



# Characteristics and RISM of sliding flow landslides triggered by prolonged heavy rainfall in the loess area of Tianshui, China

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**Abstract.** Shallow loess landslides induced by prolonged heavy rainfall are common in loess dominated areas and often result in property loss, human casualties, and sediment pollution. Building a suitable prediction model for shallow landslides in loess areas is critical for landslide mitigation. In 2013, prolonged heavy rains from July 19th to the 25th triggered shallow loess landslides in Tianshui, China. The “7.25 loess landslides” were used as a case study for this current study. Landslide data, along with the characteristics of the loess shallow landslides were obtained through multiple field investigations and remote sensing interpretations. The “7.25 loess landslides” demonstrated clustering, high density, small areas, and long travel distance. The depth of the sliding surface correlates with the saturated layer (i.e., liquid limited water content) arising from rainfall infiltration, with a sliding depth that is typically less than 2 m and is negatively correlated with the slope. Based on the common characteristics of shallow loess landslides, the mechanisms involved in the sliding flow landslide are proposed. The Revised Infinite Slope Model (RISM) was proposed using equal differential unit method and corrected the deficiency that the safety factor increases with the slope increasing when the slope is larger than 50° calculated using the Taylor slope infinite model. The relationship between the critical depth and the slope of the shallow loess landslide was determined. The intensity-duration (I-D) prediction curve of the rainfall-induced shallow loess landslides under different slopes was constructed combined with the characteristics of rainfall infiltration and can be used in forecasting regional shallow loess landslides. Additionally, the influence of loess strength on the shallow loess landslide stability has been analysed. The shallow loess landslide stability responds to slope and cohesion but is not sensitive to the internal friction angle.

## 1 Introduction

Loess is a porous and loose aeolian deposit of silt-sized particles mainly formed during the Quaternary period, and it is widely distributed in Asia, Europe, North America, and South America (Li et al., 2020). In China, loess is widely distributed, with an area of 630,000 km<sup>2</sup>, accounting for 6.63% of the total land area in northwest, north, and northeast China. The deposit is high thickness and the integrity and continuity of loess layers are the greatest in the world (Liu 1985). However, loess dominated environments are extremely fragile, with substantial soil erosion, topographical variation, and subject to concentrated rainfall, and have now become one of the most developed geohazard areas in China (Derbyshire, 2001; Zhang and Liu 2010; Zhuang



et al. 2018). Loess creates unique soil with large pores, high compressibility, strong collapsibility, and high-water sensitivity, making it prone to surface failure (Xu et al. 2014; Li et al., 2007; Peng et al., 2015; Juang et al. 2018; Zhuang et al. 2022). The key factor in triggering loess failure is the interaction between water and loess, which can destroy the loess structure and reduce its mechanical strength. In more than 85% of loess landslides, water is the key factor, displaying the characteristics of small  
35 early deformation, long run-out distance, location unpredictability, rapid occurrence, and liquefaction, resulting in serious property damage and human casualties (Dijkstra, 1995; Wang et al., 2014; Zhuang et al. 2018).

Rainfall-induced slope failures are a common form of shallow landslides in the Chinese Loess Plateau (CLP). Field investigations revealed that more than 50,000 landslides have occurred in the loess plateau in recent decades (Zhuang et al. 2018; Zhuang et al., 2022). Most of those landslides were triggered by prolonged heavy rainfall and with a slip surface depth  
40 of no more than 2 m (Zhuang et al., 2017; Zhuang et al. 2018; Zhuang et al., 2022). Precipitation infiltrates into the soil and percolates through the loess to approximately 2 m, attributed to the decreased infiltration rate with increasing depth (Tu et al. 2009; Xu et al., 2011; Zhuang et al., 2018). Shallow loess landslide events, due to prolonged heavy rainfall events, have occurred in places such as northern Shaanxi and Tianshui in 2013, Tianshui in 2015, and northern Shaanxi in 2017 (Peng et al., 2015; Wang et al., 2015; Zhuang et al., 2017; Zhang et al., 2020). Another consequence of these landslides is that substantial  
45 amounts of sediment have been transported into rivers in the area, polluting rivers, raising the riverbeds, and increasing flooding.

Many scholars have studied rainfall infiltration, landslide mechanisms, and forecasting rainfall-induced shallow landslides. Among them, the prediction of shallow loess landslides due to rainfall is the most common, as this information can be used for geohazard mitigation (Brenning, 2005; Bordoni et al., 2015; Ahmadi-adli et al., 2017; Reichenbach et al., 2018; Thomas et al., 2018; Cogan and Gratchev, 2019; Berti et al., 2020; Bordoni et al., 2020). Shallow landslide forecasting can be  
50 divided into the three catalogies based on method. (1) Early warning of landslides through monitoring time-based deformation data is an important forecasting tool (von Ruetten et al., 2011; Galve et al., 2015; Roccati et al., 2018; Segoni et al., 2018; Lombardo et al., 2020; Marino et al., 2020). Most landslide failure processes progress through deformation stages that gradually develop into a catastrophic failure. During this process, deformation is easily observed and monitored and is  
55 considered the most important factor for landslide prediction. This approach is most relevant for large-scale landslides which have obvious early deformation trends. Common approaches include (2) Landslide forecasting can also include temporal and spatial rainfall monitoring (Giannecchini, 2006; Salciarini et al., 2006; De Vita et al., 2012; Giannecchini et al., 2012; Cevasco et al., 2013; von Ruetten et al., 2013; Stähli et al., 2015). Rainfall is a key inducing factor of geohazards, and researchers have studied the critical rainfall values for intensity, duration, and total rainfall within specific areas for predicting landslides. (3)  
60 Statistical and qualitative methods to evaluate landslide susceptibility, associated with landslide occurrence, can yield maps showing landslide hazard zones which is useful for land use management and long-term predictions (Jia et al., 2008; Zizioli et al., 2013; Cevasco et al., 2014; Goetz et al., 2015; Guzzetti et al., 2006; Di Napoli et al., 2020; Di Napoli et al., 2021). However, it is important to note that statistical method results are largely dependent on the quality of data and the specific method used. (4) Landslide early warning and forecasting can also be based on physical modelling (Montgomery and Dietrich, 1994;



65 Montrasio and Valentino, 2007; Formetta et al., 2016; Schilirò et al., 2016; Lizarrag et al., 2017; Wang et al., 2020;  
Leonarduzzi et al., 2021). Researchers have focused their efforts on elucidating the mechanisms and conditions which lead to  
soil failure. The data for analysis comes from soil tests, deriving evidence of the decay of cohesiveness and angles with  
precipitation infiltration (Skempton 1985; Iverson 2000; Baum et al. 2008; Baum and Godt 2010), and quantitative landslide  
assessment. Several physically-based models have been proposed, including steady-state hydrology (SHALSTAB and  
70 SINMAP) (Montgomery and Dietrich, 1994; Pack et al. 1999), quasi-steady hydrology (dSLAM, IDSSM) (Dhakal and Sidle  
2003), and Transient hydrology (TRIGRS) (Iverson, 2000; Baum et al. 2008).

