

Answer sheet for short comment #1

1. General comments

This paper reports a series of experiments to analyze the sinkhole formation associated with rainfall intensity by simulating a leakage of an underground damaged sewer pipe. A slit at the bottom of the experiment chamber was considered as damage of pipe, and three different rainfall intensities were designed by controlling the hydraulic head connected to the slit of the chamber. The ground settlement was measured, and the deformation of soils around the pipe is captured by the particle image velocimetry (PIV) technique. Overall, the authors in this work present a rising issue of the sinkhole and its relationship to rainfall by utilizing an experimental model set-up. I believe this paper will be of interest to the audience and would support publication after the following comments are addressed.

Answer: Thank you very much for your thorough and helpful review. Based on your concerns and comments, we believe that our manuscript has been improved. Please check our answers corresponding to your concerns.

1) Authors should clearly address and explain how the test procedure is designed to simulate the rainfall and the sewer pipes.

a. In the test procedure, the hydraulic head was selected as a variable to represent the rainfall intensity, which eventually formed different target groundwater levels. Therefore, the amount of water introduced into the chamber and the duration of water supply stage may indicate additional information related to the rainfall intensity. For example, if the water supply stage of Test 3 took longer than that of Test 1, this set-up may not properly reflect the actual rainfall intensity and its influence on the groundwater level around the pipes. In addition, the flow from the damaged sewer pipe may not be the only source of water supply into the underground.

Answer: The ground condition of each test is the same; thus, the amount of water introduced into the chamber which has a linear relationship with the groundwater level is also a function of the rainfall intensity. In addition, the time to form the target groundwater levels during the water supply stage was almost the same.

In this study, we investigated the soil erosion due to damaged sewer pipes in urban areas by performing model tests. The large area of the ground surface in an urban areas is covered with impervious pavement. Thus, we presumed the flow from damaged sewer pipes to be the main source of water supply into the underground.

b. In this work, the damage of sewer pipes is approximated as a slit of which the size is determined followed by the previous study. While this damage could be the main source of water supply into the ground, the drainage may not occur through this damage. In other words,

the water drainage set-up using the slit and drainage valve may lead to an extra discharge of soils and water. If the groundwater is discharged through a thin slit at the bottom of the chamber, it may be easily expected that the soil around the slit may easily collapse and deformed.

Answer: In this study, the model test procedure consisted of (1) the water supply stage, in which sewer water infiltrates from the pipes to the ground through damaged sections during heavy rainfall periods, and (2) the water drainage stage, which describes the drainage of groundwater into the sewer pipes through the damaged sections after heavy rainfall periods. As the reviewer noted, overflows may occur in the other direction rather than through damaged sections. After heavy rainfall, however, the hydraulic pressure of a sewer pipe becomes lower (as the sewer pipe becomes vacant); thus, it is the most likely that the groundwater will flow back through the damaged portions.

The authors found that a description of what each step actually meant in field conditions was lacking. Thus, appropriate descriptions have been added in the manuscript. (see Line 151 – 159)

2. Specific comments

1) Line 149: What's the meaning of multiple cycles?

Answer: Based on your comment, the authors removed the term “multiple cycles.”

2) Line 173: As point out by the authors, the test-set up is likely to the piping simulation. Then, is it possible to analyze the sinkholes and rainfall intensity though the piping analysis?

For example, using the critical hydraulic gradient?

Answer: The authors think that the piping analysis is valid only for the water supply stage. During the water supply stage (which describes the situation during rainfall), the effective stress decreases because upward seepage occurs through the slit; therefore, piping could occur. During the water supply stage, the water pressure (as compared to the soil pressure) was not sufficient to induce the piping in test 1 and 2; however, in test 3, piping occurred during the water supply stage, which implies that the water pressure has sufficient magnitude to reduce the soil effective stress to zero.

During the water drainage stage, however, the use of the piping concept for sinkhole analysis is limited. The critical hydraulic gradient is usually valid when the seepage has a direction different from that of the gravitational force; however, the seepage and gravitational force have the same direction near the slit during the water drainage through the slit. In this case, soil particles freely fall with water and the ground cavity (or sinkhole) expands until (apparent) cohesion recovers because of partial saturation. For all tests described in the manuscript, ground cavities (or sinkholes) occurred.

3) Line 255: How is the resistance factor determined? If there's an equation, it could be helpful

for readers.

4) Line 262: Is the matric suction analyze in a quantitative manner? Because of cohesion, this may limitedly affect the behavior of soils.

Answer: The authors think that the ability of the model tests to enable quantitative evaluation of the resistance factor or matric suction is limited. The authors are planning a numerical parametric study (such as coupled analysis between soil and groundwater) for this purpose.

5) Lines 279-280: The meaning is not clear.

Answer: The authors decided that Lines 279 and 280 were unnecessary and removed them from the manuscript.

Answer sheet for referee comment #1

1. General comments to authors

This paper examined the effect of rainfall intensity on the sewer-related soil erosion and its evolution by means of model tests and image analysis. In order to reflect the field conditions in South Korea, the backfill material, rainfall intensity, and compaction criteria were considered in the model tests. The topic is clear and suitable with the subject of this journal. There are, however, several aspects that need to be improved, especially in relation with the test procedure and actual sewer-related soil erosion. Revising the manuscript considering the following comments are also recommended.

Answer: Thank you very much for your thorough and helpful review. Based on your concerns and comments, we believe that our manuscript has been improved. Please check our answers corresponding to your concerns.

2. Specific comments to authors

Q1: The terms ‘ground cave-in’ and ‘sinkhole’ are used interchangeably which are recommended to be unified.

Answer: Based on your comment, the authors changed the term “ground cave-in” to “sinkhole.” (see Line 68, 69, 548)

Q2: L101. “The width of the slit was set to 2 cm, based on the study by Mukunoki et al. (2012), such that B/D_{max} was 4.2.” Justify the width of the slit the authors determined in relation with the listed reference.

Answer: Mukunoki et al. (2012) adjusted the ratio B/D_{max} between the slit width B and maximum grain size D_{max} of the soil to 1.05, 2.5, and 5.9 in their model tests. A ground cavity was formed after 13 cycles when $B/D_{max} = 1.05$, whereas a sinkhole was observed when both $B/D_{max} = 2.5$ and 5.9. In the model tests that were performed in our study for the adjusted Gwanak soil, which describes the typical backfill materials for the underground pipes used in South Korea, $B/D_{max} = 4.2$. (For the adjusted Gwanak soil, $D_{max} = 4.75$ mm and $B = 20$ mm.) This B/D_{max} value is between 2.5 and 5.9, corresponding to the sinkhole development described by Mukunoki et al. (2012). (see Line 99 – 101)

Q3: L107-108. Some clarification on the condition of "Relationship between the rainfall intensity and the hydraulic head in the sewage network conditions near Gangnam station" are needed. I wonder if this condition has been sufficiently considered in the model tests of this study.

Answer: The test conducted by National Disaster Management Institute of Korea (2014) shows the relationship between the rainfall intensity and hydraulic head under the sewage network conditions near Gangnam station. The sewage network was simulated by considering the distance between each sewer pipes and burial depth of the sewer pipes. In addition, the sewer pipes were assumed to be 1000 mm in diameter, as reflected in the present study. The authors noted these points in the manuscript. (see Line 106)

Q4: L117. typo (#No. 4 sieve passing).

Answer: Based on your comment, the authors removed the term of “#No. 4 sieve passing.”

Q5: L141-142. Additional information on the validation of PIV technique, such as accuracy, analysis condition, will be of interest to the readers.

Answer: In this study, to find the optimum size of the pixel subset, various-sized pixel subsets (40×40 , 60×60 , 80×80 , 100×100 , and 120×120) were tested by comparing two digital images: the original image of the model ground and the image artificially shifted by 10 pixels at the 4 edges of the model ground (where crude distortion occurs). The validation test results showed that 100×100 was the optimum size of the pixel subset, with a maximum error of 0.0069 pixels in accuracy and precision. The PIV validation results have been included in the manuscript. (see Line 139 – 144)

Q6: L149. Explanation about the multiple cycles is required. I believe that one cycle consisted of water supply and drainage stage and it was repeated, but the manuscript contains only the result of one cycle.

Answer: Based on your comment, the authors removed the term “multiple cycles.”

Q7: Additional information on the rainfall record which can prove the suggested three rainfall intensities in this study are realistic will enhance the credit of this paper.

Answer: Currently, the standard for a heavy rain watch in South Korea is 60 mm/3 h (in the case of intense heavy rain) or 110 mm/12 h (in the case of continuous heavy rain), and the standard for a heavy rain warning is 90 mm/3 h (in the case of intense heavy rain) or 110 mm/6 h (in the case of continuous heavy rain). Because the focus of this study was the formation of anthropogenic sinkholes in the event of intense heavy rainfall, the hourly rainfall intensity distributions corresponding to 60 mm/3 h and 90 mm/3 h (which are the criteria for a heavy rain watch and heavy rain warning) were confirmed using data from the Environmental Prediction Research Institute (2017) (as of 2012–2016). In the cases of 60 mm/3 h (based on a heavy rain watch) and 90 mm/3 h (based on the heavy rain warning level), the hourly rainfall intensity distributions corresponding to 30–50 mm/h and 40–60 mm/h were the highest, respectively. In the heavy rain watch case, the rainfall intensity distribution of 30–50 mm/h was 72.9 %, and in the heavy rain warning case, the rainfall intensity distribution of 40–60

mm/h was 64.9 %. Therefore, 40 mm/h and 50 mm/h were applied in this study by using the average value for the section with the highest rainfall distribution for 1 h in terms of heavy rain watch and heavy rain warning. (see Line 159 – 162)

Q8: The procedure of calculating the average cavity width in Table 4 is not clear.

