

Introducing SlideforMap; a probabilistic finite slope approach for modelling shallow landslide probability in forested situations

Feiko Bernard van Zadelhoff¹, Adel Albaba¹, Denis Cohen², Chris Phillips³, Bettina Schaeffli⁴, Lucas Karel Agnes Dorren^{1,5}, and Massimiliano Schwarz^{1,5}

¹Bern University of Applied Sciences - HAFL, Länggasse 85, CH-3052 Zollikofen, Switzerland

²COSCI Ltd.

³Manaaki Whenua - Landcare Research, Lincoln, New Zealand

⁴Institute of Geography (GIUB) & Oeschger Centre for Climate Change Research (OCCR), University of Bern, 3012 Bern, Switzerland

⁵Int. ecorisQ Association, P.O. Box 2348, 1211 Geneva 2, Switzerland

Correspondence: Van Zadelhoff F.B. (feiko.vanzadelhoff@bfh.ch)

Abstract. Shallow landslides pose a risk to infrastructure and residential areas. Therefore, we developed SlideforMAP, a probabilistic model that allows for a regional assessment of shallow landslide probability while considering the effect of different scenarios of forest cover, forest management and rainfall intensity. SlideforMAP uses a probabilistic approach by distributing hypothetical landslides to uniformly randomized coordinates in a 2D space. The surface areas for these hypothetical landslides are derived from a distribution function calibrated on observed events. For each generated landslide, SlideforMAP calculates a factor of safety using the limit equilibrium approach. Relevant soil parameters are assigned to the generated landslides from log-normal distributions based on mean and standard deviation values representative for the study area. The computation of the degree of soil saturation is implemented using a stationary flow approach and the topographic wetness index. The root reinforcement is computed by root proximity and root strength derived from single tree detection data. The ratio of unstable landslides to the number of generated landslides, per raster cell, is calculated and used as an index for landslide probability. We performed a calibration of SlideforMAP for three test areas in Switzerland with a reliable landslide inventory, by randomly generating 1000 combinations of model parameters and then maximising the Area Under the Curve (AUC) of the Receiver Operation Curve. The test areas are located in mountainous areas ranging from 0.5 – 7.5 km² with mean slope gradients from 18 - 28°. The density of inventoried historical landslides varies from 5 – 59 slides/km². AUC values between 0.72 and 0.94 indicated a good model performance. A qualitative sensitivity analysis indicated that the most relevant parameters for accurate modeling of shallow landslide probability are the soil thickness, soil cohesion and the root reinforcement. Furthermore, we show that the inclusion of single tree detection improves overall model performance. In conclusion, our study shows that the approach used in SlideforMAP can reproduce observed shallow landslide occurrence at a catchment scale.

keywords: mountain forest, shallow landslide probability, probabilistic modelling, single tree detection, root reinforcement

20 *Copyright statement.* The article and corresponding preprints are distributed under the Creative Commons Attribution 4.0 License. Unless otherwise stated, associated material is distributed under the same licence

1 Introduction

Landslides pose serious threats to inhabited areas world-wide. They are the cause of 17% of the fatalities due to natural hazards in the period of 1994–2013 (Kjekstad and Highland, 2009). Average annual monetary losses over the period of 2010–
25 2019 are approximately 25 billion US dollars (Munich RE, 2018). In addition, Swiss Re Institute (2019) notes a significant increase in damages by hydrologically related natural hazards over the past 5 years, including hydrologically-triggered shallow landslides. This has been attributed to increased urbanization in risk-prone areas and to an increase in heavy rainfall events. Furthermore, Swiss Re Institute (2019) notes that the modelling of shallow landslides is underdeveloped compared to the severity of the danger they pose. In mountainous regions, landsliding is a prominent natural hazard. For instance, in the Alpine
30 parts of Switzerland, 74 people have died as a result of landslide events between 1946 and 2015 (Badoux et al., 2016). The annual cost of landslide protective measures alone is approximately 15 million CHF each year (Dorren and Sandri, 2009). No distinction is made between deep-seated and shallow landslides in these numbers. Rain induced shallow landslides are one of the most important and dangerous types of mass movement in mountainous regions (Varnes, 1978). Shallow landslides are defined as translational mass movement with a maximum soil thickness of 2 m and are the main focus in this paper.
35 Fortunately, improvements in hazard assessment have significantly decreased the number of shallow landslide related deaths over the past decades (Badoux et al., 2016). This general trend is also supported by long-term data (Munich RE, 2018). The fatality decrease is related to better organizational measures regarding hazards, such as warning based evacuations and road closures. Biological measures, such as management of protection forests, also play a role in mitigation of natural hazards. The latter role is especially important for (shallow) landslides, rockfall, snow avalanches and debris flows (Corominas et al., 2014).
40 Modelling of shallow landslide triggering has been an ongoing process. Shallow landslide probability has been modelled mostly using a deterministic approach (Corominas et al., 2014). The deterministic approach is defined by using average values of risk components and resulting in a univariate result (Corominas et al., 2014). An example of a deterministic approach in this sense is the SHALSTAB model of Dietrich and Montgomery (1998). Other contemporary examples are TRIGRS (Baum et al., 2002) and SLIP (Montrasio et al., 2011), the latter showing good results in assessing soil saturation in a spatial het-
45 erogeneous way. In a comparative research it was noted that the SHALSTAB approach was not representative for the spatial variability of the parameters at a small scale (Cervi et al., 2010). In recent decades, the development of probabilistic models and statistical methods has improved model performance for quantifying landslide probability and the interpretation of their results (Corominas et al., 2014). In statistical methods (e.g. Baeza and Corominas, 2001), there is no explicit accounting of physical processes. In contrast, probabilistic methods take physical processes into account and additionally quantify the reli-
50 ability of the results considering the probability distribution of values of one or more input parameters (Salvatici et al., 2018). The output is a probability rather than a univariate result. A prime example of a probabilistic model in SINMAP (Pack et al., 1998). Generally, these models perform better than deterministic ones (Park et al., 2013; Zhang et al., 2018), likely due to

natural landslides having a mode of movement significantly controlled by internal inhomogeneities and discontinuities in the soil (Varnes, 1978). These control mechanisms are unpredictable at small-scales, making it hard for deterministic models to
55 identify exact locations of instabilities and adjust the heterogeneous parametrization accordingly. Below we go into more detail on the initiation of shallow landslides.

Initiation of instability is a process that combines mechanical and hydrological processes on different spatial and temporal scales and can thereby be very localized, with successive movement increasing the magnitude of the event (Varnes, 1978). In alpine environments, instabilities are typically triggered by rainfall, leading to soil wetting and ensuing increase of pore
60 pressure, which destabilizes the soil and can then initiate soil movement. An increase in pore pressure can build up in minutes to months following a rainfall event (Bordoni et al., 2015; Lehmann et al., 2013), where rapid pore pressure changes are attributed to macropore flow and slow pore pressure changes to the matrix water flow. The higher the horizontal hydraulic conductivity of the soil, the faster pore pressure changes can develop (Iverson, 2000). The reaction of pore pressure to rainfall is variable and highly dependent on soil type. A key experimental study is the work of Bordoni et al. (2015) in which in-situ measurements
65 were taken on a slope with clayey–sandy silt and clayey–silty sand soils that experienced a shallow landslide. It showed that intense rainfall and a rapid increase of pore pressure were the triggering factors of the landslide. Over the duration of the measurements, comparable saturation degrees have been reached both during prolonged and intense rainfall events. Prolonged rainfall did not result in the pore pressure required to trigger a shallow landslide. Similar behaviour has been observed in an artificially triggered landslide in Switzerland (Askarinejad et al., 2012; Lehmann et al., 2013; Askarinejad et al., 2018). In the
70 first wetting phase (in the year 2008), homogeneously induced rainfall with a duration of 3 days, an accumulated rainfall of 1700 mm and an intensity of 35 mm/hr, induced a maximum pore water pressure of 2 kPa at 1.2 m soil depth, resulting in no landslide. In the second phase of the experiment (2009), the rainfall was heterogeneous, with a maximum intensity of 50 mm/hr in the upper part of the slope that induced an increase of pore water pressure up to 5 kPa at 1.2 m soil depth, resulting in the triggering of a shallow landslide. The triggering was reached after 15 hours with a cumulative rainfall of 150 mm. In
75 addition, a computational study by Li et al. (2013) showed that at a high rainfall intensity (80 mm/hr), the pore water pressure at a depth of 1 m reached a constant value within 1 hour. For a lower intensity of 20 mm/hr, this took approximately 3 hours. This shows that landslide triggering is related to a fast build up of pore water pressure proportional to rainfall intensity. The work of Wiekenkamp et al. (2016) suggests that preferential flow dominates the runoff in a heterogeneous catchment during extreme precipitation events. Water can move downslope very rapidly through macropores (in experimental conditions) under
80 both saturated and unsaturated conditions (Mosley, 1982). The role of macropores can be important in a closed soil structure or in the presence of a shallow impermeable bedrock, where they control the soil hydrological behavior. Further examples of the influence of macropores on hillslope hydrology in various soil types are presented in the work of Weiler and Naef (2003) and Bodner et al. (2014). Additionally, Torres et al. (1998) demonstrates the strong role of macropore in preferential flow paths for landslide triggering in an artificial rain experiment in a loamy sandy soil. Montgomery et al. (2002) and Montgomery and
85 Dietrich (2004) also underline the importance of macropore flow, but state that the vertical flow governs response time and build up of pore pressure rather than the lateral flow in their study areas.

The mechanical aspect of shallow landslide initiation usually results from local instabilities that could extend indefinitely in a infinite constant slope if the shear resistance is low (Varnes, 1978). In complex topography, however, the passive earth pressure at the bottom of the triggering zone reacts with a resisting force, contributing thereby to landslide stabilisation (Schwarz et al., 2015; Cislighi et al., 2018). It is important to note here that the passive earth pressure is activated in a later phase of the triggering of a shallow landslide and should not be added to active earth pressure or tensile forces acting along the upper half of the shallow landslide (Cohen and Schwarz, 2017).

Besides hydrology, slope and soil characteristics, vegetation plays a key role in landslide triggering (Salvatici et al., 2018; Corominas et al., 2014; Greenway, 1987; González-Ollauri and Mickovski, 2014). The role of vegetation can be subdivided in hydrological and mechanical effects. The hydrological effect influences effective soil moisture by interception, increased evapotranspiration and increased infiltration (Greenway, 1987; Masi et al., 2021). Over the short timescale with intense rainfall these hydrological effects are negligible (Feng et al., 2020). Among the mechanical effects, root reinforcement, mobilized during soil movement, is an essential component (Greenway, 1987; Schwarz et al., 2010). It is a leading factor in the failure criterion for many vegetated slopes (Dazio et al., 2018). In modelling studies, the influence of root reinforcement on slope stability is often quantified as an apparent added cohesion (Wu et al., 1978; Borga et al., 2002). This apparent cohesion in turn can be added in the limit equilibrium computation of a Safety Factor (SF). Using a Monte Carlo approach of this method (Zhu et al., 2017), it was found that the SF can gain up to 37% stability when including vegetation root reinforcement. In another study in New Zealand, trees showed an effect on soil stability up to 11 meter away from their position and had the ability to prevent 70% of instability events (Hawley and Dymond, 1988). Computational research furthermore shows that root reinforcement by the larger roots is dominant over the smaller roots, even though they are far less numerous (Vergani et al., 2014). The planting pattern and management of the vegetation can have a profound effect on root reinforcement and thus on slope stability (Sidle, 1992). Therefore a detailed approach to calculate the spatial distribution of root reinforcement is important for slope stability calculations. Root reinforcement can be subdivided into two major components: Basal root reinforcement and lateral root reinforcement. Basal root reinforcement is the anchoring of tree roots through the sliding plane into the deeper soil. Lateral root reinforcement is the reinforcement from roots on the edges of the potential slide that stick into the soil outside of the potential slide (Schwarz et al., 2010). In contrast, the mechanical influence of vegetation weight on slope stability is often considered negligible (Reinhold et al., 2009). In current shallow landslide probability modelling, whether deterministic or probabilistic, root reinforcement is generally modelled in a simplified or unrealistic way, for example, including homogeneous and displacement independent root reinforcement (Montgomery et al., 2000). This method limits the evaluation of the effects of different forest spatial properties such as forest structure, and the contribution of different root reinforcement mechanisms to slope stabilisation (Schwarz et al., 2012). In order to overcome this limitation, we develop a shallow landslide probability model, named SlideforMAP. To ensure a wide applicability, SlideforMAP is specifically designed to be applied on a scale of 1 - 1000 km². The main objectives of this work are to:

- Present the SlideforMAP model as a tool for shallow landslide probability assessment.

- 120 – Show a calibration of SlideforMAP through a performance indicator over three study areas with 78 field recorded shallow landslide events in Switzerland
- Provide a qualitative sensitivity analysis and identify the parameters that are of greatest influence on the slope stability of a given area.

Strong emphasis within the SlideforMAP framework and this paper is put on the quantification of root reinforcement on a regional scale. We will show the effect of accurate, quantitative, representation of root reinforcement has on slope stability over three study areas. Simplifications and calibration constraints make it hard to use SlideforMAP as an exact forecast tool. The main application for SlideforMap is as a tool to quantify the effects of vegetation planting, growth and/or management for land managers in relation to shallow landslides.

2 Methods: SlideforMap

130 2.1 Probabilistic modelling concept

SlideforMAP is a probabilistic model that generates a 2D raster of shallow landslide probability (p_{SL}). It is an extension of the approach of Schwarz et al. (2010) and Schwarz et al. (2015). It generates a large number of hypothetical landslides (HLs, singular: HL) within the limits of a pre-defined region of interest. These HLs are assumed to have an elliptic shape and are characterized by a mix of deterministic and probabilistic parameters, from which the landslide stability is computed following the limit equilibrium approach (section 2.2). The probabilistic parameters are the HL location, its surface area and its soil cohesion, internal friction angle and soil thickness parameters (drawn from appropriate random distributions). The location and surface area are approached in a probabilistic way to compute a spatial probability distribution. The soil parameters are probabilistic because we assume their variation is high and important in mountainous environments. The deterministic parameters include several vegetation parameters and hydrological soil parameters. A key originality of the approach stems from the fact that the vegetation parameters can be derived from single-tree scale information (section 2.5). The number of generated landslides is high enough such that each point in a region of interest is overlain by multiple HLs from which a relative p_{SL} can be estimated by considering the ratio of unstable HLs. A general flow chart of SlideforMAP is given in Fig. 1. More details on the modules follow in the subsequent sections.

