



Ground motion prediction maps using seismic microzonation data and machine learning

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Abstract. Past seismic events worldwide demonstrated that damage and death toll depend on both the strong ground motion (i.e., source effects) and the local site effects. The variability of earthquake ground motion distribution is caused by local stratigraphic and/or topographic setting and buried morphologies, that can give rise to amplification and resonances with respect to the ground motion expected at the reference site. Therefore, local site conditions can affect an area with damage related to the full collapse or loss in functionality of facilities, roads, pipelines, and other lifelines. To this concern, the *near real time* prediction of damage pattern over large areas is a crucial issue to support the rescue and operational interventions. A machine learning approach was adopted to produce ground motion prediction maps considering both stratigraphic and morphological conditions. A set of about 16'000 accelometric data and about 46'000 geological and geophysical data were retrieved from Italian and European databases. The intensity measures of interest were estimated based on 9 input proxies. The adopted machine learning regression model (i.e., Gaussian Process Regression) allows to improve both the precision and the accuracy in the estimation of the intensity measures with respect to the available *near real time* predictions methods (i.e., Ground Motion Prediction Equation and shaking maps). In addition, maps with a 50 x 50 m resolution were generated providing a ground motion variability in agreement with the results of advanced numerical simulations based on detailed sub-soil models. The variability at short distances (hundreds of meters) was demonstrated to be responsible for 30-40% of the total variability of the predicted IM maps, making it desirable that seismic hazard maps also consider short-scale effects.

1 Introduction

Spatial distributions of ground motion induced by seismic events should be properly estimated to support risk mitigation policies over large areas. Moreover, seismic risk analysis, extended to spatially distributed anthropic systems, presents new challenges in characterising the seismic risk input, regarding the spatial correlation of the ground motion values. The ShakeMaps (Wald et al., 2021), provided by the US Geological Survey, is used globally for post-earthquake emergency management and response, engineering analyses, financial instruments, and other decision-making activities. Moreover, in Italy post-event ShakeMaps are delivered by the National Institute of Geophysics and Volcanology (Michellini et al., 2019,



31 <http://shakemap.rm.ingv.it/shake4/>). Such ShakeMaps are based on Ground Motion Prediction Equation (GMPE; Bindi et al.,
 32 2011, among the others) and data recorded from accelerometric stations when available.

33 Recently, artificial intelligence-based procedures were proposed to produce *near real time* ground motion in terms of
 34 acceleration time histories (Jozinović et al., 2021, Tamhidi et al., 2021) and Intensity Measure (briefly, IM; Kubo et al., 2020,
 35 among the others). In general, ground motion maps were generated using earthquake source parameters (location, magnitude,
 36 and the finite fault if available), IM (Peak Ground Acceleration, Peak Ground Velocity, and Spectral acceleration, briefly
 37 named PGA, PGV, and Sa, respectively) at the recording accelerometric stations and the mean shear wave velocity in the upper
 38 30 m, V_{S30} , as a proxy to account for site lithostratigraphic amplifications. Bearing in mind that shaking maps become available
 39 only when the first location and magnitude estimation are available, Jozinović et al. (2021) propose to use waveforms to predict
 40 the ground motion intensity by means of a Machine Learning (briefly, ML) approach (i.e., it utilizes only a training set of
 41 earthquake waveforms recorded at a pre-configured network of recording stations). Moreover, ML has been adopted to produce
 42 seismic amplification factors maps, as in the Japan case study proposed by Kim et al. (2020), rather than to provide ground
 43 motion maps. Finally, Zhou et al. (2020) propose a seismic topographic effect prediction model.

44 Overall, the above-mentioned works have pointed out what follows:

- 45 - hypocentral depth (H), epicentral distance (R), and magnitude (M) are widely used to estimate ground motion over large
- 46 areas considering the source effect; moreover, H, R, and M are provided few minutes after an earthquake;
- 47 - V_{S30} , the fundamental frequency of the deposit (f_0), and the depth to the engineering bedrock (H_{800}) are the key-parameters
- 48 which well gauge the effect of local sub-soil conditions on the seismic wave propagation (i.e., lithostratigraphic effect);
- 49 - elevation (h), topographic gradients (h_x and h_y , where x and y are two orthogonal directions), and second-order topographic
- 50 gradients (h_{xx} and h_{yy}) are proxies which allow to describe the morphological effects on the seismic amplification phenomena.

51 In this view, this work focuses on the improvement of ground motion prediction over large areas by using ML technique. The
 52 main task of this work is to suggest a procedure including all the main key-parameters together (i.e., H, R, M, V_{S30} , h, h_x , h_y ,
 53 h_{xx} , h_{yy}).

54 Damage pattern induced by seismic events is related to both geological/geomorphological conditions and vulnerability of
 55 structures and infrastructures (Brando et al., 2020; Fayjaloun et al., 2021; Mori et al., 2020b, 2019). The ground motion
 56 prediction (i.e., seismic site response) is generally evaluated by means of numerical simulations which are time consuming
 57 and require well detailed models capable of properly represents sub-soil and topographic conditions (see for example,
 58 Bouckovalas and Papadimitriou, 2005; Falcone et al., 2020a, 2020b, 2018; Gatmiri and Arson, 2008; Gazetas, 1982; Luo et
 59 al., 2020; Moscatelli et al., 2020b; Pagliaroli et al., 2014; Pitilakis et al., 1999; Régnier et al., 2016, 2018).

60 Hence, ML approach was adopted to:

- 61 i) implement H, R, and M parameters available few minutes after a seismic event;
- 62 ii) include both lithostratigraphic (V_{S30}) and morphological effects (h, h_x , h_y , h_{xx} , h_{yy});
- 63 iii) capture the spatial correlation at short distances (hundreds of meters) due to local site effects, which is essential for
- 64 reliable hazard assessments.



65 The main results of these elaborations are ground motion prediction maps (i.e., PGA, PGV, Sa) with the resolution of 50 x 50
 66 meters, which can reproduce the variability captured by advanced numerical modelling.

67 Seismological data (i.e., H, R, M, PGA, PGV, and Sa) retrieved from European and Italian networks (Luzi et al., 2016, 2019,
 68 2020), geological, geophysical, and geotechnical data from seismic microzonation (hereafter SM) studies (DPC, 2018), and
 69 morphological data (available at <http://www.eorc.jaxa.jp/ALOS/en/aw3d30/>) are presented in § 2. The ML approach is
 70 discussed in § 3. In detail, the § 3.1 is focused on the adopted ML approach in term of training and validation phase.
 71 Performances, presented in terms of Root Mean Square Error (RMSE) and residuals (i.e., difference between the base-10
 72 logarithms of observed and predicted values of PGA, PGV, and Sa), are compared to the results proposed by other studies
 73 (Jozinović et al., 2021; Michelini et al., 2019, Bindi et al., 2011).

74 For the seismic sequence that hit Central Italy in 2016-2017, ML results and maps are shown in § 3.2 and § 4, respectively.
 75 The seismic events in Central Italy of 2016 and 2017, began in August 2016 with epicentres located between Latium, Marche,
 76 and Umbria Regions. The first strong shock occurred on August 24, 2016, at 3:36 a.m. and had a magnitude of 6.0, with its
 77 epicentre located along the Tronto River valley, between the small municipalities of Accumoli and Arquata del Tronto. Two
 78 powerful replicas took place on October 26, 2016, with epicentres on the Umbria-Marche border, the first shock with
 79 magnitude 5.4 and the second with magnitude 5.9. On October 30, 2016, the strongest quake was recorded, with a moment
 80 magnitude of 6.5 with its epicentre in Umbria Region. On January 18, 2017, a new sequence of four strong tremors with a
 81 magnitude greater than 5 (with a maximum of 5.5) and epicentres located in Abruzzi Region took place. This set of events
 82 caused a total of about 41'000 displaced persons, 388 injured, and 303 deaths.