Answer: Based on your comment, the authors specified the calculation procedure for the average cavity width in the footnote of Table 4. (see Line 549)

Answer sheet for referee comment #2

1. General comments

An experimental study about the relationships between rainfall intensity and development of sinkholes caused by damaged sewer pipes in Korea is described in the paper. The topic is certainly of interest to NHESS, and the work contains interesting data and considerations. I have listed in the accompanying file a number of small corrections, and a few requests of clarification on some issues that are not clear to me.

Answer: First we are very grateful for your thorough and helpful review. Based on your concerns and comments, we believe that our manuscript has been improved. Please check our answers corresponding to your concerns.

2. Specific comments

1) I discourage throughout the manuscript the use of the term “ground cave-ins”, since this is not used in the international literature, and may induce confusion and misunderstandings in the readers.

Answer: Based on your comment, the authors changed the term “ground cave-in” to “sinkhole.” (see Line 68, 69, 548)

2) How were the different rainfall intensity chosen? It is briefly said in the initial part of the paper that this was based upon the rainfall values in South Korea, but then no rainfall data was provided to justify the choice of the adopted values. It would be good to add a few lines, or a figure, to describe the rainfall trend in the area. Further, a brief text explaining the importance of establishing relationships between rainfall and geological hazards could be useful, also referring to other hazards such as landslides (see for instance the works by Peruccacci et al. (2012), Rossi et al. (2012), and Vessia et al.(2012)).

Answer: Currently, the standard for a heavy rain watch in South Korea is 60 mm/3 h (in the case of intense heavy rain) or 110 mm/12 h (in the case of continuous heavy rain), and the standard for a heavy rain warning is 90 mm/3 h (in the case of intense heavy rain) or 110 mm/6 h (in the case of continuous heavy rain). Because the focus of this study was the formation of anthropogenic sinkholes in the event of intense heavy rainfall, the hourly rainfall intensity distributions corresponding to 60 mm/3 h and 90 mm/3 h (which are the criteria for a heavy rain watch and heavy rain warning) were confirmed using data from the Environmental Prediction Research Institute (2017) (as of 2012–2016). In the 60 mm/3 h (based on heavy rain watch) and 90 mm/3 h (based on heavy rain warning) cases, the hourly rainfall intensity distributions corresponding to 30–50 mm/h and 40–60 mm/h were the highest, respectively. In the heavy rain watch case, the rainfall intensity distribution of 30–50 mm/h was 72.9 %, and in the heavy rain warning case, the rainfall intensity distribution of 40–60 mm/h was 64.9 %.

Therefore, 40 mm/h and 50 mm/h were applied in this study by using the average value for the section with the highest rainfall distribution for 1 h in terms of heavy rain watch and heavy rain warning. (see Line 159 – 162)

In addition, following your comment, we added a brief description of the importance of establishing the relationships between rainfall and geological hazards with suggested references. (see Line 51 – 53)

3) When quoting figures throughout the manuscript, please avoid the use of multiple brackets.

Answer: Based on your comment, the authors removed all of the multiple brackets in manuscript. (see Line 199, 200, 202, 207, 210, 227, 236, 238, 240, 245, 261, 264, 268, 272, 281, 285)

4) In general, the reference list can be improved, especially by adding the main international works about sinkhole classification, which are lacking in the present version of the manuscript. Apart from some references directly suggested in the accompanying file, I am enclosing to this comment a list of possible additional references that might be useful to the Authors to improve their paper.

Answer: Based on your comment, the authors included the main international works about sinkhole classification (as recommended by reviewer) in the manuscript. (see Line 30 – 33, 34, 36, 51 – 53, 55 – 56)

5) When quoting more than one paper in the text, the references must be listed in chronological order. This guideline is not followed in the manuscript. Please correct it throughout the text.

Answer: Based on your comment, the authors rearranged the references according to chronological order. (see Line 30 – 33, 34, 39 – 40, 51, 52 – 53, 112 – 113, 127 – 128)

Suggested references:

Beck, B.: Soil Piping and Sinkhole Failures. In: Encyclopedia of Caves (Second Edition),

White, W. B. and Culver, D. C. (Eds.), Academic Press, Amsterdam, 2012.

Closson D, Abou Karaki N (2009) Human-induced geological hazards along the Dead Sea coast. *Environ Geol* 58:371–380.

Gutiérrez, F., Guerrero, J., Lucha, P., 2008. A genetic classification of sinkholes illustrated from evaporite paleokarst exposures in Spain. *Environ. Geol.* 53, 993–1006.

Gutierrez F., Parise M., De Waele J. & Jourde H., 2014, A review on natural and human-induced geohazards and impacts in karst. *Earth Science Reviews*, vol. 138, p. 61-88, doi: 10.1016/j.earscirev.2014.08.002.

Parise M., 2015, A procedure for evaluating the susceptibility to natural and anthropogenic sinkholes. *Georisk*, vol. 9 (4), p. 272-285, DOI:10.1080/17499518.2015.1045002.

Parise M., 2019, Sinkholes. In: White W.B., Culver D.C. & Pipan T. (Eds.), *Encyclopedia of Caves*. Academic Press, Elsevier, 3rd edition, ISBN 978-0-12-814124-3, p. 934-942.

Parise M., Pisano L. & Vennari C., 2018, Sinkhole clusters after heavy rainstorms. *Journal of Cave and Karst Studies*, vol. 80 (1), p. 28-38. DOI: 10.4311/2017ES0105.

Peruccacci, S., Brunetti, M. T., Luciani, S., Vennari, C., and Guzzetti, F.: Lithological and seasonal control on rainfall thresholds for the possible initiation of landslides in central Italy, *Geomorphology*, 139–140, 79–90, 2012.

Rossi, M., Peruccacci, S., Brunetti, M. T., Marchesini, I., Luciani, S., Ardizzone, F., Balducci, V., Bianchi, C., Cardinali, M., Fiorucci, F., Mondini, A. C., Reichenbach, P., Salvati, P., Santangelo, M., Bartolini, D., Gariano, S. L., Palladino, M., Vessia, G., Viero, A., Antronico, L., Borselli, L., Deganutti, A. M., Iovine, G., Luino, F., Parise, M., Polemio, M., and Guzzetti, F.: SANF: a national warning system for rainfall-induced landslides in Italy, in: *Proceedings of the 11th International Conference and 2nd North American symposium on landslides*, Banff, Alberta, Canada, 3–8 June, 2012.

Vessia G., Parise M., Brunetti M.T., Peruccacci S., Rossi M., Vennari C. & Guzzetti F., 2014, Automated reconstruction of rainfall events responsible for shallow landslides. *Natural Hazards and Earth System Sciences*, vol. 14, p. 2399- 2408.

Waltham, T., Bell, F., Culshaw, M., 2005. *Sinkholes and Subsidence*. Springer, Chichester, (382 pp.).

White, W.B., 2002. Karst hydrology: recent developments and open questions. *Eng. Geol.* 65, 85–105.

For all the considerations above, I recommend minor revision. I believe that, after some corrections, and following the journal guidelines for citations, the manuscript may become acceptable for publication.

6) Please also note the supplement to this comment:

<https://nhess.copernicus.org/preprints/nhess-2020-143/nhess-2020-143-RC2-supplement.pdf>

Answer: The authors considered the comment made by the reviewer in the revision.

1 **Experimental assessment of the relationship between**
2 **rainfall intensity and sinkholes caused by damaged sewer**
3 **pipes**

4
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15 **ABSTRACT**

16 In several countries, the rising occurrence of sinkholes has led to severe social and economic damage. Based
17 on the mechanism of sinkhole development, researchers have investigated the correlation between rainfall
18 intensity and sinkholes caused by damaged sewer pipes. In this study, the effect of rain fall intensity on the
19 formation of eroded zones, as well as the occurrence of sinkholes caused by soil erosion due to groundwater
20 infiltration through pipe defects, has been analyzed through model tests. The ground materials in Seoul were
21 represented by weathered granite soil, which is generally used for backfill sewer pipes, and groundwater
22 levels corresponding to three different rainfall intensity conditions were considered. The ground level
23 changes and ground displacements were measured continuously, and the particle image velocimetry (PIV)
24 algorithm was applied to measure the displacement at each position of the model ground. The results indicate
25 that impeding the excessive rise of groundwater levels by securing sufficient sewage treatment facilities can
26 effectively prevent the development of sinkholes caused by pipe defects.

메모 포함[K1]: Referee comment #2 - 6)

27 **1 Introduction**

28 In recent times, cases of sinkholes have been reported in several countries, such as the US, Japan, Italy, South
29 Africa, China, Spain and South Korea. Major social and economic issues have ensued owing to the resulting
30 structural problems, such as the collapse of buildings and road erosion (Galloway et al., 1999; Waltham et
31 al., 2005; Gutierrez et al., 2008; Kuwano et al., 2010a; Oosthuizen and Richardson, 2011; Beck et al., 2012;
32 Guarino and Nisio, 2012; Yokota et al., 2012; Gao et al., 2013; Intrieri et al., 2015; Bae et al., 2016; Parise,
33 2019). In general, sinkholes can be classified into two types: (1) natural sinkholes and (2) anthropogenic
34 sinkholes (Guarino and Nisio, 2012; Gutierrez et al., 2008, 2014; Beck, 2012; Parise, 2019). Natural
35 sinkholes occur when the underlying ground layer (e.g., karst landscape) is easily soluble in water, whereas
36 anthropogenic sinkholes may occur also in a non-karst environment (Parise, 2015), caused by human activity
37 such as sewage damage, inadvertent excavation, or groundwater lowering.

