Seismogenic potential and tsunami threat of the strike-slip Carboneras Fault in the Western Mediterranean from physics-based earthquake simulations

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Abstract. Strike-slip fault ruptures have a limited capacity to generate vertical deformation, and for this reason they are usually dismissed as potential destructive tsunami sources. At the western tip of the western Mediterranean, in the Alboran Sea, tectonics is characterized by the presence of large transcurrent fault systems and minor reverse and normal faults in a zone of diffuse deformation. The strike-slip Carboneras fault is one of the largest sources in the Alboran Sea, and therefore, with the greatest seismogenic capacity. It is also one of the active structures with higher slip rates in the Eastern Betic Fault Zone and has been proposed as source of the damaging 1522 (M6.5; Int. VIII-IX) Almeria earthquake. The dimensions and location of the Carboneras fault imply a high seismic and tsunami threat. In this paper we present tsunami simulations from seismic sources generated with physics-based earthquake simulators. We have generated a 1 Myr synthetic seismic catalogue consistent on 773,893 events with magnitudes ranging between $M_W$ 3.3 and 7.6. From these events we have selected those sources producing a potential energy capable of generating a noticeable tsunami, being earthquakes with magnitudes ranging from 6.71 to 7.62. The Carboneras Fault has the capacity to generate locally damaging tsunamis, however, on a regional scale its tsunami threat is limited. The frequency – magnitude distribution of the generated seismic catalogue reflects the variability of magnitudes associated to the rupture of the entire fault, departing the upper limit from the classical Gutenberg-Richter potential relation showing a bell-shaped distribution. The inter-event time for the maximum earthquake magnitudes is usually between 2000 and 6000 years. The use of physics-based earthquake simulations for tsunamigenic sources allows a robust characterization of the scenarios, allowing a qualitative leap in their parametrization.

1 Introduction

Tsunamis are generated by any natural event that involves an immediate alteration of the elevation of the free surface of the sea. This alteration may be due to events that directly alter the sea surface (usually meteorological, meteoric or volcanic events) or by geological events that abruptly modify the ocean floor (earthquakes or submarine landslides). Earthquakes are the geological events that most often generate destructive tsunamis (NGDC, 2022), and this ability depends on their mode of seismic rupture (e.g., Burbidge et al., 2015; Geist, 1998; Gibbons et al., 2022). The rake, the orientation of the slip vector on
the fault plane during seismic rupture, is one of the most determining parameters in the generation of tsunamis, presenting the thrust and normal faults, with dip-slip rupture, the greatest capacity. On the other hand, the strike-slip ruptures, with rakes close to the horizontal, have a limited capacity to generate vertical deformation on the seafloor, and for this reason they are usually dismissed as potential destructive tsunami sources.

Although the lower capacity of strike-slip faults to generate tsunamis is a proven fact, it is not negligible, as has been numerically demonstrated (Elbanna et al., 2021; Legg et al., 2003; Tanioka and Satake, 1996; Ulrich et al., 2019) and observed (Frucht et al., 2019; Gusman et al., 2017; Heidarzadeh et al., 2017; Ho et al., 2021), occasionally linked to submarine landslides also (Hornbach et al., 2010; Xu et al., 2022). This is of special relevance in local sources, where the dispersion of the tsunami waves is low, and the local fault complexities and rupture-slip variations are key parameters on tsunami impact (Geist, 2002).

The study of tsunami hazard, due to the scarcity of events from a statistical point of view, is frequently approached from numerical modelling. These models are usually based on the simulation of tsunamis generated by ruptures of simple, rectangular, fault planes with homogeneous slip. Codes based on the Okada (1985) or Mansinha and Smylie (1971) equations are used to obtain the seafloor deformation produced by the earthquake.

However, the variability in the slip distribution on the fault plane is a fundamental parameter to understand the occurrence of maximum amplitudes in destructive events (Fujii et al., 2011; Gusman et al., 2012; McCloskey et al., 2008; Satake et al., 2013; Yamazaki et al., 2011). This variability is of special relevance in local sources, which if modelled as simple ruptures, cannot capture the complexity of the earthquake rupture process. Wave propagation and flooding are highly non-linear processes, very sensitive to local variations in shallow waters. To overcome this limitation, methodologies have been proposed based on the stochastic (or random) generation of slip patterns in faults (Goda et al., 2015; Lavallée et al., 2006; Løvholt et al., 2012; Mai and Beroza, 2002), or on the use of physical dynamic rupture models for particular events (Elbanna et al., 2021; Kozdon and Dunham, 2013; Madden et al., 2021; Maeda and Furumura, 2013; Ryan et al., 2015; Wendt et al., 2009; Wilson and Ma, 2021).

