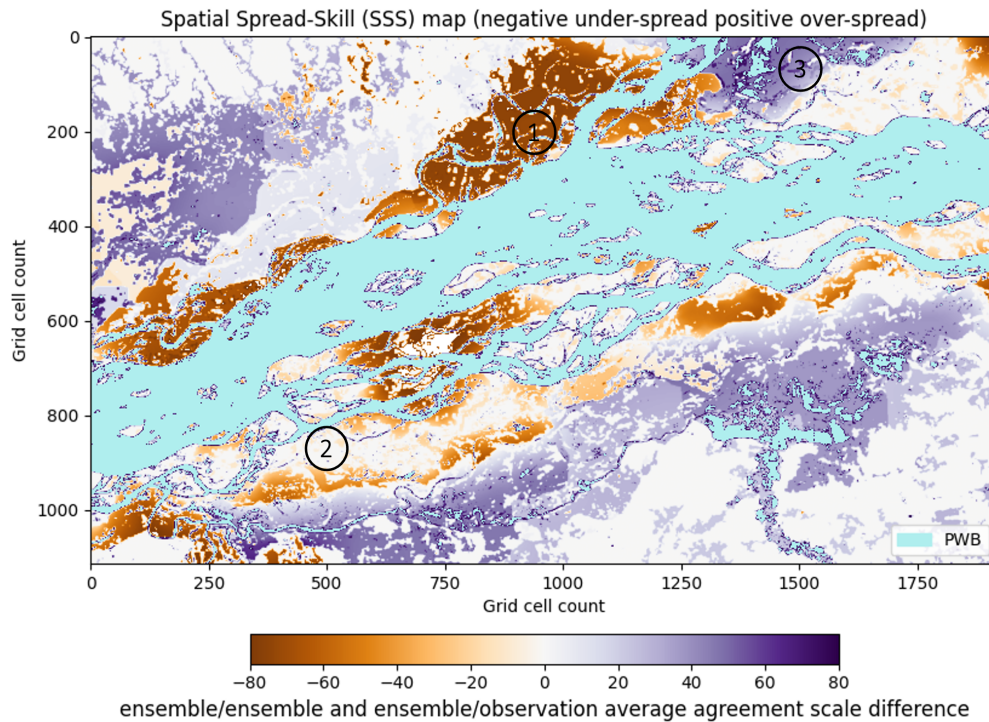
Figure 9. Brahmaputra River, Assam region, August 2017. The Spatial Spread-Skill (SSS) map shows the difference between the ensemble/ensemble and the ensemble/observed average agreement scales at each grid cell. Negative values (orange) ~~areas~~ indicate where the ensemble is under-spread and positive values (purple) ~~areas~~ indicate where the ensemble is over-spread. White areas ~~areas~~ ~~show that the~~ indicate where the average agreement scales match and indicate good spatial spread-skill. ~~Lighter shades show the average agreement scales are more closely matched with very dark shades indicating over- (dark purple) or under- (dark orange) prediction by the ensemble forecast.~~ Areas labelled (1, 2 and 3) are discussed in Section 4.3. For georeferencing see Figure 5. Note PWB means permanent water bodies.

5   Conclusions

500 ~~The uncertainty information given by forecast ensemble flood maps is determined in large part by initial condition perturbations at the top of the~~ Differences between ensemble members in ensemble forecast flood map systems are mostly driven by initial condition perturbations at the top of the hydro-meteorological forecast chain within the NWP system. Presently, there is limited understanding or evaluation of how these meteorological uncertainties link to mapped flooding predictability, which involves additional ~~where multiple other~~ sources of uncertainty~~exist~~. An evaluation of the spatial predictability and the spread-

505 skill relationship of the ensemble flood map forecast ~~will enable~~ provides an improved understanding of the performance of the forecast system. Uncertainties in other parts of the forecast chain are not truly represented by the ensemble flood maps and evaluating ~~their skill~~ the spatial spread-skill of the flood maps is important for understanding the likelihood of flooding that the ensemble flood maps capture. In this paper, we present a new scale-selective approach to assess the spatial predictability and spread-skill of an ensemble flood map forecast by comparing against a satellite SAR-derived observation of flooding extent.