38 Both types of sinkholes have similar mechanisms, and the detailed process of occurrence is as follows
39 (Rogers, 1986; Brinkmann et al., 2008; Caramanna et al., 2008; Kuwano et al., 2010a; Oosthuizen and
40 Richardson, 2011; Martinotti et al., 2017): (1) A cavity is formed underground by external factors (the water-
41 soluble ground layer dissolves in groundwater to cause a natural sinkhole, or soil erosion occurs along with
42 the groundwater outflow due to sewage damage or excavation to cause an anthropogenic sinkhole). (2) The
43 groundwater level rises during rainfall and falls after the rainfall, causing the soil around the cavity to be lost
44 and the cavity to expand. (3) A sinkhole is finally generated because of the repeated increase and decrease of
45 the groundwater level.

46 Based on the mechanism for both types of sinkholes (natural and anthropogenic), a direct relationship can be
47 inferred between the rainfall intensity, which leads to the transition of the groundwater level (rise and fall),
48 and the occurrence of sinkhole. Notably, the change in climate due to global warming has resulted in higher
49 rainfall intensity with fewer rainy days (Alpert et al., 2002; Kristo et al., 2017; Rahardjo et al., 2019). In
50 South Korea, the maximum daily rainfall has increased over the decades in most regions and is expected to
51 increase significantly in the future (Nadarajah and Choi, 2007; Wi et al., 2016; Choi et al., 2017). For
52 landslides, many studies have established the influences of rainfall on those geological hazards (Peruccacci
53 et al., 2012; Rossi et al., 2012; Vessia et al., 2012). In this context, there is a growing need to study the
54 correlation between rainfall intensity and sinkhole occurrence.

55 Martinotti et al. (2017) and Parise et al. (2018) showed that a period of torrential rain and the rainfall intensity
56 triggered natural sinkholes in Italy. Gao et al. (2013) confirmed that the groundwater level rise due to
57 extremely heavy rainfall has a significant effect on sinkhole generation in a karst environment in China. Van
58 Den Eeckhaut et al. (2007) showed that the formation of numerous natural sinkholes in Belgium
59 corresponded with periods of high rainfall and high groundwater recharge, which commonly increased the
60 weight of the overburden and decreased its cohesion.

61 The majority of sinkholes in non-karst environments are known to occur because of damaged sewer pipes.
62 In Seoul, South Korea, an average of 677 sinkholes and subsidence occurred annually from 2010 to 2015, of

메모 포함[K2]: Referee comment #2 - 4), 5)

메모 포함[K3]: Referee comment #2 - 4), 5)

메모 포함[K4]: Referee comment #2 - 6)

메모 포함[K5]: Referee comment #2 - 4), 6)

메모 포함[K6]: Referee comment #2 - 5)

메모 포함[K7]: Referee comment #2 - 5)

메모 포함[K8]: Referee comment #2 - 2), 4)

메모 포함[K9]: Referee comment #2 - 4)

63 which 81.4 % were due to damage to old sewer pipes (Bae et al., 2016). In Japan, local governments in
64 sewage projects were surveyed to identify cases of subsidence due to damage to sewer pipes. As a result, a
65 total of 17,000 data were reported from 2006 to 2009 (Yokota et al., 2012).

66 Considering these factors, several researchers have conducted statistical analysis and model experiments to
67 investigate the correlation between rainfall intensity and sinkholes caused by damaged sewer pipes. Kwak et
68 al. (2016) showed that the number of anthropogenic sinkhole cases increased with the increase in total
69 monthly precipitation. In addition, it was confirmed that anthropogenic sinkholes are prone to occur after
70 exceptionally heavy rains. By quantifying Pearson's correlation coefficient between two relevant
71 observations, Choi et al. (2017) showed that the monthly accumulated precipitation and the quantity of
72 subsidence are related to a certain extent. Guo et al. (2013) and Tang et al. (2017) used model experiments
73 and evaluated the effect of the defect size, groundwater level, and particle size on soil erosion due to
74 groundwater infiltration through pipe defects. However, they only used non-cohesive soils and covered
75 extreme cases with groundwater levels significantly exceeding the ground level.

76 In this study, the urban area in Seoul has been simulated, and model tests have been conducted to analyze the
77 effect of rainfall intensity on the formation of eroded zones, as well as the occurrence of sinkholes caused by
78 soil erosion due to groundwater infiltration through pipe defects. The model ground was constructed using
79 weathered granite soil (which is generally cohesive), mainly used to backfill the sewer pipes in Seoul. Three
80 rainfall intensity conditions (heavy rainfall, very heavy rainfall, and extremely heavy rainfall) were set for
81 the groundwater level, based on summer rainfall patterns in Korea, to be applied in the model tests. The
82 groundwater level change, discharged soil volume, and ground displacement were measured continuously
83 throughout the tests. In particular, the particle image velocimetry (PIV) method, which can continuously
84 measure and analyze the displacements in the ground, was applied to quantify the ground deformation with
85 the occurrence and expansion of underground cavities.

86 The remainder of this paper is organized as follows. Section 2 describes the model test device, model grounds,
87 and test conditions. Section 3 discusses the model test results. Finally, Section 4 presents the conclusions.

88 2 Experimental program

89 2.1 Experiment apparatus

90 In this study, experiments were performed using the model tester developed by Kwak et al. (2019) to simulate
91 ground subsidence (Figure 1). The distance between each pipe in the sewer pipe network in Seoul was
92 examined and found to be around 1.2 m. In order to exclude the effects of unnecessary boundary conditions,
93 the width of the model soil was set to 1.4 m, with respective left and right margins of 0.1 m. Considering that
94 the average landfill depth of a sewage pipe in Seoul is 0.9 m (Kim et al., 2018), the soil chamber was built to
95 a height of 1.0 m, including a 0.1 m clearance to facilitate sample composition. The depth of the soil chamber

메모 포함[K10]: Referee comment #1 - 1)
Referee comment #2 - 1)

메모 포함[K11]: Referee comment #1 - 1)
Referee comment #2 - 1)

메모 포함[K12]: Referee comment #2 - 6)

메모 포함[K13]: Referee comment #2 - 6)

메모 포함[K14]: Referee comment #2 - 6)

96 was set to 0.1 m to simulate the plane strain condition, and the front plate of the chamber was made of acrylic
97 plate to allow the inside of the ground to be photographed during the test.
98 A slit was installed at the bottom of the soil chamber to simulate the damage of the sewer pipe allowing the
99 inflow and outflow of sewage and the outflow of soil during the model test. [The width of the slit(B) was set
100 to 2 cm, based on the study by Mukunoki et al. (2012), such that B/D_{max} was 4.2 (maximum particle diameter
101 of weathered soil $D_{max} = 4.76$ mm)]. A supply valve and a drain valve were installed under the slit to control
102 the inflow and outflow of groundwater as well as the outflow of eroded soil. The external water tank
103 connected to the inlet valve was designed to maintain a constant level even when water is continuously
104 supplied to the model ground. Through experimental assessment (Table 1), the National Disaster Management
105 Institute of Korea (2014) suggested a relationship between the rainfall intensity and the hydraulic head in the
106 sewage network conditions near Gangnam station (sewer pipe with 1000 mm of diameter was simulated). It
107 should be noted that the hydraulic head increases linearly with the rainfall strength until the rainfall strength
108 is 40 mm/h, but thereafter increases sharply. In the present study, the height of the external tank was made
109 adjustable to simulate the various rainfall intensity (related to hydraulic head).

메모 포함[K15]: Referee comment #1 - 2)

메모 포함[K16]: Referee comment #1 - 3)

110 2.2 Model ground

111 The vast majority of prior studies that have experimentally assessed the ground subsidence and sinkhole due
112 to sewer pipe damage have been conducted on poorly-graded non-cohesive soils (Kuwano et al., 2010a,
113 2010b; Guo et al., 2013; Sato and Kuwano, 2015; Indiketiya et al., 2017; Tang et al., 2017). However, in
114 several countries, the sewage reclamation specifications allow the landfill soil to contain 15–25 % of fine
115 contents. There are no restrictions on particle size distribution apart from the maximum particle size (Japan
116 Road Association, 1990; Ministry of Environment of Korea, 2010). In the present study, to simulate the
117 ground in Seoul in which weathered granite soil, which is a well-graded cohesive soil, is widely distributed,
118 the model ground was created by collecting Gwanak weathered soil and adjusting the fine content to 7.5% to
119 meet the fine content standard. The degree of compaction was also set to 93 % of the standard maximum unit
120 dry weight $\gamma_{d,max}$ to satisfy the sewer pipe landfill standards, and the model ground was constructed with the
121 optimum moisture content. Figure 2 shows the particle size distributions of the adjusted and natural Gwanak
122 soil in comparison with the sewer pipe landfill standards in South Korea and Japan. Table 2 lists the basic
123 physical properties, strength parameters and saturated permeability coefficient of the adjusted Gwanak soil
124 used in the model test.

