A Dynamic Bidirectional Coupled Surface Flow Model for Flood Inundation Simulation

Chunbo Jiang[1], Qi Zhou[1], Wangyang Yu[1,2], Chen Yang[3], and Binliang Lin[1]

[1]State Key Laboratory of Hydroscience and Engineering, Department of Hydraulic Engineering, Tsinghua University, Beijing, 100084, China
[2]China Institute of Water Resources and Hydropower Research, Beijing, 100038, China
[3]School of Water Conservancy, North China University of Water Resources and Electric Power, Zhengzhou, 450046, China

Correspondence: Wangyang Yu (sea198719@126.com)

Abstract. Flood disasters are frequently threatening people and properties all over the world. Therefore, an effective numerical model is required to predict the impacts of floods. In this study, a dynamic bidirectional coupled hydrologic-hydrodynamic model (DBCM) is developed with the implementation of characteristic wave theory, in which the boundary between these two models can dynamically adapt according to local flow condition. The proposed model accounts both mass and momentum transfer on the coupling boundary and was validated via several benchmark tests. The results show that the DBCM can effectively reproduce the process of flood propagation and also account for surface flow interaction between non-inundation and inundation regions. The DBCM was implemented to the floods simulation occurred at Helin Town located in Chongqing, China, which shows the capability of the model for flood risk early warning and future management.

1 Introduction

Over the past decades, flood events frequently occurred threatening millions of people all over the world, which are driven by global warming, population growth, rapid urbanization and climate change (Zhu et al., 2016). It is reported that the economic loss caused by the floods reaches billions of yuan in China during the period between 1998 and 2016 (Osti, 2017). The capability of predicting and warning of flood events thus plays a significant role in the flood risk assessment and policy-making.

Numerous hydrologic and hydrodynamic models have been proposed to simulate the hydrologic processes and flood propagation (Leandro et al., 2014; Li et al., 2013, 2016; Singh et al., 2015; Yu and Duan, 2014a, b). Specifically, the hydrologic models focus on the water cycle between atmosphere, surface water and soil in a wide range of space and time scales and therefore involve the hydrological processes, such as, precipitation, evaporation, infiltration, etc. On the other hand, the hydrodynamic models solve the mass and momentum equations with a full description of water flow in the study domain, considering water depth, flow velocity, flow duration, etc (Patro et al., 2009; Singh et al., 2015; Yu and Duan, 2014a).It is worthy of noting that the initial conditions and boundary conditions are significant for the hydrodynamic simulations.

Recently, several coupled models have been proposed to combined the advantages of these two types of models and the coupled models can be classified into: the unidirectional coupling model (UCM) (Choi and Mantilla, 2015; Montanari et al., 2009) and the bidirectional coupling model(BCM) (Thompson, 2004; Yu and Duan, 2014a, 2017; Zhu et al., 2016). For the

UCM, the hydrologic model is conducted in the first stage and the obtained results are then employed as boundary conditions for the hydrodynamic model simulations. Since the flow information is transferred in one-way from the hydrologic model to the hydrodynamic model, the UCM is much easier to use than the BCM. McMillan and Brasington (2008) developed a coupled precipitation-runoff hydrological model, and the authors used a 1D dynamic wave equation to assess the flood inundation under several flood return periods. Some other similar models(either open-source or commercial) for the UCM can be found (Hdeib et al., 2018; Liu et al., 2015; Choi and Mantilla, 2015; Grimaldi et al., 2013; Montanari et al., 2009; Rayburg and Thoms, 2009).

Apparently, the UCM cannot fully capture the interaction between the two types of models due to the one-way coupling mechanism. The flood risk may be underestimated if flow information from the hydrodynamic model affects the surface runoff yield by the hydrologic model(Lerat et al., 2012). BCM is one possible solution for this problem, which couple the hydrologic model with the hydrodynamic model and can use rainfall, climate condition, soil distribution and other GIS information as input datasets. In line with this objective, various techniques have been proposed, ranging from simple approach through changing boundary conditions, such as point source or lateral flow conditions (Bouilloud et al., 2010), to relatively complicate models, such as using the simplified 2-D shallow water equations to simulate overland flow instead of traditional hydrologic model (Viero et al., 2014). The coupled MIKE SHE/MIKE 11 modelling system considers the discharge exchange between the hydrologic and hydrodynamic models using river links(Thompson, 2004; Thompson et al., 2004). The flow velocity is proportional to the water surface gradient and the flow is treated as lateral flow for the hydrodynamic model. Thus, the hydrologic model and hydrodynamic model are coupled via the balance of water volume (Bravo et al., 2012; Laganier et al., 2014).