83 In detail, the paper refers to the 2 mainshocks of August and October, according to the available data (for the mainshock of
 84 October 30, 2016, much more accelerometric data are available and it is therefore possible to make more detailed analyses).
 85 Referring to the seismic event occurred in Central Italy on October 30, 2016, a test is proposed in § 3.2 in terms of residuals
 86 of the ground motion IMs (i.e., PGA, PGV, and Sa). Ground motion prediction maps, referred to the Central Italy event
 87 occurred on August 24, 2016, (i.e., the first destructive event of the Central Italy seismic sequence for which a great amount
 88 of studies have been published) are shown in § 4 to enlighten the capability of the proposed ML approach to gauge the ground
 89 motion variability at the urban scale. Moreover, with reference to § 4.1, the ground motion profiles, based on the proposed ML
 90 approach, are compared with results obtained by means of two completely different methodologies: 2D numerical modelling
 91 of seismic site response (Gaudiosi et al., 2021; Giallini et al., 2020; Grelle et al., 2020) and with the mean values predicted by
 92 the Italian ShakeMaps (<http://shakemap.rm.ingv.it/shake4/>). Finally, in the § 4.2, referring to the seismic event occurred on
 93 October 30, 2016 (i.e., the strongest of the Central Italy seismic sequence), the spatial correlation structures of the maps are
 94 analyzed in terms of sill and range in order to provide the relation between local site effects and spatial resolution of ground
 95 motion maps.

96 In a nutshell, the novelty of this work is the use of the ML approach based on the analysis of a huge database of geological,
 97 geophysical, and geotechnical data, built with SM studies for the entire Italian territory. The quality and quantity of this



98 database allow a robust application of ML including the prediction of local site effects (i.e., lithostratigraphic and
 99 morphological) on the seismic ground motion.

100 2 Input and output data for machine learning training and validation

101 The input and output data for the training of ML approach, were classified into three categories: seismological, geophysical,
 102 and morphological data. The ML approach was based on 15'779 seismological data referred to the log10 geometric mean of
 103 the horizontal component (geoH) referred to each IM (i.e., PGA, PGV, and Sa at 0.3 s, 1.0 s, and 3.0 s). Each value recorded
 104 by the accelerometric station, named output data in Table 1 (i.e., data to be reproduced by means of ML), represents an observed
 105 datum. In addition, Table 1 lists the used 9 predictors, named input data. Figs. 1 and 2 show the input and output data,
 106 respectively, adopted for the training phase of the selected ML approach and presented in this section. Furthermore, some data
 107 distributions seem to be imbalanced (e.g., magnitude, M, and elevation, h, Fig.1). An imbalanced training input dataset is
 108 characterised by an unequal distribution of values. For instance, focusing on M distribution, it results that: about the 50% of
 109 the available data is in the range 4-5, each of the 3-4 and 5-6 ranges are characterised by the 20% of the available data, and
 110 only the 10% of the available data are referred to $M > 6$. Moreover, focusing on elevation distribution, it results that: each of
 111 the 0-300 m, 300-600 m, and 600-900 m ranges are characterised by the 30% of the available data, about the 10% of the
 112 available data is in the range 900-1'200 m, and only the 5% of the available data are referred to elevation higher than 1'200 m.
 113 Consequently, when the ML algorithm learns the imbalanced data (see for example, Kubo et al., 2020) the learning focus is
 114 mainly on the fit of ground motions with magnitude lower than 6 or on the fit of site characterised by elevation lower than
 115 1'200 m. With reference to the selected training input dataset, the imbalance seems to be caused by a sampling bias since no
 116 high magnitude ground motions were registered by the available accelerometric stations and since few accelerometric stations
 117 have been installed at high elevation where the exposition at seismic event is very low. Hence, it seems a hard task to improve
 118 the training dataset. In addition, distributions referred to topographic gradients and V_{S30} are characterised by few data with
 119 respect to steep slopes and high V_{S30} values. Anyway, how to handle the imbalanced dataset in the regression problem was out
 120 of the scope of this work. Consequently, referring to a range of an input datum, it is expected that the lower the amount of
 121 training data the higher the uncertainty. To this end, referring to the output data, maps of standard deviation are reported in
 122 § 4.1.



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Table 1. Input and output data for ML training and validation.

Type of data	Category	Control Factors	Database	Ref.
INPUT	Seismological	H	hypocentral depth	Luzi et al., 2016 and 2020
		M	moment magnitude	Seismological DB
		R	epicentral distance	
	Geophysical	V_{S30}	the time-averaged shear-wave velocity to 30 m depth	Seismological DB or V_{S30} map
				Luzi et al., 2016 and 2020 DPC, 2018 Mori et al., 2020b
	Morphological	h	elevation	http://www.eorc.jaxa.jp/ALOS/en/aw3d30/
		h_x	first order partial derivative dx (E-W slope)	
		h_y	first order partial derivative dy (N-S slope)	ALOS World 3D-30m DEM
		h_{xx}	second order partial derivative ddy	
		h_{yy}	second order partial derivative dxx	
OUTPUT	Seismological	PGA	Peak Ground Acceleration	Luzi et al., 2016 and 2020
		PGV	Peak Ground Velocity	
		$Sa_{0.3}$	Spectral acceleration at 0.3 s	Seismological DB
		$Sa_{1.0}$	Spectral acceleration at 1 s	
		$Sa_{3.0}$	Spectral acceleration at 3 s	

129

130 *Seismological parameters*

131 Seismological parameters are retrieved from Italian and European databases. With reference to 1'434 recording accelerometric
 132 stations, PGA, PGV, spectral accelerations (i.e., Sa referred to 0.3 s, 1 s, and 3 s), H, R, and M were retrieved from European
 133 Strong Motion Database, briefly ESM, (Luzi et al., 2016) and Italian ACcelerometric Archive, herein ITACA, (Luzi et al.,
 134 2019). In detail, data referred to the Central Italy earthquake occurred on the 2016 and recorded by temporary network named
 135 3A have been archived only in the ITACA database (http://itaca.mi.ingv.it/ItacaNet_30/#/home). It is worth noting that Greek
 136 and Turkish seismic events data were collected to consider earthquake characterised by M value greater than 6.5 and up to 7.6.
 137 Moreover, earthquake characterised by H, R, and $\log_{10}PGA$ value greater than 30 km, 400 km, and 2 (cm/s^2), respectively,
 138 were selected. It should be noted that the ITACA and ESM selected data are referred to the shallow active crustal region (i.e.,
 139 SACR zone characterised by shallow events, $H < 35$ km, in agreement to Michelini et al., 2019). The distributions of



seismological data of the chosen events are shown in Figs. 1 and 2. The same figures also show the distribution of data described in the next part of this section.