메모 포함[K17]: Referee comment #2 - 5)

125 2.3 Digital image analysis

126 In geotechnical engineering, digital imaging techniques are primarily used to measure the deformation of
127 target samples (Alshibli and Sture, 1999; White et al., 2003; Indiketiya et al., 2017; Kim et al., 2017; Kwak
128 et al., 2019). In the present study, the displacement at each position of the model ground was measured by
129 applying the PIV algorithm (Adrian, 1991), which is the most widely used technique in the field of

메모 포함[K18]: Referee comment #2 - 5)

130 geotechnical engineering. The PIV cross-correlation on the pixel sets of the pre-deformation and post-
131 deformation images were calculated to obtain the point with the highest correlation. The position of the
132 sample set with the highest correlation is used to estimate the relative displacement at each position of the
133 sample (Kim et al., 2011; White et al., 2003). In this study, the internal displacement of the sample was
134 evaluated using GeoPIV (White and Take, 2002), a commercial program that is widely used to apply the PIV
135 technique in geotechnical engineering. With the displacement, the volume and shear strain are estimated
136 together for the analysis.

137 In general, when applying the PIV technique, high accuracy analysis results can be obtained when the
138 uniqueness of the pixel set increases with the size of the pixel set. However, in order to calculate
139 displacements at various positions, it is necessary to set an appropriate size for the set of pixels. Accuracy
140 and precision verification of the GeoPIV program was performed for various-sized pixel subsets (40x40,
141 60x60, 80x80, 100x100, and 120x120) by comparing two digital images: the original image of the model
142 ground and the image artificially shifted by ten pixels at the four edges of the model ground. The optimum
143 size of the pixel set was chosen as 100 by 100 pixels, which shows a 0.0069 pixel maximum error in accuracy
144 and precision. As shown in Figure 3, the PIV technique was applied to the positions of a total of 2600 pixel
145 subsets (65 by 40). To minimize the boundary effect between the interface of the sample and the soil chamber,
146 the vicinity of the wall was excluded from the analysis. In addition, any excessive relative displacement due
147 to soil erosion (no highly correlated pixel sets found in the post-deformation image) was excluded from the
148 analysis.

149 2.4 Test procedures

150 Once the model ground was created, the model tests which consisted of a water supply stage and a water
151 drainage stage were conducted. The water supply stage represents the infiltration of sewer water from the
152 pipes to the ground through damaged sections during heavy rainfall periods. This phenomenon was simulated
153 in the model test by introducing water from the external water tank into the soil chamber through the supply
154 valve and slit to reach the target groundwater level (i.e. hydraulic head). After heavy rainfall, the hydraulic
155 pressure of a sewer pipe becomes lower (as the sewer pipe becomes vacant), thus, it is the most likely that
156 the groundwater will flow back through the damaged section. The water drainage stage simulates the drainage
157 of groundwater into the sewer pipes through the damaged sections after heavy rainfall periods by closing the
158 supply valve and opening the drainage valve. The soil also discharged through the lower slit along with the
159 water drainage. Table 3 shows the conditions of the three model tests conducted in this study, simulating
160 cases with rainfall intensities of 40 mm/h (represent the rainfall intensity of heavy rain watch in South Korea)
161 and 50 mm/h (represent the rainfall intensity of heavy rain warning in South Korea) presented in Table 1, as
162 well as that with the groundwater level rising to the ground surface.

163 Linear variable displacement transducers (LVDTs) were installed at three locations on the surface of the
164 ground, at 0, 30, and 60 cm from the center of the soil chamber, to measure the surface displacement during

메모 포함[K19]: Referee comment #2 - 6)

메모 포함[K20]: Referee comment #2 - 6)

메모 포함[K21]: Referee comment #1 - 5)

메모 포함[K22]: Short comment #1 - 1)b

메모 포함[K23]: Referee comment #1 - 7)
Referee comment #2 - 2)

165 the tests (Figure 1). During the model tests, digital images of the ground were continuously captured, and the
166 PIV technique was applied to analyze the displacement and deformation (Adrian, 1991; Alshibli and Akbas,
167 2007; Kim et al., 2017; Kwak et al., 2019). In addition, the amount of soil discharged through the slit was
168 measured after the water supply and water drainage stages of each test.

169 **3 Experimental results and discussion**

170 **3.1 Test 1: Heavy rainfall intensity (47 cm hydraulic head)**

171 **3.1.1 Water supply stage**

172 Test 1 was conducted by introducing groundwater to a 47 cm initial hydraulic head (the height difference
173 between the slit and weir in the water tank) to simulate a heavy rainfall intensity of 40 mm/h. In the water
174 supply stage of Test 1, no soil deformation occurred on the ground surface (measured by the LVDTs) and in
175 the ground (measured by the PIV technique) as the groundwater level approached 47 cm. Immediately after
176 opening the slit, the water pressure acting on the ground directly above the slit was 4.5 kPa, and the vertical
177 earth pressure generated by the upper soil was about 16.7 kPa. Therefore, under this condition, the soil always
178 had a positive effective stress, and the piping phenomenon did not occur. In this study, since the model ground
179 was densely constructed ($D_R = 78\%$) with a sufficient degree of compaction ($R_C = 93\%$) according to
180 domestic specification, no water compaction (Kwak et al., 2019), which occurs mainly when sewage flows
181 into a loose sandy soil, was observed. From these results, it was confirmed in this experimental case that the
182 resistance factor (due to the soil strength parameter) was greater than the sum of the drag force (upward force
183 by infiltration pressure during water supply) and the gravity (downward force).

184 **3.1.2 Water drainage stage**

185 In the water drainage stage of Test 1, no soil deformation was observed on the ground surface as in the water
186 supply stage. The deformation in the ground was evaluated by applying PIV to the images captured during
187 the test. Figures 4, 5, 6 are the PIV analysis results showing the estimated displacement vector, volume, and
188 shear strain increments in six phases: (a) 0–30 s, (b) 30–60 s, (c) 60–90 s, (d) 90–120 s, (e) 120–150 s, and
189 (f) 150–180 s. For the volumetric strain, the red grid (the area with positive values) indicates that the area has
190 expanded, and the blue grid (the area with negative values) indicates that the area has been compressed.

191 In the water drainage stage, the water pressure applied through the slit disappeared, and the groundwater in
192 the soil chamber was discharged quickly through the slit. Unlike in the water supply stage, the ground below
193 the groundwater level became saturated and lost its apparent cohesion. The rapid outflow of groundwater
194 resulted in a downward infiltration into the ground, and the soil was discharged from the area immediately
195 above the slit, where there was no active restraining pressure (and thus, no shear strength), along with the
196 groundwater.

197 During the initial phase of the water drainage stage (0–60 s), the soil was discharged through the slit, causing
198 a downward displacement in the periphery of the cavity, and a triangular cavity was formed just above the
199 slit (Figure 4a and b). In addition, volume and shear strain increments occurred intensively around the cavity
200 (Figure 5a, b, Figure 6a and b). In the 60–90 s interval of the water drainage stage, as shown in Figure 4c,
201 the soils on both sides of the cavity collapsed, and the cavity expanded laterally. The volume and shear strain
202 increments were concentrated in small areas near the cavity, similar to the initial stage (Figure 5c and Figure
203 6c).

204 As shown in Figure 4d, during the 90–120 s interval of the groundwater drainage stage, the lateral expansion
205 of the cavity inside the ground was completed, and no downward displacement was observed in the upper
206 part of the cavity and the soils on the sides. The volume and shear strain increments were also not observed
207 in the outer region of the cavity (Figure 5d and Figure 6d). In this phase, the cavity collapsed; the soil
208 accumulated near the slit gradually shifted to escape into the slit, and the deformation was concentrated near
209 the slit. After 120 s, the soil regained its apparent adhesion due to surface tension, and its outflow stabilized
210 as the drainage completed. Finally, a mushroom-shaped cavity was formed (Figure 4e and f).

메모 포함[K24]: Referee comment #2 - 3)

메모 포함[K25]: Referee comment #2 - 3)

메모 포함[K26]: Referee comment #2 - 3)

메모 포함[K27]: Referee comment #2 - 3)

메모 포함[K28]: Referee comment #2 - 3)

211 3.2 Test 2: Very heavy rainfall intensity (70 cm hydraulic head)

212 3.2.1 Water supply stage

213 Test 2 was conducted by setting the maximum groundwater level to 70 cm to simulate a high rainfall intensity
214 of 50 mm/h. During the water supply stage of Test 2, no soil deformation was observed on the ground surface
215 and in the ground by both LVDT and PIV analyses. As a result, owing to the soil strength parameter, the
216 resistance factor was found to remain greater than the sum of the drag force (upward force by infiltration
217 pressure during water supply) and the gravity (downward force), despite the application of a higher hydraulic
218 pressure in Test 2 as compared to that in Test 1.

219 3.2.2 Water drainage stage

220 During the water drainage stage of Test 2, no vertical displacement was observed on the surface of the model
221 ground. The displacement of the soil element according to the development of the underground cavity was
222 observed by the PIV technique. Figures 7, 8, and 9 show the displacement increment vectors, incremental
223 volumetric strain distribution, and incremental shear strain distribution, respectively; the analysis was
224 conducted in four phases: 0–30 s, (b) 30–60 s, (c) 60–90 s, and (d) 90–120 s (the displacement ended within
225 120 s).