The two types of models, either the UCM or the BCM, still have limitations for the flood simulation and prediction. First, the location of the coupling boundary need to be predefined before conducting the simulation. Though the predefined coupling boundary can improve the computational efficiency, the non-inundation and inundation regions are time-dependent. Second, the flow information transfer is not fully considered in the existing models. The UCM does not consider the feedback from the hydrodynamic model to the hydrologic model and the BCM only consider the water volume exchange between the two models without local velocity and momentum information. For instance, the MIKE SHE/MIKE 11 coupling model computes the velocity at the coupling boundary according to the difference of water depths rather than the velocities obtained in different models, which limits the model only suits for a 1D flow. Therefore, a fully-coupled model considering the velocities computed at different models and the evolutions of coupling boundary is required for more physical and precise simulations.

In this study, a dynamic bidirectional coupling hydrologic-hydrodynamic model (DBCM) has been developed based on the characteristic wave theory. As far as the authors' knowledge, this is the first time the characteristic wave theory is employed to connect hydrologic and hydrodynamic models. The model can automatically evolve the surface flow and fully consider the flow states with both mass and momentum transfer. Section 2 presents the methodology of the proposed DBCM. In Section 3, the model is verified by comparisons between simulations results and analytical results or experimental data. Section 4 shows an application of the model to a real engineering project. Section 5 concludes the paper with remarks..

2 Methodology

The DBCM model combines a hydrologic model including three sub-models i.e. precipitation, infiltration and runoff routing, and a hydrodynamic model involving the 2D shallow water equations for the simulations of channel and overland flows. Both models are solved simultaneously within each time step, and the mass and momentum transfer on the coupling boundary are determined based on the characteristic wave propagation theory which is commonly employed in solving Riemann problems (Toro, 2001).

2.1 Runoff generation

The hydrologic model used in this study is a raster-based distributed model. The runoff yield of a catchment involves precipitation and infiltration while the overland flow is modelled using the 2D diffusion wave equations. The precipitation is interpolated from rainfall stations data and infiltration is computed by solving the Green-Ampt equation. The Green-Ampt equation is shown as follows.

$$f_p = K_s(1 + \frac{(\theta_s - \theta_i)S_a}{F_c}),$$ (1)

where f_p is the infiltration rate(mm h^{-1}), K_s is the hydraulic conductivity(mm h^{-1}), S_a is the average effective suction of the wetting front (mm), θ_s and θ_i are saturated and initial soil moisture content respectively (%), F_c is the cumulative infiltration amount (mm). This equation is well-known and widely used since it can reflect the runoff yield conditions for both saturated storage and excess infiltration(Rawls et al., 1983).

2.2 Diffusion wave approach

Since the conceptual models for the surface flow cannot provide detailed information about the water movement over the entire basin (Rallison and Miller, 1982), the diffusion wave equations (Bates and De Roo, 2000) are used to determine the runoff routing, which are composed of mass conservation equation and momentum equations:

$$\frac{\partial h}{\partial t} + \frac{\partial q_x}{\partial x} + \frac{\partial q_y}{\partial y} = Q_m,$$ (2)

$$Q_x = \frac{A_x R_x^{0.67} S_x^{0.5}}{n},$$ (3)

$$Q_y = \frac{A_y R_y^{0.67} S_y^{0.5}}{n},$$ (4)

where q_x,q_y are unit discharge along the x and y direction(m^2 s^{-1}), h is the water depth(m), Q_m equals to the rainfall rate minus the infiltration rate (m s^{-1}), Q_x,Q_y are the flow rate in the direction of x and y (m^3 s^{-1}), respectively, A is the flow area (m^2), R is the hydraulic radius (m), S is the water surface gradient, and n is the roughness coefficient.