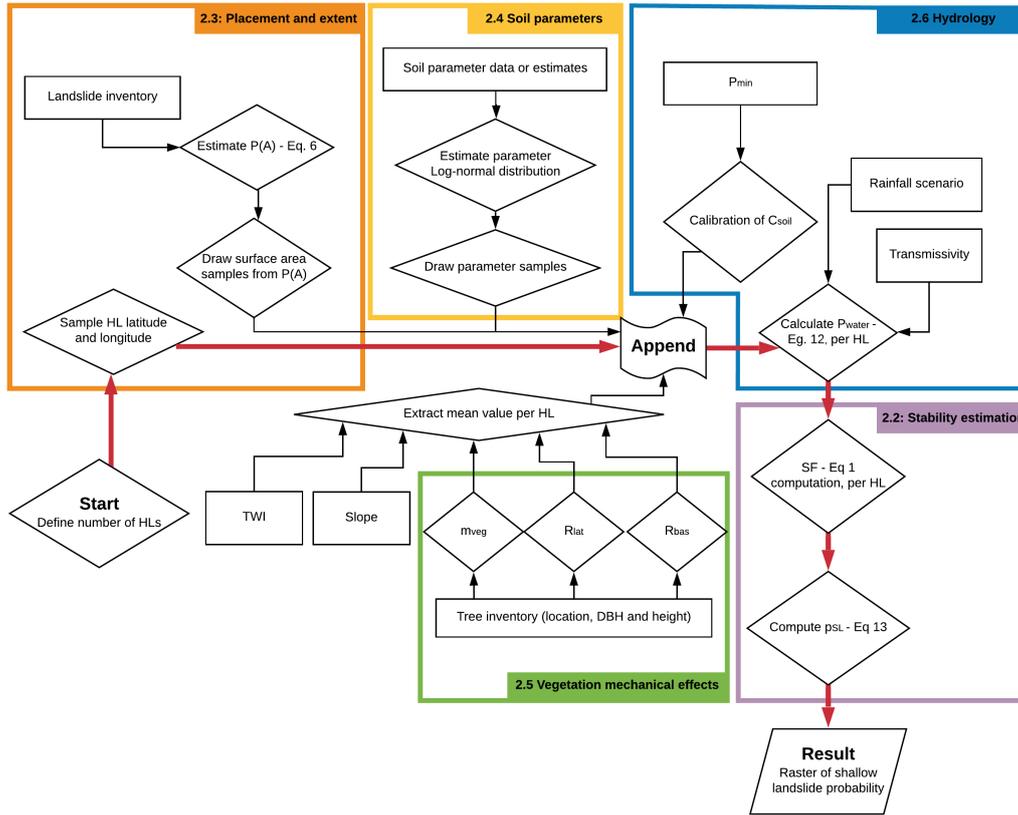


Figure 1. Flowchart of the computational steps in SlideforMAP. Separate sections are outlined in colors. The central workflow is highlighted in red.

2.2 Stability estimation

145 The estimate of the stability of each HL is calculated following the limit equilibrium approach (described in the work of Day (1997)). In this method, a landslide is assumed to be stable if its safety factor (SF) is greater than 1.0. The SF is computed as the ratio of the perpendicular (stabilizing) forces and the parallel (destabilizing) forces:

$$SF := \frac{F_{res}}{F_{par}} \quad (1)$$

150 where F_{par} [N] is the force parallel to the slope, F_{res} [N] is the maximum mobilized resistance force. The assumed forces that act upon a hypothetical landslide are schematically shown in Fig. 2.

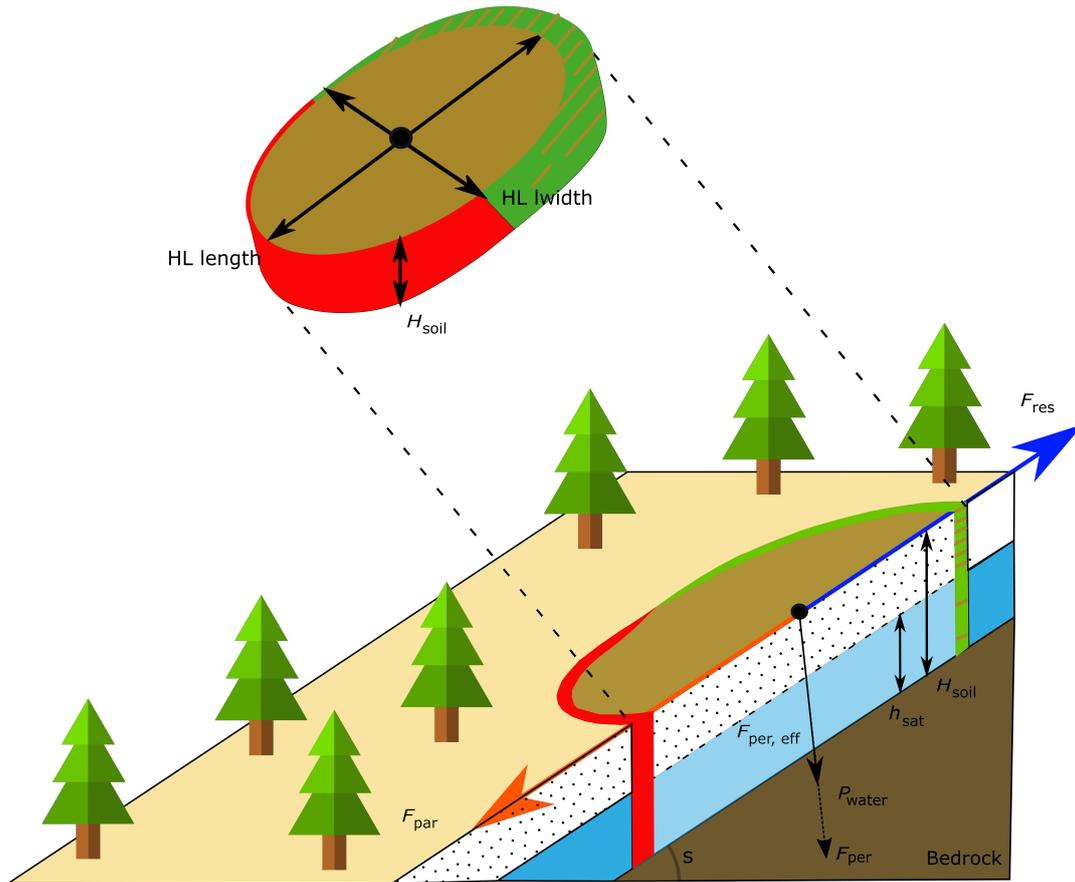


Figure 2. Schematic overview of the forces acting upon a hypothetical landslide, as assumed in SlideforMAP. Blue indicates the stabilizing forces and orange indicates the destabilizing forces. Lateral root reinforcement only acts upon the green part of the hypothetical landslide, where tension takes place. In the red is the compression zone in the shallow landslide. Basal root reinforcement and soil shear strength act on the whole potential failure surface.

As seen in Fig. 2, all landslides are assumed to be elliptical (Rickli and Graf, 2009) with a ratio between length and width, $l_{wr} = 2$. The forces assumed in SlideforMap are typical for the second stage of the activation phase, as described in the introduction, where minor movement has occurred. This coincides with the maximum mobilization of lateral root reinforcement under tension along the tension crack and the absence of passive earth pressure, lateral root compression and lateral soil cohesion.

155 This is different from most landslide models involving root reinforcement (e.g. Montgomery et al., 2000; Schmidt et al., 2001), that assume lateral root reinforcement along the entire landslide perimeter. Quantification of the forces in the safety factor calculation follows the limit equilibrium assumptions. This method is outlined in equations 2 to 5 below:

$$F_{par} = g(m_{soil} + m_w + m_{veg}) \sin(s) \quad (2)$$

$$F_{res} = \frac{c_{ls}}{2} R_{lat} + F_{res,bas} \quad (3)$$

$$160 \quad F_{res,bas} = A_{ls} C_{soil} + A_{ls} R_{bas} + F_{per,eff} \tan(\phi) \quad (4)$$

$$F_{per,eff} = g(m_{soil} + m_w + m_{veg}) \cos(s) - P_{water} \quad (5)$$

In these equations, m_{soil} is the soil mass [kg], m_w is the mass of the groundwater [kg], m_{veg} is the vegetation mass [kg], g is the gravitational acceleration assumed at $9.81 \text{ [m/s}^2\text{]}$, s is the slope [$^\circ$], c_{ls} is the circumference of the landslide [m], $R_{lateral}$ is the lateral root reinforcement [N/m], $F_{res,bas}$ is the basal resisting force, A_{ls} [m^2] is the area of the landslide, C_{soil} [Pa] is the soil cohesion [Pa], R_{basal} is the basal root cohesion [Pa], $F_{per,eff}$ is the effective perpendicular resisting forces [N], ϕ is the angle of internal friction [$^\circ$] and P_{water} is the water pressure [Pa].

2.3 Random landslide placement and extent

The location of the center of mass of the HLs is generated from two uniform distributions covering the latitudinal and longitudinal extent of the study area. HLs on the edge of the study area are taken into account as well, though cut to the extent of the study area in the later spatial processes of SlideforMAP. The total number of HLs is determined by multiplying the landslide density parameter (ρ_{ls}) with the total surface area of the study area. This number is then uniformly sampled with replacements from the latitudinal and longitudinal distribution. The value of ρ_{ls} should be high enough such that each raster cell of the study domain is covered by several HLs. The HL surface area is sampled from an inverse gamma distribution following the work of Malamud et al. (2004), which showed that the probability distribution of shallow landslide surface areas follows an inverse gamma distribution (Johnson and Kotz, 1970). The parameterization of a three parameter inverse gamma distribution is shown in equation 6 below.

$$P_A = \frac{1}{a\Gamma(b)} \left(\frac{a}{A_{ls} - c} \right)^{(b+1)} e^{\left(\frac{-a}{A_{ls} - c} \right)}, \quad (6)$$

where A_{ls} is the landslide surface area, P_A is the probability of A , Γ is the gamma function, a , b and c are the scale, shape and location parameters. These distributional parameters are estimated using the landslide surface area data of the inventory (section 3). The estimation is based on minimizing the Root Mean Square Error (RMSE) between the histogram counts (size of histogram bins = 10) of the surface areas from the inventory and the distribution of equation 6. Users can follow this approach with an inventory or use a custom parametrization. The maximum HL surface area is set for all case studies based on the maximum surface area observed in the landslide inventory. This maximum is set to 3000 m^2 , based on the rounded up maximum value of a well-distributed landslide inventory in Switzerland (section 3.3), but users can vary this parameter.

185 2.4 Soil parameters

Steep-sloped mountainous areas are prone to extreme and unpredictable heterogeneity in soil parameters (Cohen et al., 2009). This makes a heterogeneous deterministic parameterization inaccurate, even if based on observations. To overcome this limitation, a probabilistic approach in the parameterization of soil parameters of the model is applied. Values of soil cohesion, internal friction angle and initial soil thickness of each HL are randomly generated from independent probability distributions. 190 This is an approach similar to the one taken in Griffiths et al. (2009), who use the log-normal distribution for soil cohesion only and Pack et al. (1998) who use a uniform distribution for soil cohesion and friction angle. We choose the log-normal distributions in our parametrization because it has shown to give a good fit (example for soil thickness in the Appendix; Fig. A1), it ensures generating positive values only and its accuracy has been shown in Griffiths et al. (2009). The two parameters of the log-normal distribution can be estimated from the mean and the standard deviation of observed samples; here we define 195 the mean and the standard deviation based on different information such as field soil classification or a geotechnical analysis. The soil cohesion in our computations is assumed to be representative for saturated, drained and unconsolidated conditions. Definitive values for soil thickness are generated following a slightly different approach to account for the shallow soils found on steep slopes. The initial soil thickness (h_{soil}) is transformed as a function of slope inclination as shown in equation 7. Soil thickness is defined here perpendicular to the slope as opposed to soil depth, that is measured straight down.

$$200 \quad H_{\text{soil}} = h_{\text{soil}}(1 - P_{\mathcal{N}}(S \leq s | \mu_1, \sigma_1)), \quad (7)$$

where H_{soil} [m] is the soil thickness and s is the observed slope, extracted for the HL. $P_{\mathcal{N}}(S \leq s | \mu_1, \sigma_1)$ is the cumulative normal distribution of the slope S with $\mu_1 = 1.35 \cdot m_h$ and $\sigma_1 = 0.75 \cdot \sigma_h$. m_h and σ_h are the assumed mean and assumed standard deviation of the slope angle of shallow landslides from an inventory or a best guess. Other relations than used by SlideforMap to correct the soil thickness to the slope (e.g. Prancevic et al., 2020) are possible as well.

205 2.5 Mechanical effects of vegetation

Three properties of vegetation are included in the model. These are vegetation weight, lateral root reinforcement and basal root reinforcement. SlideforMap only incorporates trees and ignores possible effects by shrubs, grasses and other vegetation. This choice is due to the fact that trees are predominant in influencing slope stability (Greenway, 1987). Single tree detection (Korpela et al., 2007; Menk et al., 2017) serves as a basis to estimate these properties. Single tree position and dimensions 210 are derived from a Canopy Height Model (CHM), which is the difference between the Digital Surface Model (DSM) and the Digital Elevation Model (DEM), using a local maxima detection method (LMD) described in the work of Eysn et al. (2015) and Menk et al. (2017). First, the trees are rasterized. The resolution of this raster has to exceed the effective radial dimension of the trees, in order to calculate representative vegetation parameter values at stand scale. The weight of the tree is calculated by using the tree height and the Diameter at Breast Height (DBH), assuming that the trees are cone shaped. The tree mass, 215 m_{veg} , used in equation 2 and 5, is calculated assuming a mean tree density (ρ_{tree}) of 850 kg/m^3 . Root reinforcement is added

in the model using the method proposed by Schwarz et al. (2015), which relates the root reinforcement to the distance to a tree, the size of the tree and the tree species. Subsequently two rasters are computed. 1) A raster with the nearest distance to a tree (D_{trees}). 2) a raster with the average DBH of all trees within a (maximum) distance radius. In SlideforMAP, 7 m is the default setting for this maximum distance. The lateral root reinforcement, R_{lat} [Nm^{-1}], is then computed assuming that it is a function of D_{trees} and DBH (Moos et al., 2016) according to equation 8 below:

$$R_{\text{lat}} = c \cdot \Gamma \left(\frac{D_{\text{trees}}}{\text{DBH} \cdot D_{\text{trees,max}}} \middle| \alpha_1, \beta_1 \right) \cdot \int_0^{H_{\text{soil}}} \Gamma(\alpha_2, \beta_2) dh \quad (8)$$

where c is a fitting parameter, $\Gamma(x|\alpha_1, \beta_1)$ is the gamma density function evaluated at x with shape parameter α_1 and scale parameter β_1 . $D_{\text{trees,max}}$ is the coefficient between the DBH of a tree and the maximum radial distance of the root system from the tree stem (Gehring et al., 2019), This is set to $D_{\text{trees,max}} = 18.5$ based on the work of Schwarz et al. (2010). The parameters of the gamma density function should be selected such that the function has a strictly decreasing behavior to avoid that R_{lat} increases with D_{trees} . These parameters should ideally reflect any knowledge about how root reinforcement decreases with distance for specific tree species. $\Gamma(\alpha_2, \beta_2)$ is the general gamma probability density function for the normalized root distribution through the soil thickness with shape parameter α_2 and scale parameter β_2 . The parameters α_2 and β_2 should be selected such that the function is decreasing with increasing H_{soil} . This method computes the root reinforcement where only one tree can influence a cell. A spatially representative minimum root reinforcement value is calculated in a stand assuming a triangular lattice. Under this assumption, three root systems interact additively. The Gamma probability density function is used to calculate the effect of lateral root reinforcement R_{lat} within the soil thickness of each HL. Basal root reinforcement, R_{bas} [Nm^{-2}], is assumed to be proportional to lateral root reinforcement and dependent on soil thickness according to the relation shown in equation 9:

$$R_{\text{bas}} = k \cdot R_{\text{lat}} \Gamma(H_{\text{soil}}|\alpha_2, \beta_2) \quad (9)$$

where $\Gamma(H_{\text{soil}}|\alpha_2, \beta_2)$ is the root probability density function. A correction factor ($k = 1 \text{ [m}^{-1}\text{]}$) is used to convert the value of lateral root reinforcement in [N/m] to the basal root reinforcement in Pa under the assumption of isotropic conditions.