226 In the initial phase of the water drainage stage (0–30 s), the soil was discharged through the slit, causing an
227 internal collapse near the slit. Thus, an underground cavity was formed (Figure 7a), differing from that in
228 Test 1 in terms of shape as well as location; it was located close to the maximum groundwater level (about
229 60 cm from the bottom plate). These results indicate that the hydraulic pressure (related to rainfall intensity)
230 affects the shape and location of the underground cavity in the water drainage stage. In Test 1, the eroded

메모 포함[K29]: Referee comment #2 - 3)

231 zone was formed up to about 89 % of the maximum groundwater level. In Test 2, it developed up to about
232 86 %. When a poorly-graded non-cohesive soil was used under the same experimental conditions, the cavity
233 developed up to 107 % of the maximum groundwater level (Kwak et al., 2019). This shows that the well-
234 graded cohesive soil used in this study has a greater resistance to soil erosion. In addition, during the initial
235 stage (0–30 s), the incremental volumetric and shear strains were found to be concentrated in the upper area
236 of the underground cavity (Figure 8a and Figure 9a).

메모 포함[K30]: Referee comment #2 - 3)

237 During the 30–90 s phase, downward displacement was no longer observed at the top of the cavity;
238 displacement in the slit direction occurred only in the left and right areas adjacent to the cavity (Figure 7b
239 and c). The volumetric and shear strains also showed a tendency to be concentrated in the left and right areas
240 where the displacement occurred, indicating that the cavity gradually increased laterally (Figure 8b, c, Figure
241 9b, and c). In the process of forming a cavity, the downward infiltration pressure was low, and the soil that
242 had lost strength accumulated near the slit. On the other hand, when the downward infiltration pressure was
243 higher, all the soil that had lost strength escaped, resulting in the formation of an oval cavity. After 90 s, as
244 the groundwater level was exhausted, the unsaturated strength of the ground was restored, and no further
245 displacement or deformation were observed inside the ground (Figure 7d, Figure 8d, and Figure 9d).

메모 포함[K31]: Referee comment #2 - 3)

메모 포함[K32]: Referee comment #2 - 3)

메모 포함[K33]: Referee comment #2 - 3)

246 3.3 Test 3: Extremely heavy rainfall intensity (90 cm hydraulic head)

247 3.3.1 Water supply stage

248 Test 3 was conducted to simulate the intensity of an extremely heavy rainfall that causes the groundwater
249 level to rise up to the surface of the ground. In the water supply stage of Test 3, significant displacements
250 were measured on the surface (LVDTs) and inside the model ground (PIV). Figure 10 shows the surface
251 displacement over time, with a gradual subsidence after approximately 2400 s. The ground displacements
252 identified by the PIV technique from 0–2000 s also showed no specific behaviors. Therefore, the internal
253 displacement vectors identified as a result of the PIV technique after 2000 s are shown in Figure 11, overlaid
254 onto the final photograph of each step: (a) 2000–2400 s, (b) 2400–2800 s, (c) 2800–3200 s, and (d) 3200–
255 3600 s.

256 As the groundwater level reached about 75 cm (83 % of ground height), soil particle displacement was
257 observed in the soil from 2000–2400 s. This result indicates that, owing to the strength of the soil, the
258 resistance factor becomes smaller as the model ground is saturated, and the weight of the soil in the saturated
259 region cannot be supported. Since the soil in the upper part of the groundwater level still maintained its
260 unsaturated strength, the downward displacement appeared only in the area adjacent to the groundwater level.
261 There was still no subsidence observed on the surface (Figure 11a).

메모 포함[K34]: Referee comment #2 - 3)

262 From 2400–2800 s, downward displacement towards the slit was observed throughout the soil area. In
263 particular, a larger downward displacement was observed in the inverted triangle region above the slit, which
264 was significantly affected by the inflow of groundwater (Figure 11b). As the groundwater level rose, the
265 matric suction expressed in the unsaturated region of the ground decreased. Therefore, the subsidence on the

메모 포함[K35]: Referee comment #2 - 3)

266 ground surface was also measured from this phase. From 2800–3200 s, the groundwater level reached 80 cm
267 from the bottom (89 % of ground height), and the maximum downward displacement of the entire water
268 supply stage was observed during this phase (Figure 11c). This indicates that infiltration occurs when the
269 groundwater level approaches the ground surface, and the soil structure is no longer supported as there is no
270 longer sufficient matric suction in the ground directly above the groundwater level. After 3200 s, downward
271 displacement occurred continuously throughout the soil area until groundwater level reaches the target level
272 (Figure 11d).

메모 포함[K36]: Referee comment #2 - 3)

메모 포함[K37]: Referee comment #2 - 3)

273 3.3.2 Water drainage stage

274 The water drainage stage of Test 3 was divided into four phases for the analysis: (a) 0–30 s, (b) 30–60 s, (c)
275 60–90 s, and (d) 90–120 s. The displacement increment vectors, incremental volumetric strain distributions,
276 and incremental shear strain distributions of each stage are shown in Figures 12, 13 and 14, respectively,
277 overlaid onto the photograph of the target ground taken at the end of each phase.

278 In the initial phase (0–30 s) of the water drainage stage of Test 3, the groundwater was rapidly discharged
279 into the slit owing to high downward infiltration pressure. As the soil particles escaped along with the
280 groundwater discharge, the upper ground collapsed, forming an anthropogenic sinkhole similar in shape to
281 the punching shear failure (Figure 12a). In the previous tests, the cavities formed up to about 86 % and 89 %
282 of the maximum groundwater level. The shape of the formed anthropogenic sinkhole indicated significant
283 downward displacement (of the soil that had lost strength) towards the slit. The sudden collapse of the ground
284 clogged the slit, which in turn prevented soil discharge. At this time, the shear deformation also showed a
285 tendency to be concentrated around the collapsed soil (Figure 14a). After the soil was completely drained,
286 no significant deformation inside the ground and on the ground surface were observed via the PIV technique
287 and the LVDTs after 30 s, as the matric suction allowed the ground to recover its unsaturated strength.

메모 포함[K38]: Referee comment #2 - 3)

메모 포함[K39]: Referee comment #2 - 3)

288 3.4 Comparative Study

289 To quantitatively analyze the effect of rainfall intensity on ground cavity and sinkhole development, the
290 evolution of the cavity size with time in the water drainage stage was obtained for each test, and the time at
291 which the water was completely drained was also displayed, as shown in Figure 15. For the hydraulic pressure
292 of 45 cm and 70 cm, the time taken for the groundwater to drain completely was 70 s and 90 s, respectively.
293 However, in Test 3, although the groundwater level was higher, the soil collapsed instantly, resulting in an
294 anthropogenic sinkhole, and the time taken for complete drainage was 80 s, which was faster than that in Test
295 2. After the drainage was completed, the cavity sizes measured in Test 1 and Test 2 were 497 cm² (66 % of
296 the final cavity size of 742 cm²) and 1286 cm² (87 % of the final cavity size of 1482 cm²), respectively. In
297 both Tests 1 and 2, the cavity expanded for about 30 s after the drainage was completed, at which time its
298 size tended to stabilize. In Test 3, where the anthropogenic sinkhole occurred, a cavity of 1207 cm² (56 % of

299 the final cavity size of 2171 cm²) was formed after the drainage was completed, after which the cavity
300 continued to expand for approximately 200 s.
301 Table 4 shows the ratio of the weight of the total soil volume to the weight of the discharged soil volume, the
302 volume ratio of the area corresponding to the cavity, and the weight ratio of the loosening zone, respectively.
303 The size and internal density change of the loosening zone were calculated by the following method. (1)
304 After completion of the test, the discharged soil was dried to measure the weight. (2) The weight of the area
305 corresponding to the cavity was calculated by multiplying the calculated volume of the cavity by the initial
306 density of the soil. The soil weight corresponding to the loosening zone was calculated through the difference
307 between the results of steps (1) and (2). (3) The size of the loosening zone was calculated by excluding the
308 area corresponding to the cavity from the area overlapping with the volumetric strain calculated in each step.
309 (4) The internal density change was confirmed using the results of steps (2) and (3).
310 As shown in Table 4, the size and density change of the loosening area were found to be nearly identical in
311 the three tests. On the other hand, as the hydraulic head increased, the weight and volume of the eroded zone
312 and the average width of the cavity relative to the slit width increased linearly. However, recalling the fact
313 that the hydraulic head increased drastically when the rainfall intensity exceeds a certain threshold, it can be
314 inferred that the volume of the discharged soil and the size of the eroded zone may also increase exponentially
315 with rainfall intensity. The threshold value is definitely specific to a given sewer-system. Thus the
316 experimental results of this study suggest that to prevent sinkholes caused by pipe defects, sewage pipe
317 network facilities need to be expanded to inhibit the rapid rise of groundwater levels in preparation for
318 increased torrential rain caused by climate change.

319 **4 Conclusions**

320 In this study, model tests were used to analyze the effects of rainfall intensity on the formation of the eroded
321 zone and the occurrence of sinkholes caused by soil erosions due to groundwater infiltration through pipe
322 defects. The model tests were conducted to simulate the actual site conditions as far as possible by using the
323 soil used around sewer pipe networks and the sewer pipe landfill standards as well as a large-scale soil
324 chamber. The groundwater level was applied to the model tests by setting three hydraulic heads based on the
325 heavy rainfall characteristics of South Korea: (1) heavy rainfall intensity (47 cm hydraulic head); (2) very
326 heavy rainfall intensity (70 cm hydraulic head); and (3) extremely heavy rainfall intensity (90 cm hydraulic
327 head). Throughout the model tests, the groundwater level changes and the ground surface displacements were
328 measured continuously from the start to the end of the tests. In addition, the PIV technique, which can
329 continuously measure and analyze the displacement of the entire ground, was applied to quantify the ground
330 deformation (volumetric strain and shear strain), generation, and expansion of the underground cavity. Based
331 on the results of the three tests, the following observations were drawn:
332 (1) The rainfall intensity considerably affected on the ground deformation during and after a rainfall.