Geophysical data

Dynamic site condition was described by means of the time-averaged shear-wave velocity (V_s) to a depth of 30 meters, the V_{s30} parameter. It is worth noting that the V_{s30} parameter has been successfully adopted to gauge lithostratigraphic effect on seismic wave propagation by Falcone et al. (2021). V_{s30} data (i.e., input data in ML approach), determined by means of *in situ* investigations, are also archived in the ESM and ITACA databases. With reference to ESM and ITACA sites not characterised by *in situ* surveys, the V_{s30} values were retrieved from Mori et al. (2020a). Fig. 1 shows the distribution of the V_{s30} data, referred to the selected sites.

The V_{s30} map proposed by Mori et al. (2020a), based on SM studies, was here adopted. The SM studies have been carried out for the Italian municipalities through the funds allocated after the 2009 L'Aquila earthquake, in the framework of the Italian program for seismic risk prevention and mitigation (Moscatelli et al., 2020a). Approximately 4'000 SM studies have been already planned, representing about 99.8% of the municipalities eligible for funding (i.e., having 475 years return period $PGA \geq 0.125g$). Out of the 4'000 planned SM studies, about 75% have been completed and approved (DPC, 2018; <http://www.webms.it/servizi/stats.php>). The SM studies permitted to collect, classify, and archive geological, geophysical, and geotechnical data with a uniform approach following national standard criteria (SM Working Group, 2008; TCSM, 2018). The data from *in situ* tests are organised into a database and georeferenced through an appropriate geographic information system, which is available at <http://www.webms.it> (DPC, 2018). About 35'000 borehole logs and 11'300 V_s profiles, related to about 1'700 Down-Hole and 9'600 MASW tests, were extracted from the SM dataset. Starting from the 11'300 V_s profiles, V_{s30} values were calculated. Mori et al. (2020b) derive a large-scale V_{s30} map for Italy, starting from the global morphological classes after Iwahashi et al. (2018), by integrating the large amount of data from the Italian SM dataset. The V_{s30} map by Mori et al. (2020a) was used here to integrate data where site-specific information was not available.

Morphological data

The morphological elevation h (i.e., an input morphological datum) was retrieved by the Advanced Land Observing Satellite (ALOS) World 3D-30m (herein AW3D30) digital elevation model (DEM). The free version of the DEM (available at <http://www.eorc.jaxa.jp/ALOS/en/aw3d30/>) adopted here has 1 arcsec resolution, which is equivalent to approximately 30 m at the Equator. AW3D-30m global DEM data were produced using the data acquired by the Panchromatic Remote Sensing Instrument for Stereo Mapping operated on the ALOS from 2006 to 2011. The Japan Aerospace Exploration Agency, that is the operator of the satellite, produced the global DEM using approximately 3 million images. Bearing in mind that AW3D30 model is the digital surface model which represents the canopy top and building roofs' elevations, Caglar et al. (2018) found that AW3D30 is the most accurate DEM among other similar data elevation products freely available. In detail, it was shown that the AW3D30 root mean square error is equal to 1.78 m.



Finally, a GRASS GIS command *r.slope.aspect* (<https://grass.osgeo.org>) was used to generate the other morphological proxies (i.e., h_x , h_y , h_{xx} , and h_{yy}). Such command generates raster maps of first and second order partial derivatives from a raster map of true elevation values (i.e., AW3D30 data in this study). Fig. 1 shows the distribution of the morphological data, referred to the selected sites.

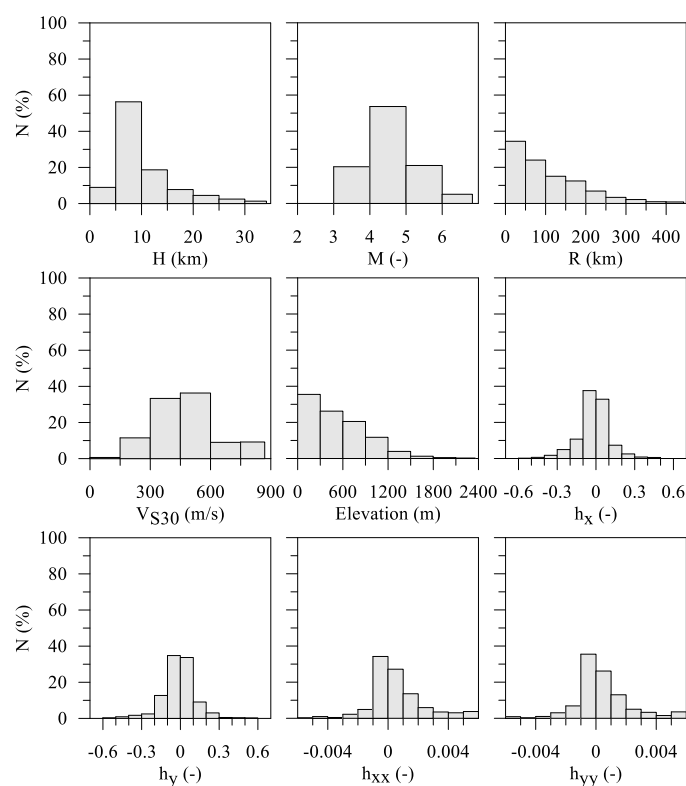


Figure 1. Distribution of input data referred to the training dataset.

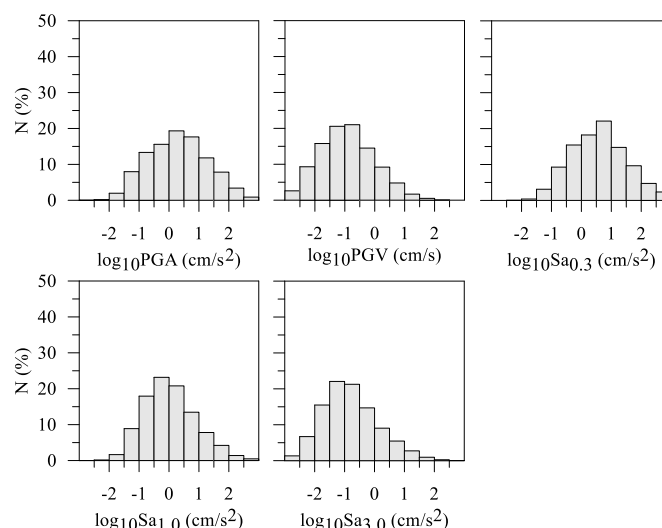


Figure 2. Distribution of output data referred to the training dataset in terms of geoH IMs.

3 Method

The “Matlab Regression Learner App” tool (<https://it.mathworks.com/help/stats/regression-learner-app.html>) was employed to produce ground motion prediction maps using a supervised ML approach. With this application, users can choose the desired models among many different methods to automatically train and validate regression models. After training multiple models, they can be compared to choose the best one. The application includes commonly used regression methods such as linear regression models, decision trees, support vector machines, ensembles of tree models, and Gaussian Process Regression (GPR). These models have all been tested; among them the best fitting performance in terms of RMSE was provided by the GPR model with exponential kernel (Table 2). GPR is a nonparametric, Bayesian approach to regression, which provides uncertainty measurements on the predictions. A detailed description of GPR method is outside the scope of this work. Suggested references for comprehensive descriptions of the GPR method are Rasmussen and Williams (2006) and chapter 6 of MathWorks (2019). A k-fold cross-validation (k=5) method as described in chapter 24 of Mathworks (2019) was used on the training dataset to make validation sets. The fitting performance (in term of RMSE) on the validation set was considered as an indicator for the generalization ability of model.

After this training and cross-validation phase, described in § 3.1 and comparison in terms of residuals with the performance of the existing methods, an external test is presented in § 3.2.