2.6 Hydrology

The hydrological module in SlideforMAP is based on the TOPOG model (Montgomery and Dietrich, 1994), which includes a specific topographic index as inspired by Kirkby (1975). In this framework we specifically assume macropore flow dominates hillslope hydrology. The identical model is used in the SHALSTAB stability model (Pack et al., 1998). It is assumed that the saturated soil fraction of each cell holds a relation to its specific catchment area, its slope angle, a constant precipitation intensity and the soil transmissivity (equation 10). This is in close correspondence to the parameterization used in the widely used TOPMODEL (Beven and Kirkby, 1979). Limitations of this approach is the assumption of uniform soil transmissivity,

245 steady state flow and lateral flow governing of soil moisture pattern. These limitations and generalizations make the model
insufficient in capturing detailed hydrological pattern, especially in mountainous regions modelled by SlideforMAP. Despite
this, we assume the approach to be suitable for a general pattern of saturated fraction and subsequent pore pressure. In addition
to this shortcoming we ignore the apparent hydrological cohesion (Chae et al., 2017) prominent in unsaturated fine and clayey
soils, but of little prominence in other conditions (Montrasio and Valentino, 2008). The saturated soil fraction, h_{sat}^* [-], of a
250 soil column is defined in equation 10 below:

$$h_{\text{sat}}^* = \frac{P a}{T b \sin(s)}, \quad (10)$$

P [m/s] is the constant precipitation intensity, T [m^2/s] is the transmissivity, a is the contributing catchment area [m^2], s
is the slope inclination [$^\circ$], and b is the contour length [m] that in our model corresponds to the cell size (see Section 3.2 for
details on its computation). We assume dominant macropore flow, which has the ability to quickly reach an equilibrium state
255 with the precipitation input. Based on the literature data discussed in the introduction, we assume that this equilibrium state is
reached with an order of magnitude of one hour. Using this estimated h_{sat}^* , pore water pressure is computed as:

$$P_{\text{water}} = H_{\text{soil}} \cdot \cos^2(s) \cdot h_{\text{sat}}^* \cdot g \cdot \rho_w, \quad (11)$$

where P_{water} [Pa] is the pore water pressure (used in equation 5), H_{soil} [m] is the soil thickness, s is the slope angle, $g = 9.81$
 m/s^2 is the gravitational acceleration, ρ_{water} is the density of water assumed equal to 998 kg/m^3 . The same value for water
260 density is used in the computation of the water mass in the HL.

2.7 Model initialisation

The model has a total of 3 probabilistic parameters and 16 deterministic parameters (Table 1). The deterministic parameters
as well as the distributional parameters for the probabilistic parameters are determined from in-situ data or from literature
(see Section 3). In a first step of the workflow for the application of SlideforMAP, after assigning the deterministic parameter
265 values and sampling a value for each probabilistic parameter, a minimum value of soil cohesion is computed for each HL to
obtain stable conditions (safety factor, $SF \geq 1.0$) under uniform a precipitation intensity of 28.3 mm/day or 1.2 mm/hr . This
threshold of precipitation intensity is chosen according to Leonarduzzi et al. (2017), who statistically analyzed 2000 landslides
in Switzerland over the period 1972–2012 and found this as a triggering threshold. The minimum value of soil cohesion is
obtained by equating F_{par} (equation 2) and F_{res} (equation 3). If the minimum value of soil cohesion is larger than the sampled
270 soil cohesion, the soil cohesion is updated to the minimum value. This procedure can be altered by users when another threshold
or no threshold at all applies.

Table 1. An overview of all variable model parameters of SlideforMAP. The second to last column indicates how the parameters are estimated (from data or literature). The last column indicates whether the default is general or specific for this research in Switzerland (CH)

| Parameter | Description | Default value | Unit | Source | Extent |
|-----------------------|--|---------------|-------------------|------------|--------|
| m_d, σ_d | Soil thickness, mean and standard deviation | 1, 0.25 | m | Estimate | Global |
| m_C, σ_C | Soil cohesion, mean and standard deviation | 2, 0.5 | kPa | Estimate | Global |
| m_ϕ, σ_ϕ | Angle of internal friction, mean and standard deviation | 30, 4 | ° | Estimate | Global |
| ρ_{ls} | Density of the random generated landslides | 0.1 | HL/m ² | Estimate | Global |
| ρ_{soil} | Dry soil density | 1500 | kg/m ³ | Estimate | Global |
| T | Soil transmissivity | 0.1 | m ² /s | Estimate | Global |
| P | The precipitation event that is tested | 10 | mm/hr | Estimate | Global |
| P_{min} | Precipitation intensity threshold for instability | 1.2 | mm/hr | Literature | CH |
| D_t | Raster resolution for the tree distance computation | 15 | m | Estimate | CH |
| r_{xy} | Raster resolution of the SlideforMap run | 2 | m | Estimate | Global |
| l_{wr} | Ratio between length and width of the elliptical landslides | 2 | - | Estimate | Global |
| c | Fitting parameter for the lateral root reinforcement | 25068.54 | - | Literature | CH |
| α_1, β_1 | Gamma function shape and scale of the lateral root reinforcement | 0.862, 3.225 | - | Literature | CH |
| $D_{trees,max}$ | maximum distance for influence of tree roots | 18.5 | m | Literature | CH |
| α_2, β_2 | Gamma function shape and scale of the basal root reinforcement | 1.284, 3.688 | - | Literature | CH |
| ρ_{tree} | Density of a tree | 850 | kg/m ³ | Estimate | CH |
| ρ_{water} | Density of water | 998 | kg/m ³ | Estimate | Global |

2.8 Landslide probability computation

After model initialisation, SF (equation 1) is computed for each of the generated HLs. Based on the SF for all generated HLs, landslide probability per raster cell (with the resolution of the original DEM), p_{SL} , is computed as:

$$275 \quad p_{SL} = \frac{n_{us}}{n_{HL}} \quad (12)$$

where n_{us} is the number of unstable HLs, i.e. of HLs with SF<1.0 and n_{HL} is the total number of generated HLs (the HLs are overlapping). Finally, this results in a raster of shallow landslide probability on a resolution of the input DEM.

3 Data

3.1 Study areas

280 Three study areas were chosen to test SlideforMAP based on the availability of elevation data and detailed records of historical shallow landslide events (Fig. 3), each varying in size and location to test the robustness and the general applicability of the model.

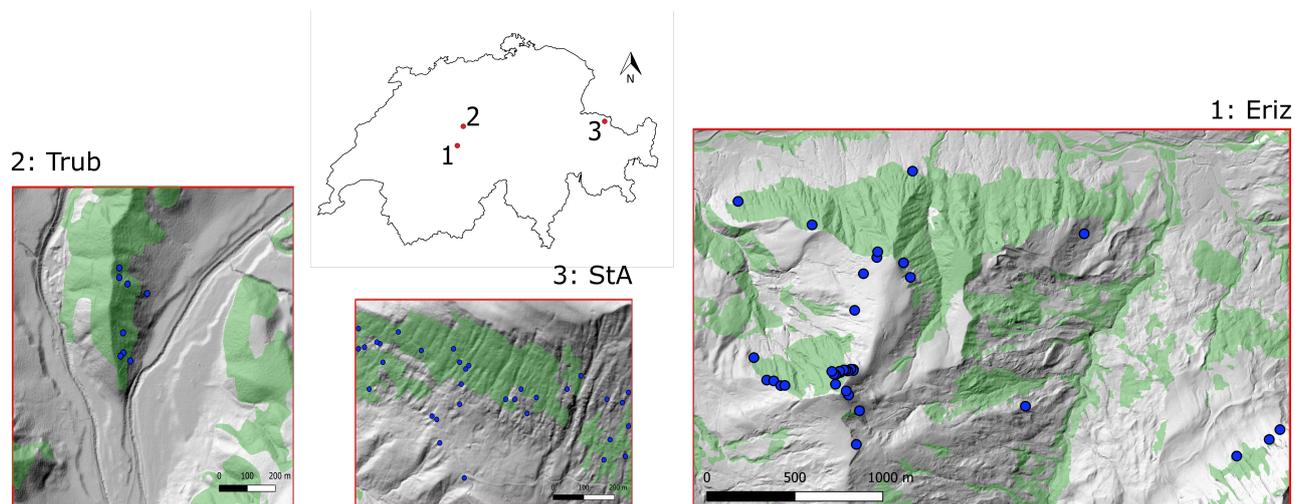


Figure 3. Locations of the study areas in Switzerland with observed Shallow landslide occurrence over the period 1997 - 2012 (blue dots); the case study names are given according to nearby villages: Trub, St. Antönien and Eriz. Forest covered area is presented in green (source: Swisstopo, 2020).

The geological formations in the Eriz study area vary from Oligocene freshwater Molasse in the lower northern part, morainic material in the central part and Cretaceous Limestone in the highest parts. Forests are dominated by spruce (*Picea abies*),
285 except for the lower regions where broad-leaved trees are dominant. In the Trub study area, the dominant geological formation is Miocene Marine Molasse and forests are dominated by spruce. In the St. Antönien (from here forward abbreviated to 'StA') study area, the dominant geological formation is Flysch (Prättigauer Flysch), partially covered by till (Moos et al., 2016). The forest in this study area is also dominated by spruce (Moos et al., 2016). Further characteristics of the study areas are given in Table 2.

Table 2. Study area characteristics. Meteorological data is from the HADES yearly average precipitation for the time period 1981 - 2010 (Frei et al., 2020). Shallow landslide number and density from the inventory in section 3.3.

| Name | Centre coordinate lat;lon (WGS84) | Surface area km ² | Mean prec. mm/year | Elevation m.a.s.l. | Number of slides | Slide density Slides/km ² | Mean slope ° |
|------|--------------------------------------|---------------------------------|-----------------------|-----------------------|------------------|---|-----------------|
| Eriz | 7.81; 46.78 | 7.54 | 1700 | 960 - 1750 | 37 | 4.9 | 20.4 |
| Trub | 7.90; 46.96 | 1.00 | 1620 | 820 - 1020 | 8 | 8.0 | 18.3 |
| StA | 9.80; 46.98 | 0.56 | 1310 | 1540 - 2010 | 33 | 58.9 | 27.5 |

290 3.2 Input data

To accurately measure p_{SL} for each study area, the following data are required.

- Digital Surface Model (DSM) and Digital Elevation Model (DEM)
- Average and standard deviation values for soil cohesion, thickness and friction angle
- A representative landslide inventory containing at least:

- 295 • Average landslide soil thickness
- Landslide surface area

In addition to the DEM, the DSM is applied in the vegetation section of SlideforMAP. The DEM and the DSM are both acquired from the SwissAlti3D database (Swisstopo, 2018), which makes use of aerial laserscanning (ALS). Both the DSM and DEM are available at a resolution of 0.5 m. As an alternative to the use of a landslide inventory and the DSM for single
300 tree identification, users can also use synthesized values for the parameters derived from this data. After pit filling, the DEM is used to compute a slope map following the method of Zevenbergen and Thorne (1987). The topographic wetness index θ for equation 10 is computed on a raster cell basis based on the 2 m DEM using equation 13.

$$\theta = \frac{A_{cat}}{\sin(s)}, \quad (13)$$

where A_{cat} is the specific upslope catchment area and s is the slope angle. To avoid numerical problems for elongated catch-
305 ments, θ is computed using a 2 km buffer around the catchment. The large buffer size is chosen arbitrarily, but can be reduced by other users. The standard D8 method is applied for the computation of the upslope catchment area from the DEM (O’Callaghan, J and Mark, D, 1984). For single tree detection, the FINT algorithm (Menk et al., 2017) is used. Since the results of such detection methods are strongly influenced by the resolution and smoothness of the input data (Eysn et al., 2015), we applied the local maxima detection (LMD) method to the a canopy height model (CHM). This canopy height model is computed by
310 subtracting the DEM from the DSM and is resampled to a resolution of 1, 1.5 and 2 m. In addition, three different Gaussian

filters were applied on the 1 m resolution CHM. These three filters have a radius of 3, 5 and 7 cells and a standard deviation of 2 m. To identify the input data that leads to LMD results with the highest accuracy, we evaluated the identified trees in three randomly selected forest inventory plots with an area of 20 m x 20 m for each study site. In these plots, we visually identified all recognisable tree crowns, on the basis of aerial photos (Swisstopo, 2017) and the CHM. The identified trees were then compared to the LMD result, using the difference in the number of detected trees. The input data leading to the most accurate results in all three study sites was the 1 m resolution CHM with a Gaussian filter of a 3 cells radius and with the fixed standard deviation of 2 m. This combination has been applied to the entire area of the three study sites. To estimate the diameter at breast height (DBH) from the tree heights of all detected trees, the following empirical equation (Dorren, 2017) was used:

$$DBH_{\text{tree}} = H_{\text{tree}}^{1.25} \quad (14)$$

where DBH_{tree} [cm] is the diameter at breast height of a given tree and H_{tree} [m] its height. Details resulting from the LMD method for the three study areas are shown in Table 3.