333 (2) Under heavy and very heavy rainfall intensity conditions, no internal soil deformation occurred while the
334 groundwater level was rising. However, under extremely heavy rainfall intensity conditions, ground
335 subsidence was observed. This result indicates that the resistance factor (due to the soil strength parameter)
336 becomes smaller than the sum of the drag force (upward force by infiltration pressure during water supply)
337 and the gravity (downward force) when the rainfall intensity exceeds a certain threshold, which was found
338 to have a hydraulic head between 70 cm and 90 cm under the given system.

339 (3) After heavy rainfall (that leads to the rise of the groundwater level due to the infiltration of groundwater
340 through the sewer pipe defects), the soil was discharged from the area above the slit with the rapid outflow
341 of groundwater, where there was no active restraining pressure. During the formation and development of
342 cavity along with the drop in the groundwater level, the incremental volumetric and shear strains were
343 concentrated in the vicinity of the underground cavity.

344 (4) The height and average width of cavities increased linearly with the applied hydraulic head, and notably,
345 sinkhole opened under extremely heavy rainfall intensity. Referring the previous study which showed the
346 relationship between the hydraulic head and rainfall intensity, the discharged soil and the size of the eroded
347 zone may increase exponentially with rainfall intensity.

348 It should be noted that the hydraulic head-rainfall intensity relationship used in this study is site-specific. The
349 induced hydraulic head under the same rainfall intensity can be different site to site. Nevertheless, the
350 experimental observations of this study confirm the influence of rainfall intensity on the soil erosion near the
351 sewer pipe defects as well as sinkhole occurrence and suggest a necessity of sewage pipe network facilities
352 rehabilitation in preparation for increased torrential rain caused by climate change.

353 **Author contribution**

354 The conceptualization was done by TYK, CKC, and JK planned methodology. TYK performed the analysis
355 using software, and validation was performed by SIW and CKC. JK performed formal analysis. TYK
356 prepared the original draft, while all authors contributed to the review and editing. Visualization and graphics
357 were designed by TYK and JK. SIW and CKC supervised the research work.

358 **Competing interests**

359 The authors declare that they have no conflict of interest

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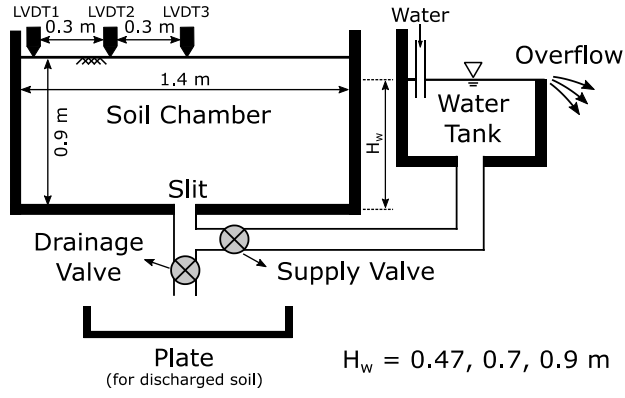
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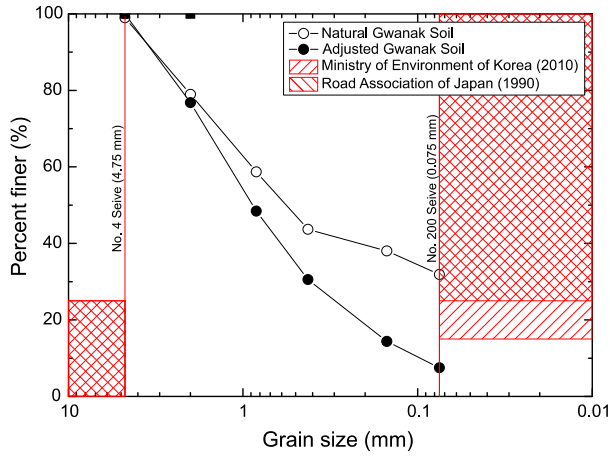
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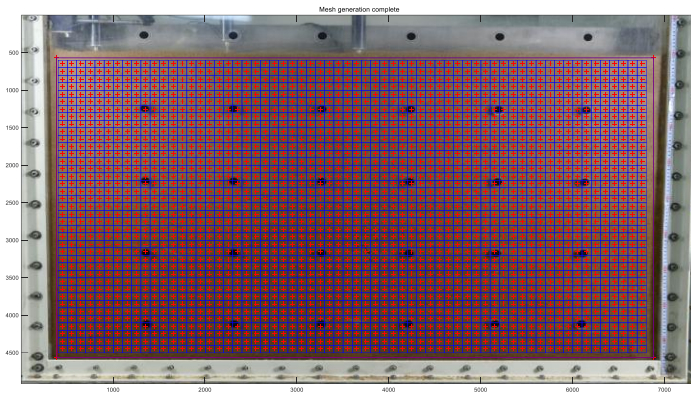
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Figure 1: Schematic of the model test device.



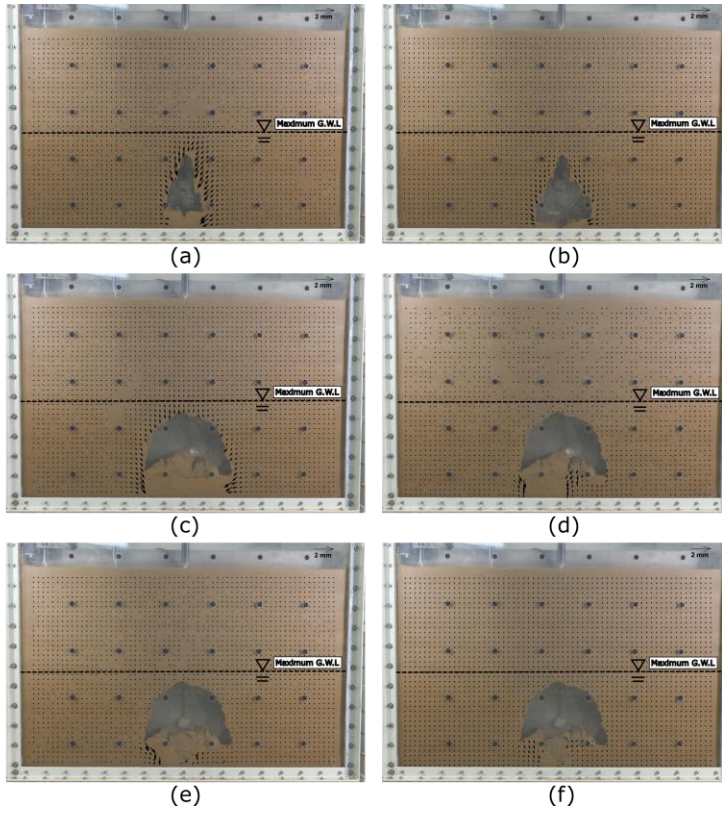
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Figure 2: Grain distribution of the natural Gwanak soil and the Gwanak soil adjusted as per the requirements for backfill materials in South Korea (Ministry of Environment of Korea, 2010) and Japan (Japan Road Association, 1990).



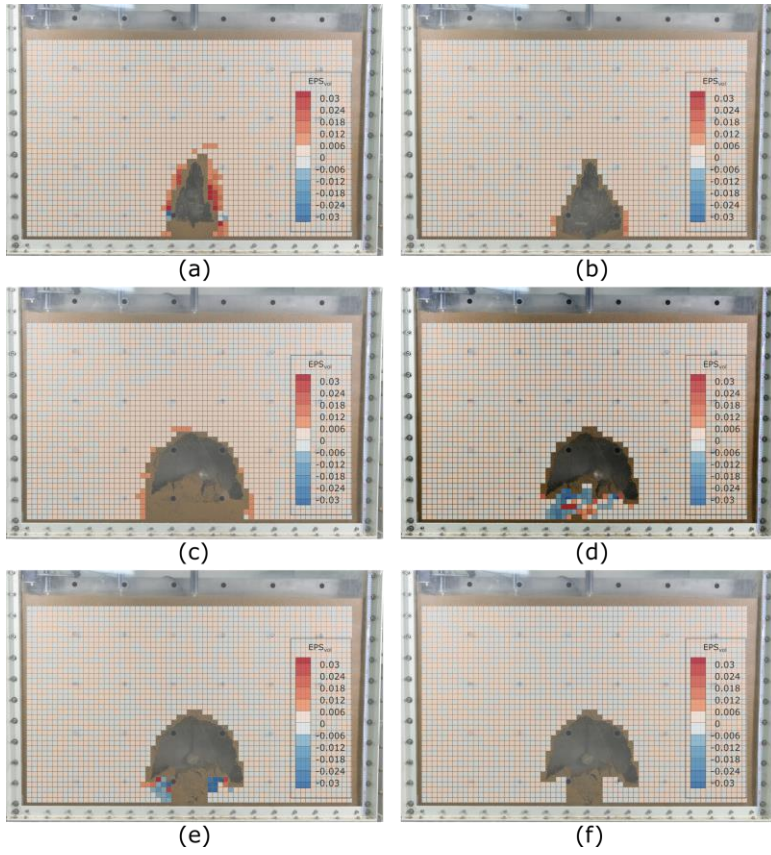
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Figure 3: Selected pixel subsets and center points for digital image analysis.