Compared to gravitational and frictional effects, the influence of acceleration and inertial terms of overland flow is negligible (Chen et al., 2012; Hsu et al., 2000). Time dependent terms in the original momentum equations is omitted and thus obtain the diffusive wave equations. The numerical scheme can be found in the JFLOW model (Bradbrook, 2006; Yu and Duan, 2014b,

2017). The full shallow water equations are reduced to the diffusive wave equations by omitting the time dependent terms. The flow velocity only depends on the local water surface gradient and roughness, and the water depth determines by water volume balance and discharge from the neighbour grids. As shown in Fig.1a, the possible flow at one cell is linked to two adjacent cells at each time step.

$$Q_i = \frac{wh^{5/3}S_i}{n(S_i^2 + S_j^2)^{1/4}}, Q_j = \frac{wh^{5/3}S_j}{n(S_i^2 + S_j^2)^{1/4}}, \tag{5}$$

where

$$S_i = \frac{\eta_{i,j} - \eta_{i\pm1,j}}{w}, S_j = \frac{\eta_{i,j} - \eta_{i,j\pm1}}{w}, \tag{6}$$

$$h_i = \eta_{i,j} - max(z_{i,j}, z_{i\pm1,j}), h_j = \eta_{i,j} - max(z_{i,j}, z_{i,j\pm1}), \tag{7}$$

$$h = \frac{h_iS_i^2 + h_jS_j^2}{S_i^2 + S_j^2}, \tag{8}$$

where w is the width of the cell, S_i, S_j are the water surface slopes in the orthogonal direction of i and j, respectively, h_i, h_j are the effective depths in orthogonal direction of i and j, respectively, $\eta_{i,j}$ and $z_{i,j}$ are the water surface level and the ground elevation(m), respectively, and h is the effective depth. The change of water depth in each of cell is then calculated using the following equation:

$$\Delta h = \frac{(\sum Q_{in\,i,j} - \sum Q_{out\,i,j} - Q_m)\Delta t}{w}, \tag{9}$$
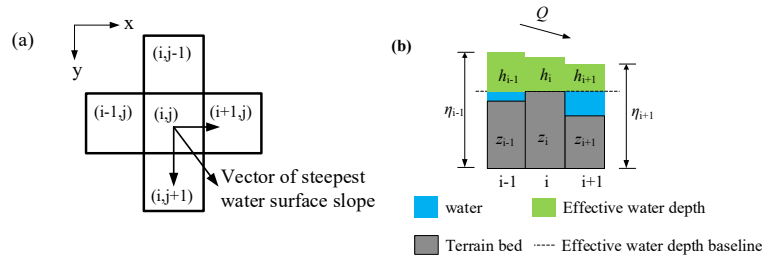
Figure 1. typical grid and water depth definition

2.3 Hydrodynamic model

The 2D shallow water equations are the most widely used in the hydrodynamic models for the inundation simulations(Bradbrook et al., 2004; Yu and Duan, 2014a, 2017). Neglecting the Coriolis force, wind resistance and viscosity, the equations are composed of the continuity equation

$$\frac{\partial h}{\partial t} + \frac{\partial hu}{\partial x} + \frac{\partial hv}{\partial y} = Q_m, \tag{10}$$

and the momentum equations

$$\frac{\partial hu}{\partial t} + \frac{\partial}{\partial x}(hu^2 + \frac{1}{2}gh^2) + \frac{\partial}{\partial y}(huv) = -gh\frac{\partial z}{\partial x} - C^2 u\sqrt{u^2 + v^2}, \tag{11}$$

$$\frac{\partial hv}{\partial t} + \frac{\partial}{\partial x}(huv) + \frac{\partial}{\partial y}(hv^2 + \frac{1}{2}gh^2) = -gh\frac{\partial z}{\partial y} - C^2 v\sqrt{u^2 + v^2}, \tag{12}$$

where u,v are velocities along the x and y direction(m s^{-1}), respectively, h is water depth(m), g is gravity acceleration (m s^{-2}), z is bottom elevation(m), C is Chezy coefficient representing roughness, Q_m is the source term which equals to rainfall rate minus infiltration rate (m s^{-1}).