However, since shallow loess landslides often occur in the saturated, or nearly saturated, models such as the TRIGRS  
model, which is based on the infinite slope model and focuses on forecasting shallow landslides in areas with a gentle slope,  
are difficult to apply in loess areas (Wang et al., 2015; Zhuang et al., 2017). SINMAP and SHALAD are prediction models  
75 also based on infinite slope models and the sliding or soil depths are fixed parameters related to landforms (Montgomery and  
Dietrich, 1994; Pack et al. 1999; Michel et al., 2020). According to previous studies, shallow loess landslides with sliding-  
flow landslide characteristics are mainly induced by prolonged heavy rainfall and the sliding surface is the saturated or nearly  
saturated layer (Wang and Sassa, 2001; Zhang et al., 2013; Peng et al., 2015; Wang et al., 2015; Zhuang et al., 2017; Guo et  
al., 2019). Due to their small scale and difficult identification, shallow landslides on the CLP are a significant safety threat to  
80 local residential areas (Peng et al., 2015; Wang et al., 2015; Guo et al., 2019; Zhang et al., 2020). As most shallow loess  
landslides occur within the top 2 m, the depth of the saturated layer is a critical factor when studying loess sliding-flow landslide  
induced by prolonged heavy rainfall.

The current study comprehensively evaluates the unique characteristics of shallow loess sliding flow landslide, combined  
with an infinite slope model. The objectives were to determine the sliding depths of the saturated layer at different slopes, and,  
85 to consider rainfall intensity and duration for developing a shallow loess landslide prediction model using loess infiltration  
characteristics. The probability of regional loess shallow landslides under different rainfall intensities and durations was  
assessed and combined with GIS spatial analysis and high-precision DEM (Digital Elevate Model) data. The model was  
verified using the 2013 “7.25” loess sliding-flow landslide events in Tianshui Gansu province that were triggered by prolonged  
precipitation, confirming the reliability of the loess shallow sliding-flow landslide prediction model proposed in this paper.

## 90 **2 Study area and landslide data**

### **2.1 Setting area**

The study area is a hilly loess region located southwest of the CLP and is part of the transition zone between the Qinling  
Mountains and the Longshan Mountains (Peng et al., 2015; Zhang et al., 2020). The loess is deeply and widely distributed  
with vertical joints and fissures, creating a fragile geological environment where geohazards such as landslides and debris  
95 flows frequently occur (Peng et al., 2015; Zhang et al., 2020; Qi et al., 2021). The terrain of the study area is generally high in  
the southeast and low in the northwest, with altitudes ranging from 748.5 to 2,120 m and has a relative height difference of





and ended on June 21 at 4:00, with a cumulative rainfall of 285 mm, then from 3:00 to 20:00 on July 8 (128.9mm), followed  
by 16:00 on July 21 to 4:00 on July 22 (43.5mm), and the last period was from 23:00 on July 24 to 10:00 on July 25 (174.4mm)  
115 (Table 1). Over 45,000 shallow landslides were triggered, characterized by shallow and small scar areas, resulting in the death  
of 25 people.

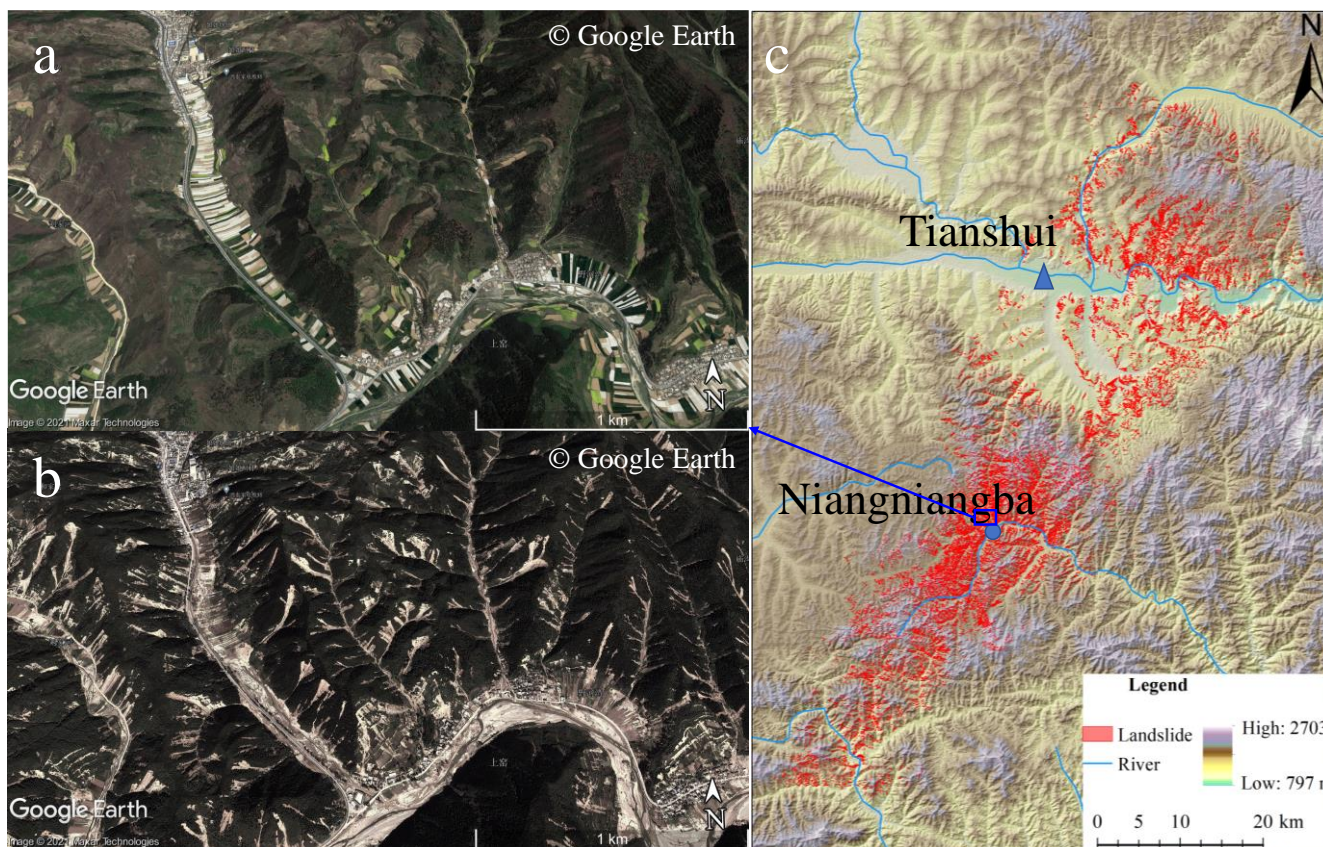
**Table 1.** The precipitation data from the “7.25” loess sliding-flow landslide events.

Date	Accumulative rainfall / mm	Duration / h	Average intensity / mm/h	Max intensity/ mm/h
19:00 on June 19 to 4:00 on June 21	285	34	8.382353	35.8
3:00 to 20:00 on July 8	128.9	17	7.582353	22.6
16:00 on July 21 to 4:00 on July 22	43.5	12	3.625	19
23:00 on July 24 to 10:00 on July 25	174.4	11	15.85455	32.2

## 2.2 Landslide data

Utilizing high-precision remote sensing imaging (~2 m resolution) from October 2012 and December 2013, before and after  
120 the landslides and field investigations, a total of 47,005 landslides were identified in the study area. It can be seen from Figure  
2 that the landslides distribution is primarily concentrated in the middle of the study area along the NNE direction and  
decreased gradually to the southeast and northwest.





