



# Multiscale effects caused by the fracturing and fragmentation of rock blocks in rock mass movement: Implications for rock avalanche propagation

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10 **Abstract.** Fracturing and fragmentation of rock blocks are important and universal phenomena during the propagation of rock avalanches. Here, the movement of a rectangular rock block characterized by different joint sets along an upper inclined and lower horizontal traveling path is simulated, aiming to quantify the fracturing and fragmentation effect of the block in propagation. The preset of the joint sets allows the block to break along the weak joint planes at the very beginning of fragmentation. With this design, the fracturing and fragmentation processes in the sliding rock block and their influences on energy transformation in the system are investigated. The results show that fragmentation can alter the horizontal velocities and kinetic energies of fragments in the block system with the front subblocks being accelerated and the rear part being obviously decelerated. Such energy conversion and transfer between the front and rear subblocks is attributed to the elastic strain energy release and transformation caused by fragmentation. The energy transfer induced by fragmentation is more efficient than that induced by collision. A positive trend between the kinetic energy increase of the front subblocks induced by fragmentation and the rock strength can be fitted well with a linear function. However, no good relationship is reached between the strain energy incremental ratio and travel distance, which implies that the fragmentation effects may be weakened with the increasing complexity of the fragmenting rock mass system. Three elastic strain wave release effects caused by rock fragmentation are further inferred and discussed based on simulation results.

## 1 Introduction

25 Rock avalanches are one of the most destructive geophysical flows and can effectively shape mountainous landscapes on Earth and other planetary surfaces (Lucas et al., 2014; Crosta et al., 2018). They have also caused numerous casualties and large economic losses in recent decades due to their extremely long travel distances (Evans et al., 2007; Fan et al., 2017). Hypermobility, i.e., exceptionally long runout distances of rock avalanches, is usually quantified by the apparent friction coefficient ( $H/L$ , where  $H$  and  $L$  represent the vertical and horizontal distances between the crest of the failure mass and the distal point of deposition, respectively) (Heim, 1932). When the volume of the failure mass  $>10^6$  m<sup>3</sup>,  $H/L$  shows a decrease



with volume, leading to hypermobility in mega rock avalanches. The hypermobility of rock avalanches has drawn much scientific interest because it cannot be simply solved by a Coulomb frictional model of a sliding rock block (Legros, 2002). To explain the hypermobility of rock avalanches, many dynamic mechanisms have been proposed. Some mechanisms involve fluid media, such as air (Kent, 1966), water (Wang et al., 2002; Hungr and Evans, 2004), a fluid-like fine grain matrix (Hsü 1975), melted rock or vapor (Habib, 1975; Goguel, 1978; Hu et al., 2018), thermal pressurization and thermal moisture fluidization (Wang et al., 2017, 2018a). Others invoke the interactions of materials in avalanche systems, such as shearing and impacting between a sliding mass and undulate path-generated acoustic fluidization (Melosh, 1979; Collins and Melosh, 2003), shearing between a rock mass and the ground (Foda, 1994; Wang et al., 2015), shearing between particles in the basal layer (Preuth et al., 2010), momentum transfer caused by collisions of particles or different parts of the rock mass (Heim, 1932; Van Gassen et al., 1989; Miao et al., 2001), and dispersive pressure caused by dynamic fragmentation (Davies et al., 1999; Davies and McSaveney, 2009). Nevertheless, a universal consensus is still far beyond reach (Weidinger et al., 2014). For a rigorous ~~mechanism to explain~~ hypermobility, geological evidence coming from the travel path and the deposition of the sliding mass must be considered. Many field observations suggest that the following phenomena commonly occur in large rock avalanches (Weidinger et al., 2014; Dufresne et al., 2016):

- 45 (1) “Volume effect”, where the apparent friction coefficient ( $H/L$ ) decreases as the volume of the rock mass increases (Scheidegger, 1973);
- (2) Intense fragmentation in the deposit (Davies et al., 1999);
- (3) Close packing of grains during movement (dense grain flows) (Pudasaini and Hutter, 2007);
- (4) “Inverse grading” at depth in the deposit (Heim, 1932; Cruden and Hungr, 1986);
- 50 (5) Shear stress concentrated in basal facies (Dufresne et al., 2016);
- (6) “Jigsaw puzzle” structures and local shear bands in the deposit (Shreve, 1968);
- (7) Preservation of the host rock massif structure in the rock avalanche deposit (Heim, 1932; Strom, 2006).

Unfortunately, few mechanisms account for the hypermobility of rock avalanches and can explain the formation of these main features listed above. Some mechanisms even contradict geological evidence (McSaveney and Davies, 2006). Among these mechanisms, dynamic fragmentation, first proposed by Davies et al. (1999), has received sustained investigation and supplementation (McSaveney and Davies, 2006; Davies and McSaveney, 2009; Zhao et al., 2017). This runout-enhanced mechanism is based on solid geological evidence that intense fragmentation occurs universally in the deposits of rock avalanches; meanwhile, this mechanism does not conflict with the main structural features in the deposits of rock avalanches. Moreover, special deposit structures, including inverse grading, jigsaw structures and local shear bands, are closely related to the fragmentation process of avalanches (McSaveney and Davies, 2006; Dufresne et al., 2016; Wang et al., 2018b).

60 Recently, fragmentation and related deposit characteristics and fragmentation effects of rock avalanches have been widely investigated ~~via field~~ events (Pollet and Schneider, 2004; Locat et al., 2006; Crosta et al., 2007; Perinotto et al., 2015; Wang et al., 2019, 2020), laboratory experiments (Imre et al., 2010; Bowman et al., 2012; Haug et al., 2016) and numerical simulations (Rait et al., 2012; De Blasio and Crosta, 2015; Langlois et al., 2015; Zhao et al., 2017, 2018). On the one hand,



65 fracture and fragmentation are considered to consume part of the kinetic energy. The fragmentation process is estimated to  
dissipate 1-30% of the total potential energy in a rock avalanche (Locat et al., 2006; Crosta et al., 2007; De Blasio et al.,  
2018), but these authors unrealistically truncate their rock avalanche particle-size distributions (as stated by Davies et al.  
(2019a)). When the existence of submicron particles is included in the estimate, the amount of energy supposedly dissipated  
by fragmentation rises to substantially exceed 100% of the initially available energy (Davies et al., 2019b). On the other  
70 hand, some studies have shown that fragmentation may enhance the travel distance of the distal part of the sliding mass  
(Bowman et al., 2012; De Blasio and Crosta, 2015; Haug et al., 2016). The flow structure of fine particle concentration  
caused by intense fragmentation will also facilitate the mobility of fragment flow (Langlois et al., 2015; Lai et al., 2018). For  
those who agree with the mobility-enhanced effects of dynamic fragmentation, elastic strain energy release caused by  
fragmentation is considered to be a key dynamic process accounting for hypermobility (Davies and McSaveney, 2009; De  
75 Blasio and Crosta, 2015; Zhao et al., 2017). Based on the theory of rock dynamics and fracture mechanics, rock cracking  
occurs when the peak of the stress wave exceeds the strength of the rock itself, and then, part of the strain energy is  
consumed by cracking or so-called new surface generation, while the remaining elastic strain energy may release outward as  
elastic stress waves or transfer to the kinetic energy of the fragments (Grady and Kipp, 1987; Zhang et al., 2000; Ghaffari et  
al., 2019). McSaveney and Davies (2006) proposed that elastic energy release induced by dynamic fragmentation may  
80 generate universe outward dispersed stress, which can offset part of the overburden pressure and result in lower shear  
resistance. Perinotto et al. (2015) examined the fractal dimension and circularity variation with the deposit distance of the La  
Reunion volcanic debris avalanche and then indicated that the exceptional mobility of the debris avalanche is caused by the  
comprehensive effect of dynamic disintegration-induced elastic energy release of larger clasts and frictional reduction due to  
the interactions between fragmentation-formed fine particles. Davies et al. (2019a) stated that the main fraction of the energy  
85 acting on fragmented rock radiates to the surrounding material as elastic body waves when rock fragments, while only a  
small fraction of the energy is dissipated by newly created fragment surfaces. However, the experimental results from high-  
speed rotary shear tests conducted by Hu et al. (2020) indicate that the hypermobility of fragmenting granular flows is not  
directly induced by grain fragmentation but may be invoked by the “after-fragmentation” effects (e.g., a fractal grain-size  
distribution).