These equations are solved using the finite volume method similar to TELEMAC(Ata et al., 2013), and the convection flux is calculated using the HLL scheme with WAF approach (Toro, 2001).

$$F^{hll} = \begin{cases} F_L & S_L \geq 0 \\ \frac{S_R F_L - S_L F_R + S_L S_R (U_R - U_L)}{S_R - S_L} & S_L \leq 0 \leq S_R \\ F_R & S_r \leq 0 \end{cases}, \tag{13}$$

$$S_L = U_L - \sqrt{gh_L}, S_R = U_R + \sqrt{gh_R},$$

where U_L, U_R, h_L, h_R are the components of the left and right Riemann states , respectively for a local Riemann problem, and S_L, S_R are estimations of the speeds of the left and right waves respectively, and F^{hll} is the fluxes in the star region. Using this flux, the WAF method of a second-order accuracy in time and space is achieved:

$$F_{i+\frac{1}{2}} = \sum_{k=1}^{N+1} \beta_k F_{i+\frac{1}{2}}^{(k)}, \tag{14}$$

$$\beta_k = \frac{1}{2}(c_k - c_{k-1}), c_k = \frac{\Delta t S_k}{\Delta x}, c_0 = -1 \ and \ c_{N+1} = 1,$$

where $F_{i+\frac{1}{2}}^{(k)} = F(U^{(k)})$, N is the number of waves in solving of the Riemann problem, and β corresponds to the differences between the Courant numbers c_k of successive wave speeds S_k.

The topography term on the right side of equation 11 and 12 is calculated by the hydrostatic reconstruction scheme:

$$-gh\frac{\partial z}{\partial x} = \nabla\frac{gh^2}{2} = \frac{g}{2}\frac{\Delta t}{\Delta x}[(h_i^R)^2 - (h_i^L)^2], \tag{15}$$

$$\begin{cases} h_i^R = max[0.0, h_i + z_i - max(z_i, z_{i+1})] \\ h_i^L = max[0.0, h_i + z_i - max(z_{i-1}, z_i)] \end{cases},$$

The friction term is computed by a semi-implicit scheme to ensure numerical stability(Liang et al., 2007):

$$(hu)^{n+1} = \frac{(hu)^n}{1 + \Delta t\left(\frac{g\sqrt{(hu)^2 + (hv)^2}}{h^2 C^2}\right)^n}, \tag{16}$$

The time step is determined under the CFL condition as follows.

$$\Delta t = C_r min \left(\frac{\Delta x_i}{|u_i| + \sqrt{gh_i}}, \frac{\Delta y_i}{|v_i| + \sqrt{gh_i}} \right) \tag{17}$$

where C_r is Courant number, limited by $0 < C_r \leq 1$ for simulation stability, and a typical value of 0.9 is used for the following simulation cases. More details of the numerical schemes can be found in Ata et al. (2013).

2.4 Coupling approach

The computation domain in the DBCM is divided into non-inundation and inundation regions, and the diffusion wave equation(DWE) is solved in the non-inundation regions with small water depth while the hydrodynamic model(SWE) is applied in the inundation regions with high water depths. The model for a specific grid is determined based on its local and neighbouring flow states. The boundary between the non-inundation regions and inundation regions forms a dynamic coupling boundary which is time dependent. Besides, special treatment on discharge through the coupling boundary need to be taken based on the local flow state using the characteristic theory.

The adopted models for different regions are based on the temporally evolving flow statuses. They leads to the change in coupling boundary positions. As shown in Fig.2, when the rainfall intensity increases, the inundation region expands as a consequence of the gradually accumulating of surface water volume from upstream regions. The position of the in-flow boundary, flow path and discharge change subsequently. The coupling models proposed by other researchers, either UCM or BCM, did not fully consider this phenomenon.
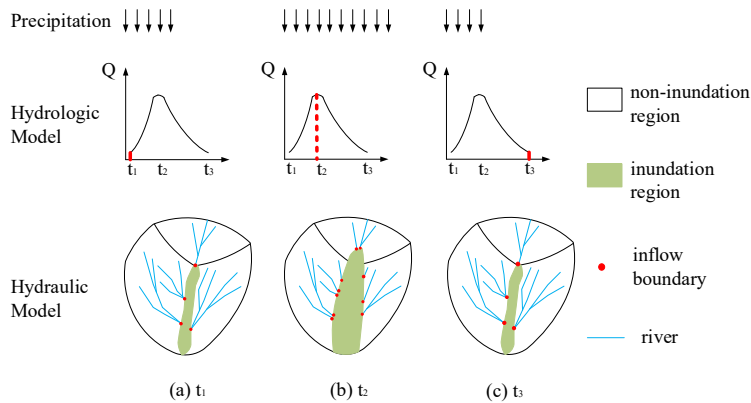
Figure 2. Schematic diagram of DBCM