Our approach is based on the use of physics-based earthquake simulators (Rundle, 1988). These simulators have been developed in recent decades in order to overcome the temporal limitation of the instrumental seismic catalogue in probabilistic seismic hazard assessment (PSHA) (Robinson et al., 2011; Shaw et al., 2018), especially in the characterization of large events. Through the development of models based on earthquake physics, synthetic catalogues of hundreds of thousands of years can be generated whose characteristics reflect those of the instrumental catalogue but incorporating the long-term evolution of the seismic cycle and the complex interactions of fault systems (Console et al., 2018, 2015; Robinson and Benites, 1995). Moreover, recent development of numerical codes based on the rate-and-state constitutive law for fault slip and frictional behaviour (Dieterich, 1992, 1995) allows not only the modelling of long-term seismic cycle deformation, but also the short-term rupture process based on a quasi-dynamic physical approximation to the rupture propagation (Richards-Dinger and Dieterich, 2012) producing earthquake ruptures similar to those in fully dynamic models (Whirley and Engelmann, 1993).

The western Mediterranean presents a complex tectonic history and context (e.g. Chertova et al., 2014; Gómez de la Peña et al., 2021; Romagny et al., 2020); and is characterized by the development of a series of arcuate Fold-and-Thrust Belts surrounding back-arc formed deep-water basins (Faccenna et al., 2004; Rosenbaum and Lister, 2004). The current rate of shortening between the Nubian and Eurasian plates in the western Mediterranean is approximately 5 mm/yr (Serpelloni et al.,

At the western tip of the western Mediterranean, in the Alboran Sea, tectonics is characterized by the presence of large transcurrent fault systems and minor reverse and normal faults in a zone of diffuse deformation (Ballesteros et al., 2008; Martínez-García et al., 2013). These structures, formed during the Miocene in a transcurrent and mainly extensional tectonic context, were latter reactivated in a transpressional post-tortonian setting (Bourgois et al., 1992; Comas et al., 1992; Do Couto et al., 2016; Herrero-Barbero et al., 2020; Martínez-García et al., 2017). Although the reverse faults associated with the Alboran ridge seem to have the greatest tsunamigenic potential (Álvarez-Gómez et al., 2011a, b; Gómez de la Peña et al., 2022), the mainly strike-slip faults (Yusuf, Al -Idrisi and Carboneras) are the ones with the greatest length and, therefore, the greatest seismogenic capacity (Somoza et al., 2021).

The Carboneras fault is a left-lateral transpressive structure oriented N50-60ºE with a length of ~150 km, most of them offshore (Gràcia et al., 2006; Somoza et al., 2021). It is one of the active structures with higher slip rates in the Alboran Sea and in the Eastern Betic Shear Zone (Masana et al., 2018; Moreno et al., 2015), a fault system that crosses the SE of the Iberian Peninsula forming a tectonic corridor on which a significant density of population and industry is based (Figure 1). Moreover this fault has been proposed as source of the 1522 Almeria earthquake, a damaging earthquake that reached intensities of VIII-IX in the city of Almeria (Martínez Solares and Mezcua, 2002), and possibly related to a local tsunami (Reicherter and Hübscher, 2007; Reicherter and Becker-Heidmann, 2009).
The dimensions and location of the Carboneras fault poses a high seismic and tsunami risk potential. According to previous studies this fault has the capacity to produce events with magnitudes up to 7.1 - 7.4 (Álvarez-Gómez et al., 2011a; García-Mayordomo et al., 2017; Gómez de la Peña et al., 2022; Gracia et al., 2006) with mainly horizontal left-lateral component but some reverse dip-slip motion too (Moreno et al., 2015). Although the tsunami simulations done to date (Álvarez-Gómez et al., 2011a, b; Gómez de la Peña et al., 2022) discard major damaging events, the simplicity and assumptions of such simulations must be re-evaluated.

In this paper we present tsunami simulations based on the generation of a synthetic catalogue of earthquakes whose characteristics resemble the instrumental and historical seismicity recorded in the area (Herrero-Barbero et al., 2021). From these simulations we make estimates of maximum wave elevations for seismogenic tsunamis and recurrence intervals for significant events in order to reassess the threat posed by the Carboneras fault in the context of the Alboran Sea and the western Mediterranean.