90 As mentioned above, many core issues of fragmentation dynamics and related fragmentation effects are still controversial  
and unsolved (Davies and McSaveney, 2009; Haug et al., 2016). For example, how does the elastic strain energy related to  
fragmentation transform during the propagation of rock mass, and what are the effects on surrounding rock mass? Do the  
runout-enhancing effects of elastic strain energy release via fragmentation offset and even surpass the runout-hindering  
effects of energy consumption caused by fragmentation? To further understand these questions, studies on the energy  
95 conversion process of rock avalanches caused by rock fragmentation and its effects on the fragmenting block system are  
conducted here. In this study, we reproduce the fragmenting process of a sliding rock mass with different joint sets using a  
discrete element method (DEM) model, aiming to investigate the microscopic energy conversion process caused by dynamic  
fragmentation. After that, the dynamic fragmentation effects in real rock avalanches are discussed based on the numerical




simulation results. Around these contents, section 2 provides details about the DEM setup. In section 3, the results derived  
100 from numerical simulations are presented. Section 4 is mainly focused on the discussion of the implications of the results for  
the fragmentation effects in natural rock avalanches.

## 2 DEM model setup

Previous studies have proven that DEM models can successfully simulate the dynamic behavior of dry granular flows  
(Silbert et al., 2001; Bi et al., 2005; Morgan and McGovern, 2005; Utili et al., 2015; Kermani et al., 2015; Lai et al., 2017),  
105 crack nucleation and propagation of rock blocks under different loading rates (Yoon 2007; Wang and Tonon, 2011; Shen et  
al., 2017; Ma et al., 2018) and the fragmentation process of rock avalanches (Thompson et al., 2010; Lo et al., 2011; Li et al.,  
2012; Deng et al., 2016; Zhao and Crosta, 2018). Therefore, the commercial DEM software particle flow code in two  
dimensions (PFC2D) is employed to run all of the simulations discussed here (Cundall, 1971; Cundall and Strack, 1979).

In PFC2D, the basic element is a disc, and granular material is simulated as an assembly of discs. The behavior of a granular  
110 flow is determined by the motion and interaction of disc aggregates. In general, rock blocks are modeled as cemented tightly  
packed discs via a linear parallel bond model (PBM), presenting brittle fracture characteristics as the bonds instantly break  
and disappear once the force acting on the bond reaches the failure criterion (Potyondy and Cundall, 2004). After the bond  
breaks, the interaction between dispersed particles is replaced by a linear model, in which the motions of particles and blocks  
are controlled by Newton's second law of motion. Therefore, dynamic fragmentation can be well simulated by this bonded-  
115 particle model (Zhao et al., 2017, 2018). Only the elastic strain energy carried by the bond vanishes after macrocracks  
develop during fragmentation in the rock mass; meanwhile, the remaining elastic strain energy stored in unbroken bonds and  
the overlap deformation of particles will still transform, accumulate and release. This process provides exceptional  
opportunities to observe and analyze the conversion of elastic strain energy during the fracture and fragmentation process in  
the transport of brittle materials during the movement of fragmentable blocks (Potyondy and Cundall, 2004; Timar et al.,  
120 2012; Shen et al., 2017).

A schematic view of the model configuration is shown in Fig. 1. As exhibited in Fig. 1, the traveling path of a rectangular  
rock block is mainly composed of an inclined slope and a horizontal plane. An arc connection path with a radius of 0.1 m is  
added between two planes. Joints with different strengths and numbers are predesigned in the rock blocks. Instead of trying  
to replicate the complicated fragmentation processes that occur in real rock avalanches, the aims of this simplified  
125 configuration are to provide an opportunity to investigate the detailed microprocesses of fragmentation and the effects of  
pre-existing joints on a sliding-fragmenting rock mass system. The inset table in Fig. 1 gives the forms and parameters of  
predesigned joints. With the design of pre-existing weak joints in the rock block, the rock block will break mainly along the  
weak joint planes at the initial stage of fragmentation during motion (we define the intact block as cut by joints into  
subblock ). The energy conversion of the block system and the variation in the motion of subblocks can be clearly recorded  
130 and analyzed. The blocks with joints of no tensile strength (T1, T4) aim to represent the separation process of blocks that



have been fractured, while the blocks that have joints with tensile strength are intended to simulate the blocks that crack along joints and then separate. This point is very important for the following description of the DEM setup, the results and discussion. Note that the fracturing of a rock block along specific directions or weak planes does not change the nature of rock fragmentation.

135 Choosing the microparameters of the linear parallel bond model here is based on the numerical procedure applied in  
Potyondy and Cundall (2004), in which the macroproperties of Lac Du Bonnet granite (Martin, 1993) are used. Uniaxial  
compressive tests and uniaxial tensile tests are employed to calibrate the microparameters in the simulation. The input values  
of microscopic parameters in the DEM model are selected by trial and error to ensure that the mechanical characteristics of  
the granite block in the simulation match those of the real Lac Du Bonnet granite. Table 1 shows the input microparameter  
140 values of the DEM model. The uniaxial compressive strength, Young's modulus, Poisson's ratio and tensile strength of the  
rock block in the simulation are 200.4 MPa, 67.6 GPa, 0.259 and 40.97 MPa, respectively. These microparameters in the  
DEM model match well with the mechanical properties of a natural granite block (Martin, 1993), which has a relatively high  
tensile strength. For 2D DEM simulations, which differ from the traditional plane strain or plane stress situation, there are no  
direct laboratory experimental results that can be used for the calibration of damping values. Based on our previous 3D DEM  
145 simulation and other similar simulations (Giani et al. 2004; Lo et al., 2014; Murugaratnam et al. 2015; Lin et al., 2020a), the  
local, normal, and shear viscous damping terms are set to 0.06, 0.36, and 0.11, respectively. Note that viscous damping  
affects only the efficiency of energy dissipation and the runout distance of sliding blocks (Johnson et al., 2016); the  
dynamics of the block system and the fragmentation mechanism of the rock block are not changed. Each simulation shows a  
typical rock fracture and deposition process, which validates the applicability of these microparameters for the DEM model.  
150 For the traveling path, the inclined plane is a frictionless rigid wall with a slope angle of 30 °, while the friction angle of the  
arc and horizontal planes is 30 ° to dissipate kinetic energy. Similar to Zhao et al. (2017, 2018) and Bowman et al. (2012), the  
size of the rock block is 94 mm × 45 mm. The drop height ( $H$ ) is 0.12 m. The gravitational acceleration ( $g'$ ) is enhanced to  
1962 m/s<sup>2</sup> (200  $g$ ) to mimic the real stress field. For the predesigned joints shown in Fig. 1, T1, T2 and T3 represent a rock  
block with one joint, which varies in the tensile strength of the joint. T4, T5 and T6 represent a rock block with two joints  
and vary in the tensile strength of the joints. These joints equally divide the entire block. The tensile strengths of the joints ( $\sigma$ )  
155 are 0 MPa (T1 and T4), 4.39 MPa (T2 and T5) and 8.61 MPa (T3 and T6). The joints with different tensile strengths are  
defined by reducing the bond cohesion within the joint plane, while the joint planes have a width of 1.5 mm (3 times the  
mean size of particles) and a length of 45 mm (the same as the block's height). The joints with no tensile strength are simply  
defined by debonding the particles within the joint plane. Meanwhile, the block strength is unchanged (200.4 MPa) for all  
160 simulation conditions. Table A.1 in the appendix shows the main variables used in this study.



### 3 Results

#### 3.1 Fracture and fragmentation of rock block



In this section, the processes of fractures along pre-existing joints and fragmentations of sliding masses are examined. Considering that all of the tests experience a similar process, only the evolutions of T1 and T3 are presented in Fig. 2 and described in detail in this section. For the T1 sample, local fragmentation ( $S_{1T1}$ ) first occurred at the frontal bottom as it reached the arc segment of the travel path (Fig. 2a). After that, further local fragmentation occurs at the same part of the block due to impact. Soon, fracture along the pre-existing joint began to occur, which is called the separating stage ( $S_{2T1}$ ). In this stage, the joint fractures from the bottom to the top surface of the block with time. As the joint was fractured completely, the front subblock was pushed forward by the rear subblock, and local fragmentation occurred at the middle top surface ( $S_{3T1}$ ). Finally, both of the subblocks moved and deposited along the horizontal plane with different degrees of further fragmentation. For T3 characterized by higher tensile strength, similar processes of fragmentation and separation were also observed (Fig. 2b). Similar to T1, T3 also showed local fragmentation at the frontal bottom of the block as it slid onto the arc path ( $S_{1T3}$ ). Subsequently, more intensive local fragmentation occurred ( $S_{2T3}$ ). After a while fracture along the pre-existing joint finally occurred, which is called the cracking stage ( $S_{3T3}$ ).