510 By calculating a skilful scale at each grid cell for every unique ensemble member pair we can determine the ensemble *spatial spread*, and between every ensemble member and the SAR-derived flood map we can determine the ensemble *spatial skill*. The hexbin scatter plot summarises the spread-skill relationship so that a trend across the whole domain can be assessed. The difference between these skilful scales can be mapped onto our new Spatial Spread Skill (SSS) map which ~~tells us~~ shows for each specific location in the domain whether the ensemble is over-, under- or well-spread. The methods are applied to an

515 example flooding event of the Brahmaputra River in the Assam region of India in August 2017.

In operational practice there are multiple options of ensemble flood map presentation type such as presenting the ensemble median or other exceedance probability for delivery to end-users and decision makers. ~~Using a scale-selective approach we have evaluated the performance of individual ensemble members, a combined total ensemble and the spatial ensemble median~~

520 ~~compared to a SAR-derived observation of flooding extent.~~ An important aspect of developing an inundation flood forecasting system is to determine the most useful way to present a spatial ensemble forecast. Using a scale-selective approach we have evaluated the performance of individual ensemble members, a combined total ensemble and the spatial ensemble median compared to a SAR-derived observation of flooding extent. Other options could be to exclude ensemble member outliers, to spatially cluster similar ensemble members into groups of flooding extent or to present a most likely, best and worst case ensem-

525 ble flood map. Whichever presentation method is chosen, this should be fully explored using the spatial spread-skill methods described here to evaluate the ensemble performance of historical flooding events. We found for this example flooding event that one ensemble member significantly outperformed the combined and median flood maps and that potentially in some ~~cases~~ flood forecasting scenarios this member would have been excluded as an outlier. ~~This tells us that the~~ The categorical scale maps show that the ensemble spatial median could miss vital flooding information and that all members should be considered

530 as potential future flooding scenarios.

Through mapping the spatial-spread skill relationship, which varies with location, links can be made between the spatial variations in spread-skill and the physical characteristics of the flooding event. We found that one ensemble member outperformed all others in a region close to a confluence zone and nearby observed heavy rainfall. The region correlates to an area of under-spread ensemble members indicating that not enough members were predicting flooding here. Future studies could investigate the physical processes further using the methods presented here. The ensemble flood map spatial spread-skill is investigated in the context of a particular physical process (such as rainfall intensity/location or an improved aspect of the hydrological model such as antecedent soil moisture) and how these uncertainties translate to the probabilistic flood map forecast. An understanding of the spatial predictability is particularly important for un-gauged catchments where the calibration of both forecast streamflow and return period thresholds (used to select the simulation library flood map) ~~is currently not possible~~ are rarely practiced routinely. Ideally, in operational practice, these spatial verification approaches including the categorical scale and SSS maps could be calculated and stored routinely as flooding events coincide with SAR-derived or other remotely observed flood maps to build up a verification catalogue/database. This ~~evaluation could~~ database could then be used to investigate the spatial spread-skill model performance under different scenarios such as forecast lead time, month or season, or flood type. More locally, the impact of an improved DTM or the inclusion of a Digital Surface Model (DSM) or other surface features in the hydraulic model such as embankments could be considered. Over time, ~~an evaluation~~ such a database would improve our understanding of the spatial predictability of an ensemble flood map system and how well the uncertainties present are represented by the ensemble forecast.

Code and data availability. The functions used to evaluate the ensemble forecast flood maps using a scale-selective approach along with the SAR-derived flood maps are available on the following Zenodo page: https://doi.org/10.5281/zenodo.6603101 (Hooker et al., 2022b). The forecast flood maps from the JBA Flood Foresight system are commercial data used under license for this study.

Author contributions. JB and KS provided the forecast data. HH wrote the algorithms and ran the experiments, with input from SD, DM, JB and KS. HH prepared the manuscript with contributions from all the co-authors.

Competing interests. The authors declare that no competing interests are present.

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