2 Earthquake ruptures simulation

Reproducing a long-term catalogue of earthquake ruptures requires a computationally efficient approach to the physical processes that control earthquake occurrence. Earthquake simulators (Rundle, 1988; Tullis et al., 2012; Ward, 2000) are computer codes that use fault geometry, stress interactions and frictional resistance to produce long earthquake sequences, overcoming the completeness limitations of the instrumental record. The multi-cycle earthquake simulations necessarily adopt approximations to elastodynamics to make computation feasible and, unlike fully dynamic single-event simulators (see e.g., Harris et al., 2018), seismic waves are not computed. Even so, recent modelling enhancements have successfully extended their use in more complex fault geometries (Field et al., 2014; Shaw et al., 2018) and for different representations of fault friction, rheology and stress transfer (Pollitz, 2012; Richards-Dinger and Dieterich, 2012; Sachs et al., 2012; Schultz et al., 2018; Ward, 2012); therefore, a better validation of the quasi-dynamic part of the seismic cycle is achieved.

Our approach is based on the application of the RSQSim earthquake simulator (Dieterich and Richards-Dinger, 2010; Richards-Dinger and Dieterich, 2012). The physics-based RSQSim code reproduces earthquakes into a fully interacting 3D fault model. It performs the physical processes leading rupture nucleation and propagation through a boundary element formulation that incorporates rate- and state-dependent friction based on Dieterich (1995). Given that this is a quasi-dynamic approximation, long-term stress accumulation and earthquake slip at each fault element is separated efficiently into three sliding states: 0) locked, 1) nucleating, and 2) sliding. The result is a long synthetic earthquake catalogue including a comprehensive and detailed record of complex earthquake ruptures with heterogeneous slip. Recent results obtained using the RSQSim code are promising in relation to potential practical applicability (Chartier et al., 2021; Herrero-Barbero et al., 2021; Howarth et al., 2021; Shaw et al., 2018).

The 3D structure of the Carboneras fault is integrated in a more complex fault model of the Eastern Betic Fault Zone (Figure 2), which includes kinematic properties of the main faults, such as slip rates and rakes (Herrero-Barbero et al., 2021). RSQSim simulations have been run on this fault system model of triangular elements with 1 km² resolution and fault depths between
Figure 2. a) 3D fault model used for the synthetic seismic catalogue simulation; b) example of a $M_W$ 6.85 event; c) example of a $M_W$ 7.27 event; d) example of a $M_W$ 7.62 event.

8 and 12 km. The Carboneras fault is defined in the model as a sub-vertical (dipping 85° SE) sinistral strike-slip structure (Bousquet, 1979; Masana et al., 2018; Moreno et al., 2015; Rutter et al., 2012), N45°-60° strike, and segmented into two fault sections: an onshore northern section, partially offshore at the SW and connecting with the Palomares fault at the NE; and a totally offshore southern section. In the northern Carboneras fault, an average lateral slip rate of 1.2 mm/yr is estimated for the last 110-130 ka (Moreno et al., 2015). In the southern section Moreno (2011)estimated a strike-slip rate of 1.3 mm/yr, which is consistent with the northern section and with geodetic lateral slip rates of 1.3±0.2 mm/yr (Echeverria et al., 2015).