3.1 Training and validation phase

The mean RMSE of the five cross-validation datasets were adopted to select the best ML approach. With reference to the tested ML approaches, Table 2 lists the RMSE values for each predicted IM.



Table 2. RMSE, referred to all ML prediction models used to forecast \log_{10} geometric horizontal mean (geoH) of PGA, PGV, and Sa at 0.3 s, 1.0 s, and 3.0 s.

ML Prediction Model	Performance in term of RMSE				
	PGA	PGV	Sa(0.3s)	Sa(1.0s)	Sa(3.0s)
Linear Regression (Linear)	0.53	0.47	0.50	0.44	0.43
Linear Regression (Interactions Linear)	0.48	0.43	0.47	0.42	0.40
Linear Regression (Robust Linear)	0.53	0.47	0.50	0.44	0.43
Stepwise Linear Regression (Stepwise Linear)	0.48	0.43	0.47	0.42	0.40
Tree (Fine Tree)	0.42	0.38	0.42	0.39	0.38
Tree (Medium Tree)	0.40	0.36	0.40	0.38	0.36
Tree (Coarse Tree)	0.40	0.36	0.40	0.37	0.36
Support Vector Machine (Linear)	0.53	0.48	0.49	0.44	0.43
Support Vector Machine (Quadratic)	0.43	0.39	0.42	0.39	0.39
Support Vector Machine (Cubic)	0.40	0.36	0.40	0.37	0.36
Support Vector Machine (Fine Gaussian)	0.48	0.46	0.48	0.45	0.46
Support Vector Machine (Medium Gaussian)	0.37	0.34	0.38	0.35	0.34
Support Vector Machine (Coarse Gaussian)	0.43	0.39	0.42	0.39	0.38
Ensemble (Boosted Trees)	0.40	0.36	0.40	0.37	0.36
Ensemble (Bagged Trees)	0.33	0.31	0.33	0.31	0.31
Gaussian Process Regression (Squared Exponential)	0.38	0.35	0.39	0.36	0.35
Gaussian Process Regression (Matern 5/2)	0.37	0.34	0.38	0.34	0.34
Gaussian Process Regression (Exponential)	0.31	0.30	0.33	0.30	0.29

Referring to the best prediction model (i.e., GPR with exponential kernel), Fig. 3 shows the comparison between predicted and observed values.

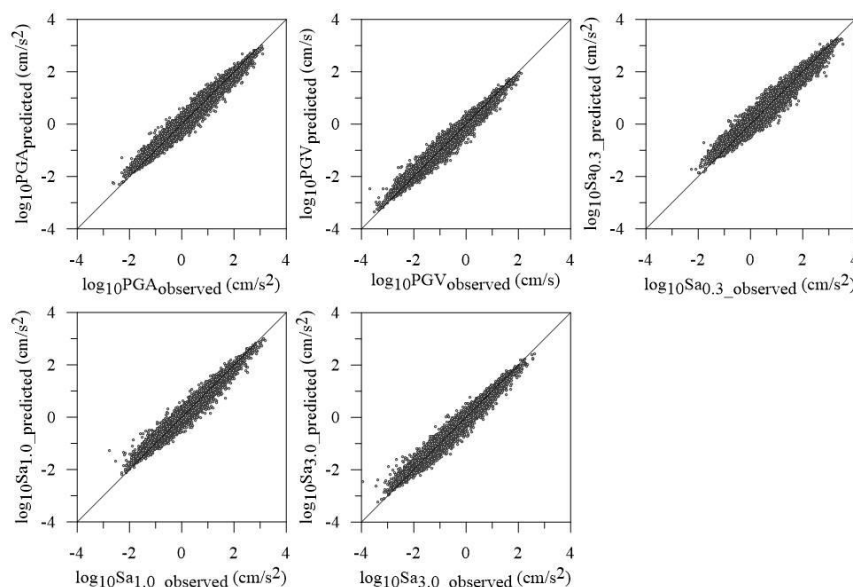


Figure 3. Comparison between observed and predicted values referring to the output data (i.e., geoH in terms of PGA, PGV, Sa_{0.3}, Sa_{1.0}, and Sa_{3.0}).



The performance of the GPR model is also presented in terms of mean value and standard deviation of the residuals' distributions (Table 3), where the residual is defined according to the Eq. (1) in agreement to what presented by other researchers (Bindi et al., 2011; Jozinović et al., 2021; Michelini et al., 2019). It should be noted that mean and standard deviation of the residuals' distributions referred to ShakeMap and GMPE were retrieved from the work of Jozinović et al. (2021) to evaluate the performance of the ML approach suggested in this study. It is worth noting that the suggested ML approach provide the best performance with respect to the approaches proposed by the other studies in terms of both accuracy (mean value) and precision (standard deviation). In detail, the standard deviation values are reduced by the 45-60%.

$$\text{residual} = \log_{10} \left(\frac{\text{IM}_{\text{observed}}}{\text{IM}_{\text{predicted}}} \right) \quad (1)$$

Table 3. Referring to the training dataset (15'779 data for each IM), comparison of mean and standard deviation values of the residuals' distributions obtained in this study and that reported by other works (geoH stays for geometrical mean of the horizontal components).

IM (geoH)	This study (ML)		ShakeMap		GMPE	
	mean	std	mean	std	mean	std
PGA	-0.000033	0.161	0.038	0.372	0.017	0.352
PGV	-0.000015	0.156	0.041	0.380	-0.151	0.330
Sa _{0.3}	0.000024	0.192	0.046	0.370	-0.252	0.359
Sa _{1.0}	0.000028	0.160	0.017	0.374	-0.198	0.303
Sa _{3.0}	-0.000072	0.159	-0.012	0.404	0.083	0.368

3.2 Testing phase

Mean and std values of the residuals' distributions are presented in this section with reference to the seismic event occurred on October 30, 2016 (briefly named test event), because it is the event with the most recordings of the whole dataset (241 accelerometric stations). It is worth noting that this event was not included in the dataset adopted for the training phase of the ML approach. Bearing in mind that 943 seismic events were characterised by $M \leq 6$ and 25 earthquakes by $M > 6$ (see Fig. 1 referred to the training dataset), the Central Italy earthquake occurred on October 30, 2016 ($M = 6.5$) provides a robust test of the adopted ML approach. The GMPE proposed by Bindi et al. (2014) (hereafter also Bindi GMPE) was selected to gauge the IMs at the 241 sites of interest aiming to compare the GMPE and this ML approach performances. It should be noted that the Bindi GMPE provide IMs depending on the V_{S30} as in this study. Furthermore, the OPENQUAKE software (Pagani et al., 2014) was used to determine the IMs values based on the selected GMPE.



Mean and std values referred to the test event (Table 4), are higher than those referred to the training and validation phase (Table 3), as expected, because the GPR model is trained on a few events with high magnitudes as discussed in § 2. Moreover, mean and std values obtained in this example are lower than those obtained by means of GMPE as shown in Table 4. In detail, the standard deviation values are reduced by the 20-30%. Therefore, the overall performance of the proposed ML approach is satisfactory also at the highest magnitude.

Table 4. Comparison of mean and standard deviation values of the residuals' distributions obtained in this study and by means of GMPE (Bindi et al., 2014), with reference to the earthquake occurred on October 30, 2016, (241 data for each IM; geoH stays for geometrical mean of the horizontal components).