$S_{2T1}$ , the separating stage, represents two tightly packaged rock blocks disintegrating and separating along a specific orientation, which may be any type of discontinuity (rock blocks do not fragment but separate).  $S_{3T3}$ , the cracking stage, represents the rock block experiencing dynamic cracking and “fragmentation” along a specific orientation (rock blocks fragment and separate). These two stages are directly compared to examine the dynamic fragmentation effect of rock blocks on the mesoscale and the rock fragment system dynamics in the following. Note that the travel distance of the center of mass for T1 is slightly shorter than that for T3.

To determine the exact times when these fragmentation processes occur, especially the times when the blocks separated along the joints, six monitoring particles near the joint were selected to record their velocity variations. The monitoring particles are symmetrically distributed along both sides of the joint and equally spaced in the vertical direction, as shown in the inset picture in Fig. 3a. The distance between the joint and monitoring particles is approximately twice the mean size of the particles. Following Zhao et al. (2017), nondimensional parameters were employed. The sliding time ( $t$ ) is normalized by  $(2H/g')^{1/2}$ , and the normalized particle velocity ( $V'_p$ ) is defined as  $V'_p = V_p / (2g'H)^{1/2}$ . The velocity variations of the monitoring particles in T1 and T3 are plotted in Fig. 3a and 3b, respectively. To highlight the fracture effect along the joint, only the stage when the block reached and traveled on the arc path was plotted ( $t' = 1.443 \sim 1.808$  s). In general, the velocity curves may continuously fluctuate due to the interaction between the rock block and sliding path, which leads to stress wave propagation and a tiny velocity difference inside the block (Zhao et al., 2017), as shown in Fig. 3. At the very beginning, the velocity of all monitoring particles is the same. When the rock block reached the arc section of the path, the velocities of the monitored particles at different positions began to diverge. The first local fragmentation time ( $S_{1T1}$ ) corresponds to the time when vigorous fluctuations in the velocities of all monitoring particles appeared, i.e.,  $t' = 1.527$  s.  $S_{2T1}$  is the time when the





195 velocities of the P3 and P6 particles bifurcated, i.e.,  $t'=1.585$  s. Then, the joint fell into the transient fracturing stage (with a duration time of 0.00257 s) and completely fractured at  $t'=1.587$  s. After  $t'=1.617$  s, the three monitored particles in the front subblock maintained their velocity differences and continued to move, while the velocities of the three particles in the rear subblock gradually converged. With time passed by, further fragmentation, i.e.,  $S_{3T1}$ , occurs at  $t'=1.750$  s, at which the velocities of the monitored particles abruptly fluctuated once again. Fig. 3b shows the velocity variations of the monitored particles of T3. As revealed in Fig. 3b, two velocity variations at  $t'=1.519$  and 1.589 s of the monitored particles were recorded, which correspond to the  $S_{1T3}$  and  $S_{2T3}$  local fragmentation stages. After that, velocity separation of P3 and P6  
200 particles was observed at  $t'=1.627$  s, i.e., the  $S_{3T3}$  stage, which is similar to  $S_{2T1}$ . The duration time of the fracturing stage in  $S_{3T3}$  (0.00154) is significantly shorter than that of T1.

The velocity increases of P5 and P6 at  $S_{3T3}$  are larger and more transient than those at  $S_{2T1}$  at the cracking stage. The velocities of P1 and P3 at  $S_{3T3}$  experience energetic increases and decreases at the very beginning of the cracking stage,  
205 which does not occur for  $S_{2T1}$ . As revealed by Fig. 3, the microvelocity variation between the block separating stage ( $S_{2T1}$ ) and block cracking stage ( $S_{3T3}$ ) has different characteristics, which may indicate different microkinetics and energy conversion styles between block interaction/collision and the dynamic fragmentation of rock mass (which will be discussed in the following section).

The velocity variations in the monitoring particles show a certain difference between the separating ( $S_{2T1}$ ) and cracking ( $S_{3T3}$ )  
210 stages of the block. To quantify the influences of the microscopic differences in the separating and cracking processes on the movement of the block system, the mean horizontal velocities ( $V_b$ ) of the entire block and rear and front subblocks were calculated.  $V_b$  is defined as

$$V_b = \frac{\sum_i^n v_{x,i} m_i}{\sum_i^n m_i} \quad (1)$$

where  $n$  is the total number of particles in the calculated region and  $v_{x,i}$  and  $m_i$  are the horizontal velocity and mass of  
215 particle  $i$ , respectively. Here,  $V_b$  is normalized as  $V'_b = V_b / (2g'H)^{1/2}$  for analysis. Fig. 4a plots the normalized mean horizontal velocities ( $V'_b$ ) of T1 and T3 versus time. Corresponding to Fig. 2, the times when different local fragmentation and joint separations of blocks occurred, i.e.,  $S_{1T1}$ ,  $S_{2T1}$ ,  $S_{3T1}$ ,  $S_{1T3}$ ,  $S_{2T3}$  and  $S_{3T3}$ , are also marked in Fig. 4a. From Fig. 4a, it can be reached that the obvious fluctuation times of  $V'_b$  also appear at that marked time, which matches well with the times when the velocities of the monitored particles abruptly change (Fig. 3). At the local fragmentation stages ( $S_{1T1}$ ,  $S_{1T3}$ ,  $S_{2T3}$ ),  $V'_b$  of  
220 the front subblock increased rapidly when collision occurred, while  $V'_b$  of the rear subblock first presented a rapid decrease and then recovered in a short time. Additionally, it was observed that  $V'_b$  of the T3 rear subblock recovered to a higher level than before after a rapid decrease at  $S_{1T3}$  and  $S_{2T3}$ .  $V'_b$  of the T1 rear subblock only recovers to the precollision value after a rapid decrease at  $S_{1T1}$ . Meanwhile,  $V'_b$  of the T3 entire block increased significantly at the local fragmentation stages (i.e.,  $S_{1T3}$  and  $S_{2T3}$ ), while that of T1 only presented a minor increase at its local fragmentation stage  $S_{1T1}$ . This contrast may be  
225 due to the local fragmentation at the frontal bottom of the front subblock causing the horizontal ejection of some fragments that gain high velocity from strain energy release (Fig. 2).



At the separating stage ( $S_{2T1}$ ),  $V'_b$  of the T1 front subblock rapidly increases, while  $V'_b$  of the rear subblock inversely decreases. The  $V'_b$  of the T1 entire block first experienced a slight decrease, and then part of the lost velocity recovered in a short time. Similar to  $S_{2T1}$ ,  $V'_b$  of the T3 front subblock and rear subblock experienced the same increasing and decreasing phases at the cracking stage ( $S_{3T3}$ ), respectively. However, the increase in  $V'_b$  of the T3 front subblock is more energetic than that of the T1 front subblock at this stage. Moreover, as illustrated in Fig. 4a, the  $V'_b$  of the T3 entire block shows a slight increase at  $S_{3T3}$ , which is different from that of the T1 entire block at  $S_{2T1}$ . Particularly, in  $S_{3T1}$ ,  $V'_b$  of the entire block and rear and front subblocks all decrease when the two subblocks collide at the middle top point, and then,  $V'_b$  of the T1 entire block recovers to the value before collision or slightly higher than before. Notably, the  $V'_b$  values of T3 are generally higher than those of T1 after the blocks slide onto the arc path (1.48 s-1.78 s).

To analyze the energy variations in the fragmentation process, the kinetic energy of the entire block, the rear subblock and the front subblock in both T1 and T3 are calculated. Here, the kinetic energy of the block is calculated as

$$E = \sum_i^n \frac{1}{2} m_i (v_{x,i}^2 + v_{y,i}^2) \quad (2)$$

where  $n$  is the total number of particles in the calculated region;  $v_{x,i}$  and  $v_{y,i}$  are the horizontal and vertical velocities of particle  $i$ , respectively; and  $m_i$  is the mass of particle  $i$ . Fig. 4b shows the variations in the normalized kinetic energies ( $E'=E/mg'H$ ) of T1 and T3 versus travel time. It should be noted that only  $E'/2$  of the entire block (half-value of the normalized kinetic energy of the entire block) is plotted in Fig. 4 for better observation.

Similar to the variations in the mean horizontal velocity for the rock block (Fig. 4a), in the local fragmentation stages of T1 and T3 ( $S_{1T1}$ ,  $S_{1T3}$ ,  $S_{2T3}$ ), the kinetic energy of the rear subblock significantly decreases, while that of the front subblock obviously increases. Corresponding to such variation, ejection of small fragments at the frontal bottom part of the block after impact was observed, as shown in Fig. 2. Meanwhile, this local fragmentation caused by impact is accompanied by a sudden decrease in the total kinetic energy of the entire block, which indicates that the impact-fragmentation process consumes energy. However, although  $E'$  of the T3 entire block shows a decreasing trend at the local fragmentation stage, the mean horizontal velocity ( $V'_b$ ) of the T3 entire block presents an increasing trend at this stage, as described above (Fig. 4a). Thus, this increase in the mean velocity of the T3 entire block may be derived from energy conversion due to greater vertical velocity loss.