Besides the input kinematic data, the simulations are governed by rate- and state-dependent friction parameters, a and b, that reproduce the effect of the velocity-change on the coefficient of friction (Dieterich, 1979; Ruina, 1983). These frictional parameters have a notable impact on the slip distribution and spatio-temporal clustering (Noda and Lapusta, 2013; Richards-Dinger and Dieterich, 2012; Scholz, 1998). We define reference rate-and-state values based on experimental data taken from a nearby location in the fault zone (Niemeijer and Vissers, 2014; Rodriguez Escudero, 2017) to generate multiple test catalogues. The aims of the testing process were to match frequency distributions with a Gutenberg-Richter b value close to 1.0±0.1, and to correlate the synthetic seismicity with instrumental and paleoseismic data (Herrero-Barbero et al., 2021). Finally, a preferred set of input model parameters is selected for the best-fit catalogue: rate-and-state friction parameters $a=0.001$ and $b=0.010$; a steady-state friction coefficient $\mu_0=0.6$; a depth-variable normal stress with a 20 MPa/km gradient, and a b-value of 1.05 (Figure 3). Defined frictional parameters in this study entail a totally seismogenic behaviour of this fault system, although Faulkner et al. (2003) also suggested possible creeping sections in the Carboneras fault zone due to the mechanical heterogeneity of its fault gouge.
According to the selected input model parameters, a 1 Myr-synthetic earthquake catalogue has been generated (Figure 3), from which the first 2000 years have been discarded to avoid artefacts until the simulation stabilizes. In total, 773,893 events have been obtained, with a magnitude range of $3.3 \leq M_W \leq 7.6$. The Carboneras Fault is the seismogenic source that generates the most frequent synthetic seismicity, with almost a 30% of the events in the catalogue, of which 0.6% of total events are $M_W \geq 6$ earthquakes. For $6.5 \leq M_W < 7.0$ events, the most frequent inter-event time intervals range between 800 and 6,000 years (Figure 4), excluding the aftershocks. Logically, the earthquake frequency decreases as the magnitude increases (Figure 4). However, from magnitude $M_W \geq 7.0-7.1$, the simulation shows an increase in the frequency of events, therefore the recurrence intervals of the most damaging $M_W \geq 7.0$ earthquakes would be shortened. The largest number of these major simulated ruptures in the Carboneras Fault is nucleated in the northern section, being physically capable to propagate a complete fault-length rupture. Between them, 115 ruptures are also transferred to a portion of the southern branch of the Palomares Fault (Figure 2d), increasing the rupture area and therefore the released seismic moment.
The epicentres of the generated events are not homogeneously distributed along the fault; being more frequent the generation of events at the tips of the sections and bending (Figure 5a). Towards the ends of the fault is also where the average magnitude is higher (Figure 5c). However, the maximum magnitude of the generated event does not show an important variation; being generated events with magnitudes M > 7.3 along the entire fault trace (Figure 5b).

### 3 Tsunami modelling

Simulations for seismic triggered tsunamis are based on modelling the deformation of the ocean bottom produced by the earthquake rupture. These models use analytical solutions in an elastic half-space to reproduce the behaviour of the upper crust. The most commonly used codes for this are often based on equations derived for rectangular dislocations (Mansinha and Smylie, 1971; Okada, 1985, 1992), which makes it difficult to model complex rupture geometries without incorporating numerical artefacts. To solve this problem other mathematical approaches and alternative algorithms have been developed, also using analytical equations, but for triangular dislocations (Gimbutas et al., 2012; Meade, 2007; Nikkhoo and Walter, 2015). In this work we have used the calculation algorithm developed by Nikkhoo and Walter (2015) for artefact-free triangular geometries.

To evaluate the potential of tsunami generation of the modelled earthquakes, we have initially selected events with magnitudes greater than 6.0; obtaining a total of 1344 events. Many of these events will not have the capacity to generate detectable
tsunamis on the coast, so to avoid an excessive computational load, we have filtered these pre-selected events based on the surface deformation generated. As the sea-floor deformation generated by the earthquake is usually transferred instantly to the elevation of the water free surface we can use it to directly estimate the event capacity to generate a tsunami.

Each earthquake rupture is characterized by its unique finite fault model composed by a number of triangular elements. The smaller events considered here, with magnitudes 6.0, are formed by a few tens of elements (∼40); while the biggest ones, with magnitudes of ∼7.6 are formed by the rupture of a few thousands of elements (up to 5279). In total we have modelled the rupture of 1150265 triangular elements for the 1344 finite fault models.

We have parametrized each sea-floor deformation modelled with the following quantities (Bolshakova and Nosov, 2011; Wessel, 1998) (Figure 6):

i) maximum uplift or water elevation

\[ \eta_{\text{max}} = \max[\eta_Z(x, y)] \]  

(1)

ii) maximum vertical displacement double-amplitude defined as

\[ A_\eta = \max[\eta_Z(x, y)] - \min[\eta_Z(x, y)] \]  

(2)

iii) displaced volume

\[ V = \iint_S |\eta_Z(x, y)|\,dS \]  

(3)

and iv) potential energy

\[ E_{ts} = \frac{1}{2}\rho g \iint_S \eta_Z^2(x, y)dS \]  

(4)

where \( \rho \) is the density of water (taken as 1038 kg/m\(^3\) (Borghini et al., 2014)) and \( g \) the acceleration due to gravity.