Table 3. Vegetation parameters in the study areas. The forest cover is derived from Swisstopo (2020)

| Study area | Trees identified | Forest cover % | Mean stem density Stems/ha | Mean DBH cm | Std. deviation DBH cm |
|------------|------------------|-------------------|-------------------------------|----------------|--------------------------|
| Eriz | 38923 | 32 | 165 | 51 | 27 |
| Trub | 7267 | 26 | 270 | 55 | 30 |
| StA | 1796 | 27 | 120 | 31 | 18 |

The lateral and the basal root reinforcement (equations 8 and 9) are parameterized using the values from Gehring et al. (2019) ($\alpha_1 = 0.862$, $\beta_1 = 3.225$, $c = 25068.54$, $\alpha_2 = 1.284$, $\beta_2 = 3.688$). In their work, the calibration was performed on beech (*Fagus Sylvatica*) stands over varying elevations. Our study areas, however, are predominantly vegetated by spruce trees. Therefore a discrepancy in the estimated root reinforcement will likely arise. Unfortunately, however, this is the only published set of calibrated values.

3.3 Landslide inventory

A landslide inventory is required to quantify a distribution for slope, surface area and soil thickness for the HLs. This inventory does not necessarily have to be well distributed in the study area, or even be present in the area. However, it should be representative of the conditions in the area of interest as much as possible. A dataset of 668 shallow landslides that occurred between 1997 and 2012 in Switzerland has been created by the Swiss Federal Office for the Environment (Rickli et al., 2019). Statistical information on the landslides can be seen in Fig. 4. We assume the properties in this inventory to be representative for shallow landslides in Switzerland. All landslides are triggered by rainfall and the majority of the landslides are shallower

than 1.5 m (Fig. 4). The landslides in the St. Antönien and Trub area took place in 2005 during or shortly after heavy rainfall in August. The landslides in the Eriz area from 2012 are related to heavy rainfall in July. Exact amounts and intensities are unknown. The data is formatted with centre points and surface area of the shallow landslide initiation area. In our analysis we assume they have a circular shape.

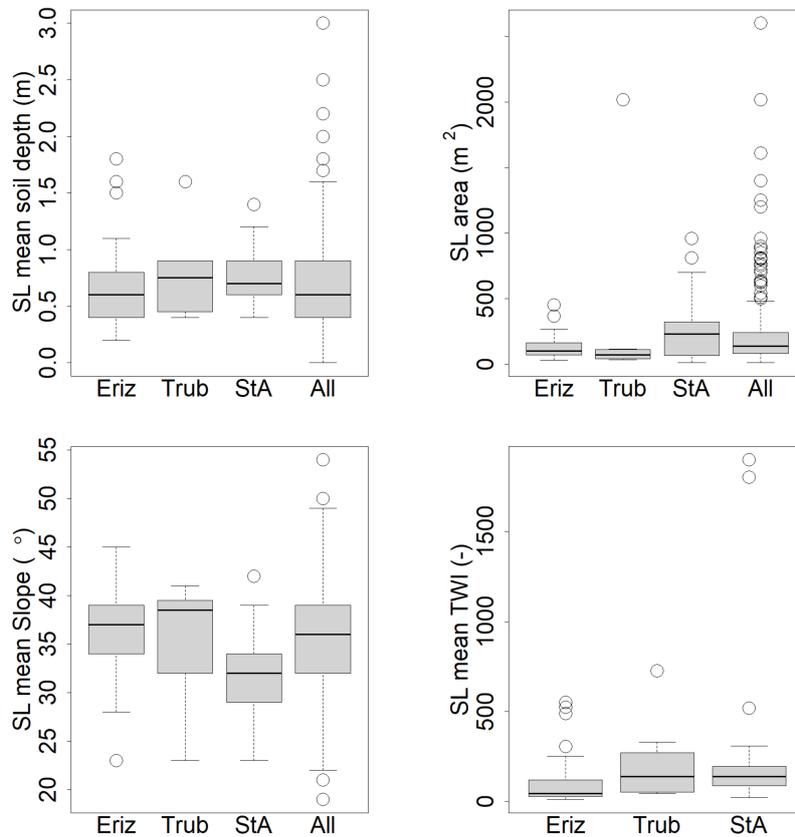


Figure 4. Overview of landslide properties for the studied regions. Top row: mean soil thickness (left) and the surface area (right) of the shallow landslide (SL) for the test areas and the total inventory; bottom row: mean slope (left) and mean TWI (right). The box plots show the 25, 50 and 75 percentiles, the whiskers extend to 1.5 times the length between the 25 and 75 percentile. Outliers are marked as circles. The TWI was extracted from the TWI raster cells that lie inside the landslide inventory polygons.

The inventory is used to estimate the parameters for the surface area distribution used in SlideforMAP (equation 6), via minimization of the RMSE between observed frequencies and theoretical frequencies. The estimated values of the slope, scale and location parameters are: $a = 1.40$, $b = 1.5^{-4} \text{ m}^2$, $c = 4.28^{-8} \text{ m}^2$.

3.4 Model calibration and sensitivity analysis

The model has a total of 22 parameters that are derived from observed data, from literature or that are set to default values; their values, given in Table 1, are not further varied in the model behavior analysis due to their assumed low variance. The remaining parameters can potentially influence the landslide probability, mostly given their variation as observed in nature. These parameters are: P_{\min} , D_t , l_{wr} , c , α_1 , β_1 , $D_{\text{trees,max}}$, α_2 , β_2 , ρ_{tree} , ρ_{water} . The remaining 12 parameters are then calibrated by Monte Carlo simulation, drawing a high number of parameter samples for all calibration parameters and evaluating the corresponding model performance based on the Area Under the Curve (AUC) method (Metz, 1978; Fawcett, 2006). We hereafter first present the used performance evaluation method, followed by the parameter sampling method used for the calibration as well as for the sensitivity analysis. In addition, we present four vegetation parameter scenarios that are developed to test the potential influence of vegetation. Due to the limited size of the landslide inventory we do not include an independent validation of SlideforMap.

3.4.1 Model performance evaluation

The basis of the application of the AUC method is a spatial representation of the landslide inventory in a boolean raster (0 = no past landslide present, 1 = past landslide present). For each randomly generated parameter set, the simulated p_{SL} (section 2.8) is also converted to a boolean raster, by selecting a threshold to assign 0 or 1. Overlaying the inventory raster on the modelled raster, results in a confusion matrix with four possible combinations, as shown in Table 4.

Table 4. The confusion matrix, as used in the calibration.

| | | Model | |
|-----------|-------|---------------------|---------------------|
| | | True | False |
| Inventory | True | True positive (TP) | False negative (FN) |
| | False | False positive (FP) | True negative (TN) |

For every threshold value, the sensitivity, $TP/(TP+FN)$, and the specificity, $TN/(TN+FP)$ are computed. Plotting the sensitivity and specificity against each other for all thresholds results in a Receiver Operator Curve (ROC). The area under the ROC curve is the AUC and defines the accuracy of the model on a scale of 0.5 - 1.0, where 0.5 is being no better than a random guess and 1.0 is a perfect prediction.

3.4.2 Parameter sampling and qualitative sensitivity

The parameter samples for the Monte Carlo-based model calibration and the subsequent sensitivity analysis are generated using the Latin Hypercube Sampling (LHS) technique (McKay et al., 1979). This makes use of semi-random samples of variables over pre-defined ranges. The outcome of a Monte Carlo-based calibration is highly influenced by the ranges chosen for the parameters. For this reason, parameter ranges were chosen as realistically as possible. To estimate the parameter ranges for soil

properties, soil types in USCS classes are taken from the shallow landslide inventory (a total of 377 had their soil type listed). Soil types present more than ten times are taken into account and aggregated into a hybrid table of soil cohesion and angle of internal friction values per soil type based on the values given in the work of Dysli and Rybisar (1992) and VSS-Kommission (1998) (see Appendix, Table A1).

370 In order to obtain a realistic range for the soil cohesion, first the mean soil cohesion (weighted on USCS soil type occurrence) is computed and then the weighted standard deviation is subtracted and added twice to the weighted mean. This is to account for 95% of the variation in the observed soil cohesion (assuming a normal distribution). The same procedure is performed for the angle of internal friction. The range of transmissivity values is obtained by taking the saturated hydraulic conductivity from the work of Freeze and Cherry (1979) for the respective soil classes and by multiplying these saturated hydraulic conductivities
375 with the minimum and maximum soil thickness of the soil class. From the resulting list of possible transmissivity values per soil class, the minimum and maximum are taken for the LHS range.

The precipitation intensity range is defined by the lowest 1 hour intensity corresponding to a return period of 10 years and the highest 1 hour intensity corresponding to a return period of 100 years over the study areas. This was chosen arbitrarily in line with forest management timescales. The one hour time period for the rainfall intensity is in line with the SlideforMap
380 assumption of macropore-flow dominance. These are computed using data from the work of Jensen et al. (1997) and the methodology as described in the work of HADES (2020). The R-script with this methodology and a description is included in the supplementary material. The maximum value for vegetation weight is taken from a biomass study in Switzerland by Price et al. (2017). For the other parameters, realistic ranges have been assumed. In Table 5 an overview is given of the tested parameters and the ranges used to generate the parameter samples. Since the precipitation intensity and transmissivity together
385 determine the saturation degree of the soil (equation 10), we grouped them as an additional parameter, the P/T ratio.

Table 5. Parameters used in the SlideforMAP qualitative sensitivity analysis and corresponding ranges for parameter sampling via LHS. R_{lat} and W_{veg} are given as parameters directly in contrast to the components as given in Table 1. This is to create scenarios that are comparable with and without single-tree detection.

| Parameter | Unit | Description | LHS Range |
|---------------|--------------|--|-----------------------|
| ρ_{ls} | m^{-2} | Density of the randomly generated landslides | 0.02 - 0.10 |
| ρ_{soil} | kg/m^3 | Dry soil density | 1.00 - 1.50 |
| m_d | m | Mean soil thickness | 0.20 - 1.80 |
| σ_d | m | Standard deviation of the soil thickness, as a fraction of m_d | 0.00 - 0.50 |
| m_C | kPa | Mean saturated soil cohesion | 0.00 - 12.5 |
| σ_C | kPa | Standard deviation of the soil cohesion, as a fraction of m_C | 0.00 - 0.50 |
| m_ϕ | ° | Mean angle of internal friction | 24.00 - 41.50 |
| σ_ϕ | ° | Standard deviation of the angle of internal friction | 0.00 - 5.00 |
| T | m^2/s | Soil transmissivity | 10^{-8} - 10^{-3} |
| P | mm/h | The precipitation event that is tested | 32.0 - 50.0 |
| P/T | m^{-1} | Ratio between precipitation and transmissivity | 8.9^{-3} - 1390 |
| R_{lat} | kPa | Assumed lateral root cohesion | 0.00 - 15.0 |
| W_{veg} | tonne/ m^2 | The weight of the vegetation | 0.00 - 0.10 |

For the model calibration and qualitative sensitivity analysis, 1000 LHS parameter sets were generated per study area by drawing samples from the ranges in Table 5. The number 1000 was chosen arbitrarily for computational constraints. The vegetation is set to a global uniform vegetation, which results in constant root reinforcement and vegetation weight in space. This is necessary because the same runs are used for model calibration and for model sensitivity analysis, where we need such uniform vegetation to ensure that the sensitivity of the (hypothetical) vegetation has an effect on all raster cells of the whole study area (and not only on the actually vegetated cells). The parameter set with the highest AUC value is retained for model calibration. In addition, all 1000 parameter sets are used for a qualitative sensitivity analysis. The response variables are the AUC as a measure for accuracy and the ratio of unstable landslides as a measure for instability. The AUC is chosen as the main response variable since it is calibrated to the independent landslide inventory. The influence of each individual parameter on the AUC is observed by filtering the runs on best performance.

3.4.3 Vegetation parameter scenario analysis

SlideforMAP has potential in testing the effect of different vegetation scenarios on the landslide probability. For this research, besides the reference scenario for model calibration and sensitivity analysis (global uniform vegetation), three additional scenarios are tested: i) without vegetation, ii) with uniform vegetation in forested areas and iii) with a fully diverse vegetation based on single-tree detection. The single-tree version uses the input data as mentioned in section 3.2. The forested areas are

defined as areas where the single tree detection method leads to a lateral root reinforcement (Fig. 10) which is not equal to zero.

4 Results

4.1 Sensitivity analysis

405 We use the 1000 model simulations corresponding to the 1000 generated parameter sets per study area for a sensitivity analysis of the model. The objective of this analysis is to quantify how the distribution of AUC values and of the landslide probability vary as a function of the parameters. A sensitivity analysis involving small changes to the parameters in the vicinity of their optimal values (optimal with respect to reference data), sheds light on potential interplay between parameters. The effect of subsampling (i.e. retaining only part of all parameter sets) is analyzed based on the empirical parameter distributions (i.e. 410 histograms) of each parameter, which represents their empirical marginal distribution (i.e. the distribution of one parameter given all other parameter distributions).

For some parameters, the histogram shape (i.e. their marginal distribution) does not significantly deviate from a uniform distribution, even if we retain only the best 10% (in terms of AUC) of all parameter sets (Fig. 5). This apparent lack of sensitivity does not necessarily mean that the model is not sensitive to this parameter; in fact, the sensitivity could be hidden by 415 strong parameter correlation, (see Bárdossy, 2007, for a discussion of how uniform marginal distributions can result from strong parameter correlation). Our addition of the P/T ratio gives a hint at such behaviour. From Fig. 5 it appears that the sensitivity to AUC of the P/T ratio is slightly stronger than either the precipitation or transmissivity independently. Some parameters, in exchange, show very strong sensitivity of their marginal distributions if only the best (in terms of AUC) parameter sets are retained. For the Trub case study (Fig. 5), we see that the mean thickness m_d , the mean cohesion m_c , the P/T ratio and 420 the transmissivity show a well defined maximum around the parameter values retained for calibration (the best performing ones). This suggests a good sensitivity of the model to these parameters in terms of model performance. Two of these three parameters also show a clear sensitivity if we retain subsamples that lead to successively higher unstable landslide ratio (Fig. 6): high unstable ratios are obtained for high m_d values or for low m_c . Also for R_{lat} , highest ratios are clearly obtained for low lateral root reinforcement values (for all three case studies, Fig. 6, Supplementary Material S-2, S-4). For transmissivity, while 425 it shows a clear effect on model performance, there is no clearly visible relation between its marginal distribution and the ratio of unstable landslides.

