

Review

of NHESS-2021-369 “*Characteristics of two tsunamis generated by successive Mw 7.4 and Mw 8.1 earthquakes in Kermadec Islands on March 4, 2021*” by Yuchen Wang, Mohammad Heidarzadeh, Kenji Satake, and Gui Hu

This is an interesting and, in general, is well written paper. However, I believe that some of the results can be and should be presented in a more informative and spectacular way and the entire text and figures should be polished! Therefore, my recommendation “Acceptable after revision”.

(1) My main suggestion is related to Figure 4 and the respective text. The most noteworthy point of this event and the corresponding study is that there were TWO earthquakes with an interval less than 2 hours between them. The authors declare that the tsunami waves associated with both events are clearly seen in Figure 4. But for readers (in contrast to the authors) this is not obvious! What the authors should do is to construct the theoretical *dispersion curves* for both events (following papers of *González and Kulikov, 1993* and *Kulikov, 2006*) and demonstrate that the observed *f-t* extrema are in good agreement with the theory. BTW, the source regions of these two events are relatively small; therefore, the dispersive effects for propagating waves should be clearly seen in the wavelet plots. All details and necessary equations can be found in *Fine et al. (2019)*.

The dispersion curves and corresponding *f-t* diagrams are constructed as functions of *frequency* (not of period!) (e.g. *Thomson and Emery, 2014*); now all plots in Figure 4 are upside down and wave dispersion is difficult to identify. (Actually, the authors themselves call these plots “frequency-time analyses”, not “period-time”). So the figures should be presented in the standard way.

I believe that if the authors prepare everything in the best way, the corresponding figure will become striking and highly quoted! The authors of the listed papers used the *f-t* diagrams to identify a specific event and to examine the dispersive properties of tsunami waves. However, I do not know any study where this approach has been used to identify and separate two events following each other!

(2) Spectral analysis, Figure 3. This figure is prepared in a very “unfriendly manner”! I know that the second author loves to combine a numerous number of plots in one figure. However, in that case the value of each plot tends to zero. What are the specific spectral features that the authors would like to demonstrate? Spectral peaks? The differences of the tsunami spectra from the background spectra? The differences between two tsunamis? Any of these features are unclear in this figure.

The spectra are strongly vertically compressed; the scale of the Y-axis looks strange: 10^{-5} , then 10^0 and nothing between! As a result, all spectra look flat. BTW, I believe that the dimension of the Y-axis is cm^2/Hz , not cm/Hz .

An additional question is units. Typical periods of seismic waves are second; therefore, it is natural use Hz for their frequencies. However, typical periods of tsunami waves are minutes and fractures of an hour. Besides, the sampling interval of the data is 1 min. Thus, it would be natural for tsunami spectra to use cycles per minute (cpm) or cycles per hour (cph). This will be helpful for readers, and they will not need to use a calculator to estimate the period of a specific spectral peak. (The same comment is just for Figures 5c and 5d).

Also, what is the meaning of the magic numbers for periods: 1,7, 16.7 and 166.7 min in the scale of periods?! The Nyquist period for these spectra is 2 min, the fundamental period is 120 min (2 hours). The meaning of the shown magic periods remains totally unclear and does not help a reader to detect the periods of spectral maxima.

The last but not least comment to these spectra: the confidence levels are not shown and without confidence levels all results of spectral analysis are senseless (e.g. *Thomson and Emery*, 2014).

(3) Figure 5c. The idea to estimate “relative spectra of tsunamis” as the ratio of various tsunami events was first proposed by *Miller* (1972). The authors mention this study (Line 44), but it is absent in the List of references. Also, they do not mention this paper when they discuss their Figure 5c.

It should be emphasized that this approach (the authors call it “empirical Green’s function”, EGF) does not allow to reconstruct the tsunami source spectrum because it shows not the properties of the second source themselves, but the *differences* of the second source from the first one. As was indicated by the authors (e.g. Lines 168-169), the seismic mechanisms of the two events are very similar. Therefore, the mutual part of the two sources (in particular, mutual spectral peaks) is not seen in Figure 5c. From this point of view, it would be interesting to see the tsunami/background ratio for the first event (i.e. a figure similar to Figure 5d, but for the first tsunami).

(4) Equation (1) (Line 183) is the exact solution for periods of standing (eigen) modes in a closed rectangular basin of uniform depth $h = \text{const}$. This equation for $n = 1$ allows to estimate very roughly the *order* of periods of generated tsunami waves. However, a real tsunami source is far away from being uniform and rectangular; thus, even for the first mode, this estimate is a very approximate. So, this estimate is rather qualitative than quantitative. From this point of view, it is strange to see that the authors use this equation for PRECISE estimation (with fractures of minutes!) the “source periods”, and even not only for the first but also for the secondary modes.

(5) The authors use a high-pass filter to remove tides from the original records; this is definitely not the best way to suppress tides! Any unnoticed spike, shift or gap (small in comparison with tides) will strongly distort the tsunami signal (and even create some “artificial tsunamis”; the corresponding examples are well known!). It is much better to subtract predicted or calculated tides (as was done by the authors in some other their papers. BTW, the authors write: “...we applied a second-order high-pass filter with the corner frequency of 0.00014 Hz (7,200 s) to remove the tidal components”. Why “Hz”, why “seconds”?! The sampling interval of the data is not seconds, but 1 min; it would be much easier for readers if the authors write: “We applied a 2-hour (or 120-min) high-pass window”!

Some polishing of the paper language will be useful; there are some problems with articles, etc.

Alexander Rabinovich

References

- Fine, I. V., Thomson, R. E., Chadwick, W. W., Jr, and Fox, C. G. (2019), Toward a universal frequency of occurrence distribution for tsunamis: statistical analysis of a 32-year bottom pressure record at Axial Seamount, *Geophysical Research Letters*, 47, e2020GL087372. <https://doi.org/10.1029/2020GL087372>
- González, F. I., & Kulikov, E. A. (1993). Tsunami dispersion observed in the deep ocean. In S. Tinti (Ed.), *Tsunamis in the World* (pp. 7–16). Dordrecht: Kluwer Acad. Publ.
- Kulikov, E. (2006), Dispersion of the Sumatra Tsunami waves in the Indian Ocean detected by satellite altimetry, *Russian Journal of Earth Sciences*, 8, ES4004, doi:10.2205/2006ES000214.
- Miller, G.R. (1972), Relative spectra of tsunamis. *Publ. HIG-72-8*, Hawaii Institute of Geophysics, University of Hawaii, Honolulu, 7 pp.
- Thomson, R. E., & Emery, W. J. (2014). *Data Analysis Methods in Physical Oceanography* (3rd ed., p. 716). New York: Elsevier Science.