Nosov et al. (2014) analysed a series of tsunamis generated by earthquakes whose source were characterized with a finite fault model. They compared the modelled surface deformation with the size and intensity of the generated tsunami. Based on these data, they established a series of relationships between the Soloviev-Imamura intensity of the tsunami (Gusiakov, 2011) and different parameters of the sea-floor deformation, among them the displaced volume and the potential energy. Figure 6a shows the ranges of intensity values defined as a function of the potential energy:

\[ i = 1.16\log_{10}(E_{ts}) - 14.2 \]  

(5)

We have selected to simulate those events with a potential energy capable of generating a tsunami of intensity of at least -2. This criteria restricts the number of tsunami propagations to model from 1344 events with \( M > 6 \) to 331 events with earthquake magnitudes ranging from 6.71 to 7.62 and double amplitudes \( A_\eta \) from 0.3 m to 1.2 m.

Bolshakova and Nosov (2011) examined some relevant tsunamis for which they also parametrized the sea-floor deformations. It is noteworthy that those events with double amplitudes below 0.4 m were only perceptible in tide gauges, not generating a
notable impact on the coast. As can be seen in Figure 6 there is a good correspondence between the events selected to simulate with those whose double amplitudes are above 0.3 - 0.4 m.

In order to model the tsunami propagation we have resort to the highly used and validated code COMCOT (Cornell Multi-grid Coupled Tsunami) (Liu et al., 1995; Wang and Liu, 2006). This algorithm is based on the Non-linear Shallow Water Equations built over a modified leap-frog nested grids scheme.

The bathymetry used is composed of three independent sources (Figure 7). On the one hand, the bathymetric data corresponds to the EMODnet 2020 mesh (EMODnet, 2022), with a horizontal resolution of 1/16’ (∼115 m). On the other hand, for the regional topography, we have used the MERIT global DEM (Yamazaki et al., 2017), with a horizontal resolution of 3” (∼90 m). For the highest resolution mesh, on the coast of Almeria, we have used the topography of the digital model of 25 m from the National Geographic Institute of Spain (CNIG, 2022). The regional mesh has been resampled with a cell size of 500 m and the local one with 100 m.

For each of the 331 tsunami propagations we have computed the maximum elevation for a model running during 90 minutes, which is enough time for the waves to propagate through the basin and capture the wave reflections. In Figure 8 tsunami travel times are shown as well as examples of the results for three events with different magnitudes.

As expected, for the smaller magnitude events, the location of the rupture, as well as the slip distribution along the fault plane, are the determining factor in the location of the maximum wave elevations (Figure 8a-d). However, for the maximum events (Figures 8e-f), in which slip occurs along the entire fault plane (see Figure 2d), the location of the maximum wave elevations are clearly determined by the morphology of the sea-floor.

Figure 6. Relations of seafloor deformation parameters with earthquake magnitude. a) Potential energy. Dashed lines show the tsunami intensity according to equation 5. b) Displaced volume. Dash-dotted line shows the Bolshakova and Nosov (2011) upper limit for the magnitude - volume relation. c) Displacement double amplitude. Dash-dotted line shows the Bolshakova and Nosov (2011) upper limit for the magnitude - double amplitude relation and the dashed line the Dotsenko and Soloviev (1990) empirical relation. d) Maximum vertical displacement.

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Figure 7. Bathymetric grids used in the propagation modelling. The Grid 0, with a cell size of 500m is composed by the EMODnet 2020 bathymetry (EMODnet, 2022) and the topography by the MERIT DEM (Yamazaki et al., 2017). The Grid 1, with a cell size of 100m, is composed by the EMODnet bathymetry and the 25 m resolution topographic DEM of the IGN (CNIG, 2022). The dashed polygon labelled with CB marks the location of the Chella Bank bathymetric feature. The labels show the main localities mentioned in the text: Car, Cartagena; PM, Puerto de Mazarron; Ag, Aguilas; Crb, Carboneras; CG, Cabo de Gata; Al, Almeria; RM, Roquetas de Mar; Adr, Adra; Mo, Motril; Nj, Nerja; TM, Torre del Mar; M, Malaga; Mb, Marbella; G, Gibraltar; Ce, Ceuta; T, Tetouan; OL, Oued Laou; EJ, El Jebha; Ah, Al Hoceima; Me, Melilla; Nd, Nador; Gh, Ghazaouet; BS, Beni Saf; O, Oran.

The classical tsunami hazard deterministic approach consist on the definition of the worst-case scenario based on the dimensions of the source and the employ of a series of empirical relations to define the magnitude of the event and the average slip over the fault. Alternatively, instead of defining a single average homogeneous slip model, a set of stochastic variable slip models can be produced and analysed statistically.