At the separating stage,  $S_{2T1}$ , the kinetic energies of the entire block, rear subblock and front subblock all suddenly decrease, while  $E'$  of the front block rapidly recovers and increases after the sudden decrease. The variation in  $E'$  of T3 shows different characteristics at  $S_{3T3}$ , with  $E'$  of the T3 front subblock increasing more than that of T1. More interestingly,  $E'$  of the entire block for T3 quickly rebounds after a transient slight decrease. The magnitudes of the variations in  $E'$  for the rear and front subblocks of T3 at  $S_{3T3}$  are much larger than those at  $S_{2T1}$ .

Moreover, after the separation of subblocks for T1, the rear subblock impacts and pushes the front block at the middle top part ( $S_{3T1}$ ). At  $S_{3T1}$ ,  $E'$  of the T1 entire block and the rear and front subblocks all decrease. After this point,  $E'$  of the T1 front subblock gradually recovers, but  $E'$  of the T1 entire block and rear subblock continuously decrease. This phenomenon





260 illustrates a typical collision-induced momentum transfer process (Heim, 1932; Van Gassen & Cruden, 1990; Miao et al., 2001).

### 3.2 Energy variation

At the local fragmentation stage ( $S_{1T1}$ ,  $S_{1T3}$ ,  $S_{2T3}$ ), one can clearly see an increasing trend of velocity and kinetic energy for the front part of the block mass and an opposite trend for the rear part of the block mass. More importantly, the variations in the block velocity and the kinetic energy of the entire block are very different between  $S_{2T1}$  and  $S_{3T3}$ . In this section, the effects of joint fracturing and block fragmenting on the redistribution of energy are quantified. For this analysis, the mean horizontal velocity before and after subblock separation in each test ( $v_{be}$  and  $v_{af}$ ) is calculated; then, the incremental ratio in the separation stage of each test is calculated ( $\varphi_v = (v_{af} - v_{be}) / v_{be}$ ).  $\varphi_v$  of the entire block, and rear and front subblocks in the tests are all obtained. For the two-joint conditions (T4, T5 and T6) (Fig. 1, insert table), subblocks usually separate along the

270 frontal joint first. Then, separation along the other joint will occur that is accompanied by concomitant impacting, fragmenting, rolling and sliding of fragments, resulting in very complicated monitoring curves. Thus, only the velocity incremental ratio of the front joint separation under such conditions is presented and analyzed here. The same method is used to calculate their block kinetic energy incremental ratios ( $\varphi_e = (E_{af} - E_{be}) / E_{be}$ , where  $E_{be}$  and  $E_{af}$  are the kinetic energies of the rock block before and after joint separation). Fig. 5 is the calculated results of  $\varphi_v$  and  $\varphi_e$ .

275 From Fig. 5, it can be observed that the  $\varphi_v$  and  $\varphi_e$  values of the rear subblock in each test are all less than 0, indicating that the rear subblock lost its horizontal velocity and kinetic energy in the joint fracturing stage. For the tests with the same joint set,  $\varphi_v$  and  $\varphi_e$  of their entire blocks show increasing trends versus joint strength. For  $\varphi_v$  under different joint sets, both of them increase from nearly 0 to higher values, and the increased rate of the tests with both joint sets is higher than that characterized by one joint set. Different from  $\varphi_v$ ,  $\varphi_e$  of the entire blocks under both joint set conditions are all negative values, and both display increasing trends versus joint strength with their values tending to 0, while  $\varphi_v$  increases to a positive value and  $\varphi_e$  gradually approaches 0 when the joint has strength.  $\varphi_v$  of the front subblocks in both joint sets present increasing trends versus increasing joint strength with all values positive. The highest incremental ratio of  $\varphi_v$  reaches 15%.  $\varphi_e$  of the front subblocks also show increasing trends versus joint strength, with the highest incremental percentage exceeding 15%. Different from the regular increasing variations of  $\varphi_v$  and  $\varphi_e$  of the entire block and front subblock, those of the rear

285 subblocks present a different feature versus joint strength, which is composed of an increasing part and a following decreasing trend.

According to the curves shown in Fig. 5b, the relationship between the kinetic energy incremental ratio ( $\varphi_e$ ) of the front subblock and the tensile strength of the joints ( $\sigma$ , which represents the general strength of rock mass) can be described by a linear fitting function:

$$290 \begin{cases} \varphi_e' = 0.022\sigma - 0.037 & (T1, T2, T3) & R^2 = 0.980 \\ \varphi_e'' = 0.012\sigma + 0.057 & (T4, T5, T6) & R^2 = 0.998 \end{cases} \quad (3)$$



The linear fitting function (3) shows that the energy of the front subblock is greatly enhanced after joint fracturing (which represents the cracking process or the simplest fragmentation process) as the rock mass strength increases. Note that the linear fitting function (equation 3) is only presented here to describe the increasing trend of  $\varphi_e$  with rock strength but is not enough to be considered as a real relationship between  $\varphi_e$  and  $\sigma$  because of insufficient data points.

### 295 3.3 Deposit characteristics

Fig. 6 presents the final deposit features of all simulated conditions. The yellow line represents the distal travel distance of each test. As exhibited in Fig. 6, the travel distance of the simulated conditions with one joint set presents an increasing trend versus joint strength. The higher the joint strength is, the higher the fragmentation degree of the propagated rock mass. Different laws were revealed for the tests with both joint sets designed. For the tests with both joint sets designed (i.e., T4, T5, and T6), their fragmentation degrees are more intensive compared with the tests with one joint designed (i.e., T1, T2, and T3). However, as the joint strength increases, their travel distance presents a decreasing trend. Their fragmentation presents an increasing trend first and then falls into a decreasing trend. Furthermore, the fragmentation degrees of the frontal subblocks are obviously higher than that of the rear subblock for all tests. The deposits of all tests show good preservation of their initial rock mass sequence, which has also been reported in many natural rock avalanches.

## 305 4 Discussion

### 4.1 Elastic strain energy conversion caused by fragmentation



#### 4.1.1 Variation in elastic strain energy during fragmentation

Here, the energy conversion and transformation of the sliding mass during the joint fracturing period are discussed. McSaveney and Davies (2006) indicated that the remaining strain energy stored in fragmented rock pieces after cracking may convert to kinetic energy, which allows fragments to fly outward during dynamic fragmentation in avalanching. Over a long period of time, few direct experiments or numerical simulations illustrate this energy variation related to the fragmenting rock mass movement process (Haug et al., 2016; Zhao et al., 2017). In this study, conversion of the elastic strain energy during rock mass fragmentation and sliding was observed. In the linear parallel bond model, both the linear and bond springs can bear stress and generate elastic strain when acted on by a force, although part of the energy may be consumed by dashpots (Potyondy & Cundall, 2004). Thus, the strain energies carried by both the linear ( $E_s$ ) and bond ( $E_{bs}$ ) springs were calculated with the total strain energy ( $E_{ts} = E_s + E_{bs}$ ) being obtained by PFC2D. The elastic strain energy variations of T1 and T3 versus time are shown in Fig. 7a, which are normalized by the maximum total strain energy ( $E_{ts-max}$ ) for better comparison. As shown in Fig. 7a,  $E_{bs}$  is larger than  $E_s$  most of the time, indicating that the parallel bonds carry more strain energy than linear springs between discs when pressuring. Clearly, it is difficult to distinguish the deformation partitioning between minerals (discs) and substrates (bonds) in a rock block. Thus, this energy distribution between linear springs and parallel



bonds is controlled by the contact model that we selected and the microparameters that we used and cannot be compared with that of real rock. The variation in these two strain energy components is synchronized. Compared with Fig. 3 and Fig. 4, one can find that the time of the peak values of the total strain energy is consistent with the time when abrupt fluctuations of the particle velocity, block velocity and kinetic energy occurred. In addition, the value of the elastic strain energy in the cracking stage of T3 ( $S_{3T3}$ ) is greatly larger than that in the cracking stage of T1 ( $S_{2T1}$ ), indicating that the rock block accumulated more strain energy before fracture.