IM (geoH)	This study		GMPE	
	mean	std	mean	std
PGA	0.0019	0.30	-0.19	0.43
PGV	0.0130	0.34	-0.16	0.42
Sa _{0.3}	0.0170	0.32	-0.18	0.39
Sa _{1.0}	-0.0550	0.35	-0.38	0.46
Sa _{3.0}	-0.0360	0.39	-0.23	0.55

4 Ground motion prediction map

After having demonstrated the goodness of the proposed method to reproduce IM values, this chapter presents examples of predictive maps produced by means of the exponential GPR model with a 50 x 50 m resolution. In § 4.1 the map for the August 24, 2016 seismic event of Central Italy is produced to compare some significant IM profiles produced with independent advanced numerical simulations and data retrieved from ShakeMaps (<http://shakemap.rm.ingv.it/shake4/>). In § 4.2 the map of the event of October 30, 2016, already used for the test phase, is analyzed in terms of spatial correlation structure.

4.1 Ground motion prediction map for August 24, 2016 seismic event of Central Italy and comparison with numerical modelling

The adopted GPR model was used to produce ground motion prediction maps referring to the earthquake occurred on August 24, 2016 (Fig. 4), with close ups for the Amatrice and Arquata villages (Fig. 5), where profiles of modelled spectral acceleration are already available (Gaudiosi et al., 2021; Giallini et al., 2020; Grelle et al., 2020).

The ground motion prediction map of the Sa_{0.3} reported in Fig. 4 is one of the cartographic results of this study; maps of PGA, PGV, and other spectral ordinates are in the supplementary materials. The theme of the map is the Sa parameter at T=0.3 s for an area around the epicenter of the event occurred on August 24, 2016, showing a maximum value equal to 2.25 g. Furthermore, referring to Fig. 4, macroseismic intensities, I_{MCS}, retrieved by Galli et al. (2017) are also reported next to the name of the



260 villages. The maps of Fig. 5 show close ups referred to Arquata del Tronto (top) and Amatrice (bottom). These maps were
 261 chosen because the 0.3 s period is the fundamental vibration period of most buildings in the area (i.e., 2-3 storey buildings).
 262 Moreover, 0.3 s is compatible with the results of modelling provided by Gaudiosi et al. (2021), Giallini et al. (2020), Grelle et
 263 al. (2020) for the same areas.

264 The maps of Figs. 4 and 5 show an output that is in good agreement with the geological and geomorphological characteristics
 265 of the territory and, therefore, highlights local site effects. In fact, referring to Fig. 4, it can be noted that the highest $S_{a0.3}$ values
 266 well describe the valleys' trend (i.e., the largest and continuous Tronto River valley) and the two extended areas in the southern
 267 part of the map (i.e., near Petrana and Torrita villages), which are characterized by lowest values of V_{S30} (Mori et al., 2020a).
 268 Fig. 5 shows the mean values of $S_{a0.3}$ in the left side and the standard deviation values in the right side. It should be noted that
 269 the uncertainty is provided by a combination of the input data values. The uncertainty increases referring to input data values
 270 for which the ML is not well trained (Fig. 1 and discussion in § 2). For instance, values around 0.3-0.4 are in the areas of
 271 inhabited villages, characterised by input data values widely represented in the training dataset, while values in the range 0.6-
 272 0.8 are observed in correspondence with the combination of high slope values and high V_{S30} values, which are underrepresented
 273 in the training dataset.

274 In addition to the maps, Fig. 6 show the profiles (2 at Amatrice and 1 at Arquata) of S_a at 0.3 s and the comparison with the
 275 values of the same shaking parameter, calculated with different methodological approaches: ground motion prediction with
 276 ML approach (this study), 2D numerical simulations (modified after Gaudiosi et al., 2021; Giallini et al., 2020; Grelle et al.,
 277 2020), and ShakeMap (<http://shakemap.rm.ingv.it/shake4/>). The three profiles were chosen because they represent three very
 278 different geological and geomorphological structures: narrow valley (section AA' in Fig. 6, Arquata del Tronto), plateau of
 279 soft ground (section BB' in Fig. 6, Amatrice), morphology of a mountain peak with coverage of soft ground (section CC' in
 280 Fig. 6, close to Amatrice). As a matter of fact, the adopted ML approach reproduces the so-called valley effect, as in the case
 281 of Arquata del Tronto shallow valley (see the trend for $200 \leq x \leq 400$ m in AA'), the combined lithostratigraphic and
 282 topographic effects, as in the case of Amatrice village (see the trend for $200 \leq x \leq 500$ m in BB'), and the topographic
 283 amplification, as in the case of the AMT accelerometric station (Luzi et al., 2019; see the trend for $100 \leq x \leq 200$ m in CC'). It
 284 should be noted that the trend of the values of our study reproduces that of the numerical simulations, also getting closer to the
 285 recorded values at Osservatorio Sismico delle Strutture (OSS, a network of buildings and bridges monitored *in continuum* by
 286 the Italian Civil Protection Department) site and AMT station (stars in BB' and CC'). Moreover, the profiles provided by the
 287 ML approach are much more articulated and complex than the constant value (horizontal dashed line) of the ShakeMap
 288 (<http://shakemap.rm.ingv.it/shake4/>), which obviously fails to grasp the local site effects at this scale.