A common procedure is to show the maximum wave elevation expected for each model cell from a series of modelled sources. This kind of map is usually called aggregated maximum elevation map; and is very useful to determine the worst impact of the wave considering all the potential sources. An extension of this reasoning is the aggregation of maximum elevations produced by a set of tsunamis produced by variable slip models on a single source or a set of sources. With this latter approach we have produced the aggregated maximum elevation map shown in Figure 9.

The maximum elevations produced by the Carboneras strike-slip fault exceed 1 m consistently, and with relevant inundations, in the Almerian coast (Figure 9). The maximum elevations are located in front of the fault rupture, from Adra to Almeria city, but with relevant local inundations in the Cabo de Gata area. Towards the west the maximum elevations can reach locally 1 m but usually show values of a few decimetres. In the opposite coast, in northern Africa, the maximum elevations are always in the range of 0.1 - 0.8 m with the highest values from Melilla to Ghazouet. For north Africa only the coarse bathymetry has been used and local reflections and resonances not modelled could produce higher elevations locally.

Having produced hundreds of rupture scenarios that obey both dimensional and temporal characteristics to the regional seismotectonic context, we can statistically analyse the propagation results. For each calculation point on the map we obtain a statistical distribution of elevations. In Figure 10 some examples are shown for localities along the coast. These elevations
Figure 8. Example of maximum wave elevations obtained for three events (out of 331) with different magnitudes. The ruptures corresponding with these events are shown in Figure 2. See Figure 7 for labels of localities.

have been taken for the 5 m depth isobath. The distribution shown is common for the entire calculation domain, where several local maxima in the distribution can be interpreted, being far from a normal distribution. The highest frequency is commonly related with the lower elevation values, denoting the lower recurrence interval of small events. The second peak observed is usually related to the highest wave elevations, with values ranging from 1.2 m to 2 m. In some places these higher elevations constitute the most frequent values (as is seen in the example of Figure 10a, corresponding to the locality of Adra). Between these two local maxima in the distribution two more local peaks can be interpreted, although of less importance.

In a simple way we have decided to show the statistical complexity of the distributions of maximum elevations on the coast through the use of quartiles; thus Figure 11 shows the maximum elevations corresponding to the 25%, 50% (median) and
Figure 9. Maximum wave elevation aggregated a) regional and b) local maps. See Figure 7 for labels.

Figure 10. Tsunami wave maximum elevations frequency distribution for locations in a) Adra; b) Roquetas de Mar; c) Almería and d) Genoveses Cove.

75% quartiles. The difference between the regional and local maximum elevations arise from the different cell size used in the propagation modelling. The regional bathymetry (grid 0 in Figure 7) has a cell size of 500m, while the local bathymetry (grid 1) has a cell size of 100 m. The coarser bathymetry is unable to reproduce with precision the nearshore complexities and the maximum wave elevations are underestimated. This is clearly shown in the 75% quartile maximum elevations (Figure 11c,f), where the elevations along the coast are consistently higher using the local bathymetry compared with the regional. A specially illustrative example is shown in the area of Cabo de Gata (near the eastern edge of the local grid); where a peak on the elevation stands out. This peak is located in the Genoveses cove (Figures 11f) where resonance effects are probably responsible of exceptionally high elevations.
4 Discussion

Tsunamigenic potential of the Carboneras Fault

In line with results obtained in previous analyses of the tsunamigenic potential of strike-slip faults (Elbanna et al., 2021; Frucht et al., 2019; Gusman et al., 2017; Heidarzadeh et al., 2017; Ho et al., 2021); this work demonstrates the tsunamigenic capacity of the Carboneras Fault. This is a strike-slip fault, with some dip-slip component (rake $\sim 10^\circ$ based on field analysis of its outcrops onshore according to (Moreno et al., 2015) and with the capacity to generate locally damaging tsunamis. However, on a regional scale considering the Alboran Sea basin, its tsunamigenic capacity is more limited, being able to produce tsunamis of small entity in the North African coast between Melilla and Ghazaouet (Figure 9) although with a low frequency (Figure 11).

If we compare the results of this work with previous results (Álvarez-Gómez et al., 2011a, b; Gómez de la Peña et al., 2022) we can see that the tsunamigenic capacity modelled here is higher. While the fault geometry is essentially the same with minor variations due to the higher resolution and fidelity used in our models than in those of Álvarez-Gómez et al. (2011a) and Gómez de la Peña et al. (2022), there are other parameters that differ significantly. The maximum magnitude, estimated according to
empirical relationships, in previous models was $M_W$ 7.1 - 7.2, notably lower than the maximum magnitude reached with our physical model, $M_W$ 7.62, which is close to the maximum magnitude proposed by Moreno (2011). This difference in magnitude consequently produces an important difference in net slip. The one used by Álvarez-Gómez et al. (2011a) is 1.9 m and 1.38 m by Gómez de la Peña et al. (2022); these being average slips over the entire rupture area. In the models that we have developed in this work, the slip is variable, but the average slip for a worst-case of magnitude 7.62 would be $\sim$6 m, with maximum slips $\sim$9 m. On the other hand, the rake used in our models is 10º while Álvarez-Gómez et al. (2011a) used 15º and Gómez de la Peña et al. (2022) used 0º.