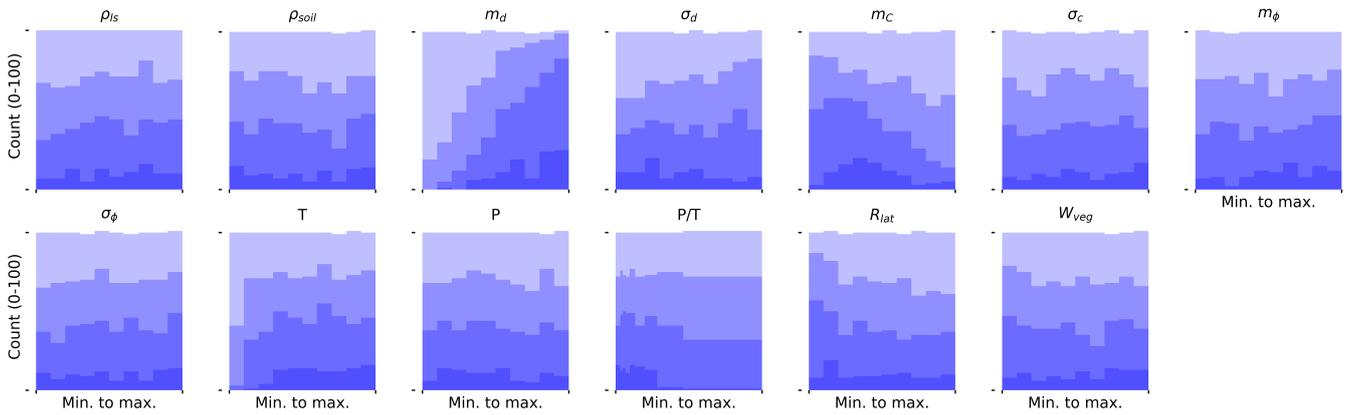


Figure 5. Histograms of different subsamples of the LHS parameter sets for the Trub study area. The shading (from light to dark) corresponds to subsamples retaining only the $x\%$ highest parameter sets in terms of AUC; the shown fractions are: 1, 0.7, 0.4, 0.1.

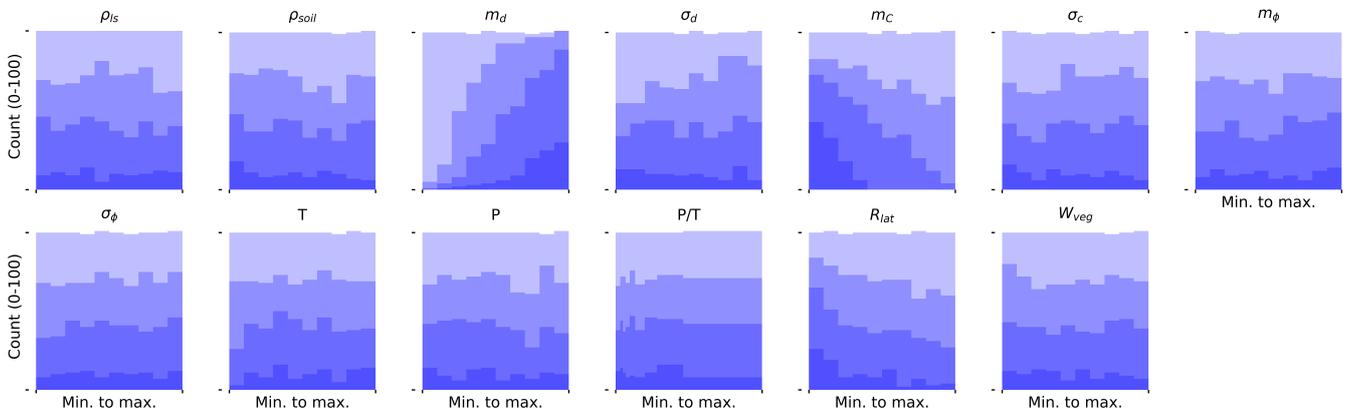


Figure 6. Histograms of different subsamples of the LHS parameter sets for the Trub study area. The shading (from light to dark) corresponds to subsamples retaining only the $x\%$ highest parameter sets in terms of Unstable ratio; the shown fractions are: 1, 0.7, 0.4, 0.1.

4.2 Model calibration

Based on the generated 1000 parameter sets, we identified the parameter set that resulted in the highest AUC value and assumed this to be an optimal calibration of the model. These calibrated parameter sets for each study area and their AUC values are shown in Table 6 together with the ratio of generated HLs that are unstable.

Table 6. Outcome of the Monte Carlo-based calibration: the parameter sets per study area resulting in the highest AUC value. The last row shows the ratio of unstable HL resulting from these parameter sets.

| Parameter | Eriz | Trub | StA | Parameter | Eriz | Trub | StA |
|---------------|-------|-------|-------|-----------------|----------|----------|----------|
| ρ_{ls} | 0.090 | 0.058 | 0.082 | T | 0.000349 | 0.000663 | 0.000951 |
| ρ_{soil} | 1.28 | 1.33 | 1.46 | P | 46.0 | 34.3 | 37.8 |
| m_d | 1.58 | 1.50 | 1.04 | P/T | 0.004 | 0.014 | 0.011 |
| σ_d | 0.33 | 0.03 | 0.28 | R_{lat} | 13.4 | 1.5 | 0.3 |
| m_C | 6.21 | 3.36 | 2.89 | W_{veg} | 0.05 | 0.04 | 0.08 |
| σ_C | 0.18 | 0.04 | 0.50 | AUC | 0.899 | 0.939 | 0.721 |
| m_ϕ | 24.1 | 40.3 | 41.1 | Unstable Ratio. | 0.085 | 0.379 | 0.367 |
| σ_ϕ | 3.52 | 1.67 | 4.63 | | | | |

Parameter consistency between the study areas is visible in ρ_{soil} , m_d , P/T , m_C and P/T . Other parameters show stronger variation between case studies. The shallow landslide probability computed with SlideforMAP for the three areas with their calibrated parameter set is given in Fig. 7. The corresponding ROC curves to Fig. 7 are given in Fig. 8.

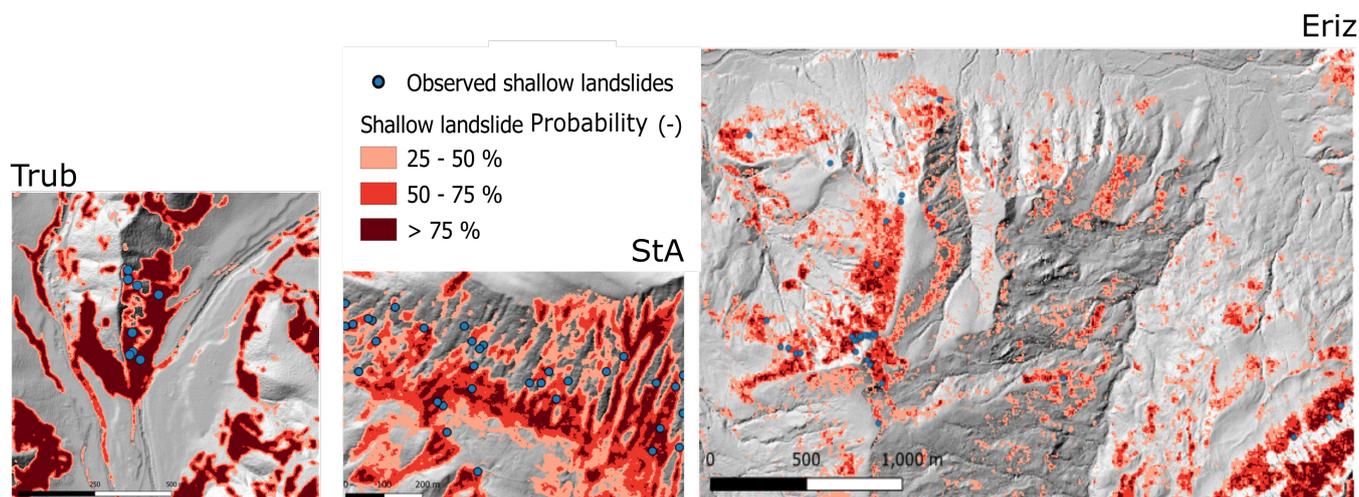


Figure 7. Overview of the landslide probability of the study areas simulated with the calibrated parameter sets of Table 6. Added as blue points are the observed landslides from the inventory.

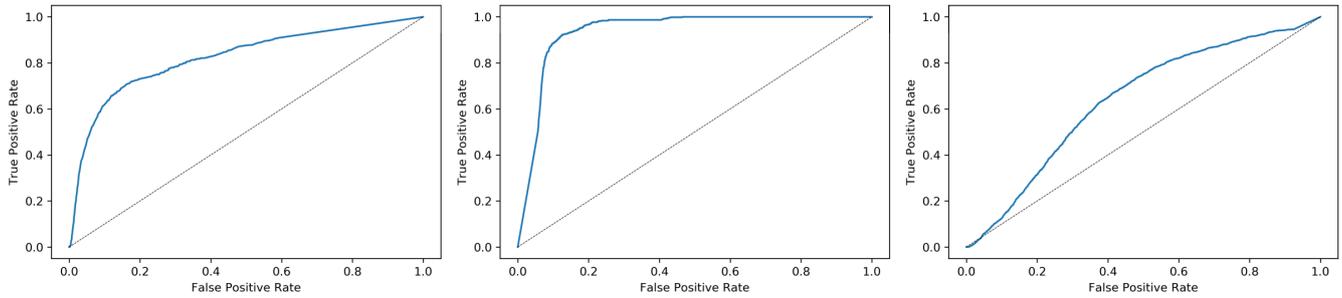


Figure 8. ROC curves corresponding to Fig. 7. Corresponding study areas from left to right are: Eriz, Trub and StA.

In general The model represents well the spatial distribution of the shallow landslides from the inventory. A cumulative plot of
 435 the shallow landslide probability for the study areas is given in Fig. 9

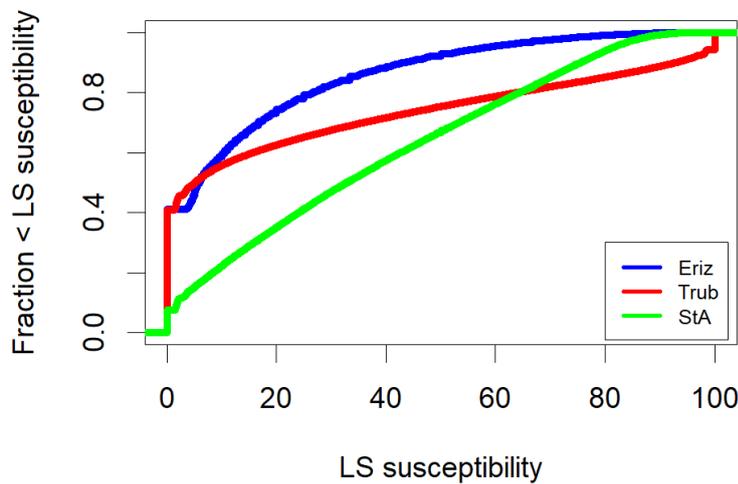


Figure 9. Cumulative plots for shallow landslide probability in the study areas, derived from the results in Fig. 7.

4.3 Mechanical effects of vegetation

To test the impact of vegetation on the model behavior, we compare the different vegetation scenarios. The spatial distribution of lateral root reinforcement, resulting from single tree detection and SlideforMAP, is given in Fig. 10.

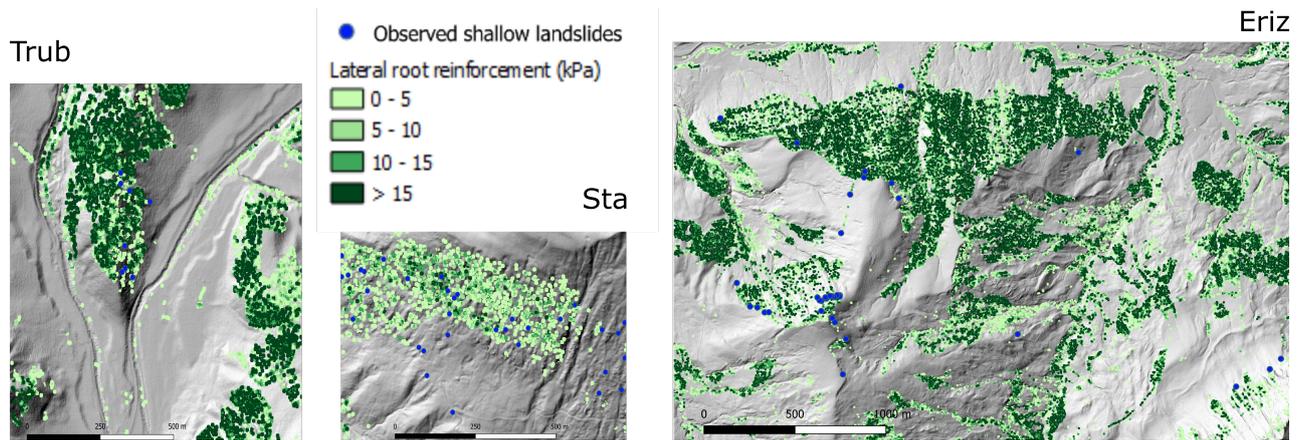


Figure 10. The spatial distribution of root reinforcement in the study areas as used in SlideforMAP under an assumed soil thickness of 2 m.

The selected vegetation scenarios (no vegetation, global uniform vegetation, forest area uniform vegetation, single tree detection) affect the computation of the vegetation weight, the lateral root reinforcement and the basal root reinforcement. The latter is due to its dependence on lateral root reinforcement (equation 9). Accordingly, the vegetation scenario has a direct impact on SF (equation 1, 3, 4) and on p_{SL} (equation 12). For the analysis, we use the optimal parameter set from Table 6, obtained for a global uniform vegetation cover. The model runs are repeated 10 times to produce an average result and to show the variation from the probabilistic approach. Due to sampling from distributions every realization produces a (slightly) different result. The resulting influence of the selected vegetation scenarios on AUC and ratio of unstable landslides is given in Table 7.

The results show that compared to the reference scenario used for calibration, the AUC remains almost unchanged or slightly increases for the vegetation based on single tree detection. In exchange, the ratio of unstable landslides significantly decreases for all case studies with single tree detection and significantly increases without vegetation. This result clearly shows that the model shows a good sensitivity to the vegetation scenarios and that it correctly predicts lower ratios of unstable ratios for single tree detection, which corresponds to the assumed stabilizing effect of the realistic vegetation cover compared to a uniform vegetation cover. This underlines the value of the model for future scenario analyses. The model performance, in exchange, is not sensitive enough to decide during model calibration, which vegetation scenario is more likely for a given case study. While not being critical for scenario analysis, this problem could be related to the amount of reference data and could be overcome by redesigning a new performance criterion that accounts explicitly for a potential lack of reference data.