289

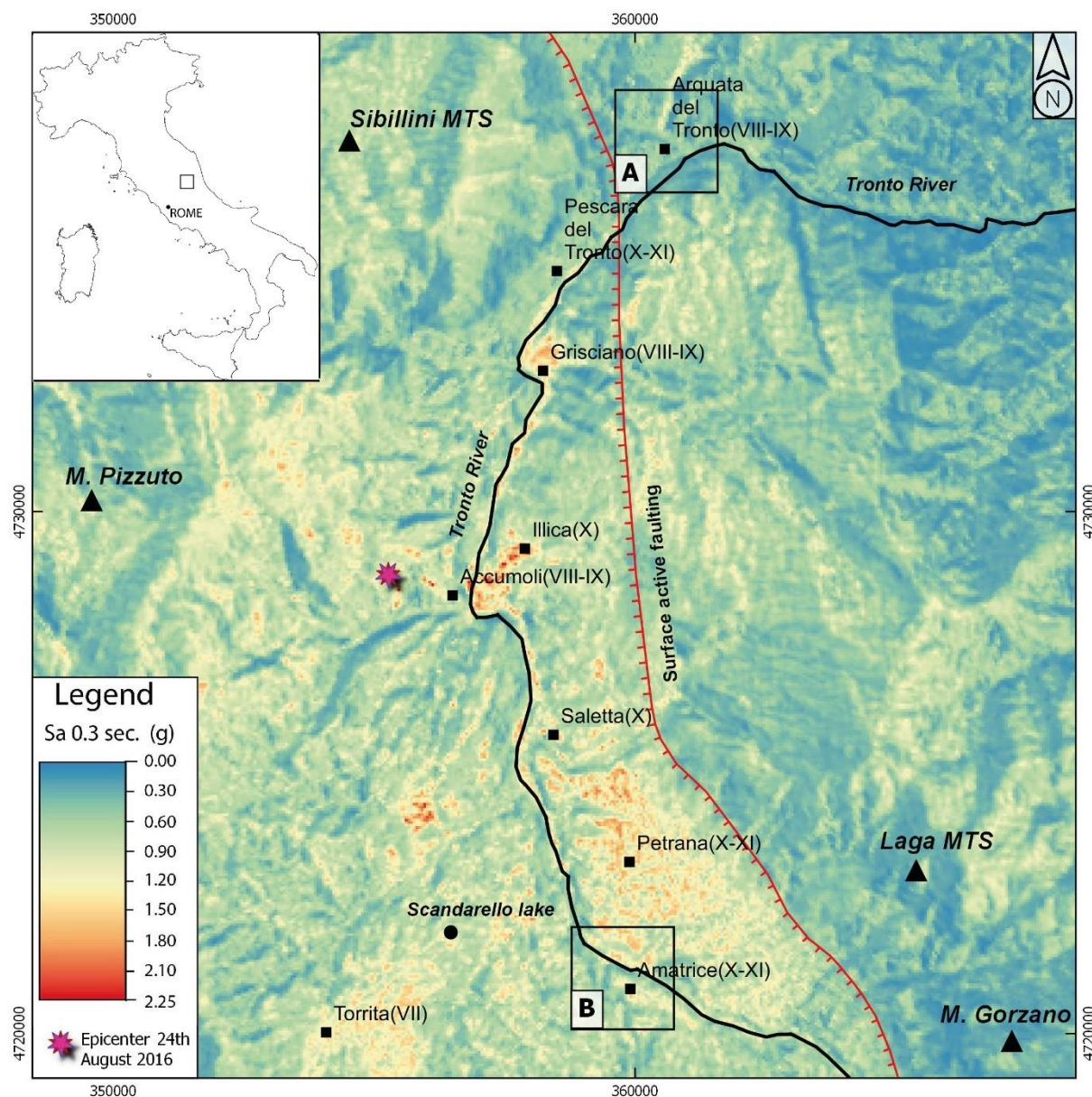


Figure 4. Ground motion prediction map of $Sa_{0.3}$ (resolution 50 x 50 m) referred to the Central Italy earthquake occurred on August 24, 2016. I_MCS values retrieved by Galli et al. (2017) are reported next to the name of the villages. A and B squares are referred to the close ups at Arquata del Tronto and Amatrice, respectively. The surface active faulting, sketched in the figure, has been slightly modified after Galli et al. (2017).

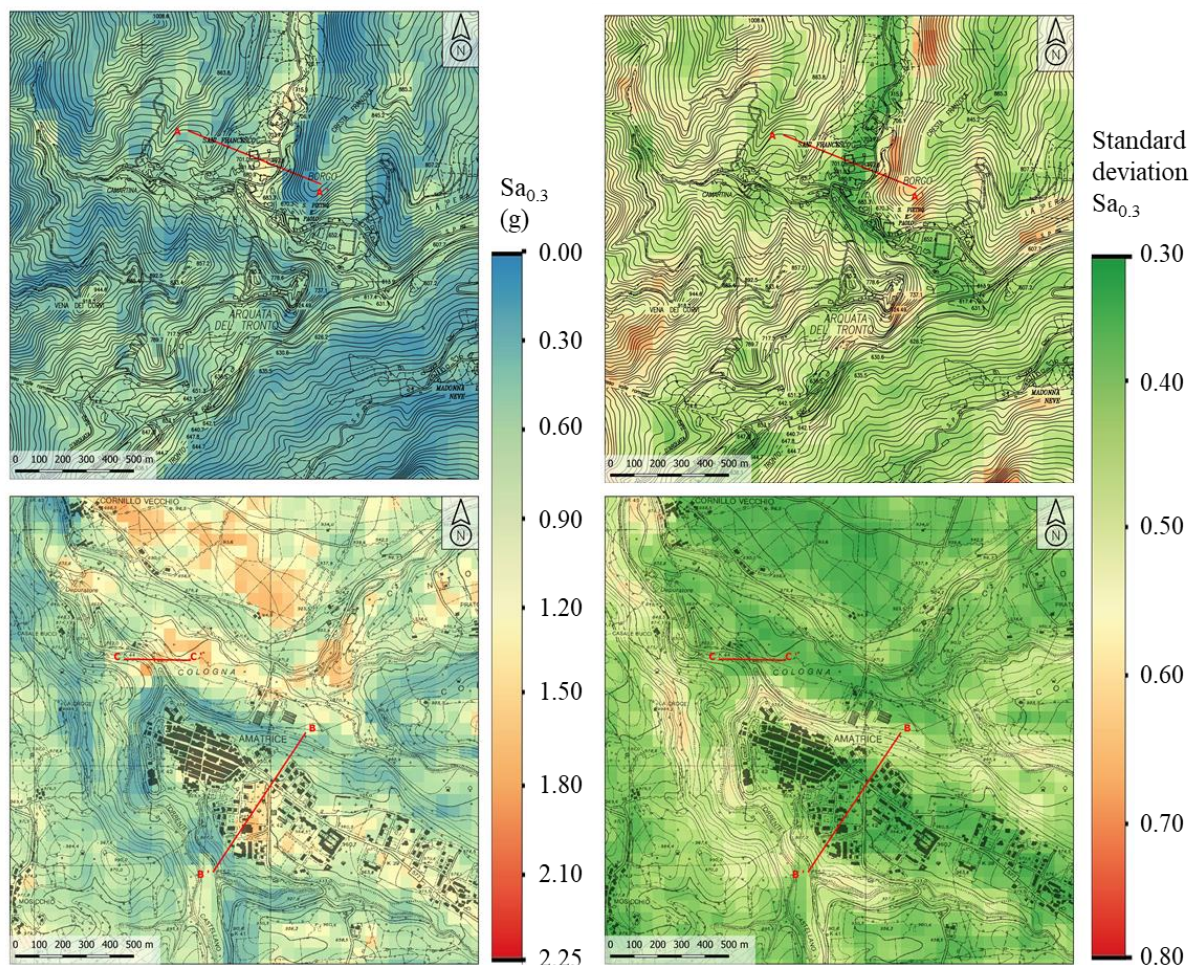


Figure 5. Ground motion prediction maps (Central Italy earthquake occurred on August 24, 2016) referred to the Arquata del Tronto (top) and Amatrice (bottom) in terms of $Sa_{0.3}$ mean value (left) and standard deviation (right) (resolution 50 x 50 m). The base topographic layer was retrieved from <https://www.regione.marche.it/Regione-Utile/Paesaggio-Territorio-Urbanistica/Cartografia/Repertorio/Cartatecnica numerica110000> and https://sciamlab.com/opendatahub/dataset/r_lazio_carta-tecnica-regionale-1991 with reference to Arquata del Tronto and Amatrice maps, respectively.