125 **Figure 2** The landslides triggered by “7.25” loess sliding-flow landslide events (a: before “7.25” loess sliding-flow landslide  
events in October 2012; b: after “7.25” loess sliding-flow landslide events in December 2013; c: the landslides distribution  
triggered by “7.25” loess sliding-flow landslide events)

130 The landslides occurred in the shallow loess layer at a depth of no more than 2 m and with sliding-flow landslide  
characteristics observed via a large number of field investigations. Normally, shallow landslides are triggered during prolonged  
heavy rainfall events by the rapid increase of pore pressure or loss of the cohesion (Iverson 2000; Wang and Sassa 2001; Sassa  
and Wang 2005; Tu et al., 2009; Zhang et al., 2013). As a result, a failure surface develops within the soil profile or at the  
depth of the precipitation infiltration. This means that the sliding soil layer is close to liquid limit water content when the  
landslide starts and flowing characteristics occur after the slope failure.



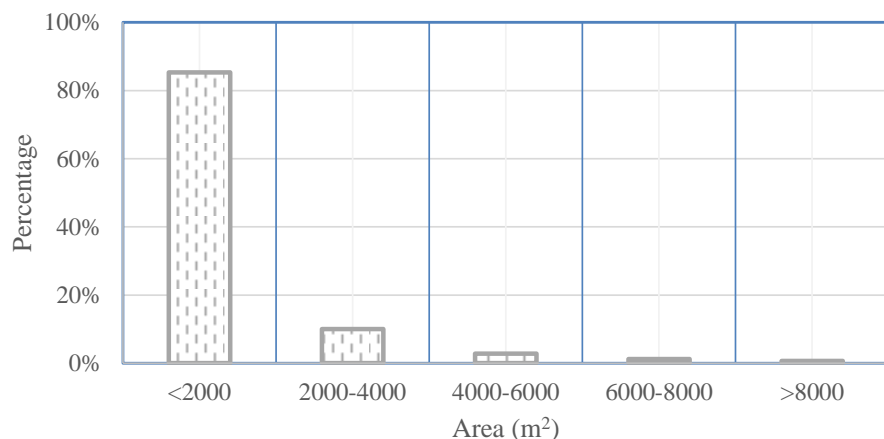
### 3 The “7.25” loess sliding-flow landslide events characters

#### 3.1 Size characters

135 The landslide impacted area is 65.69 km<sup>2</sup> and the density is greater than 25 landslides per/km<sup>2</sup>. As shown in the Fig. 2, the area  
 of shallow landslides in Tianshui Niangniangba accounts for more than 35% of the total area and shallow flow slips occurred  
 on most of the slopes. The mean landslide area was 0.0013 km<sup>2</sup>, which is smaller than what is typical for landslides triggered  
 by rainfall or earthquakes (Table 2). Fig. 3 shows the proportion of landslides in different areas. It can be seen that most of the  
 140 m<sup>2</sup> accounted for only 3% (Fig. 3), indicating that the “7.25” loess sliding-flow landslide events were primarily small landslides  
 occurring in groups.

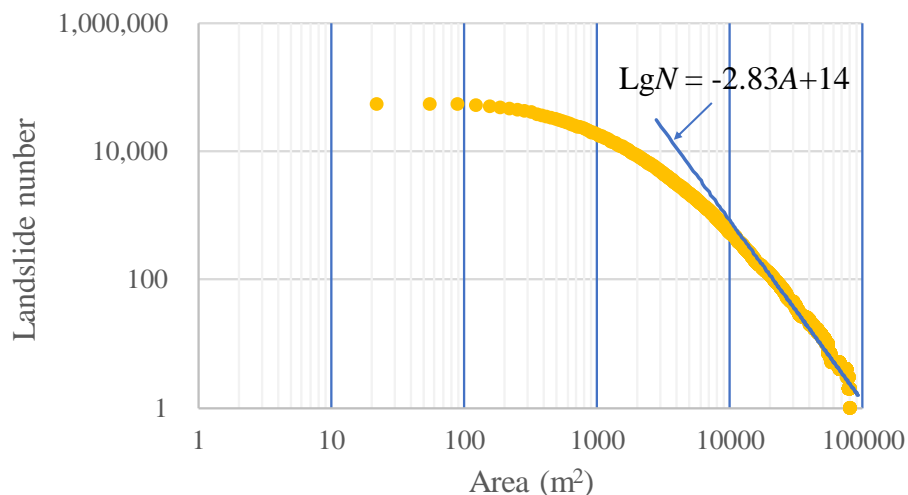
**Table 2.** Landslide size and numbers triggered by earthquakes or rainfall in recent years.

Items	Study area (km <sup>2</sup> )	Number of landslide (km <sup>2</sup> )	Landslide areas (km <sup>2</sup> )	Average area of the landslide (per km <sup>2</sup> )
Northridge earthquake (Harp and Jibson, 1996)	10,000	11,111	23.8	0.00214
Haiyuan Earthquake (Zhuang et al., 2018)	40,000	3,700	117.45	0.03162
Wenchuan Earthquake (Dai et al., 2011)	41,750	56,000	811	0.01448
Chi-Chi earthquake (Lin and Tung, 2004)	--	9,297	128	0.01374
Kashmir earthquake (Owen et al., 2008)	7,500	2,424	--	--
Umbria, Central Italy[rapid snowmelt] (Guzzetti et al., 2002)	2,000	4,233	12.7	0.00301
Guatemala [heavy rainfall] (Bucknam et al., 2001)	10,000	9,594	29.5	0.00307
“7.25” loess sliding-flow landslide events in Tianshui	<b>1,936</b>	<b>47,005</b>	<b>65.69</b>	<b>0.0013</b>



145 **Figure 3.** Proportion of landslides in different areas.

Fig. 4 depicts the landslide area, cumulative frequency distribution, and statistical significance of landslides with an area of failure  $\geq 5,000 \text{ m}^2$  and accounts for 90% of the total landslides. The largest landslide was only  $0.099 \text{ km}^2$ . We examined the area-frequency distribution of the “7.25” loess sliding-flow landslide events via log-binning a normalized non-cumulative size-frequency distribution to plot frequency-density ( $\text{Lg}N = aA + b$ , where  $N$  refers to the number of landslides in each bin) as a function of binned landslide area ( $A$ ) (Fig.4) (Stark and Hovius, 2001; Malamud et al., 2004;). The higher value  $a$  may reflect a greater ability to identify smaller landslides via high-quality imagery. The value for the “7.25” loess sliding-flow landslide events ( $a = -2.83$ ) is higher than exponents reported for other coseismic inventories. For example  $a = -2.39$  for Northridge, California,  $a = -2.30$  for Chi Chi, Taiwan,  $a = -2.19$  for Wenchuan, China, and  $a = -2.3$  for the average of event-based and historical inventories reported by Van den Eeckhaut et al. (2007) (Roback et al., 2018), also showing that landslides triggered by the “7.25” loess sliding-flow landslide events were primarily small landslides occurring in groups.