Table 7. AUC and unstable ratio under different vegetation scenarios with the optimal parameter sets of Table 6 and averaged over 10 runs. The "Overall" is composed of the mean value of all three study areas. In the global uniform vegetation scenario, the reference scenario is used during parameter optimisation.

| | | AUC | | | | Unstable ratio | | | |
|-----------|--------------------------------|---------|-------|-------|-------|----------------|-------|-------|-------|
| | | Overall | Eriz | Trub | StA | Overall | Eriz | Trub | StA |
| mean | Global uniform vegetation | 0.799 | 0.868 | 0.861 | 0.669 | 0.279 | 0.087 | 0.382 | 0.368 |
| | Forest area uniform vegetation | 0.795 | 0.868 | 0.846 | 0.670 | 0.327 | 0.161 | 0.412 | 0.408 |
| | Single tree detection | 0.807 | 0.865 | 0.917 | 0.640 | 0.234 | 0.137 | 0.239 | 0.326 |
| | No vegetation | 0.784 | 0.840 | 0.846 | 0.665 | 0.363 | 0.242 | 0.428 | 0.420 |
| Std. dev. | Global uniform vegetation | 0.019 | 0.011 | 0.031 | 0.016 | 0.001 | 0.000 | 0.001 | 0.002 |
| | Forest area uniform vegetation | 0.022 | 0.015 | 0.036 | 0.015 | 0.001 | 0.001 | 0.001 | 0.002 |
| | Single tree detection | 0.016 | 0.021 | 0.008 | 0.019 | 0.001 | 0.000 | 0.001 | 0.002 |
| | No vegetation | 0.019 | 0.015 | 0.026 | 0.017 | 0.002 | 0.000 | 0.002 | 0.003 |

455 5 Discussion

It is important to point out that the inventory to which the model performance is calibrated plays a key role in all the results discussed below. The inventory was obtained after triggering rainfall events, for which the precipitation intensity, duration and the spatial distribution are not known exactly. Despite this shortcoming, the inventory represents a unique source of information and the spatial localisation of the landslides can be assumed to be of high quality. Below, we discuss the model behavior as a
 460 function of the different model parameter groups and the performance of the model and give directions for future research.

5.1 Soil parameters

The best performing parameter sets show coherently high values for the soil thickness for all study areas (by comparing the values of Table 6 and Table 5). The qualitative sensitivity analysis (Fig. 6) also shows that the highest unstable ratios are obtained for highest soil thicknesses; this indicates that a certain minimum soil thickness is required for landslide triggering,
 465 which is in line with previous findings by D'Odorico and Fagherazzi (2003) and by Iida (1999). In these studies, soil thickness is noted as the conditional factor for landslide triggering along with precipitation intensity and duration. The best performing parameter sets display a certain variation for the mean cohesion across the three case studies (Table 6), with a clear tendency to low values in all study areas (Fig. 6, Supplementary Material S-4, S-2), which suggests that the observed landslides can only
 470 be reproduced with low soil cohesion for all case studies. The mean angle of internal friction shows a high variation, from a very low value for StA to close to the maximum tested value for Trub (which suggests that even higher values could be tested in the future). This might be attributed to the difference in geology and soils between the study areas.

5.2 Hydrological parameters

Soil transmissivity showed considerable sensitivity to the AUC (Fig. 5) and the values are consistently high for all three case studies for the test LHS range (Fig. 6), which is a hint that a correct estimation of soil transmissivity is paramount for a reliable estimate of shallow landslide occurrence. Regarding precipitation intensity, we see a certain variability between the best values for the three case studies and no clear univariate sensitivity of the model performance or the model output (ratio of unstable landslides). It is notable, however, that calibrated conditions in all study areas resulted in a majority of HLs being in fully saturated soil conditions. The application of the TOPOG/TOPMODEL approach has the major shortcoming that it assumes a groundwater gradient parallel to the surface gradient. It has been shown in the past that this assumption decreases the accuracy of water content simulations as compared to distributed dynamic hydrological models (Grabs et al., 2009). However, as discussed earlier, it has also been shown in the past that macropore flow is omnipresent in landslide triggering and SlideforMAP has been parameterized assuming an important role of macropore flow. In macropore-driven systems, steady state groundwater flow is easily reached (section 1), which implies that the TOPOG assumption holds well in this case. In the landslide inventory underlying the study here, the dominant soil types are GM (silty gravel), GC (clayey gravel) and CL (low plasticity clayey silt); accordingly, we can assume that the TOPOG assumptions are valid for a wide range of the domain (for GM and GC soil type), even if it holds probably less well for the CL soil types.

5.3 Vegetation

A key aspect of the model is the use of single tree detection to parameterize vegetation, a method that was previously found by Menk et al. (2017) to be reliable to detect single trees and derive their DBH's from the detected tree heights for sloped forests. As mentioned in Section 3.1, we found for the selected case studies that single tree detection provides the best results in terms of correct number of trees counted if applied on a 1 m resolution DSM with a 3 cell kernel Gaussian filter. This is in line with the results of Menk et al. (2017) who found in a similar scenario-testing approach that a 1 m resolution DSM with no Gaussian correction provided the most accurate results, noting, however, that the difference in performance between these two methods (with and without Gaussian filter) is small. In SlideforMAP, we are not only considering basal but also lateral root reinforcement. This is unique for shallow landslide probability models. As shown in the sensitivity analysis (Fig. 6), R_{lat} has a clear effect on the ratio of unstable landslides, with low values leading to high ratios. However, in the SlideforMAP workflow and calibration, a fixed relationship between the lateral and the basal root reinforcement is assumed, accordingly, the model sensitivity cannot be attributed to R_{lat} or R_{bas} . Mobilization of the lateral root reinforcement in the SlideforMAP workflow is independent of time and not countered by passive earth pressure. A shortcoming in this parameterization of the effect of vegetation is the assumption of uniform forest structure and a uniform tree species (beech) within a landslide area. The field recordings in the St. Antönien area of Moos et al. (2016) show that the forest consists mainly of Norway spruce. For the Trub and Eriz area, visual interpretation of aerial photos allowed us to identify mixed forests with Norway spruce and beech. The latter are known for having a high root reinforcement and therefore the beech assumption will overestimate both the lateral and the basal root reinforcement (Gehring et al., 2019). Subsequently, vegetation weight shows no clear relation to both the AUC

505 and the unstable Ratio (Fig. 5, Fig. 6). However, this does not mean that vegetation weight does not influence the response variables. The relationship could depend on other parameters and therefore obscured (Bárdossy, 2007). In contrast to the soil and hydrological parameters, vegetation configures both the magnitude and the spatial pattern of the probability. Vegetation can be modified by land management practices with relative ease (Amishev et al., 2014) and is therefore of ultimate importance on shallow landslide mitigation.

510 **5.4 Implementation of the mechanical effects of vegetation**

In Table 7 it can be seen that the vegetation scenario has a considerable impact on the modelled unstable ratio for all study areas. Unstable ratio is lowest in the single tree detection scenario for the Trub and StA study area. In the Eriz study area, it is the lowest for the uniform vegetation. We assume this is caused by the high calibrated uniform root reinforcement in Eriz and a lower value in the other study areas (Table 6). Both single-tree detection and uniform vegetation have the ability to decrease
515 instability. From a practical perspective vegetating parts of a study area is more realistic than uniformly vegetating the whole area. Influence of the vegetation scenario on the AUC is considerably more limited, with an absolute increase of 0.008 AUC points, corresponding to a relative gain of 2%. The overall relative gain, however, is the outcome from the performance in the Trub study area. Results in the Eriz study area show no difference and in StA single-tree detection shows a lower AUC. Our overall finding that the model output is highly sensitive to the vegetation scenario and gives lowest values in unstable
520 ratio and highest values in AUC for single-tree detection (realistic vegetation cover). We argue that even though the model is calibrated on a global uniform vegetation scenario (Table 6) and the single-tree detection gives a better overall performance, single tree detection is more accurate in assessing shallow landslide susceptibility. Adding to this explanation is that in these study areas where slope angle is a highly predictive factor, even marginal gains in AUC due to vegetation are important and the result of extensive parameterization. Our analysis is in line with the findings of Roering et al. (2003), who state that single tree
525 based modelling, including the tree dimensions, has the highest accuracy in the prediction of shallow landslides. Moreover, Vergani et al. (2014) state that a site specific estimation of vegetation and root extent is essential in the correct estimation of root reinforcement.

5.5 Model performance

As pointed out by Corominas et al. (2014), the absolute values of AUC are dependent on the characteristics of the study area.
530 In larger areas, with low overall landslide activity, the AUC will overestimate the predictive performance. This most likely explains why the StA study area has a low overall AUC compared to Eriz and Trub (Table 7). In particular, StA study area shows a higher prevalence of steep slopes. The Trub and the Eriz study area show both relatively high AUC values, indicating high model performance, with very similar AUC values; this is in agreement with a similar occurrence of steep and gradual slopes in these areas. Another explanation for the discrepancy in model performance between the study areas could be the
535 assumption that all trees are beech trees. This does not hold equally well for all three study areas. Based on visual inspection and on elevation, the mismatch between actual vegetation and this assumption is probably most pronounced in the StA area, where the dominant tree species appears to be Spruce. Though no published data is available, it can be estimated from the

work of Moos et al. (2016) that the root reinforcement of a spruce forest is lower than that of a beech forest, but this cannot be confirmed by our parameter analysis at this stage.

540 A comparison between the shallow landslide density (Table 2) and the calibrated unstable ratio (Table 6) shows moderate consistency. The Eriz study area has a lower unstable area corresponding to a lower shallow landslide density. However, the proportion is not equal. The low landslide density of the Trub area is not reflected in the calibrated unstable ratio. From the consistency in Table 6 and the sensitivity analysis results of Fig. 5, it can be concluded that the main configuration of the model lies in the parametrization of the mean soil thickness, the mean cohesion and the P/T ratio. These parameters gravitate to a consistent value. In addition, the vegetation scenario strongly influences the model performance and is of high influence on calculated shallow landslide probability (Table 7). Equifinality between precipitation intensity and the transmissivity appears to be at play, judging from the low variation in P/T ratio in Table 6. Additional equifinality is likely as it is very common in similar multi-parameter modelling (Beven and Binley, 1992). However, the sensitivity as observed in Fig. 5 is valid and a good indicator for important parameters in SlideforMAP. The calibrated optimal parameter set (Table 6) is still within realistic bounds as is the ranges for the sensitivity analysis. In addition, the calibrated combination of mean friction angle and mean soil cohesion are possible, though unlikely, according to Supplementary material Table A1. Finally, we would like to add here that the case study dependence of the used model performance measure is a limitation that typically occurs for all model performance measures that compare the model behavior to some reference model (Schaeffli and Gupta, 2007) (the reference model for AUC is a random process). Accordingly, we cannot compare the performance of SlideforMAP to other published AUC values despite of the fact that values around 0.8 are generally considered as indicating good performance (e.g. Xu et al., 2012).

5.6 Comparison to other slope stability models

The main advantage of SlideforMAP to other similar models is the more realistic approach to implement root reinforcement. It includes a spatial distribution in both the basal and lateral root reinforcement and the focus on second stage of the activation phase in accordance with the Root Bundle Model as described in Gehring et al. (2019).

560 Compared to previous slope stability models that include the effect of root reinforcement, SlideforMAP uses a more realistic implementation of root reinforcement based on recent knowledge of shallow landslides triggering mechanisms and root reinforcement activation (Schwarz et al., 2012, 2013; Cohen and Schwarz, 2017). In particular, only part of the lateral root reinforcement under tension is considered for the force balance calculation, and the spatial distribution of root reinforcement as function of forest structure is considered. The assumption made in SlideforMAP allow a probabilistic calculation at regional scale that are not possible with more complex models such as SOSlope (Cohen and Schwarz, 2017). In comparison to more simple models based on infinite slope calculations (Pack et al., 1998; Montgomery and Dietrich, 1994, SINMAP,SHALTAB), SlideforMAP considers the effect of lateral root reinforcement on landslide of different sizes.

5.7 Future research

570 SlideforMAP uses a relatively simple hydrological module to estimate soil saturation. The used TOPOG approach could be improved and multiple papers have presented simple to more advanced rewriting of formulas (e.g. Beven and Freer, 2001; Blazkova et al., 2002). Common denominator is the inclusion of time dependency, since the stationary flow assumption rarely, if ever, holds in nature. This time dependency is a solution to simulate a different response to a precipitation event at different locations within a study area. Future work could also focus on improving the vegetation module by including different tree
575 species (those that are often used in protection forest) in the parametrization of lateral root reinforcement (equation 8). For practical application of SlideforMAP we have not found a specific lower boundary in landslide density, to still generate reliable results. More specific testing on this would be useful for future application of SlideforMAP. A comparison between SlideforMAP and SHALSTAB and/or SINMAP would be interesting. It can validate whether the uniform vegetation scenario in SlideforMAP produces similar results to these models in terms of shallow landslide probability. Finally doing a validation over
580 study areas with a larger shallow landslide inventory would be a vital procedure to further analyze the SlideforMAP model.

6 Conclusions

In this paper, we present a probabilistic model to assess shallow landslide (landslides with a scar thickness < 2 m) probability. The main motivation to develop yet another model is to provide a detailed inclusion of the influence of root reinforcement. The key elements of the model parameterization are the mean soil thickness, the mean soil cohesion, the soil transmissivity and the
585 lateral root reinforcement. Its application is illustrated based on three mid-elevation case studies from Switzerland, for which a detail landslide inventory is available. The model has a total of 22 parameters, of which 12 are calibrated using the AUC of the Receiver Operator Curve as performance measure to identify the best parameter set among a large set generated using Latin hyper cube sampling. The AUC maximum values for the three study areas vary between between 0.69 and 0.94 under a spatially uniform vegetation scenario, which reflects an overall good model performance. Our model parameter analysis has
590 shown that root reinforcement, in conjunction with soil thickness, transmissivity and soil cohesion, are the key parameters to predict slope stability in the studied mountainous regions. A major focus of the presented work was the assessment of the model's ability to study scenarios of vegetation distribution. Comparison of different scenarios ranging from uniform to single-tree detection-based vegetation clearly showed that the model output, in terms of shallow landslide probability, is highly sensitive to the spatial distribution of vegetation. Accordingly, the model is fit for future scenario analysis, including e.g.
595 different protection forest management scenarios. In fact, a single-tree scale model parameterization provides the opportunity to run hypothetical vegetation scenarios reflecting on small scale managements strategies or disturbances. Future improvements in the hydrological approach, concerning a more catchment based approach to compute saturation degree, could likely further improve the performance of SlideforMAP.