**Seismogenic potential and Frequency-Magnitude distribution**

Although the difference in maximum magnitudes may seem large, it must be taken into account that those provided by the empirical relations are the mean values of the regressions best fits, with standard deviations that may be high. On the other hand, in our models we have selected the largest magnitude generated throughout a 1 Myr. catalogue; and not the average value of the maximum magnitudes generated. If we look at Figure 3, we see that the maximum magnitudes, generated by the complete rupture of the Carboneras fault, vary roughly between magnitudes 6.9 and 7.7 (maximum absolute value of 7.62). If we use the empirical relationship of Leonard (2014) for example, for a maximum rupture length of 71 km (using the Gómez de la Peña et al. (2022) value) we obtain magnitudes of 7.25 and using the rupture area we obtain values of 7.14. However, these values represent the mean of the best fit, with a one standard deviation range between 6.86 and 7.64 for the empirical length-$M_W$ relationship and between 6.88 and 7.4 for the area-$M_W$ relationship. Therefore, the values obtained in our model are within the range of one standard deviation of this empirical relationship, with the advantage that we can obtain the maximum magnitudes in a robust manner from a statistical point of view.

The distribution of frequencies and magnitudes (FMD) of the generated seismic catalogue (Figure 3) reflects the variability of magnitudes associated to the rupture of the entire fault. Since the long-term behaviour of the modelled system is complex, although the construction of the model is deterministic, the statistical distribution of the generated events reflects the stochastic behaviour characteristic of dynamical systems showing self-organized criticality (SOC) (Bak et al., 1988; Bak and Tang, 1989). This stochastic behaviour of the system is reflected also in the non-linearity of the relationship between the size of the earthquake rupture and the slip; thus, for the same rupture size we obtain different slip distributions and therefore different magnitudes are generated. Maybe as a consequence of this, the upper limit of the FMD departs from the classical Gutenberg-Richter potential relation (GR), showing a distribution markedly different that can be seen on the discrete counts of the plot in Figure 3. This distribution resembles that of the characteristic earthquake behaviour (Schwartz and Coppersmith, 1984), but instead of showing a characteristic single magnitude there is a bell-shaped distribution of the characteristic earthquake magnitudes. In our models this behaviour can be related to the physical limit imposed to the maximum rupture area and consequently limiting the self-similar range of the dynamic system (Ben-Zion and Rice, 1995); maybe if the rupture area could be modelled as infinite, the FMD would reflect a GR relation.
Figure 12. Comparison of source simplifications. a) Realistic geometry and variable slip maximum earthquake, $M_{W} 7.62$, model; b) realistic geometry with average homogeneous slip; c) simplified geometry and homogeneous slip.

Worst-case scenario approximation

This concept of characteristic earthquake, or worst-case scenario, is frequently used in deterministic hazard approximations. In these models, simple rectangular sources with homogeneous slips over the fault rupture are used. There has been much debate about the appropriateness of using these simple models and whether they can roughly reflect the tsunamigenic potential of a source. To address some of the drawbacks of this methodology, stochastic probabilistic approaches have been proposed for the generation of variable slips on the fault plane. In principle, the variable slip should play a key role on the impact of local sources, which has been seen in the models shown in Figure 8 for events of different magnitudes (see supplementary models for comparison). To analyse the influence of these aspects we have compared one of the maximum scenarios modelled, with magnitude $M_{W} 7.62$ (Figure 12a), with scenarios of equal magnitude but with homogeneous slip in the detailed geometry (Figure 12b), as well as with a simplistic model based on 3 rectangular sections like the one used by Álvarez-Gómez et al. (2011a) (Figure 12c).

At first glance, the propagations are very similar and share their main features. If we compare them at a local scale (Figure 13), we see that the differences are below 0.5 m in general, although locally the differences may be greater on the coast (up to 3 m). From the regional point of view, the differences are minor (Figure 14).