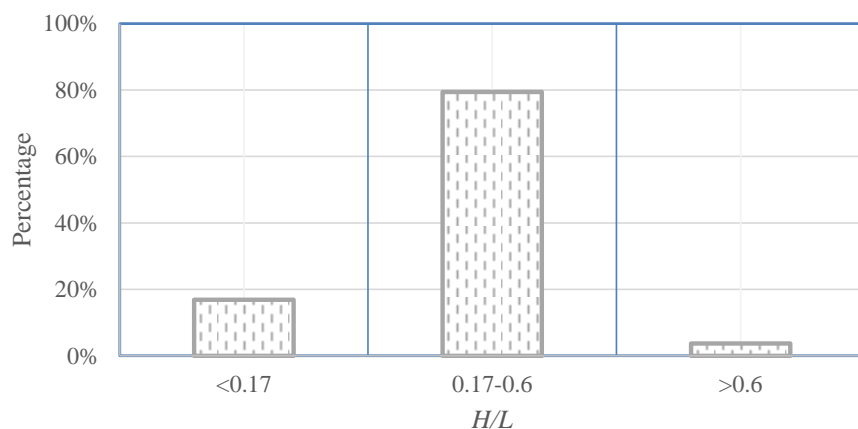


**Figure 4.** The landslide area, cumulative frequency distribution “7.25” loess sliding-flow landslide events.

### 3.2 Mobility characteristics

We examined the probability densities of equivalent friction coefficients (landslide height ( $H$ ) / landslide travel distance ( $L$ )) for the shallow landslides triggered by the “7.25” loess sliding-flow landslide events using Matlab (Fig. 5). The landslide height ( $H$ ) was based on the altitudes of the highest and the lowest points, and the movement distance was the distance between the highest point and the lowest point. The above two parameters were obtained and calculated using ArcGIS spatial analysis.

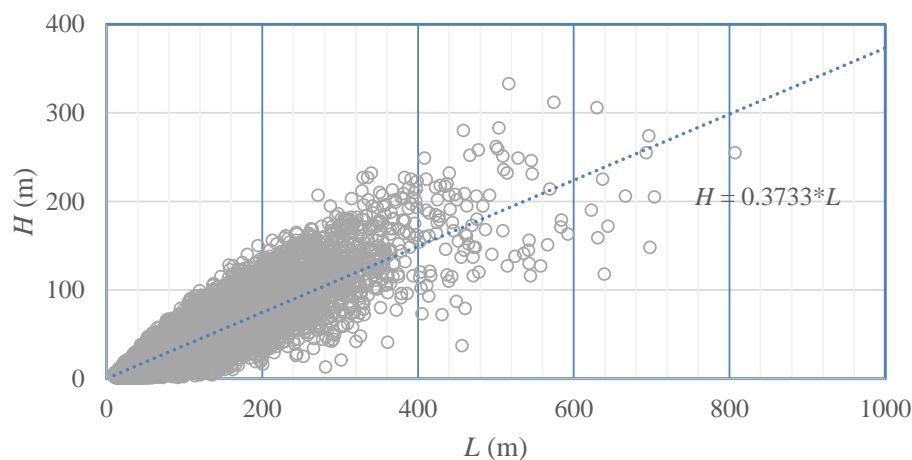
The  $H/L$  ratio frequency ratio of the “7.25” loess sliding-flow landslide events, ranged from 0.01 to 0.88 with a mean of 0.32. According to a study by Wang (2000), landslide fluidization occurs when the equivalent friction coefficient is below 0.17. In our study, 16.85% of the loess landslides had equivalent friction coefficients below 0.17, indicating that the loess landslides moved with flow motion and resulted in longer sliding distances. For more than 96.27% of landslides,  $H/L$  was less than 0.6 ( $H/L < 0.6$  indicates a long-runout landslide) and belong to long run-out landslides.



**Figure 5.** The probability densities of equivalent coefficients of friction.

To model the empirical relationship between landslide height and travel length, which was later verified using images and field investigations, the aforementioned datasets were analyzed to plot  $H$  and  $L$  on a single graph (Fig. 6), where  $L$  (x-axis) is the landslide travel distance and  $H$  (y-axis) is the landslide height.

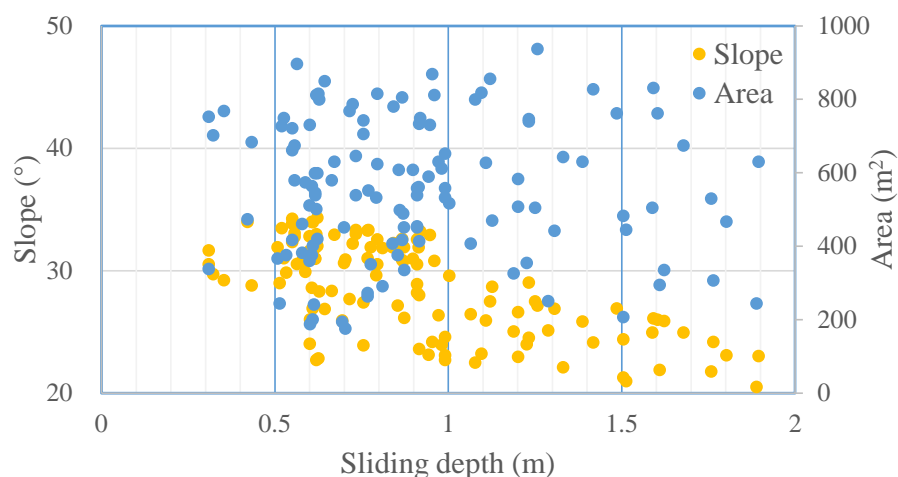
The relationship between height difference and travel distance is positively correlated. With an increase in height difference, the travel distance increases, and the slope of the fitting trend line between the height difference and travel distance is less than 1 and only is 0.37, indicating that the travel distance is greater than the height difference and has obvious long-runout travel distance characteristics.



**Figure 6.** The relationship between height difference and travel distance.

### 3.3 Sliding depth characteristics

180 To obtain landslide depths, we conducted a detailed investigation of sites throughout the study area, such as Niangniangba town, and obtained depth data for 89 landslides based on the characteristics of the landslide and the thickness of the loess scar at the edge of the landslide. Fig. 7 displays the distribution of landslide depths and area; no landslide had a depth greater than 2.0 m and over 70% ranged from 0 to 1 m (Fig. 7). Additionally, we found that the depth of the landslide had no correlation with the landslide area and had a negative correlation with the slope. With increasing slope, the depth of the landslide decreased, 185 that is, the greater the slope, the shallower the sliding surface, and the smaller the slope, the greater the depth of the sliding surface.