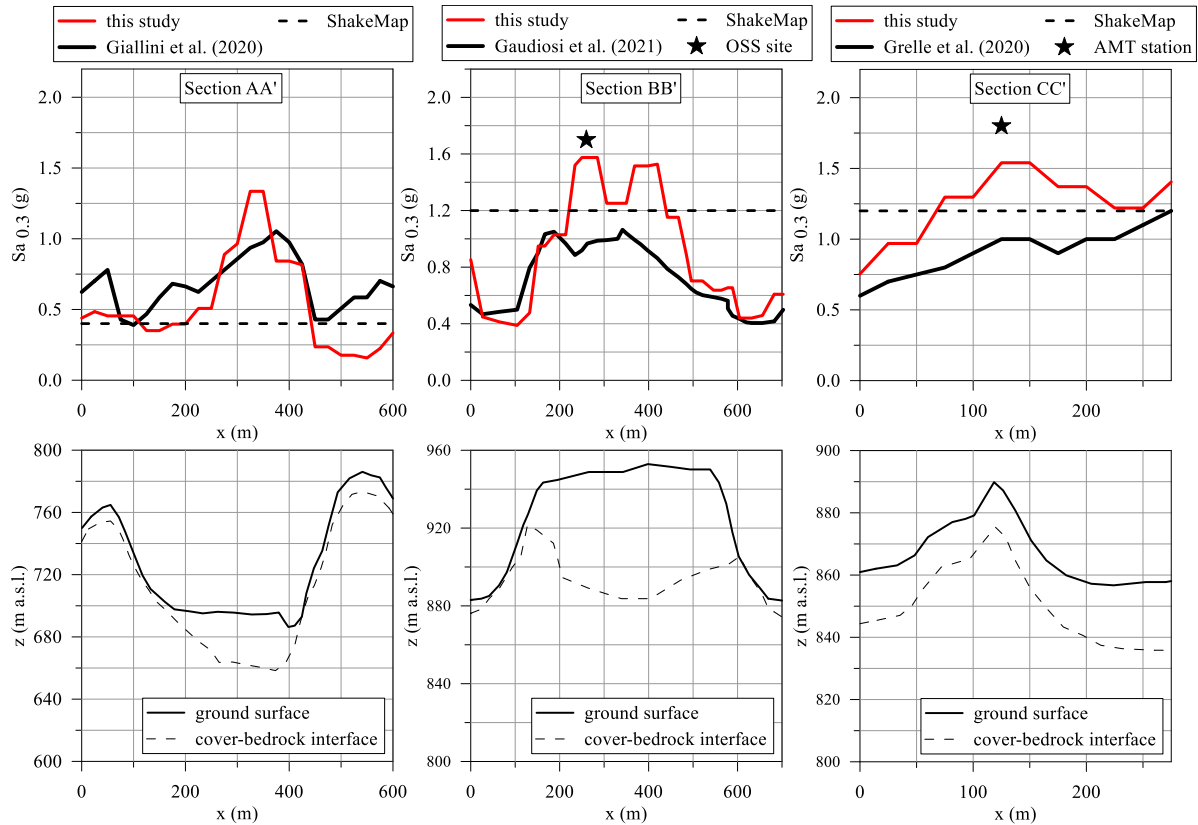


Figure 6. With reference to the Central Italy earthquake occurred on August 24, 2016, profiles of $Sa_{0.3}$ (top) and simplified sub-soil sections (bottom) referred to Arquata del Tronto (Section AA') and Amatrice (Sections BB' and CC'). $Sa_{0.3}$ profiles and geological information retrieved and modified after Gaudiosi et al. (2021), Giallini et al. (2020), Grelle et al. (2020); ShakeMap available at <http://shakemap.rm.ingv.it/shake4/>. The black stars indicate values recorded at the OSS site and AMT station (for details see the text).

4.2 Spatial correlation structure of the predicted maps

In this section we want to preliminarily deal with the spatial correlation of the IM parameters. In fact, the spatial correlation of ground-motion IMs represents a key issue in the seismic risk assessment, particularly in loss analysis (Infantino et al., 2021; Schiappapietra et al., 2020, 2021). The geostatistical tool widely adopted to analyse the spatial correlation of geological and geotechnical data (Paolella et al., 2021, Raspa et al., 2008, Salvatore et al., 2019, Spacagna et al., 2018) is the semi-variogram (Chilès and Delfiner, 2012). The spatial structure is evaluated by assessing the dissimilarity of the variables measured at different locations. First, referring to the variable of interest (in this case, one of the selected IMs), the experimental semi-variogram $\hat{\gamma}(h)$ is calculated from data using the method of moments (Chilès and Delfiner, 2012):



$$\hat{\gamma}(\mathbf{h}) = \frac{1}{2n(\mathbf{h})} \sum_{i=1}^{n(\mathbf{h})} \{z(\mathbf{x}_i) - z(\mathbf{x}_i + \mathbf{h})\}^2 \quad (2)$$

320

321 where $z(\mathbf{x}_i)$ and $z(\mathbf{x}_i + \mathbf{h})$ are the observed values of the variable z (i.e., one of the selected IMs) at the location \mathbf{x}_i and $\mathbf{x}_i + \mathbf{h}$
 322 separated by \mathbf{h} , and $n(\mathbf{h})$ is the number of pairs at lag \mathbf{h} . Under the assumption of second-order stationary, the semi-variogram
 323 increases with \mathbf{h} up to a constant value of $\hat{\gamma}(\mathbf{h})$. In this study, to assess the spatial structure of the variables (predicted IMs),
 324 the experimental variogram estimated from the predicted maps is fitted with the best fit model (i.e., the exponential model):
 325

$$\gamma(h) = C \left[1 - \exp\left(\frac{-3h}{a}\right) \right] \quad (3)$$

327

328 where the parameters a and C are called respectively range and sill. The range defines the correlation distance, namely, the
 329 separation distance at which the data are spatially independent, and the sill represents the variance of the random process, limit
 330 value of $\gamma(\mathbf{h})$.

331 For the Central Italy event occurred on October 30, 2016 and for all the predicted IMs maps (i.e., PGA, $Sa_{0.3}$, Sa_1 ; see Fig. 4
 332 and supplementary materials), the spatial structure was performed with the GSTAT package (Pebesma, 2004) of the R software
 333 (R Core Team, 2021). The IMs values were extracted from the predicted maps with a regular punctual grid of 50 x 50 m. The
 334 isotropic experimental semi-variograms were computed and fitted with the above-mentioned exponential model. As an
 335 example, Fig. 7 shows the semi-variogram of the predicted $Sa_{0.3}$ map. The spatial structure of all predicted IMs maps was
 336 characterized by the nested exponential model. The nested variograms highlight the presence of a double structure at different
 337 scales, i.e., a short-scale and a long-scale variability.
 338

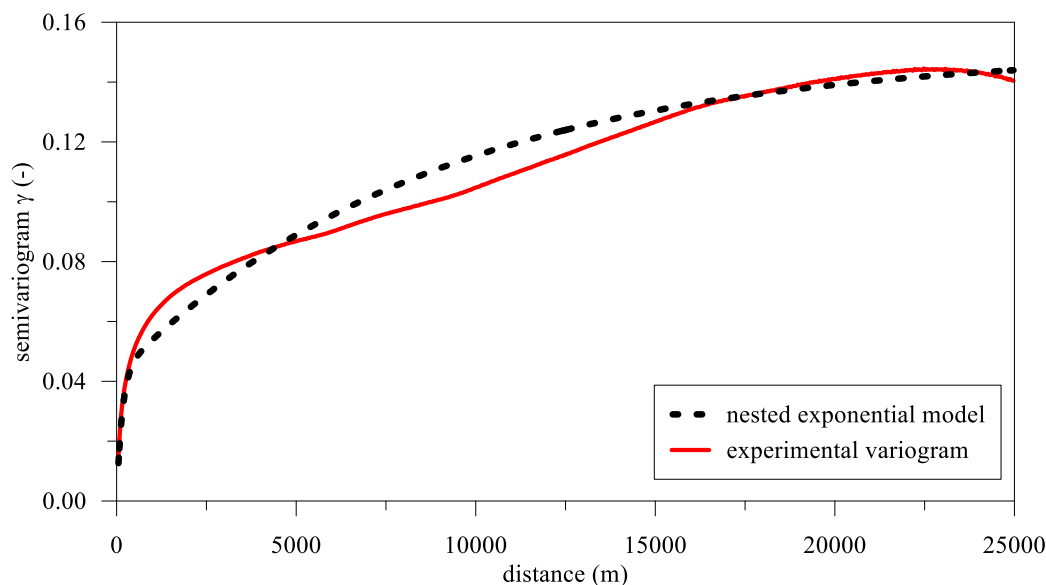


Figure 7. Semi-variogram of the predicted $Sa_{0.3}$ map (Central Italy event occurred on October 30, 2016): experimental variogram based on the adopted ML approach and best-fitting model (nested exponential).