Appendix A: Appendix

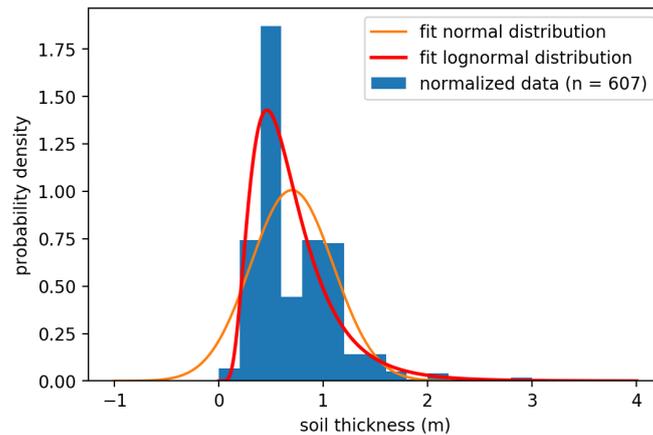


Figure A1. Plot of the probability density of the soil thickness data from the BAFU dataset as used in this paper. The best fit is given of a normal and a log-normal distribution. The mean square errors are 0.096 and 0.053 for the normal and log-normal fit respectively.

Table A1. The hybrid table for the soil cohesion and angle of internal friction for the relevant set of USCS soil classes. Derived from laboratory experiments (VSS-Kommission, 1998; Dysli and Rybisar, 1992) and combined in this research to exclude values that seemed unrealistic.

| USCS soil class | Mean soil cohesion | Std. dev. soil cohesion | Mean friction angle | Std. dev. friction angle |
|-----------------|--------------------|-------------------------|---------------------|--------------------------|
| SM | 0 | 0 | 34.5 | 5.0 |
| CL-ML | 0.4 | 1.3 | 32.7 | 4.8 |
| GM | 0.0 | 0.0 | 35.0 | 5.0 |
| GC-GM | 5.0 | 5.0 | 33.0 | 3.0 |
| CL | 6.2 | 11.3 | 27.1 | 5.2 |
| OL | 2.5 | 5.0 | 32.8 | 2.2 |
| GC | 20.0 | 52.9 | 31.4 | 3.6 |

600 *Data availability.* All data used in this research is open data. The topographical data and the landslide inventory as used in this research are published on Zenodo

Author contributions. A.A. collected the landslide inventory and made it ready for use. D.C. and M.S. developed the basic concept of SlideforMap. L.D. contributed in the further development. F.Z. executed further development, the sensitivity analysis and testing. F.Z. is the main writer. B.S. L.D. C.P. A.A. and M.S. revised the text. C.P. and M.S. organized funds.

605 *Competing interests.* The authors declare no conflict of interest.

Disclaimer. The shallow landslide probability maps generated by SlideforMAP are a guideline and should be interpreted by an expert before application.

Acknowledgements. We thank the STEC (Smarter Targeting of Erosion Control) project by the Ministry of Business, Innovation and Employment of New Zealand for the financial support. In addition we would like to thank the two anonymous reviewers and a community review
610 by David Milledge. Their contribution was of great improvement to the quality of this paper.

References

- Amishev, D., Basher, L., Phillips, C., Hill, S., Marden, M., Bloomberg, M., and Moore, J.: New Forest Management Approaches to Steep Hills, vol. 7, <http://www.mpi.govt.nz/news-resources/publications.aspx>, 2014.
- Askarinejad, A., Casini, F., Bischof, P., Beck, A., and Springman, S. M.: Rainfall induced instabilities: a field experiment on a silty sand slope in northern Switzerland, *rivista italiana di geotecnica*, pp. 50–71, <http://www.associazionegeotecnica.it/rig/archivio>, 2012.
- Askarinejad, A., Akca, D., and Springman, S. M.: Precursors of instability in a natural slope due to rainfall: a full-scale experiment, *Landslides*, 15, 1745–1759, <https://doi.org/10.1007/s10346-018-0994-0>, 2018.
- Badoux, A., Andres, N., Techel, F., and Hegg, C.: Natural hazard fatalities in Switzerland from 1946 to 2015, *Natural Hazards and Earth System Sciences*, 16, 2747–2768, <https://doi.org/10.5194/nhess-16-2747-2016>, 2016.
- Baeza, C. and Corominas, J.: Assessment of shallow landslide susceptibility by means of multivariate statistical techniques, *Earth Surface Processes and Landforms*, 26, 1251–1263, <https://doi.org/10.1002/esp.263>, 2001.
- Bárdossy, A.: Calibration of hydrological model parameters for ungauged catchments, *Hydrology and Earth System Sciences*, 11, 703–710, <https://doi.org/10.5194/hess-11-703-2007>, 2007.
- Baum, R. L., Savage, W. Z., and Godt, J. W.: TRIGRS—A Fortran Program for Transient Rainfall Infiltration and Grid-Based Regional Slope-Stability Analysis, Open file report 02-424, p. 25, 2002.
- Beven, K. and Binley, A.: The future of distributed models: Model calibration and uncertainty prediction, *Hydrological Processes*, 6, 279–298, <https://doi.org/10.1002/hyp.3360060305>, 1992.
- Beven, K. and Freer, J.: A dynamic topmodel, *Hydrological Processes*, 15, 1993–2011, <https://doi.org/10.1002/hyp.252>, 2001.
- Beven, K. J. and Kirkby, M. J.: A physically based, variable contributing area model of basin hydrology, *Hydrological Sciences Bulletin*, 24, 43–69, <https://doi.org/10.1080/02626667909491834>, 1979.
- Blazkova, S., Beven, K., Tacheci, P., and Kulasova, A.: Testing the distributed water table predictions of TOPMODEL (allowing for uncertainty in model calibration): The death of TOPMODEL?, *Water Resources Research*, 38, 39–1–39–11, <https://doi.org/10.1029/2001wr000912>, 2002.
- Bodner, G., Leitner, D., and Kaul, H. P.: Coarse and fine root plants affect pore size distributions differently, *Plant and Soil*, 380, 133–151, <https://doi.org/10.1007/s11104-014-2079-8>, 2014.
- Bordoni, M., Meisina, C., Valentino, R., Lu, N., Bittelli, M., and Chersich, S.: Hydrological factors affecting rainfall-induced shallow landslides: From the field monitoring to a simplified slope stability analysis, *Engineering Geology*, 193, 19–37, <https://doi.org/10.1016/j.enggeo.2015.04.006>, 2015.
- Borga, M., Dalla Fontana, G., Gregoretti, C., and Marchi, L.: Assessment of shallow landsliding by using a physically based model of hillslope stability, *Hydrological Processes*, 16, 2833–2851, <https://doi.org/10.1002/hyp.1074>, 2002.
- Cervi, F., Berti, M., Borgatti, L., Ronchetti, F., Manenti, F., and Corsini, A.: Comparing predictive capability of statistical and deterministic methods for landslide susceptibility mapping: A case study in the northern Apennines (Reggio Emilia Province, Italy), *Landslides*, 7, 433–444, <https://doi.org/10.1007/s10346-010-0207-y>, 2010.
- Chae, B. G., Park, H. J., Catani, F., Simoni, A., and Berti, M.: Landslide prediction, monitoring and early warning: a concise review of state-of-the-art, *Geosciences Journal*, 21, 1033–1070, <https://doi.org/10.1007/s12303-017-0034-4>, 2017.
- Cislaghi, A., Rigon, E., Lenzi, M. A., and Bischetti, G. B.: A probabilistic multidimensional approach to quantify large wood recruitment from hillslopes in mountainous-forested catchments, *Geomorphology*, 306, 108–127,

- <https://doi.org/https://doi.org/10.1016/j.geomorph.2018.01.009>, <https://www.sciencedirect.com/science/article/pii/S0169555X1830014X>, 2018.
- 650 Cohen, D. and Schwarz, M.: Tree-root control of shallow landslides, *Earth Surface Dynamics*, 5, 451–477, <https://doi.org/10.5194/esurf-5-451-2017>, 2017.
- Cohen, D., Lehmann, P., and Or, D.: Fiber bundle model for multiscale modeling of hydromechanical triggering of shallow landslides, *Water Resources Research*, 45, 1–20, <https://doi.org/10.1029/2009WR007889>, 2009.
- Corominas, J., van Westen, C., Frattini, P., Cascini, L., Malet, J. P., Fotopoulou, S., Catani, F., Van Den Eeckhaut, M., Mavrouli, O., Agliardi, F., Pitilakis, K., Winter, M. G., Pastor, M., Ferlisi, S., Tofani, V., Hervás, J., and Smith, J. T.: Recommendations for the quantitative analysis of landslide risk, *Bulletin of Engineering Geology and the Environment*, 73, 209–263, <https://doi.org/10.1007/s10064-013-0538-8>, 2014.
- 655 F., Pitilakis, K., Winter, M. G., Pastor, M., Ferlisi, S., Tofani, V., Hervás, J., and Smith, J. T.: Recommendations for the quantitative analysis of landslide risk, *Bulletin of Engineering Geology and the Environment*, 73, 209–263, <https://doi.org/10.1007/s10064-013-0538-8>, 2014.
- Day, R. W.: State of the art: Limit equilibrium and finite-element analysis of slopes, *Journal of Geotechnical and Geoenvironmental Engineering*, 123, 894, [https://doi.org/10.1061/\(ASCE\)1090-0241\(1997\)123:9\(894\)](https://doi.org/10.1061/(ASCE)1090-0241(1997)123:9(894)), 1997.
- Dazio, E. P. R., Conedera, M., and Schwarz, M.: Impact of different chestnut coppice managements on root reinforcement and shallow
- 660 landslide susceptibility, *Forest Ecology and Management*, 417, 63–76, <https://doi.org/10.1016/j.foreco.2018.02.031>, <https://doi.org/10.1016/j.foreco.2018.02.031>, 2018.
- Dietrich, W. E. and Montgomery, D. R.: SHALSTAB: a digital terrainmodel for mapping shallow landslide potential., Tech. rep., NCASI (National Council of the Paper Industry for Air and Stream Improvement), 1998.
- D’Odorico, P. and Fagherazzi, S.: A probabilistic model of rainfall-triggered shallow landslides in hollows: A long-term analysis, *Water*
- 665 *Resources Research*, 39, 1–14, <https://doi.org/10.1029/2002WR001595>, 2003.
- Dorren, L.: FINT – Find individual trees. User manual., ecorisQ paper (www.ecorisq.org), p. 5 p, 2017.
- Dorren, L. and Sandri, A.: Landslide risk mapping for the entire Swiss national road network, *Landslide Processes*, pp. 277–281, <http://eost.u-strasbg.fr/omiv/Landslide{ }Processes{ }Conference/Dorren{ }et{ }al.pdf>, 2009.
- Dysli, M. and Rybisar, J.: Statistique sur les caractéristiques des sols suisses- Statistische Behandlung der Kennwerte der Schweizer Boeden.,
- 670 Bundesamt fuer Strassenbau, 1992.
- Eysn, L., Hollaus, M., Lindberg, E., Berger, F., Monnet, J. M., Dalponte, M., Kobal, M., Pellegrini, M., Lingua, E., Mongus, D., and Pfeifer, N.: A benchmark of lidar-based single tree detection methods using heterogeneous forest data from the Alpine Space, *Forests*, 6, 1721–1747, <https://doi.org/10.3390/f6051721>, 2015.
- Fawcett, T.: An introduction to ROC analysis, *Pattern Recognition Letters*, <https://doi.org/10.1016/j.patrec.2005.10.010>, 2006.
- 675 Feng, S., Liu, H. W., and Ng, C. W.: Analytical analysis of the mechanical and hydrological effects of vegetation on shallow slope stability, *Computers and Geotechnics*, 118, <https://doi.org/10.1016/j.compgeo.2019.103335>, 2020.
- Freeze, R. A. and Cherry, J. A.: *Groundwater*, No. 629.1 F7, 1979.
- Frei, C., Isotta, F., and Schwanbeck, J.: Mean Precipitation 1981-2010, in: *Hydrological Atlas of Switzerland*, Geographisches Institut der Universität Bern, 2020.
- 680 Gehring, E., Conedera, M., Maringer, J., Giadrossich, F., Guastini, E., and Schwarz, M.: Shallow landslide disposition in burnt European beech (*Fagus sylvatica* L.) forests, *Scientific Reports*, 9, 1–11, <https://doi.org/10.1038/s41598-019-45073-7>, 2019.
- González-Ollauri, A. and Mickovski, S. B.: Integrated Model for the Hydro-Mechanical Effects of Vegetation Against Shallow Landslides, *EQA - International Journal of Environmental Quality*, 13, 37–59, <https://doi.org/10.6092/issn.2281-4485/4535>, <https://eqa.unibo.it/article/view/4535/4013>, 2014.