Figure 3 shows a detailed process of flow state change on both sides of the coupling boundary. For the case in Fig.3a , the discharge on the coupling boundary equals to the upstream discharge and not affected by the downstream flow, which means that the local discharge is completely determined by the DWE. After the water depth is updated, the location of the coupling boundary point O moves to point A according to the comparison of its water depth to the water depth threshold. Moreover,

the flow in the inundation region may move from downstream to upstream, as shown in Fig.3b. The discharge and water depth on the coupling boundary should be determined using the flow information on both sides. In this case, the coupling boundary moves to point B due to inundation area expanding.
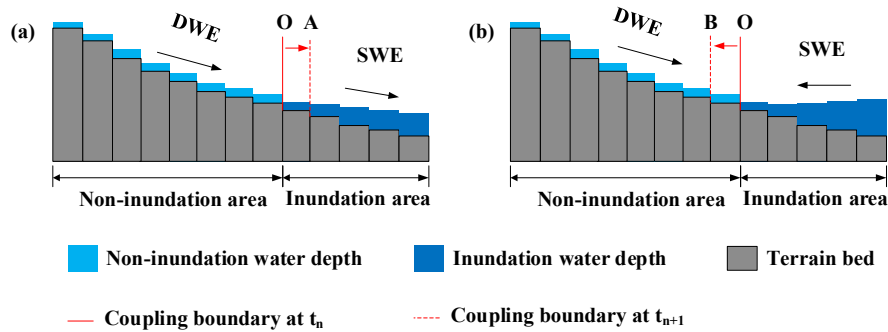
Figure 3. Flow state change and position of the coupling boundary

In previous studies, the discharge on the coupling boundary may be computed directly through the hydrologic model, using empirical formulae, or by interpolation approaches according to the water level or velocity gradient on both sides. Such methods may fail to provide an overall understanding of the flow regime status of the combined hydrologic and hydrodynamic model. In using the DBCM, the following procedures is conducted at the coupling boundary: the flow state is obtained by both the hydrologic and hydrodynamic models in their local grids, then the discharge through the coupling boundary is computed and the entire water depth is updated according to the water volume variation. After that, the location of the coupling boundary is updated and the area of the non-inundation region and inundation region are remapped. The key issue using the DBCM is to establish a reasonable approach to determine the discharge on the coupling boundary, which should integrate the effect of current flow state obtained by the two models on both sides of the coupling boundary.

According to Godunov theory(Godunov, 1959), the solution of convective flux implementing the finite volume method can be considered as a local Riemann problem. The discontinuity characteristics speed between each grid represents the propagation of local fluid variables in time and space, as shown in Fig.4. When the characteristic speeds are all positive, the flux depends entirely on the left-side flow state, and vice versa. However, when the characteristic speeds have a negative value and a positive value, both the current flow state in the two grids must be taken into consideration. Applying this approach to DBCM, the computational scheme at the boundary can be specified. It is known that the hydrologic model only transfers water mass, while the hydrodynamic model transfers both water mass and momentum. More details of the different coupling cases are shown Fig.5.