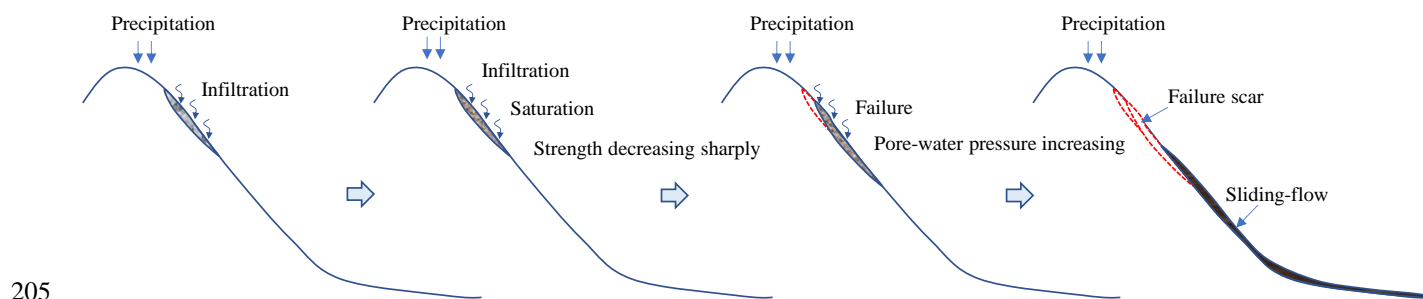


**Figure 7.** The distribution of landslide depths and area.



### 3.4 The shallow sliding-flow landslide formation process

190 Force analysis shows that a slope will fail when the gravity component along the slope direction is greater than the shear strength of the soil (Sassa, 2000; Ochiai et al., 2004; Gabet and Mudd, 2006). If the stability coefficient of the slope is high and the soil reaches its liquid limit water content before the failure, the slope will spontaneously liquefy and flow during the sliding process (Wang and Sassa, 2001; Wang et al., 2015). Usually, the ratio of pore-water pressure to the total normal stress of the soil is used to express the soil liquefaction ratio. When the liquefaction rate is 1, the pore-water pressure equals the normal stress of the soil and the failing slope is in a state of complete liquefaction (Hung et al., 2001; Wang and Sassa, 2001; Sassa and Wang, 2005; Wang et al., 2015). Typically, the normal stress of shallow landslides is low and once the slope is deformation due to the strength decrease, the loess will have an obvious volume reduction due to the large pore structure of the loess collapsing, and then the pore-water pressure increasing sharply (Wang and Sassa, 2001; Sassa and Wang, 2005; Peng et al., 2018). The formation process of shallow loess sliding-flow landslide triggered by prolonged heavy precipitation can be summarized as follows: infiltration of persistent heavy precipitation leads to a certain depth of loess becoming close to liquid limit water content and the strength of the loess will decrease. When the anti-slip force of the saturated loess is less than the sliding force, the saturated soil layer will fail. Due to the large pore structure of loess, once loess deformation occurs, the water in the pores cannot be released, resulting in the pore-water pressure increasing sharply which causes liquefaction of the saturated loess to form a mudflow (Fig. 8).



**Figure 8.** The shallow sliding-flow landslide formation process.

## 4 Forecast model of shallow loess landslide development

### 4.1 Infinite Slope Model

210 According to field investigations and other research results, the shallow loess landslides are concentrated within 2 m of the surface and are negatively correlated with slope. Therefore, infinite slope models considering the thickness of the soil layer and the maximum infiltration depth cannot be directly applied in shallow loess landslide assessments. Previous studies have shown that short-duration heavy precipitation has less effect on the stability of loess slopes and prolonged heavy precipitation can increase the water content significantly, reducing its stability (Wang and Sassa, 2001; Wang et al., 2015; Peng et al., 2018).

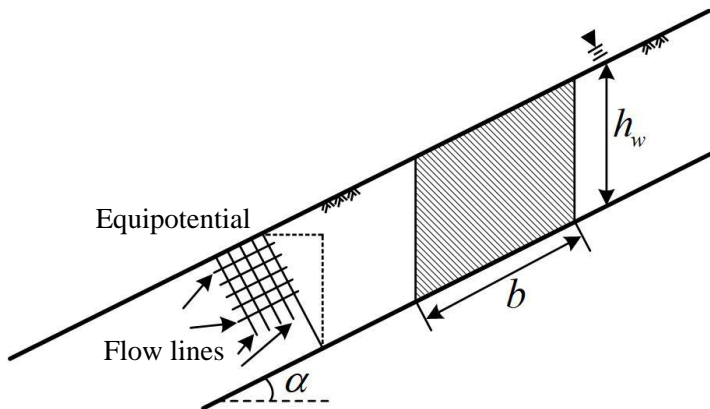


215 Loess landslides transformation to mudflows occur most often on slopes of 25 to 45°, and the sliding body is close to the liquid  
 limit water content before slope instability. Pore-water pressure is a key factor for soil slope failure (Iverson 2000). Previous  
 studies have shown that pore water pressure is the cause of soil landslides, and excess pore-water pressure is the triggering  
 factor for its fluidization (Iverson et al., 1997; Sassa and Wang 2005; Gabet and Mudd, 2006). Failure of the sliding body is  
 primarily due to a decrease in soil strength which results in the sliding force being greater than the cohesive forces following  
 rainfall infiltration which saturates the soil (Wang et al., 2015; Peng et al., 2018).

220 According to the infinite slope model (Fig. 9), Taylor proposed the equation of the safety factor as:

$$K = \frac{(\gamma_{sat} - \gamma_w) h_w \cos^2 \alpha \tan \phi' + c'}{\gamma_{sat} h_w \sin \alpha \cos \alpha}, \quad (1)$$

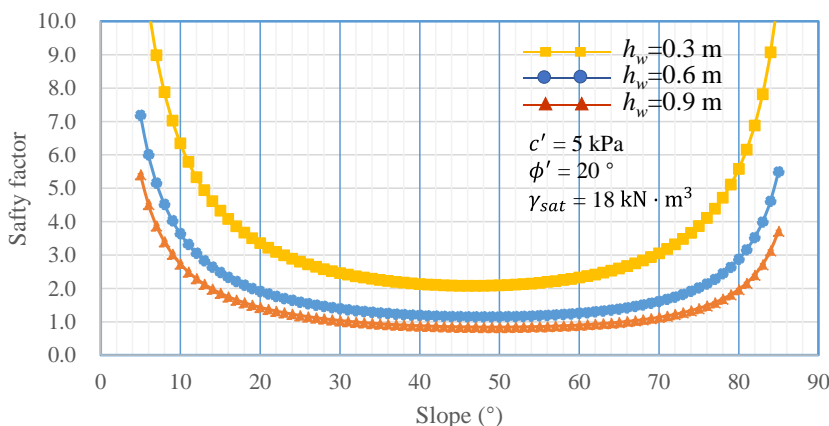
where  $\alpha$  is the slope angle,  $\gamma_w$  is the soil floating weight,  $\gamma_{sat}$  is the saturation weight of the soil,  $l$  is the length of the  
 sliding body,  $h_w$  is the depth of the sliding surface and the approximate depth of loess at the liquid limit water content due to  
 infiltration,  $c'$  (cohesive), and  $\phi'$  (internal friction angle) is the effective strength index of the soil at the sliding surface.



225

**Figure 9** The cross-section of an infinite slope.

Given any set of slope parameters, the stability factor is calculated according to the infinite slope model proposed by  
 Taylor (Taylor, 1948), and the results are shown in Fig. 10.







230 **Figure 10.** The stability factor according to the infinite slope model proposed by Taylor.

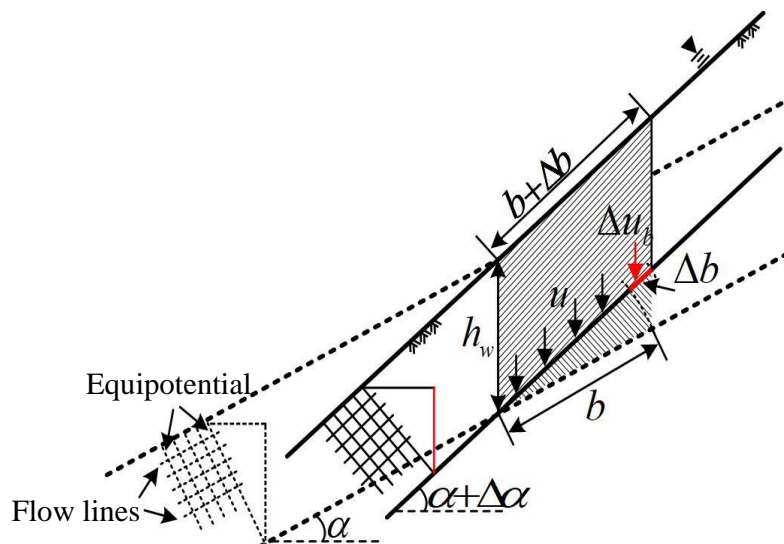
It can be seen from Figure 10 that for the cohesive soil slope, the safety factor decreases with the increase of the slope when the slope is less than 40°. While, the safety factor increases with the increase of the slope when the slope is great than 50°. And the safety factor curve is gradually horizontal with the slope is in the range of 40° to 50°. The calculated results are obviously inconsistent with the actual situation, especially the safety factor increases with the increase of the slope. However, almost all shallow landslide physical prediction models (eg: TRIGRS Model, SINMAP and SHALAD Model) are based on the infinite slope model proposed by Taylor, so these shallow landslide physical prediction models can't be applied to areas with high slope (>40°) resulting in cannot be widely used (Montgomery and Dietrich, 1994; Baum et al. 2008; Zhuang et al., 2017).