- 685 Grabs, T., Seibert, J., Bishop, K., and Laudon, H.: Modeling spatial patterns of saturated areas: A comparison of the topographic wetness index and a dynamic distributed model, *Journal of Hydrology*, 373, 15–23, <https://doi.org/10.1016/j.jhydrol.2009.03.031>, <http://dx.doi.org/10.1016/j.jhydrol.2009.03.031>, 2009.
- Greenway, D. R.: Vegetation and slope stability, *Slope Stabilization*, pp. 187–23, 1987.
- Griffiths, D. V., Huang, J., and Fenton, G. A.: Influence of Spatial Variability on Slope Reliability Using 2-D Random Fields, *Journal of Geotechnical and Geoenvironmental Engineering*, 135, 1367–1378, [https://doi.org/10.1061/\(asce\)gt.1943-5606.0000099](https://doi.org/10.1061/(asce)gt.1943-5606.0000099), 2009.
- 690 HADES: https://hydrologischeratlas.ch/downloads/01/content/Text_Tafel24.de.pdf, 2020.
- Hawley, J. and Dymond, J.: How much do trees reduce landsliding?, *Journal of Soil&Water Conservation*, 43, 495–498, 1988.
- Iida, T.: A stochastic hydro-geomorphological model for shallow landsliding due to rainstorm, *Catena*, 34, 293–313, [https://doi.org/10.1016/S0341-8162\(98\)00093-9](https://doi.org/10.1016/S0341-8162(98)00093-9), 1999.
- 695 Iverson, R. M.: Landslide triggering by rain infiltration, *Water Resources Research*, 36, 1897–1910, <https://doi.org/10.1029/2000WR900090>, <http://doi.wiley.com/10.1029/2000WR900090>, 2000.
- Jensen, H., Lang, H., and Rinderknecht, J.: Extreme Punktregen unterschiedlicher Dauer und Wiederkehrperioden 1901-1970, Tafel 2.4., in: *Hydrologischer Atlas der Schweiz*, Geographisches Institut der Universität Bern, 1997.
- Johnson, N. L. and Kotz, S.: *Continuous univariate distributions*, Houghton Mifflin, Boston, 1970.
- 700 Kirkby, M.: Hydrograph modelling strategies, 69–90, Peel R, Chisholm M, Haggert P, *Processes in Physical and Human Geography*, Heinemann, London, 1975.
- Kjekstad, O. and Highland, L.: Economic and Social Impacts of Landslides, *Landslides – Disaster Risk Reduction*, 30, 573–587, https://link.springer.com/content/pdf/10.1007/978-3-540-69970-5_{_}30.pdf, 2009.
- Korpela, I., Dahlin, B., Schäfer, H., Bruun, E., Haapaniemi, F., Honkasalo, J., Ilvesniemi, S., Kuutti, V., Linkosalmi, M., Mustonen, J., Salo, M., Suomi, O., and Virtanen, H.: Single-tree forest inventory using lidar and aerial images for 3D treetop positioning, species recognition, height and crown width estimation, *International Archives of the Photogrammetry, Remote Sensing and Spatial Information Sciences*, 36, 227–233, 2007.
- 705 Lehmann, P., Gambazzi, F., Suski, B., Baron, L., Askarinejad, A., Springman, S. M., Holliger, K., and Or, D.: Evolution of soil wetting patterns preceding a hydrologically induced landslide inferred from electrical resistivity survey and point measurements of volumetric water content and pore water pressure, *Water Resources Research*, 49, 7992–8004, <https://doi.org/10.1002/2013WR014560>, 2013.
- Leonarduzzi, E., Molnar, P., and McArdell, B. W.: Predictive performance of rainfall thresholds for shallow landslides in Switzerland from gridded daily data, *Water Resources Research*, 53, 6612–6625, <https://doi.org/10.1002/2017WR021044>, 2017.
- Li, W. C., Lee, L. M., Cai, H., Li, H. J., Dai, F. C., and Wang, M. L.: Combined roles of saturated permeability and rainfall characteristics on surficial failure of homogeneous soil slope, *Engineering Geology*, 153, 105–113, <https://doi.org/10.1016/j.enggeo.2012.11.017>, <http://dx.doi.org/10.1016/j.enggeo.2012.11.017>, 2013.
- 715 //dx.doi.org/10.1016/j.enggeo.2012.11.017, 2013.
- Malamud, B., Turcotte, D., Guzzetti, F., and Reichenbach, P.: Landslide inventories and their statistical properties, *Earth Surface Processes and Landforms*, 29, 687–711, <https://doi.org/10.1002/esp.1064>, 2004.
- Masi, E. B., Segoni, S., and Tofani, V.: Root reinforcement in slope stability models: A review, *Geosciences (Switzerland)*, 11, <https://doi.org/10.3390/geosciences11050212>, 2021.
- 720 McKay, M. D., Beckman, R. J., and Conover, W. J.: Comparison of three methods for selecting values of input variables in the analysis of output from a computer code, *Technometrics*, 21, 239–245, <https://doi.org/10.1080/00401706.1979.10489755>, 1979.

- Menk, J., Dorren, L., Heinzl, J., Marty, M., and Huber, M.: Evaluation automatischer Einzelbaumerkennung aus luftgestützten Laserscanning-Daten, *Schweizerische Zeitschrift für Forstwesen*, 168, 151–159, <https://doi.org/10.3188/szf.2017.0151>, 2017.
- Metz, C. E.: Basic principles of ROC analysis., *Seminars in nuclear medicine*, 8, 283–298, [https://doi.org/http://dx.doi.org/10.1016/S0001-7252998\(78\)80014-2](https://doi.org/http://dx.doi.org/10.1016/S0001-7252998(78)80014-2), 1978.
- Montgomery, D. R. and Dietrich, W. E.: A physically based model for the topographic control on shallow landsliding, *Water Resources Research*, 30, 1153–1171, <https://doi.org/10.1029/93WR02979>, 1994.
- Montgomery, D. R. and Dietrich, W. E.: Reply to comment by Richard M. Iverson on ‘piezometric response in shallow bedrock at cb1: implications for runoff generation and landsliding’, *Water Resources Research*, 40, W03 802, 2004.
- 730 Montgomery, D. R., Schmidt, K. M., Greenberg, H. M., and Dietrich, W. E.: Forest clearing and regional landsliding, *Geology*, 28, 311–314, [https://doi.org/10.1130/0091-7613\(2000\)28<311:FCARL>2.0.CO;2](https://doi.org/10.1130/0091-7613(2000)28<311:FCARL>2.0.CO;2), 2000.
- Montgomery, D. R., Dietrich, W. E., and Heffner, J. T.: Piezometric response in shallow bedrock at CBI: Implications for runoff generation and landsliding, *Water Resources Research*, 38, 10–1–10–18, <https://doi.org/10.1029/2002wr001429>, 2002.
- Montrasio, L. and Valentino, R.: A model for triggering mechanisms of shallow landslides, *Natural Hazards and Earth System Science*, 8, 735 1149–1159, <https://doi.org/10.5194/nhess-8-1149-2008>, 2008.
- Montrasio, L., Valentino, R., and Losi, G. L.: Towards a real-time susceptibility assessment of rainfall-induced shallow landslides on a regional scale, *Natural Hazards and Earth System Science*, 11, 1927–1947, <https://doi.org/10.5194/nhess-11-1927-2011>, 2011.
- Moos, C., Bebi, P., Graf, F., Mattli, J., Rickli, C., and Schwarz, M.: How does forest structure affect root reinforcement and susceptibility to shallow landslides?, *Earth Surface Processes and Landforms*, 41, 951–960, <https://doi.org/10.1002/esp.3887>, 2016.
- 740 Mosley, M. P.: Subsurface flow velocities through selected forest soils, South Island, New Zealand, *Journal of Hydrology*, 55, 65–92, [https://doi.org/10.1016/0022-1694\(82\)90121-4](https://doi.org/10.1016/0022-1694(82)90121-4), 1982.
- Munich RE: Relevant hydrological events worldwide 1980 - 2018, NatCatService, 2018.
- O’Callaghan, J. F. and Mark, D. M.: The Extraction of Drainage Networks from Digital Elevation Data, *Computer Vision, Graphics and Image Processing*, 28, 323–344, [https://doi.org/10.1016/0734-189X\(89\)90053-4](https://doi.org/10.1016/0734-189X(89)90053-4), 1984.
- 745 Pack, R. T., Tarboton, D. G., and Goodwin, C. N.: The SINMAP Approach to Terrain Stability Mapping, 8th Congress of the International Association of Engineering Geology, p. 8, 1998.
- Park, H. J., Lee, J. H., and Woo, I.: Assessment of rainfall-induced shallow landslide susceptibility using a GIS-based probabilistic approach, *Engineering Geology*, 161, 1–15, <https://doi.org/10.1016/j.enggeo.2013.04.011>, <http://dx.doi.org/10.1016/j.enggeo.2013.04.011>, 2013.
- Prancevic, J. P., Lamb, M. P., McArdell, B. W., Rickli, C., and Kirchner, J. W.: Decreasing Landslide Erosion on Steeper Slopes in Soil-750 Mantled Landscapes, *Geophysical Research Letters*, 47, 1–9, <https://doi.org/10.1029/2020GL087505>, 2020.
- Price, B., Gomez, A., Mathys, L., Gardi, O., Schellenberger, A., Ginzler, C., and Thürig, E.: Tree biomass in the Swiss landscape: nationwide modelling for improved accounting for forest and non-forest trees, *Environmental Monitoring and Assessment*, 189, <https://doi.org/10.1007/s10661-017-5816-7>, 2017.
- Reinhold, S., Medicus, G., Fellin, W., and Zangerl, C.: The influence of deforestation on slope (In-) stability, *Austrian Journal of Earth755 Sciences*, 102, 90–99, <https://doi.org/10.1139/t01-031>, 2009.
- Rickli, C. and Graf, F.: Effects of forests on shallow landslides – case studies in Switzerland, *Forest Snow and Landscape Research*, 44, 33–44, <http://www.issw.ch/wsl/publikationen/pdf/9696.pdf>, 2009.
- Rickli, C., Graf, F., Bebi, P., Bast, A., Loupt, B., and McArdell, B.: Schützt der Wald vor Rutschungen? Hinweise aus der WSL-Rutschungsdatenbank, *Schweizerische Zeitschrift für Forstwesen*, 170, 310–317, <https://doi.org/10.3188/szf.2019.0310>, 2019.

- 760 Roering, J., Schmidt, K. M., Stock, J. D., Dietrich, W. E., and Montgomery, D. R.: Shallow landsliding, root reinforcement, and the spatial distribution of trees in the Oregon Coast Range, *Canada Geotechnical Journal*, 40, 237–253, 2003.
- Salvatici, T., Tofani, V., Rossi, G., D'Ambrosio, M., Tacconi Stefanelli, C., Benedetta Masi, E., Rosi, A., Pazzi, V., Vannocci, P., Petrolo, M., Catani, F., Ratto, S., Stevenin, H., and Casagli, N.: Application of a physically based model to forecast shallow landslides at a regional scale, *Natural Hazards and Earth System Sciences*, 18, 1919–1935, <https://doi.org/10.5194/nhess-18-1919-2018>, 2018.
- 765 Schaepli, B. and Gupta, H.: Do Nash values have value, *Hydrological Processes*, 21, 2075–2080, <https://doi.org/10.1002/hyp>, <http://jamsb.austms.org.au/courses/CSC2408/semester3/resources/ldp/abs-guide.pdf>, 2007.
- Schmidt, K. M., Roering, J. J., Stock, J. D., Dietrich, W. E., Montgomery, D. R., and Schaub, T.: The variability of root cohesion as an influence on shallow landslide susceptibility in the Oregon Coast Range, *Canadian Geotechnical Journal*, 38, 995–1024, <https://doi.org/10.1139/cgj-38-5-995>, 2001.
- 770 Schwarz, M., Preti, F., Giadrossich, F., Lehmann, P., and Or, D.: Quantifying the role of vegetation in slope stability: A case study in Tuscany (Italy), *Ecological Engineering*, 36, 285–291, <https://doi.org/10.1016/j.ecoleng.2009.06.014>, 2010.
- Schwarz, M., Cohen, D., and Or, D.: Spatial characterization of root reinforcement at stand scale: theory and case study, *Geomorphology*, 171, 190–200, 2012.
- Schwarz, M., Giadrossich, F., and Cohen, D.: Modeling root reinforcement using a root-failure Weibull survival function, *Hydrology and Earth System Sciences*, 17, 4367–4377, <https://doi.org/10.5194/hess-17-4367-2013>, 2013.
- 775 Schwarz, M., Rist, A., Cohen, D., Giadrossich, F., Egorov, P., Büttner, D., Stolz, M., and Thormann, J. J.: Root reinforcement of soils under compression, *Journal of Geophysical Research F: Earth Surface*, 120, 2103–2120, <https://doi.org/10.1002/2015JF003632>, 2015.
- Sidle, R. C.: A Theoretical Model of the Effects of Timber harvesting on Slope Stability, *Water Resources Research*, 28, 1897–1910, 1992.
- Swiss Re Institute: Natural catastrophes and man-made disasters in 2018: “secondary” perils on the frontline., *Sigma*, 2, 1–36, 2019.
- 780 Swisstopo: SWISSIMAGE. Luftbilder Level 2 (25 cm) Wabern: Bern, 2017.
- Swisstopo: SwissALTI3D Das hoch auf-gelöste Terrainmodell der Schweiz, 2018.
- Swisstopo: Switzerland forest cover map; <https://shop.swisstopo.admin.ch/de/products/maps/national/vector/smv25>, 2020.
- Torres, R., Dietrich, W. E., Montgomery, D. R., Anderson, S. P., and Loague, K.: Unsaturated zone processes and the hydrologic response of a steep, unchanneled catchment, *Water Resources Research*, 34, 1865–1879, <https://doi.org/10.1029/98WR01140>, 1998.
- 785 Varnes, D. J.: Slope Movement Types and Processes, Special report, 176, 11–33, <https://doi.org/10.1016/j.msar.2018.11.001>, 1978.
- Vergani, C., Schwarz, M., Cohen, D., Thormann, J., and Bischetti, G.: Effects of root tensile force and diameter distribution variability on root reinforcement in the Swiss and Italian Alps, *Canadian Journal of Forest Research*, 44, 1426–1440, <https://doi.org/10.1139/cjfr-2014-0095>, <http://www.nrcresearchpress.com/doi/abs/10.1139/cjfr-2014-0095>{#}.VPm77k0tHoo, 2014.
- VSS-Kommission: Schweizer Norm, 670 010b, Tech. rep., Schweizer Norm, 1998.
- 790 Weiler, M. and Naef, F.: An experimental tracer study of the role of macropores in infiltration in grassland soils, *Hydrological Processes*, 17, 477–493, <https://doi.org/10.1002/hyp.1136>, 2003.
- Wiekenkamp, I., Huisman, J. A., Bogena, H. R., Lin, H. S., and Vereecken, H.: Spatial and temporal occurrence of preferential flow in a forested headwater catchment, *Journal of Hydrology*, 534, 139–149, <https://doi.org/10.1016/j.jhydrol.2015.12.050>, <http://dx.doi.org/10.1016/j.jhydrol.2015.12.050>, 2016.
- 795 Wu, T., McKinnel, W. P., and Swanston, D. N.: Strength of tree roots and landslides on Prince of Wales Island, Alaska, *Canada Geotechnical Journal*, pp. 19–33, 1978.

- Xu, C., Xu, X., Dai, F., and Saraf, A. K.: Comparison of different models for susceptibility mapping of earthquake triggered landslides related with the 2008 Wenchuan earthquake in China, *Computers and Geosciences*, 46, 317–329, <https://doi.org/10.1016/j.cageo.2012.01.002>, <http://dx.doi.org/10.1016/j.cageo.2012.01.002>, 2012.
- 800 Zevenbergen, L. and Thorne, C.: Quantitative analysis of land surface topography, *Earth Surface Processes and Landforms*, 12, 47–56, 1987.
- Zhang, S., Zhao, L., Delgado-Tellez, R., and Bao, H.: A physics-based probabilistic forecasting model for rainfall-induced shallow landslides at regional scale, *Natural Hazards and Earth System Sciences*, 18, 969–982, <https://doi.org/10.5194/nhess-18-969-2018>, 2018.
- Zhu, H., Zhang, L. M., Xiao, T., and Li, X. Y.: Enhancement of slope stability by vegetation considering uncertainties in root distribution, *Computers and Geotechnics*, 85, 84–89, <https://doi.org/10.1016/j.compgeo.2016.12.027>, 2017.