For the first case in Fig.5a, the hydrologic and hydrodynamic models are calculated independently, corresponding to the situation that positive bed slopes inducing confluence flows into the river, thus only the discharge calculated by the hydrological model passes through the coupling boundary (Fig.3a). The flow information in grid k and i is calculated using DWE and grid j using SWE, see Fig.5a. Firstly, a slope analysis of DWE is conducted uniformly. Obviously the water level gradient between
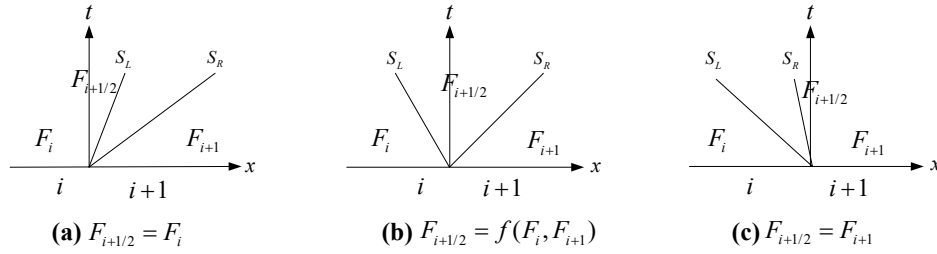
Figure 4. Direction of Characteristic wave

grid k and grid i is smaller that that between grid i and grid j. According to the calculation results from the DWE, the velocity points to the direction with the maximum water level slope(in Fig.1a, flow directs to right). Therefore, the change of water depth in grid k has nothing to do with the flow state at grid i, and the velocity change at grid k is analysed by the other grids on the left of grid k. The flow information at grid i and j forms a local Riemann problem and then the characteristic speed is analysed. The velocity at grid i is obtained from the above analysis, and the velocity at grid j is the velocity at the current moment. The water depths at discontinuity interface are calculated as: $h_i^r = h_i + z_i - max(z_i, z_j)$, $h_i^l = h_j + z_j - max(z_i, z_j)$. Thus a pair of characteristic wave at the interface are obtained:

$$S_L = u_i - \sqrt{gh_i^R}, S_R = u_j + \sqrt{gh_j^L}, \tag{18}$$

When the characteristic speeds $S_R \geq S_L > 0$, the flux calculation depends on the flow information at grid i, independent of grid j. The velocity at grid i is calculated using diffusion wave equations and only outflow is allowed. In addition to the water depth change calculated according to the hydrodynamic model at grid j, the water volume transferred from grid i should also be added. No convection term in the momentum equation of DWE indicates no momentum transfer between grid i and j, and thus the velocity values of the two grids do not interact with each other.
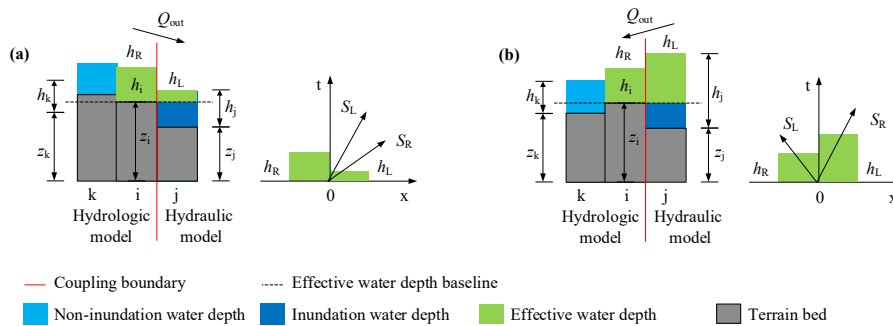
Figure 5. Coupling conditions, discharge on coupling boundary depends on (a) hydrologic model and (b) both hydrologic and hydrodynamic models

For the second case in Fig.5b, the hydrological model and hydrodynamic model are both used, corresponding to the situation when the inundation area expands(Fig.3b). As shown in Fig.5b, the water depth in grid k and grid i are small, thus the hydrologic model is applied. While grid j has a deep water depth and high water elevation, the hydrodynamic model is applied. In this case, the velocity direction is from grid i to grid k. The characteristic wave analysis at the interface of grid i and grid j reveals that $S_R > 0 > S_L$, which means that the momentum at grid j can be transferred to grid i. Grid i is involved in the computational domain of the hydrodynamic model. The water depth increment at grid i needs to deduct the current discharge output to grid k and the flow rate obtained by solving the hydrodynamic equation with the flow state at grid j. The velocity increment at grid i is obtained by solving the hydrodynamic equation with the flow state at grid j based on current velocity. Then the flow state at grid i is updated and the coupling boundary position may change when the depth varies.