In this case, two ranges and two sills are obtained for two levels of variability. Table 5 shows the sill and range values for the nested exponential models of all predicted IM maps. The first range, or short-scale structure, captures the first source of variability (first sill) over hundreds of meters and can be referred to lithostratigraphic site conditions and morphological variability. The long-scale structure captures the variability over thousands of meters and could be referred to regional geological units and large-scale morphological features. Furthermore, a significant part of the variance, around 30-40% of the total, are captured at short-scale.

An exhaustive treatment of this topic is beyond the scope of this work. We are now studying the spatial variability of input parameters that contribute to generate the target IM maps, and this will be the subject of a future paper. By the way, the preliminary results enlighten the importance to generate ground motion prediction maps with a spatial resolution in the order of hundreds of meters, to improve their quality in terms of predictivity. Seismic hazard maps should also include these specifications to consider the short-scale effects, even if starting from basic hazard maps with a resolution in the order of 2-5 km.

Table 5. Sill and range values of the nested exponential model for all the predicted IM maps.

IM	Short-scale structure		Large-scale structure	
	sill	range [m]	sill	range [m]
PGA	0.01080	600	0.022550	28500
$Sa_{0.3}$	0.04250	450	0.108000	26700
Sa_1	0.00530	450	0.010500	21600
Sa_3	0.00022	750	0.000265	20400



Discussion and conclusions

Intensity and frequency contents of ground motions can be altered by many factors. Up until now, numerous empirical models of ground motion amplification have been developed based on conventional regression analyses, considering few key factors such as intensity measures of rock motions, shear wave velocities of soils, and territory morphology. Since Machine Learning techniques have been applied to many fields, this work investigated on efficacy of using such techniques for developing models to predict ground motion over large areas with a 50 m resolution raster.

A set of about 16'000 ground motion data from Italian and European networks were adopted to train a Gaussian Process Regression model, while recordings by 241 stations of the seismic events occurred in Italy on October 30, 2016 were used to test the same model. Peak ground acceleration and velocity, and spectral acceleration referred to 3 periods (i.e., 0.3, 1, and 3 s) were compared to the recorded data allowing to obtain residuals. With reference to the training dataset, mean value and standard deviation of the residuals' distribution were found equal to about 0 and to about 0.1, respectively. With reference to the test dataset characterised by magnitude equal to 6.5, mean value and standard deviation of the residuals' distribution were found equal to 0.01 and 0.3, respectively. Hence, the performance of the adopted Machine Learning technique was confirmed satisfactory also with reference to magnitude higher than 6.

In addition, maps of ground motion in terms of peak ground acceleration, peak ground velocity, and of spectral acceleration referred to the selected three periods were produced with reference to the Central Italy seismic event occurred on August 24, 2016. Profiles of intensity measures were in satisfactory agreement with those obtained by means of advanced numerical simulations of seismic site response referring to the same seismic event. Moreover, the adopted Machine Learning approach greatly improves the performance of existing methods.

Three main novelties of the work are synthesized in the following.

- 1) Forecast of ground motion with high resolution (i.e., a 50 x 50 m raster), in agreement with results of local scale numerical modelling. This outcome is achieved by means of Machine Learning techniques and large datasets referred to morphological, geological, geophysical, and geotechnical features (mainly the seismic microzonation dataset; <https://www.webms.it/>). Moreover, about 1'000 seismic events recorded by 1'434 accelerometric stations (<https://esm.mi.ingv.it/>; http://itaca.mi.ingv.it/ItacaNet_30/#/home) were analysed. The Machine Learning approach combines morphological and subsurface proxies: elevation, first and second order topographic gradient (define the morphological characteristics of the territory), mean shear wave velocity in the upper 30 m (defines the dynamic response of a site referred to the subsoil condition). Magnitude, epicentral, and hypocentral distances provide the source conditions.
- 2) Use of robust statistical techniques such as Gaussian Process Regression. Among the machine learning based models, the model developed by the regression and Gaussian approach provides the best performance in terms of both precision and accuracy, that is referred to standard deviation and mean value of the residuals' distribution.



387 3) Production of maps with "internal" spatial correlation structures. With reference to the Central Italy earthquake occurred
 388 on October 30, 2016, the spatial structure of all predicted intensity measures maps is characterized by a nested exponential
 389 model providing a variance, captured at the short scale, in the range 30-40% of the total variability.

390 In terms of applications, the ground motion maps generated by means of the proposed Machine Learning approach are useful
 391 both for urban planning (aimed at reducing seismic risk) and for emergency management (aimed at a *near real time* estimation
 392 of damage to buildings and infrastructures). With reference to the emergency phase, by knowing the position and depth of the
 393 hypocentre and the magnitude of the event (in Italy these data are available a few minutes after the event), it is possible to
 394 predict the losses in the area struck by the earthquake in near real time. Overall, bearing in mind that the paradigm should be
 395 shifted from managing disasters to managing risk, the proposed methodology could represent a key-tool in seismic risk
 396 mitigation strategies deployed both pre and post seismic event.

397 In conclusion, the research on this topic will continue and focus on specific goals, which are listed in the following.

- 398 - Improve the method with more input proxies, made available after the seismic microzonation project for the whole national
- 399 territory. In detail, maps of the depth to the engineering bedrock and of the fundamental frequency of the deposit will be soon
- 400 available and allow to use such parameters as input data for the Machine Learning approach.
- 401 - Improve the method with worldwide seismological dataset.
- 402 - Improve the spatial resolution of existing input proxies integrating remote sensing data.
- 403 - Improve the spatial correlation analysis.

404 **Author contributions**

405 Conceptualization: FM, GA. Data curation: FM, AM, RS. Formal analysis: FM, RS. Funding acquisition: MM. Methodology:
 406 FM, AM, GF, GA, RS, MM, GN. Project administration: MM. Supervision: FM, MM, GN. Validation: FM, AM, GF, GA.
 407 Visualization: AM, GF. Writing – original draft preparation: FM, GF, GN. Writing – review & editing: FM, AM, GF, GA,
 408 RS, MM, GN.

409 **Competing interests**

410 The authors declare that they have no conflict of interest.

411 **Acknowledgements**

412 Authors would like to thank F. Bramerini, S. Castenetto, A. Gorini and D. Spina, (Italian Department for Civil Protection), for
 413 the useful discussions. We also thank S. Giallini and I. Gaudiosi (both from CNR IGAG, Italy) for providing the ground motion
 414 data obtained by means of numerical simulation referred to Amatrice and Arquata del Tronto areas (Italy).



415 Financial support

416 This research was supported by the Presidency of the Council of Ministers, Italian Department for Civil Protection, in the
 417 framework of the project “Contratto concernente l’affidamento di servizi per il programma per il supporto al rafforzamento
 418 della Governance in materia di riduzione del rischio sismico e vulcanico ai fini di protezione civile nell’ambito del PON
 419 Governance e Capacità Istituzionale 2014–2020 - CIG6980737E65” (M. Moscatelli scientific coordinator for CNR).

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