If we compare the local propagation between the simplified rectangular source and the variable slip source (Figure 13d) the main differences are located towards the tips of the fault sections. These sections behave as patches whose slip decreases towards the tips (Figure 12a), and it is therefore at these points where the simplified model overestimates sea-floor uplift (the blue colours in figure 13d show this important difference in the Adra area). On the contrary, towards the centre of the sections the simplified model underestimates the uplift. These differences are essentially the same as those that can be observed in the comparison of both realistic geometries but with variable or constant slips (Figure 13e). In this case, since both geometries are the same, the differences between both models are minor.

Regionally, the differences between the models are minor, although the slip differences towards the southern tip of the fault are evident, as has been seen locally as well. On both the Iberian and African coasts, values are overestimated by the simplified models towards the western part of the basin (negative values in Figures 14d and e), while elevations are underestimated towards the eastern part.
What is evident is the main role that bathymetry plays in the propagation features, determining to a large extent the location of the areas where there is major impact (Figure 9). In this sense, the Chella Bank, off the coast of Adra (Figure 7), determines the wave propagation and the impact on this coast, in which the highest wave elevations are observed (Figure 11).

5 Conclusions

From a deterministic point of view, the one adopted in this work, the use of physics-based earthquake simulations for tsunami-genic sources allows a more robust characterization of the scenarios, either through aggregated maps of maximum elevations (Figure 9) or the statistical exploitation of the hundreds or thousands of scenarios generated (Figure 11). In addition, the use of this tool allows characterizing the inter-event times and the recurrence intervals of the maximum events, which are those that have the greatest impact on the tsunami hazard.
Regarding the estimation of the maximum magnitude of a source, a key step in the deterministic characterization of the tsunami impact, this methodology incorporates the stochastic natural variation in rupture area, slip and magnitude that arises from the non-linear process of seismic rupture. Thus, instead of characterizing the size of the worst-case earthquake through empirical relationships, we can obtain a range of magnitudes characterized by a probability distribution, which allows a robust implementation of uncertainty estimation. In addition, each modelled seismic rupture is characterized by its own variable slip distribution and rupture process as they are modelled with a quasi-dynamic algorithm.

The strike-slip Carboneras Fault has the capacity to generate locally damaging tsunamis. However, on a regional scale, considering the Alboran Sea basin, its tsunamigenic capacity is more limited. Comparing our results with previous works (Álvarez-Gómez et al., 2011a, b; Gómez de la Peña et al., 2022) we can see that the tsunamigenic capacity modelled here is higher, basically due to the difference in maximum magnitude, which produces an important difference in maximum net slip.

The distribution of frequencies and magnitudes (FMD) of the generated seismic catalogue (Figure 3) reflects the variability of magnitudes associated to the rupture of the entire fault. The upper limit of the FMD departs from the classical Gutenberg-Richter potential relation, showing a bell-shaped distribution of the maximum earthquakes magnitude in a range between 6.9 and 7.7. The inter-event time for these magnitudes is around 2000 – 6000 years (Figure 4).
The use of physics-based earthquake simulations for tsunamigenic sources allows a qualitative leap in their characterization. From a probabilistic point of view, these models have shown in the Probabilistic Seismic Hazard Analyses (PSHA) a great potential to estimate recurrence periods and inter-event times for large earthquakes, which are poorly represented in the instrumental seismic catalogues (Chartier et al., 2021; Herrero-Barbero et al., 2021; Console et al., 2017); being one of the key pieces in the current development of seismic forecast models (Dieterich and Richards-Dinger, 2010; Field, 2019; Field et al., 2014; Shaw et al., 2018). The implementation of these methodologies in the Probabilistic Tsunami Hazard Analyses (PTHA) is a logical and necessary step.

**Code availability.** The RSQSim physics-based earthquake simulator has been developed by Richards-Dinger and Dieterich (2012) and can be obtained from the authors upon request. The COMCOT tsunami simulation has been developed by Liu et al. (1995). The version used in this work is an adaptation to gfortran compiler developed by Tao, Chiu at Tsunami research group, IHOS, NCU; available at https://github.com/AndybnACT/comcot-gfortran. GMT (Wessel et al., 2013) has been used to perform some calculations and to produce most of the figures.

**Author contributions.** JAAG conceived the work, performed the tsunami simulations and analysis and collaborated on the manuscript writing. PHB constructed the 3D fault model, performed the physics-based earthquake simulations and analysis and collaborated on the manuscript writing. JJMD collaborated on the manuscript writing and on the discussions on the EBSZ tectonics.

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