#### 4.2 Revised Infinite Slope Model

240 In order to make the calculation results of the Taylor's infinite slope model conform to the actual situation, this study modify the Taylor infinite slope model using equal differential unit method. As shown in Fig. 11, keeping the depth of the saturation zone unchanged with the slope increases, the formula for calculating the self-weight of the soil strip unit can be revised as:

$$W = \gamma_{sat} h_w (b + \Delta b) \cos(\alpha + \Delta\alpha), \quad (2)$$

245 Where  $b$  is the is the length of the sliding body,  $\Delta\alpha$  is the value of the slope increasing.



**Figure 11.** The infinite slope model with the slope variety.

Eq. (2) keeps the self-weight of the soil strip unit unchanged, and the control condition is that the area of the soil strip unit remains unchanged:



250

$$h_w(b + \Delta b) \cos(\alpha + \Delta\alpha) = h_w b \cos \alpha, \quad (3)$$

Eq. (2) shows that although the change of slope has no effect on the self-weight of the differential element, it leads to the change of the bottom area of the element, which is a cause for the change of the cohesion strength and pore water pressure of the bottom surface of the soil strip element. The change of the slope only affects the component values of the forces in the normal and tangential directions of the sliding surface. Therefore, it is necessary to remove the changes in cohesion strength and pore water pressure caused by increasing the slope of  $\Delta\alpha$  when calculating the slope stability with different slopes.

The change of cohesive strength ( $\Delta C$ ) and pore water pressure ( $\Delta u_b$ ) caused by increasing the slope of  $\Delta\alpha$  are:

$$\Delta C = c' \Delta b, \quad (4)$$

$$\Delta u_b = \gamma_w h_w \Delta b \cos^2(\alpha + \Delta\alpha), \quad (5)$$

The effective normal stress ( $N'$ ) and effective anti-sliding force ( $T_f$ ) at the bottom of the soil strip element due to the slope increasing from  $\alpha$  to  $\alpha + \Delta\alpha$  are:

$$N' = \gamma_{sat} h_w (b + \Delta b) \cos^2(\alpha + \Delta\alpha) - \gamma_w h_w (b + \Delta b) \cos^2(\alpha + \Delta\alpha), \quad (6)$$

$$T_f = [\gamma_{sat} h_w (b + \Delta b) \cos^2(\alpha + \Delta\alpha) - \gamma_w h_w (b + \Delta b) \cos^2(\alpha + \Delta\alpha)] \tan \phi' + c'(b + \Delta b), \quad (7)$$

The sliding force of the soil strip unit is changed to:

$$S = \gamma_{sat} h_w (b + \Delta b) \cos(\alpha + \Delta\alpha) \sin(\alpha + \Delta\alpha), \quad (8)$$

The revised effective anti-slip force according to the Eqs. (4), (5), and (7):

$$T_f = [\gamma_{sat} h_w (b + \Delta b) \cos^2(\alpha + \Delta\alpha) - \gamma_w h_w b \cos^2(\alpha + \Delta\alpha)] \tan \phi' + c' b, \quad (9)$$

Combining Eqs. (8) and (9), the safety factor can be obtained:

$$K = \frac{[\gamma_{sat} \cos \alpha - \gamma_w \cos(\alpha + \Delta\alpha)] h_w \cos(\alpha + \Delta\alpha) \tan \phi' + c'}{\gamma_{sat} h_w \cos \alpha \sin(\alpha + \Delta\alpha)}, \quad (10)$$

Making  $\alpha = \alpha_1$ ,  $\alpha + \Delta\alpha = \alpha_2$ ,  $(\alpha_1, \alpha_2) \in \alpha$ , the equation 10 can be expressed as:

$$K = \frac{(\gamma_{sat} - \gamma_w m_\alpha) h_w \cos \alpha_2 \tan \phi' + c' \sec \alpha_1}{\gamma_{sat} h_w \sin \alpha_2}, \quad (11)$$

Making  $m_\alpha = \frac{\cos \alpha_2}{\cos \alpha_1}$ , for the simple the equation, the term  $c' \sec \alpha_1$  in Eq. (11) can be defined as the reference cohesion strength. Since the value of  $c' \sec \alpha_1$  varies monotonically with  $\alpha_1$  changing, in order to make the reference cohesion strength corresponding to any slope angle equal, it only needs to satisfy that  $\alpha_1$  is less than or equal to  $\alpha_2$ :

$$\alpha_1 = \min\{\alpha_2\}, \alpha_2 \in \alpha, \quad (12)$$

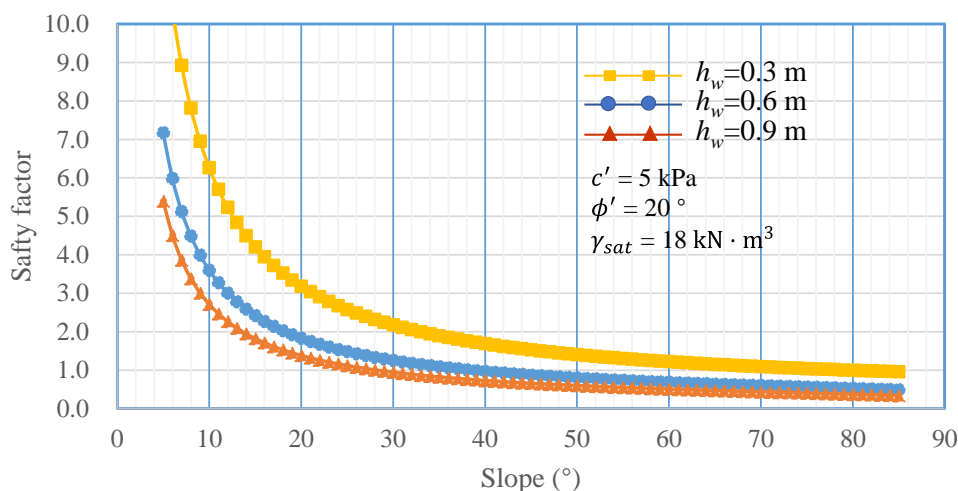
Therefore, the safety factor of the RISM can be expressed as:

$$K = \frac{(\gamma_{sat} - \gamma_w \cos \alpha) h_w \cos \alpha \tan \phi' + c'}{\gamma_{sat} h_w \sin \alpha}, \quad (12)$$

Given any set of slope parameters, the stability is calculated according to the RISM proposed by this study, and the results are shown in Fig. 12. The RISM according to the using equal differential unit method corrects the safety factor that



increases with the slope increasing when the slope is larger than 50° calculated using the Taylor slope infinite model. The calculate results obtained by the RISM maintains the consistency with the calculation result of Taylor method at low angle, and then the calculate results remain decreases with the increase of slope while the slope is larger than 50°.



285 **Figure 12.** The stability factor according to the RISM.