Fig. 7b shows the variation in energy dissipation during the rock mass movements of T1 and T3. Energy dissipation is composed of energy dissipated by frictional slip ( $E_{\mu}$ , slip energy) and energy dissipated by dashpots ( $E_{\beta}$ , dashpot energy represents the energy loss by the collision of discs). The total dissipated energy ( $E_{td}=E_{\mu}+E_{\beta}$ ) was also calculated. The dissipated energy is simply normalized by the maximum value of the total energy value ( $E_{td-max}$ ) during the joint fracturing stage. Fig. 7b also shows the variation of the bond breakage numbers of T1 and T3 versus time, which were normalized by the total number of broken bonds. As exhibited in Fig. 7b, the development of the bond breakage number and the trend of dissipated energy are synchronized, which is also consistent with the variations of the strain energy shown in Fig. 7a. In general, the dashpot energy is larger than the slip energy. Both of them increase with time. The total energy dissipation of T1 is always larger than that of T3. Additionally, the bond breakage number of T1 is greater than that of T3 at the very beginning of movement, which is attributed to the initial debonded joint of T1. Combined with the variations in the kinetic energy shown in Fig. 4, the energy conversion of the sliding mass in cracking time ( $S_{3T3}$ ) can be deduced. First, when the rock block slides along the arc path and interacts with the path surface, part of the kinetic energy is transformed into elastic strain energy stored in bonds and linear springs. Second, once the impact force is greater than the bond strength in local positions, the bond breaks, and the elastic strain energy stored in the broken bond vanishes. As the number of broken bonds increases, a crack forms. During this period, the bond breakage number increases. Third, as the crack continues to develop and the block rebounds, the impact force gradually decreases. At the same time, the remainder of the strain energy stored in the entire block is released, which eventually converts to the kinetic energy of fragments. As indicated by Fig. 7, the cracking process along the joint ( $S_{3T3}$ , the simplest fragmentation) does not consume much energy, while the energy consumption of the local fragmentation ( $S_{1T1}$ ,  $S_{3T1}$ ,  $S_{1T3}$  and  $S_{3T3}$ ) and the separation of the no-strength joint ( $S_{2T1}$ ) consume more energy.

#### 4.1.2 Energy transfer caused by fragmentation

As described above, in T1, we set a joint without tensile strength. With this design, the motion and separation process of two closely packed blocks was simulated and reproduced. During the separation stage (i.e., from  $S_{2T1}$  to  $S_{3T1}$ ), the front subblock of T1 gains horizontal velocity ( $\uparrow 3.72\%$ ), with the rear subblock losing part of its horizontal velocity ( $\downarrow 5.30\%$ ), as shown in Fig. 4a. Meanwhile, the kinetic energy of the front subblock increases after a sharp decrease during separation ( $\uparrow 4.47\%$ ), while that of the rear subblock shows a continuous decrease ( $\downarrow 4.17\%$ ), as illustrated in Fig. 4b. This is a typical momentum transfer phenomenon caused by continued collisions between the rear and front subblocks, which is very common in



granular flows (Heim, 1932; Manzella & Labiouse, 2009; Lai et al., 2017). Considering that the tensile strength of the joint  
355 in T1 is 0, collisions are the interaction form between the front and rear subblocks during the joint fracturing process. Hence,  
we describe this phenomenon as collision-induced energy transfer.

Different from T1, a joint with tensile strength is designed in T3 with the fracturing process of a rock block along a weak  
joint being simulated. As revealed in Fig. 4, the front subblock of T3 also presents an increase in the horizontal velocity  
( $\uparrow 12.56\%$ ) and kinetic energy ( $\uparrow 15.23\%$ ), with the rear subblock displaying a decrease ( $\downarrow 8.89\%$ ,  $\downarrow 6.30\%$ ). Considering that  
360 the tensile strength of the joint in T3 is not 0, we describe this phenomenon ( $S_{3T3}$ ) as fragmentation-induced energy transfer.  
According to Figs. 4, 5 and 7, the fragmentation-induced energy transfer from the rear subblock to the front subblock in T3  
is due to the release of elastic strain energy and its conversion to kinetic energy, which is also inferred in the literature  
(Zhang et al., 2000; Li et al., 2005; Davies & McSaveney, 2009; De Blasio & Crosta, 2015). Through a comparison of the  
kinetic energy evolutions of the entire blocks in T1 and T3 (Fig. 4b), it is reached that fragmentation-induced energy transfer  
365 can clearly lead to a greater kinetic energy ( $E'$ ) increase in the frontal subblock and less energy lost in the entire blocks  
( $\downarrow 0.07\%$ ) than collision-induced energy transfer (with 10.76% energy lost of entire block) (Fig. 7b). Since the efficiency of  
fragmentation-induced energy transfer is higher than that of collision-induced energy transfer and fragmentation is also a  
pervasive phenomenon in natural rock avalanches, we suggest that dynamic fragmentation may play a more efficient runout-  
enhanced role in the spreading of rock masses than particle interactions within unbreakable granular flow during the  
370 emplacement processes of rock avalanches. Field investigations show that many rock avalanches with high degrees of  
fragmentation have unpredicted thin deposits (Crosta et al., 2017; Wang et al., 2018b, 2018c), which may be related to  
fragmentation-induced energy transfer, as indicated by the results.

However, as shown in Fig. 6, the travel distance of the fragmenting rock block shows an increasing trend with joint strength  
for one joint set situation, while there are no clues that relate the deposit characteristics to the joint strength and energy  
375 boosting of frontal rock fragments for two joint situations. In our opinion, the travel distance of the sliding mass with both  
joint sets in the DEM simulation is a more complex process, which is controlled by the interaction of the fragment system  
and the contact model used in the simulation. As stated by Lin et al. (2020a), although the linear parallel bond model used in  
DEM can successfully simulate the fracture process of sliding mass and interaction of granular flow, it is unable to  
accurately replicate the energy dissipation of complex fragmenting flow. Zhao et al. (2017, 2018) also reported such results  
380 in their similar DEM simulation. In their simulation results, the relationship between the degree of fragmentation and travel  
distance of fragmenting rock mass movements is inverse with the relationship of the previous experimental results (Bowman  
et al., 2012; Haug et al., 2016). Thus, the fragmentation effects may fade away with the increasing complexity of the  
fragmenting rock mass movement system (from one joint system to two joint systems) in DEM simulations.

#### 4.2 Cross-scale effects caused by rock fragmentation

385 With the design of joints characterized by different strengths and numbers, a simplified fragmentation process of rock  
masses was simulated in this study, which provides insights into the contribution of fragmentation in rock mass propagation.



Although the simplified study cannot reproduce the real fragmentation process of natural rock avalanches, some of the results can still provide insights into rock avalanche propagation. Therefore, a primary discussion on the cross-scale effects caused by rock fragmentation based on the simulated results and natural rock avalanches is conducted in the following, hoping to provide insights into the fragmenting emplacement process of natural cases.

With this study, the elastic strain energy release caused by fragmentation is primarily indicated. Energy conveying between the front and rear subblocks caused by the fragmentation process was reached, which promoted the forward movement of the front subblock and hindered the movement of the rear subblock (Fig. 4 and Fig. 5). Such energy conversion and transfer effects caused by fragmentation have also been discussed in previous studies (Zhang et al., 2000; Lin et al., 2020b; Haug et al., 2016; Bowman et al., 2012). As shown in Fig. 8a and 8b, rock blocks at the surface of a sliding rock mass (carapace facies) may experience this kind of dynamic fragmentation (thus, fragments after block fragmentation carry much kinetic energy).

Generally, normal stress- and shear stress-induced fragmentation processes are concentrated under the carapace facies in natural rock avalanches (Estep & Dufek, 2013; De Blasio & Crosta, 2015; Zhang & McSaveney, 2017). For dense granular flow (e.g., rock avalanches), force chains commonly occur. Grains in the force chain experience a higher stress than surrounding grains (Fig. 8c); thus, they break first when the stress in the force chain is equal to the failure strength of a grain. The entire conversion and transfer process of one rock block observed in our simulation may also reproduce as one episode of rock dynamic fragmentation in this force chain for real rock avalanches (Fig. 8c). Note that for a force chain, the strain rate, confining pressure and fracture form do not change the nature of energy conversion during the fragmentation of the rock block (Ghaffari et al., 2019). However, the occurrence of confined pressure in a force chain may alter the elastic strain energy releasing mode. Based on our simulation results, the broken fragments spread out with some kinetic energy when there is no confined pressure, as mentioned above (Fig. 8b) (Zhang et al., 2000; Davies & McSaveney, 2009), causing the transformation of part of the elastic strain energy to the kinetic energy of fragments (energy transfer effects caused by fragmentation). However, since the grains in the force chains of natural rock avalanches are closely packed under high confined pressure, there is not enough space for the elastic strain energy stored inside the broken grains to be released in the form of the kinetic energy of fragments. For this reason, the strain energy is released in the form of outward elastic stress pressure, which is also called an elastic body wave by Davies et al. (2019b) (in Fig. 8d). Thus, the energy transfer effects caused by rock dynamic fragmentation indicated by our simulations will still occur by means of outward elastic body waves in a natural rock avalanche, which eventually affects the movement of the avalanche. Based on the physics of elastic stress wave propagation, there are three effects caused by elastic stress waves released from rock fragmentation for an entire rock avalanche:

(1) Sliding preferentially occurs in the local dynamic fragmentation region of a grain in a force chain. As shown in Figs. 2 and 3, fragmented fragments separate because the elastic strain energy is released outward. In a natural rock avalanche, these outward elastic stress waves introduced by rock dynamic fragmentation can eventually cause the release of pressure carried by other force chain grains and the surroundings (stress drop after dynamic fragmentation, Fig. 8e). Then, sliding may occur



as the shear stress remains unaltered and the normal stress carried by force chains suddenly decreases (de Arcangelis et al., 2018).