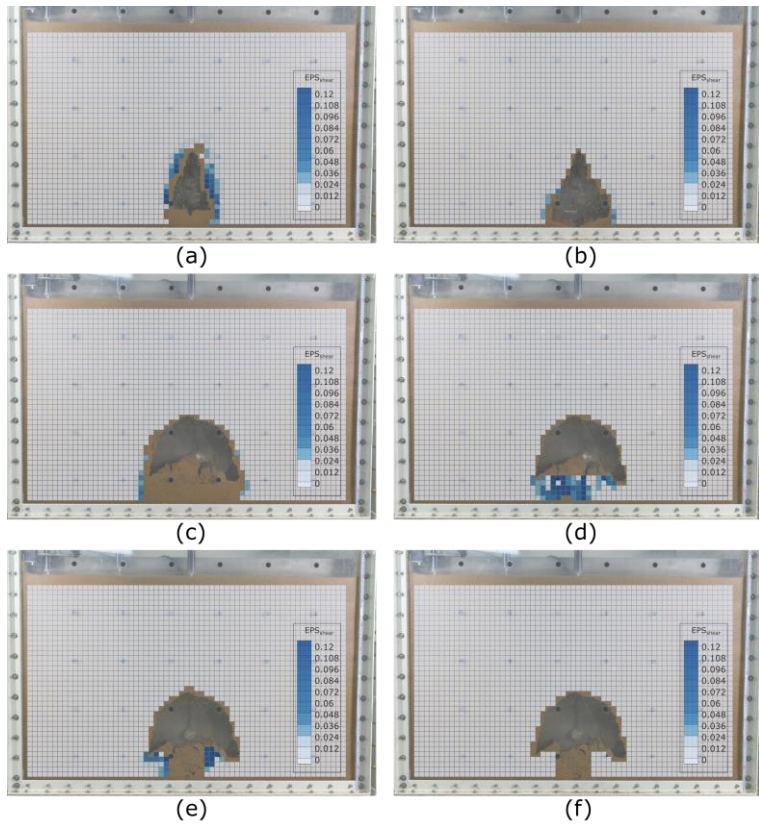
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Figure 4: Displacement increment vectors inside the model ground for Test 1 during the water drainage stage: (a) 0–30 s, (b) 30–60 s, (c) 60–90 s, (d) 90–120 s, (e) 120–150 s, and (f) 150–180 s.



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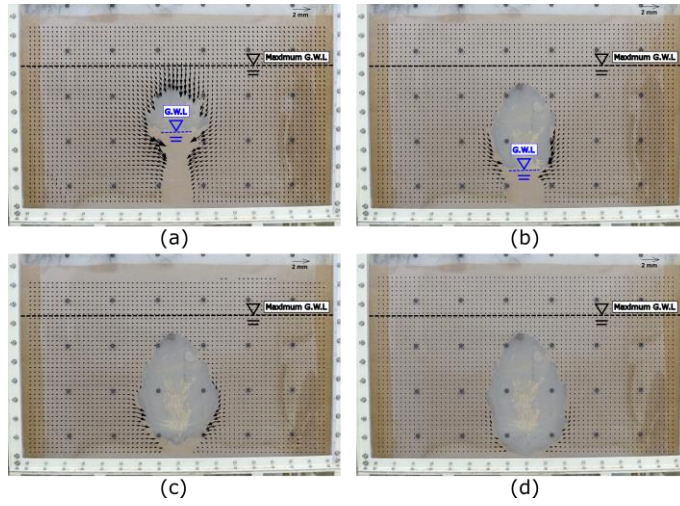
Figure 5: Volumetric strain inside the model ground for Test 1 during the water drainage stage: (a) 0–30 s (b) 30–60 s, (c) 60–90 s, (d) 90–120 s, (e) 120–150 s, and (f) 150–180 s.



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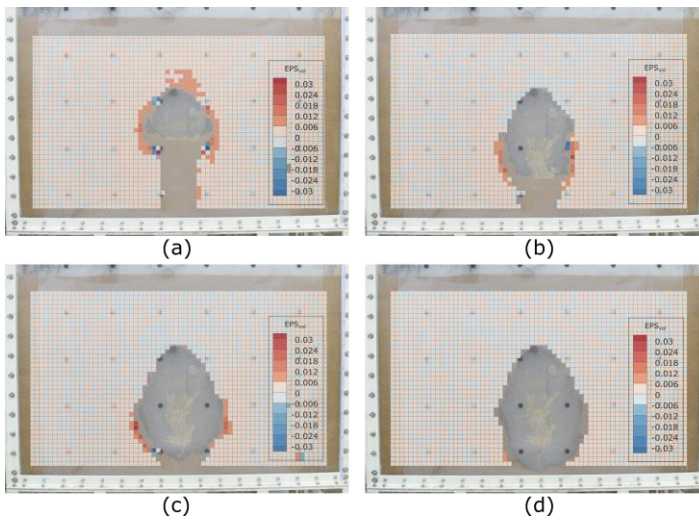
505 **Figure 6: Shear strain inside the model ground for Test 1 during the water drainage stage: (a) 0–30 s, (b) 30–60**
 506 **s, (c) 60–90 s, (d) 90–120 s, (e) 120–150 s, and (f) 150–180 s.**

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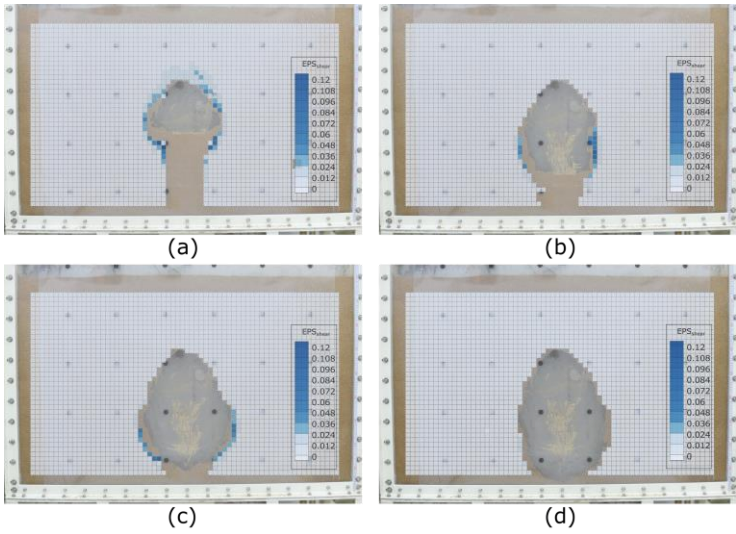
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 509 **Figure 7: Displacement increment vectors inside the model ground for Test 2 during the water drainage stage:**
 510 **(a) 0–30 s, (b) 30–60 s, (c) 60–90 s, and (d) 90–120 s.**

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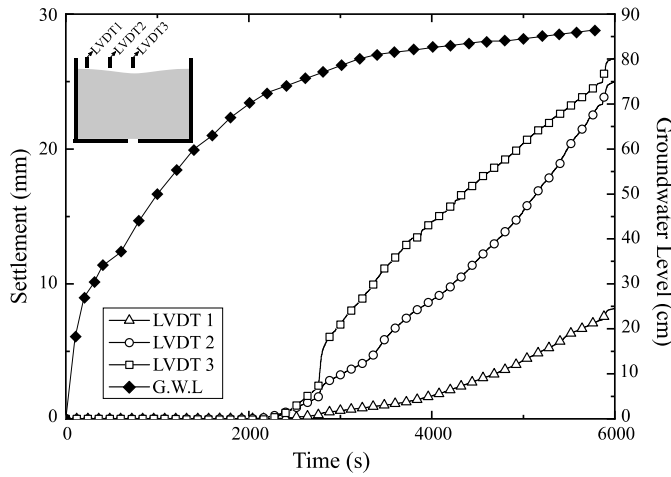
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 513 **Figure 8: Volumetric strain inside the model ground for Test 2 during the water drainage stage: (a) 0–30 s, (b)**
 514 **30–60 s, (c) 60–90 s, and (d) 90–120 s.**

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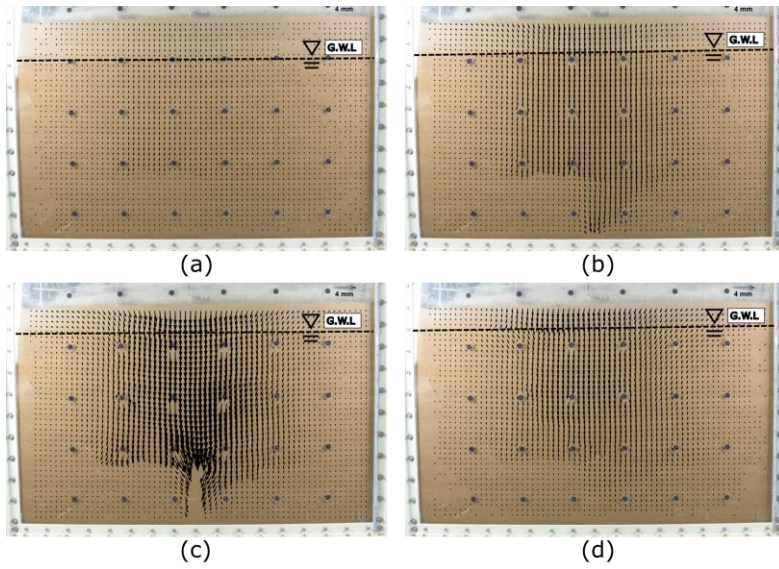
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 517 **Figure 9: Shear strain inside the model ground for Test 2 during the water drainage stage: (a) 0–30 s, (b) 30–60**
 518 **s, (c) 60–90 s, and (d) 90–120 s.**