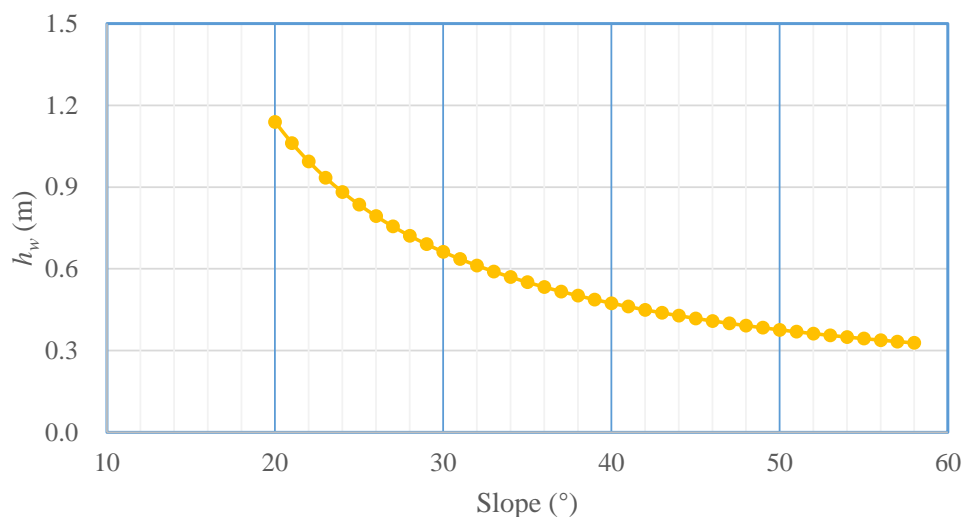
### 4.3 Critical depth of shallow loess landslides

When the stability coefficient  $K$  is 1 in Eq. (12), the critical depth of loess close to liquid limit water content, or the sliding surface of the shallow loess landslide, can be obtained:

$$h_{cr} = \frac{c'}{\gamma_{sat} \sin \alpha - (\gamma_{sat} - \gamma_w \cos \alpha) \cos \alpha \tan \phi'}, \quad (13)$$

290 The critical liquid limit water content depth, or the sliding surface of the shallow loess landslide, for different slopes can be determined by obtaining the soil strength of the nearly saturated state. When the liquid limit water content reaches the critical depth, the layer will fail. According to the loess test results, the cohesive forces of undisturbed loess at the liquid limit water content (0-2 m) range from 3 to 9 kPa with an average of 5 kPa, and the internal friction angle ranges from 11 to 21° with an average of 15° (Fig. 13). Therefore, the relationship between the critical approximate liquid limit water content depth and the slope can be calculated. It can be seen that with increasing slope, the critical approximate liquid limit water content layer gradually decreases, but the rate of decrease slows, from 1.14 m at 20° to 0.47 m at 40° (Fig. 13). This relationship can be expressed via the power-law as:

$$h_w = 34.13a^{-1.15}, \quad (14)$$



300 **Figure 13.** The relationship between the critical depth and the slope.

#### 4.4 The I-D curve of the loess shallow landslide

The critical rainfall intensity-duration (*I-D*) method is often used in forecasting rainfall-induced shallow landslides (Guzzetti et al. 2007; Guzzetti et al. 2008; Baum and Godt 2010; Zhuang et al., 2015). Thresholds empirically derived from rainfall intensity-duration have been widely used to identify rainfall conditions that result in the occurrence of landslides (Guzzetti et al. 2007; Guzzetti et al. 2008; Baum and Godt 2010). Inspection of the *I-D* thresholds reveals the general form:

$$I = \beta D^b + c, \quad (6)$$

Where *I* is the mean rainfall intensity, *D* is rainfall duration, and *c*,  $\beta$ , and *b* are other parameters. For the majority of *I-D* thresholds, *c* = 0, and Eq. 6 takes the form of a simple power law.

$$I = \beta D^b, \quad (7)$$

310 Previous studies have created statistical *I-D* curves based on landslide data and rainfall data. However, these empirical models require many years of precipitation data and calibration parameters. Even so, the determination of the landslide threshold *I-D* curve is inaccurate due to the uncertainty of rainfall monitoring, such as the location, quantity of monitoring sites, and the definition of the start and end time of rainfall events (Zhuang et al., 2015; Guo et al., 2016).

The critical *I-D* curve for slope instability for different slopes can be constructed using the critical approximate liquid  
 315 limit water content depth model combined with the saturated infiltration characteristics of loess in the study area. Six infiltration tests were carried out in the study area using the single-ring infiltration test to determine the infiltration coefficient (*i*) of loess under rainfall. The constant infiltration rates were: 38.6, 33.1, 39.1, 32.2, 36.2, and 31.6 mm/h. Additionally, it was observed that the time between initial infiltration and stable infiltration is less than 10 min. Therefore, in this study, the average stable infiltration rate of 36.0 mm/h was selected as the infiltration coefficient.

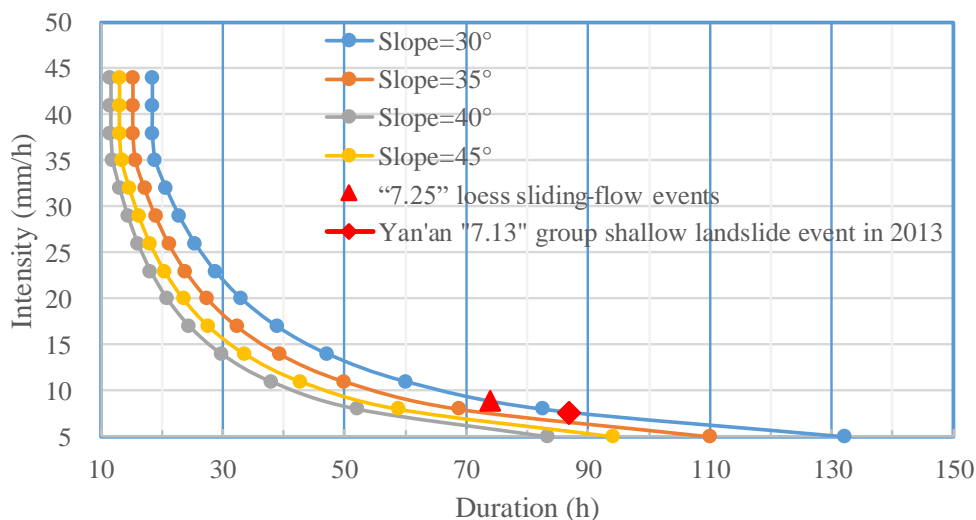
$$320 \quad D = h_w / i, \quad \text{for the precipitation intensity is higher than the infiltration coefficient} \quad (8)$$





$D = h_w / I$ , for the precipitation intensity is lower than the infiltration coefficient (9)

To model the relationship between  $I$  and  $D$ , the two variables were plotted on a single graph, where  $D$  (x-axis) is the rainfall duration and  $I$  (y-axis) is the rainfall intensity. The  $I$ - $D$  curve of the different slopes in the area can be obtained based on the infiltration coefficient and the sliding depth (Fig. 14).