(2) The propagation of elastic stress rarefaction waves superimposed on the stress field of the sliding mass causes the local normal stress to decrease and allows sliding to occur at locations where fragmentation does not occur (Fig. 8e) (Melosh, 1979; Johnson et al., 2016; Davies and McSaveney, 2016).

(3) The elastic stress wave superimposed on the stress field of the sliding mass boosts the local normal stress and allows the next fragmentation to occur at another location.

Note that all three of these effects are based on elastic stress wave fluctuations caused by fragmentation. For the entire basal layer or main body in rock avalanches, each fragmentation event may cause one elastic stress wave release according to our simulation results. Rarefaction stress wave-induced local sliding (Johnson et al., 2016) can occur within the entire sliding mass and become more concentrated near the bottom of the sliding mass (Fig. 8e). Rarefaction stress-induced local sliding is controlled by stress wave propagation and interaction, rock strength in the force chain, overburden pressure, local shear rate and so on. Therefore, the shear layer in the rock avalanche may become thicker due to the random occurrence of local sliding. Moreover, the concentration of rarefaction stress-induced local sliding in the body facies may lead to the formation of local shear bands despite the low shear rate in the main sliding mass. In contrast, rock breaks when the local superimposed stress exceeds the grain strength in the body facies (Fig. 8e); then, a jigsaw structure forms, and the main part of the strain energy is released as an elastic stress wave once again (Davies & McSaveney, 2009). The jigsaw structure may remain in the deposit due to the tightly packed rock mass during the propagation of the rock avalanche and the persistence of grain fragmentation until the rock avalanche stops.

## 440 **5 Conclusion**

The fracturing and fragmentation processes of a sliding rock block and their influences on energy transformation in the system are investigated using DEM simulations. We find that fragmentation can greatly affect the kinetic variations in different parts of the rock mass. When the joint in the middle of a rock block cracks, the front subblock gains additional kinetic energy, while the rear subblock loses part of its kinetic energy, leading to a long travel distance for the distal part (in the one-joint situation). These kinetic energy variations are due to elastic strain energy release during fracturing, which is similar to the momentum transfer process caused by collisions in a multiblock system. However, our results show that energy transfer induced by fragmentation is more efficient than that induced by collision.

The influence of rock strength on the energy transmission in the fragmented mass is also explored. The results show that the kinetic energy increase in the front subblock becomes larger with increasing strength. This variation in kinetic energy indicates that a rock mass with higher strength experiences more energetic fragmentation effects. However, no strong relationship is found between the strain energy incremental ratio and travel distance, indicating that the fragmentation effects may fade away with the increasing complexity of the fragmenting rock mass movement system.





We qualitatively examine the effects of rock dynamic fragmentation on the propagation of rock avalanches and the formation of some deposit structures. The elastic strain energy transmission process caused by fragmentation in our numerical simulations can be described as elastic body wave release based on Davies and McSaveney (2019). Then, three possible effects caused by elastic stress waves released from rock fragmentation for an entire rock avalanche are addressed.

### Data availability

The datasets supporting this research are stored open access on Zenodo (<https://doi.org/10.5281/zenodo.3729541>).

### Author contributions

All authors contributed to the data analysis, discussion and improvement of the test, which has been written mostly by QL and YW. Each author contributed to different parts, here listed: Conceptualisation: QL, QC and YW, Funding acquisition: QC and YW, Numerical simulations: YX and KD; Writing: QL and YW.

### Competing interests

The authors declare that they have no conflict of interest.

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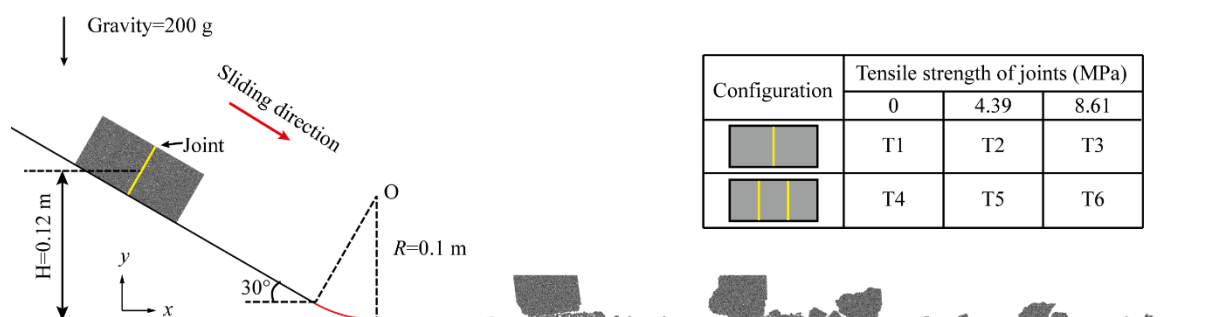


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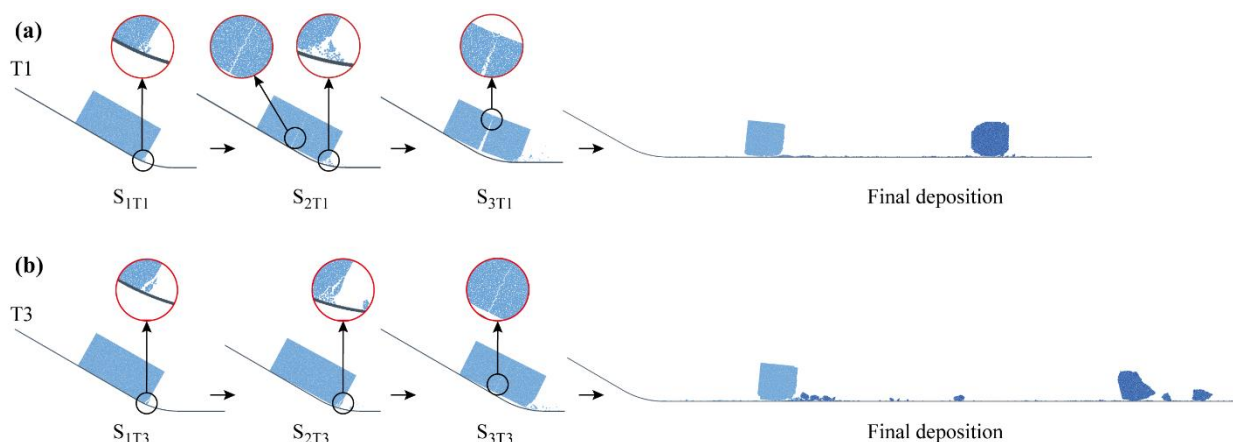




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660 **Figure 1: Schematic view of the model configuration. The detailed configurations of jointed rock blocks are shown in the inset table, and yellow lines in gray blocks represent the positions of joints. The joints with a width of 3 mm and a length of 45 mm equally divide the block.**