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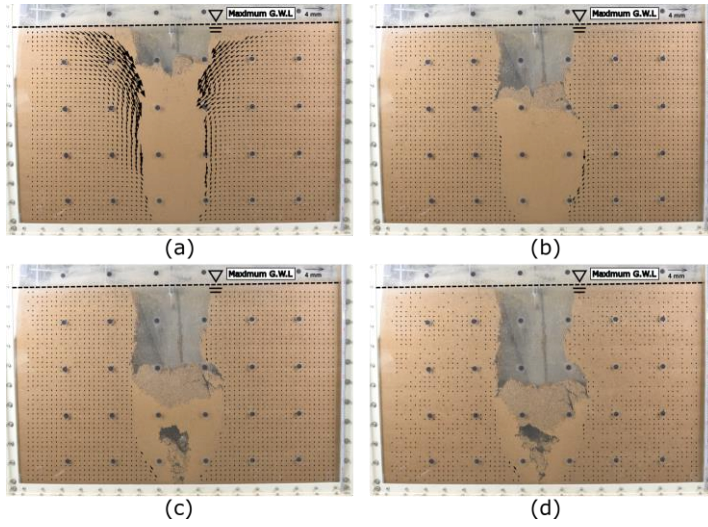
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 521 **Figure 10: LVDT measurement during the water supply stage (Test 3).**

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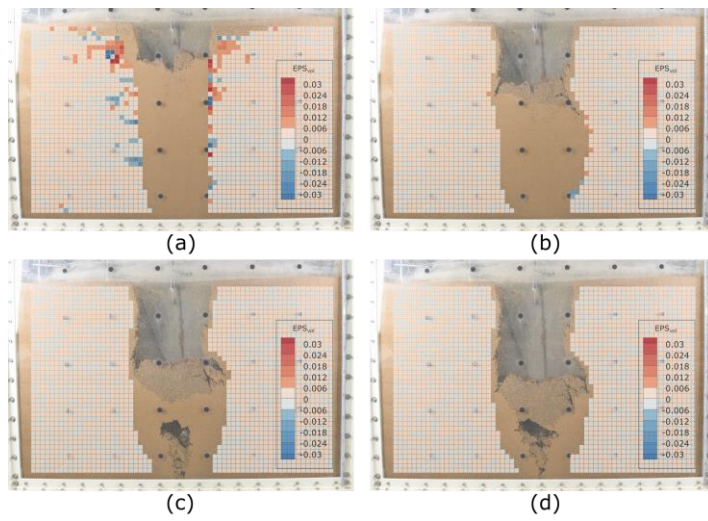
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Figure 11: Displacement increment vectors inside the model ground for Test 3 during the water supply stage: (a) 2000–2400 s, (b) 2400–2800 s, (c) 2800–3200 s, and (d) 3200–3600 s.



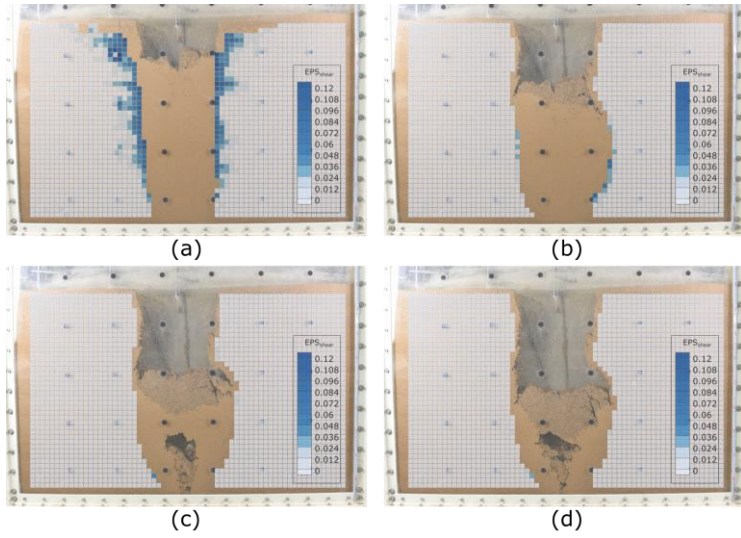
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Figure 12: Displacement increment vectors inside the model ground for Test 3 during the water drainage stage: (a) 0–30 s, (b) 30–60 s, (c) 60–90 s, and (d) 90–120 s.



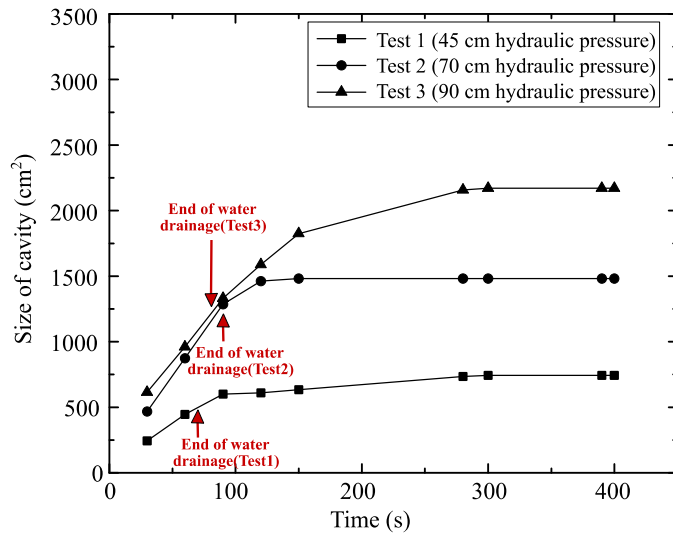
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Figure 13: Volumetric strain inside the model ground for Test 3 during the water drainage stage: (a) 0–30 s, (b) 30–60 s, (c) 60–90 s, and (d) 90–120 s.



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Figure 14: Shear strain inside the model ground for Test 3 during the water drainage stage: (a) 0–30 s, (b) 30–60 s, (c) 60–90 s, and (d) 90–120 s.



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Figure 15: Sizes of cavities developed during the water drainage stage in each test.

540 **Table 1: Relation between rainfall intensity and hydraulic head applied to sewer pipes**
 541 **(National Disaster Management Institute of Korea, 2014).**

Rainfall intensity	Hydraulic head
20 mm/h	33 cm
30 mm/h	40 cm
40 mm/h	47 cm
50 mm/h	70 cm

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543 **Table 2: Properties of adjusted Gwanak soil.**

Description	Adjusted Gwanak soil (Fine content 7.5 %)		
Classification in USCS (Unified Soil Classification System)	SW-SM		
Specific gravity G_s	2.62		
Mean grain size D_{50} (mm)	1.013		
Coefficient of curvature C_c	1.24		
Coefficient of uniformity C_u	12.4		
Standard maximum dry unit weight* $\gamma_{d,max}$ (kN/m ³)	18.5		
e_{max} / e_{min}	0.96 / 0.39		
Void ratio	0.51		
Optimum water content* (%)	11.4		
Strength parameter**	Saturation S 100 %	Cohesion c (kPa)	3.9
		Friction angle ϕ (°)	36.3
	Saturation S 44.2 %	Cohesion c (kPa)	15.8
		Friction angle ϕ (°)	38.3
Saturated permeability coefficient k_{sat} (cm/s)	1.45×10^{-4}		

544 * Estimated from the standard compaction tests

545 ** Estimated from the direct shear tests; S = 44.2 % corresponds to w_{opt} obtained from the standard compaction tests

546 **Table 3: Model test conditions used in this study.**

Test No.	Soil type	Slit size	Degree of compaction D_c (Relative density D_R)	Burial depth	Maximum groundwater level
#1	Adjusted Gwanak soil	2 cm	93 % (78 %)	90 cm	47 cm
#2					70 cm
#3					90 cm

547

548 **Table 4: Comparative studies of the model tests.**

Test	Test 1 (47 cm G.W.L)	Test 2 (70 cm G.W.L)	Test 3 (90 cm G.W.L)
Percentage of the weight of the discharged soil in the total initial weight of the model ground	6.4 %	12.9 %	18.3 %
Percentage of the volume of the eroded zone(cavity or sinkhole) in the total initial volume of the model ground	5.9 %	12.5 %	18.2 %
Ratio of average cavity width* to slit width	11.5 (22.9 / 2 cm)	13.1 (26.2 / 2 cm)	16.4 (32.8 / 2 cm)
Average density change in the loosening zone	-3.1 kN/m ³	-3.7 kN/m ³	-2.9 kN/m ³

549 * Calculated by dividing the cavity size (via Image J software) by the height of cavity.

메모 포함[K45]: Referee comment #1 - 1)
Referee comment #2 - 1)

메모 포함[K46]: Referee comment #1 - 8)