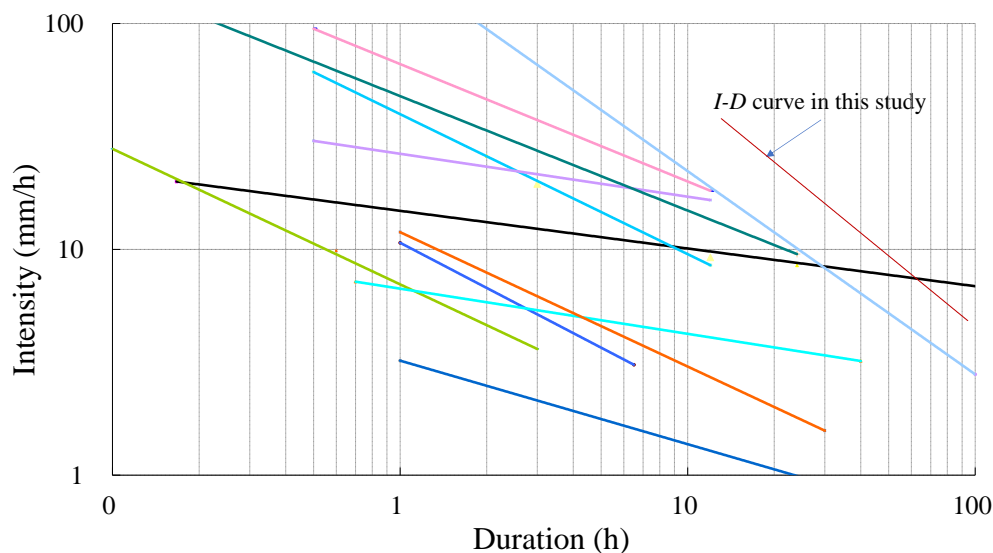


**Figure 14.** The  $I$ - $D$  curve of the different slopes in the loess area.

## 5 Discussion

### 5.1 Model compare

330 Comparing the  $I$ - $D$  curves for different slopes with the existing models, it was found that  $I$ - $D$  curves constructed based on the physical model in this study are higher than for other models which are statistical lines and a probabilistic model. Meanwhile, the  $I$ - $D$  curves of other areas are obtained through statistics, and even though a single landslide occur in this area, it will be counted as landslide event. Meanwhile, many researchers have pointed out that antecedent rainfall plays a significant role in triggering landslides in loess areas which is different for other regions, such as Hong Kong, fire impacted areas in the US, and  
335 the southwest mountains in China (Cui et al., 2008; Zhuang et al., 2015). Therefore, the  $I$ - $D$  curves of other areas will be lower than the  $I$ - $D$  curve constructed based on physical models (Fig. 15).

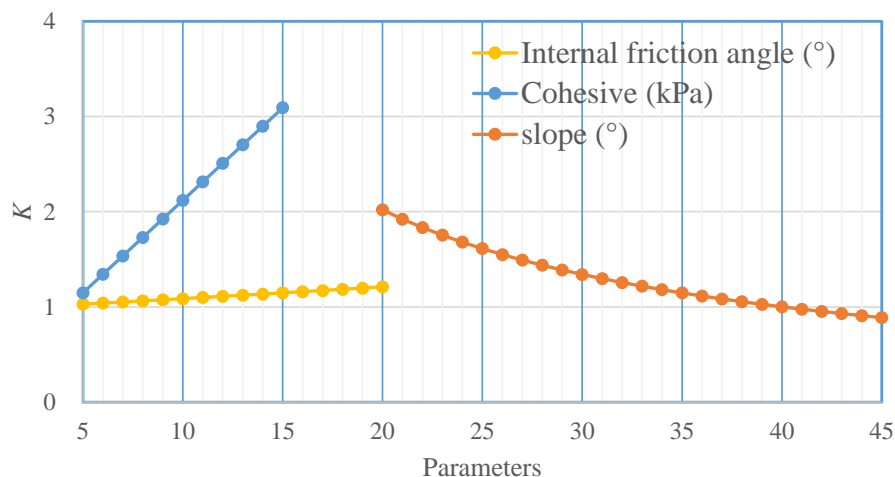


**Figure 15.** Comparison of I-D curves from the current and prior studies (Zhuang et al., 2015).

From the distribution of shallow landslides in this area, it can be seen that the shallow landslides in this area mainly occur on slopes of 35 to 50°. Marking the rainfall duration and intensity of the “7.25” loess sliding-flow landslide events and the “7.13” group shallow landslide in Yan’an in 2013 (Wang et al., 2015; Zhuang et al., 2017) on the *I-D* line, it can be seen that the rainfall duration and intensity of both events are above the *I-D* curve of 35° (Fig. 14), indicating that the constructed curve is reliable and can be used to forecast shallow landslides in this area.

## 5.2 Sensitivity analysis

Dry loess has high cohesive strength but loses strength significantly when wetted (Derbyshire et al. 2001; Zhuang et al., 2018) and has water-sensitivity characteristics, with the strength parameters changing rapidly with the water content increasing. According to existing research, the cohesion of loess can be reduced from greater than 50 kPa at a low water content to less than 10 kPa at high water content (Zhuang et al., 2018). The internal friction angle of loess varies slightly, generally from about 25 kPa in low water content to about 16 kPa in a saturated state. To assess the loess strength influence on shallow landslides caused by prolonged heavy precipitation, the response of the slope stability to the strength change of saturated loess was calculated. Our results demonstrate that slope stability is greatly affected by cohesion, while the stability of the slope is less responsive to changes in the internal friction angle. Meanwhile, by changing the slope and fixing loess strength, the relationship between safety factor and slope was obtained. The safety factor is varying obviously with slope changing, indicating that the cohesion and slope are key factors affecting soil stability and shallow landslides. Whereas the internal friction angle has minimal effect on shallow landslides in loess areas (Fig. 16).



**Figure 16.** The safety factor varies with slope, internal friction angle, and cohesion changing.

## Conclusions

A rainfall-induced slope failure is a common cause of shallow landslides in the Loess Plateau. This study examines the shallow  
360 loess landslide triggered by prolonged heavy rainfall on July 25, 2013, in Tianshui, China, as a case study. The following  
results were obtained:

1. The “7.25” loess sliding-flow landslide events triggered 47,005 landslides with a total area of 65.69 km<sup>2</sup> and the mean  
landslide area was 0.0013 km<sup>2</sup>, which is smaller than most landslides triggered by other rainfall or earthquakes. Most of the  
landslides evaluated (80%) are smaller than 2,000 m<sup>2</sup> and landslides larger than 5,000 m<sup>2</sup> accounted for only 3%, indicating  
365 that the “7.25” loess sliding-flow landslide events are primarily small landslides with group occurrences characters.

2. The  $H/L$  ratio frequency ratio of the “7.25” loess sliding-flow landslide events, ranged from 0.01 to 0.88 with a mean  
of 0.32. The equivalent coefficient of friction was below 0.17 for 16.85% of the loess landslides, indicating that the loess  
landslide travels via flow motion, resulting in sliding longer distances.

3. The Revised Infinite Slope Model (RISM) was proposed using equal differential unit method and corrected the  
370 deficiency that the safety factor increases with the slope increasing when the slope is larger than 50° calculated using the  
Taylor slope infinite model.

(4) The critical approximate liquid limit water content depth (also the sliding surface depth) of the shallow loess landslides  
with different slopes can be described as:  $h_w = 34.13a^{-1.15}$ . The critical  $I-D$  curve for slope instability for different slopes was  
constructed using the infiltration characteristics of loess in the study area.

375 *Code and data availability.* The data in this study were analysed with the Excel, and the figures were created with ArcViewTM  
GIS and Excel. All codes and data used in this work are available upon request.



*Author contributions.* Conceptualization, J. Z. and J. B.; methodology, J. Z. and C. H.; investigation, J. Z., J. B., J. X. and Y. Z.; data curation, J. Z. and J. X.; writing—original draft preparation, J. Z.; writing—review and editing, J. Z.; project administration, J. Z.; funding acquisition, J. Z. All authors have read and agreed to the published version of the manuscript.

380 *Competing interests.* The authors declare no conflict of interest.

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