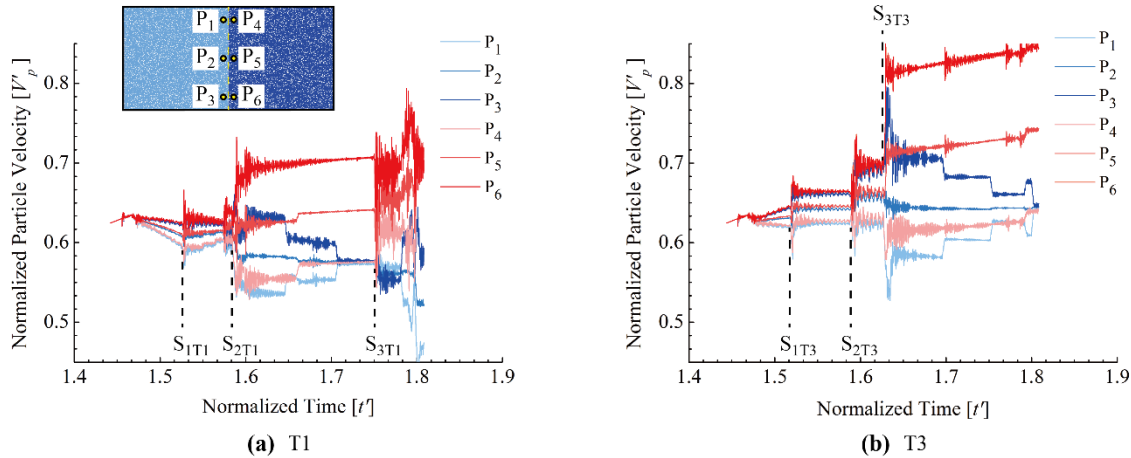


**Figure 2: (a) The evolution of T1 in the initial stage of fragmentation and its depositional characteristics. (b) The evolution of T3 in the initial stage of fragmentation and its depositional characteristics (S<sub>1T1</sub>, S<sub>2T1</sub>, S<sub>3T1</sub>, S<sub>1T3</sub>, S<sub>2T3</sub> and S<sub>3T3</sub> represent three specific**



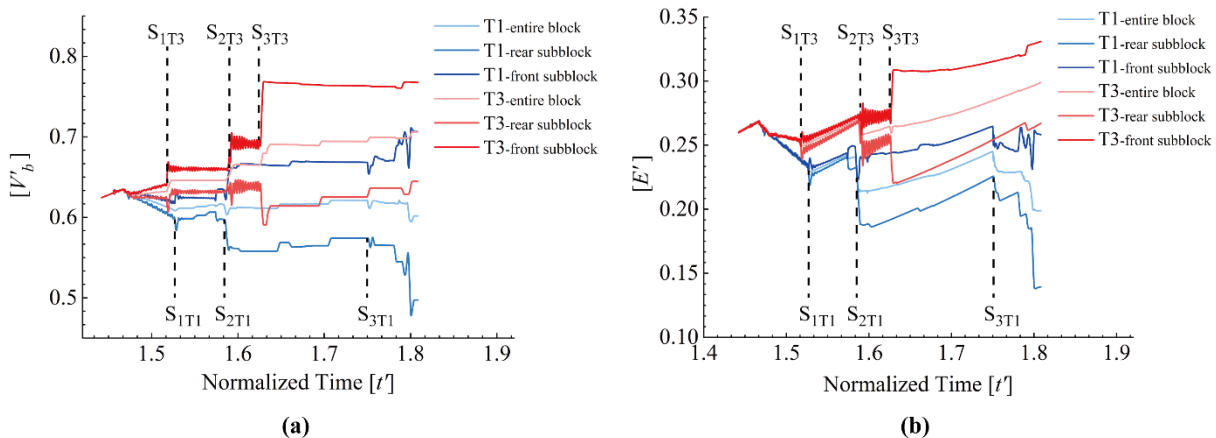
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stages/times for T1 and T3 that are described and analyzed later). The light blue subblock in the final deposition stage represents the rear part of the entire block, and the dark blue subblock represents the front part of the entire block.

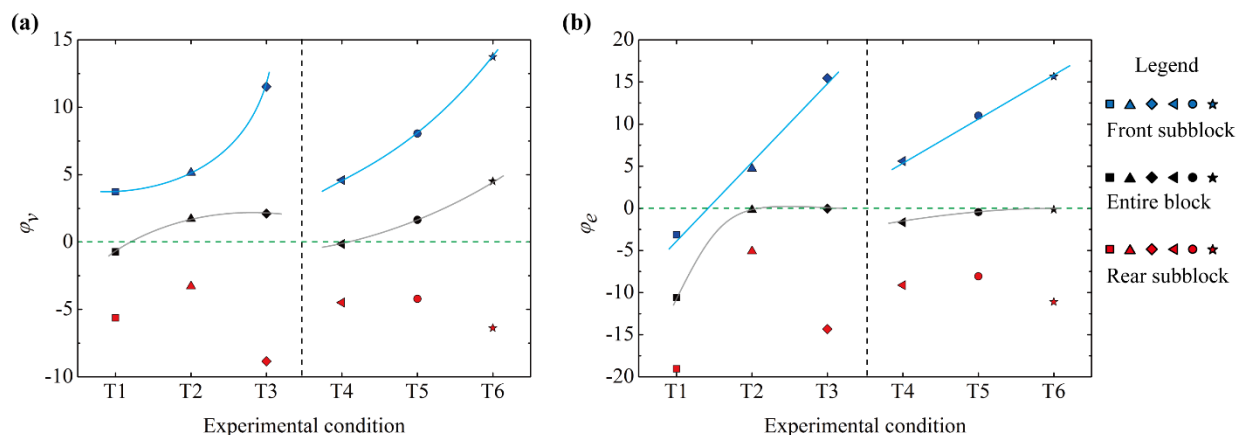


**Figure 3:** (a) Normalized particle velocities of monitoring particles in T1 versus time (inset picture shows the relative positions of the six monitoring particles;  $t' = t / (2H/g')^{1/2}$ ;  $V'_p = V / (2g'H)^{1/2}$ ). (b) Normalized particle velocities of monitoring particles in T3 versus time.

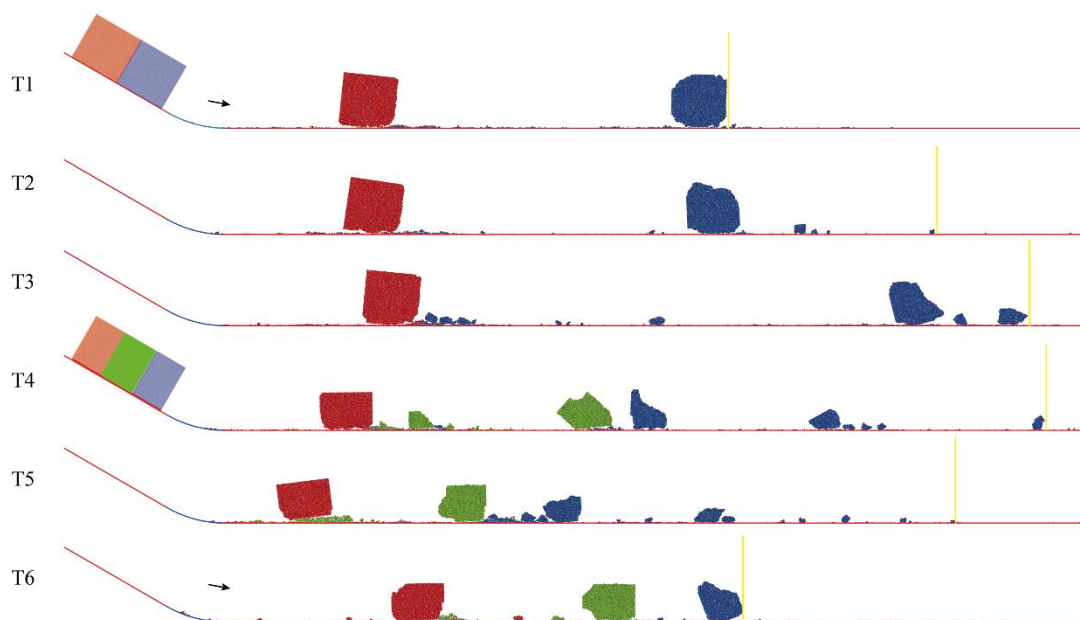
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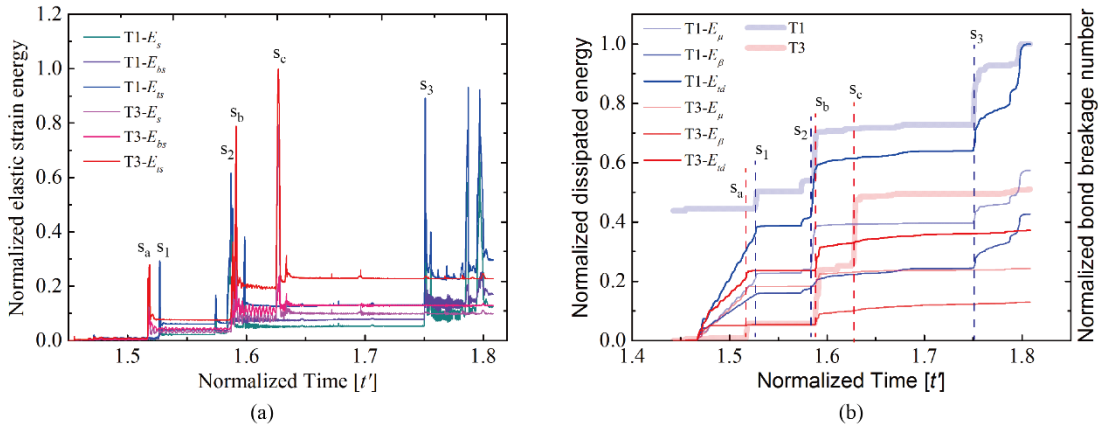
**Figure 4:** (a) The normalized horizontal velocities of blocks in T1 and T3 versus time ( $V'_b = V_b / (2g'H)^{1/2}$ ). (b) The normalized kinetic energy evolution of blocks in T1 and T3 versus time ( $E' = E / mg'H$ ). Note that  $E'/2$  of the entire block is plotted.



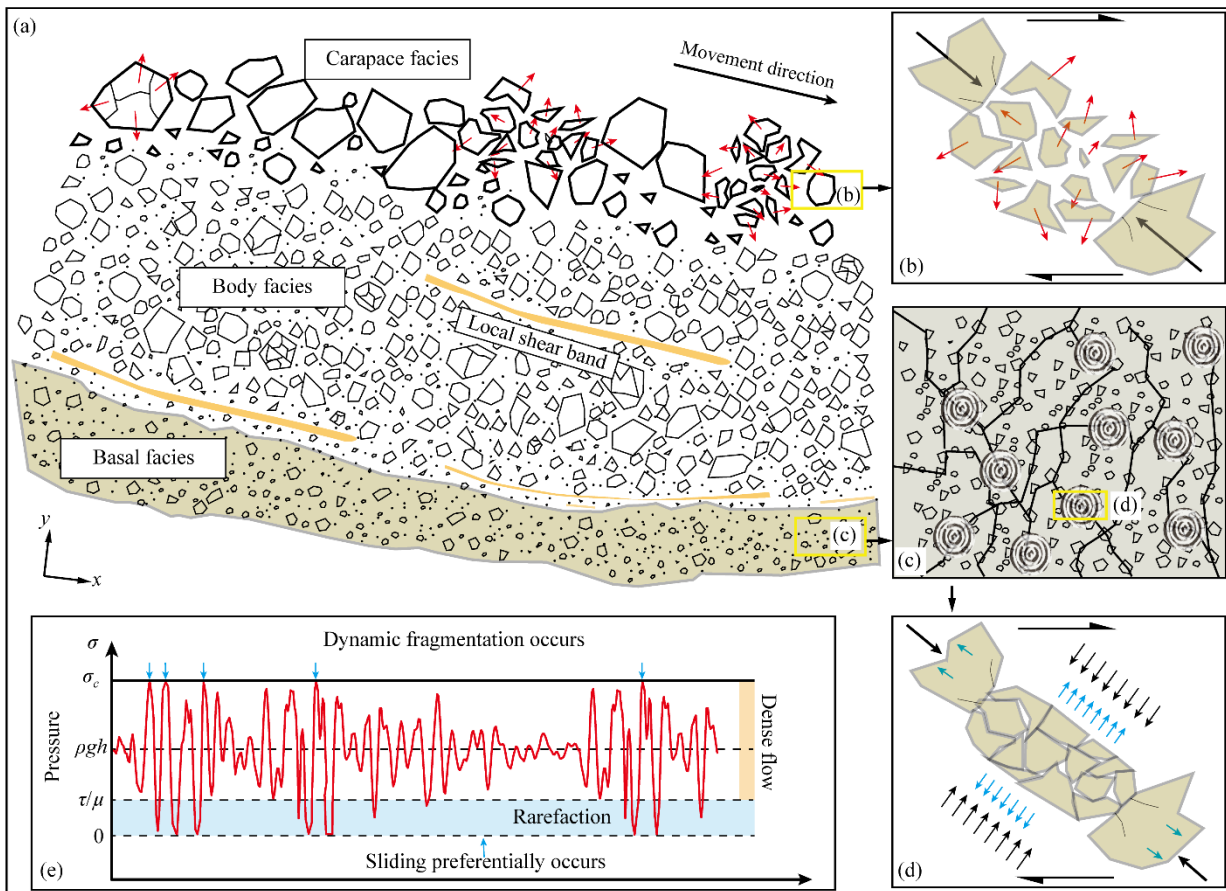
675 **Figure 5: (a) The mean horizontal velocity incremental percentage ( $\phi_v$ ) and (b) the kinetic energy incremental percentage ( $\phi_e$ ) in the block separation stage for all tests.**



**Figure 6: Deposit profiles of all simulations. Yellow line represents travel distance of rock mass.**



680 **Figure 7: (a) The normalized elastic strain energy variation in the sliding block in T1 and T3 (normalized by the maximum total strain energy,  $E_{ts-max}$ ) versus time. (b) Normalized dissipated energy variation in the sliding block in T1 and T3 (normalized by the maximum total dissipated energy,  $E_{td-max}$ ) versus time. The two bold curves represent bond breakage number variations (which are also normalized by the maximum bond breakage number) of T1 and T3 versus time.**





685 **Figure 8:** (a) Schematic illustration of fragmentation effects of countless grains during the propagation of a rock avalanche; (b)  
 dynamic fragmentation of a rock block without confining pressure (in the carapace facies); (c) force chain in the shear layer (basal  
 facies) and local fragmentation points (gray-white rings represent the fragmentation points and related radiated stress wave)s; (d)  
 690 schematic illustration of dynamic fragmentation of a rock block in a force chain with confining pressure (small black arrows  
 represent confining pressure, and small blue arrows represent outward stress caused by fragmentation, which then develop to a  
 stress wave propagating through the entire sliding rock mass) (modified from Melosh (1979)); (e) pressure variation (red curve) of  
 a point inside a rock mass caused by rock fragmentation during an avalanche (modified from Melosh (1979)). Blue arrows  
 represent the times at which dynamic fragmentation occurs.  $\sigma_c$  is the critical stress for the rock to fracture.

**Table 1: Input microparameters of the DEM model.**

Microparameters	Value	Microparameters	Value
Particle radius (mm)	[0.1, 0.5]	Cohesion (MPa)	95
Number of particles	11812	Bond friction angle	30 °
Density (kg/m <sup>3</sup> )	2650	Ball friction coefficient	0.577
Normal to shear stiffness ratio	3	Friction coefficient between ball and wall	0.577
Bond normal to shear stiffness ratio	3	Normal viscous damping	0.36
Effective modulus (GPa)	60	Shear viscous damping	0.11
Bond effective modulus (GPa)	40	Local damping	0.06
Tensile strength (MPa)	95		

## Appendix A

**Table A1: List of variables considered in this study.**

Variable	Description	Variable	Description
$H$	Drop height of a sliding rock block	$v_{be}$	Horizontal velocity of block before separation
$g$	Gravitational acceleration on Earth (9.81 m/s <sup>2</sup> )	$v_{af}$	Horizontal velocity of block after separation
$g'$	Gravitational acceleration in our DEM model (200 g)	$\varphi_e$	Kinetic energy incremental ratio of block in separation stage
$\sigma$	Tensile strength of joint	$E_{be}$	Kinetic energy of block before separation
$t$	Physical time of simulation	$E_{af}$	Kinetic energy of block after separation
$t'$	Normalized time scale	$\varphi'_e$	Kinetic energy incremental ratio of front subblock in T1, T2, and T3
$V'_p$	Normalized particle velocity in simulation	$\varphi''_e$	Kinetic energy incremental ratio of front subblock in T3, T4, and T5
$V_b$	Mean horizontal velocity of block	$E_{bs}$	Bond strain energy, stored in the parallel bond springs
$V'_b$	Normalized mean horizontal velocity of block	$E_\beta$	Dashpot energy, the energy dissipated by the dashpots
$E$	Kinetic energy of rock block	$E_{td}$	Total dissipated energy
$E'$	Normalized kinetic energy of rock block	$E_{td-max}$	Maximum dissipated energy
$i$	Particle ID	$E_s$	Strain energy of discs, stored in the linear springs
$m_i$	Mass of particle $i$	$E_\mu$	Slip energy, the energy dissipated by frictional slip
$n$	Total number of particles in rock block	$E_{ts}$	Total strain energy stored in rock block
$v_{x,i}$	Horizontal velocity of particle $i$	$E_{ts-max}$	Maximum total strain energy
$v_{y,i}$	Vertical velocity of particle $i$	$\varphi_v$	Incremental ratio of block velocity in separation stage

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