The slope gradient analysis and characteristic wave analysis are key issues of the computational theory for solving DWE and SWE respectively. The key to couple these two approaches is to successfully address the connection on the coupling boundary. As discussed earlier, in existing studies only one governing equation is solved throughout the computational domain, but cannot to consider the interaction between the two kinds of governing equations and to resize the area of a different computational domain. A reasonable and implementable approach in coupling the solution procedure of DWE and SWE is the precondition for establishing DBCM. In this study, the slope gradient analysis is performed to determine the current velocity together with the current water depth, and the characteristic wave analysis is conducted on coupling boundary as long as flow velocity and depth have been provided, no matter it is calculated from the hydrologic or hydrodynamic model. Then, the flow information exchange on the coupling boundary is determined according to the characteristic speed which reflect the propagation of flow state in time and space. This method integrates the hydrologic model and hydrodynamic model into a comprehensive system by means of joining the two steps of slope gradient analysis and characteristic wave analysis.

In the proposed DBCM, the coupling boundary position will not keep fixed in advance throughout the calculation process. The location where the runoff enters the inundation region varies dynamically, and the flood level can also submerge the original inflow points and regenerate new coupling boundaries. Such alternation mechanism is close to natural flow processes. The characteristic wave theory is used to determine the mass and momentum exchange through the coupling boundary. Compared to the "cascade" operation in UCM, the present DBCM solves DWE and SWE simultaneously. When non-inundation regions get larger, the flow movement is mainly obtained by utilizing DWE. Whereas, when the inundation regions extend, the computational domain is given priority to SWE.

3   Model validation

The numerical model results from DBCM are compared with analytical solutions, experimental data, and results obtained from existing numerical models. Considering the complexity of the numerical model schemes used in the hydrologic and hydrodynamic models, the hydrodynamic model performance will be validated in the first stage, and then the performance of DBCM will be verified using a V shaped catchment. As described in 2.2, the numerical schemes of the hydrodynamic model (referred to HM2D in the following section) used in this study have second-order accuracy in both time and space.

3.1 Oblique hydraulic jump

The oblique hydraulic jump example is a special flow pattern, with an analytical solution being available in open channel flows, which is often used to verify the capability of the numerical schemes in simulating shock wave formation. When a supercritical flow is deflected by a converging wall at an angel θ, the resulting shockwave forms an oblique hydraulic jump at an angle β, as depicted in Fig.6. Both the angles of water surface lines behind the shock wave-front can be obtained by analytical solution. In this study, the upstream flow water depth and velocity are set as 1m and 8.57m s^{-1}, and the oblique angle $\theta = 8.95°$. The width and length of channel are 30m and 40m respectively. In these conditions, the exact analytical solutions are downstream water depth $D_A = 1.49984$m, downstream velocity $V_A = 7.95308$ m s^{-1}, and angle $\beta = 30°$ (Rogers et al., 2001) when the flow reaches a steady state. The spatial step size is set as $\Delta x = \Delta y = 0.33$m. The time step is dynamic adjusted and the total
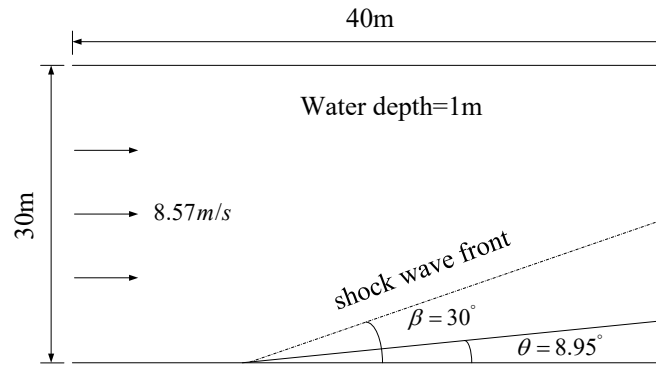
Figure 6. Oblique hydraulic jump: definition sketch

calculation time is 90s. Figure 7 shows a 3-D view of the water depth of results predicted by our model. The oblique jump is sharply captured, and has an angle $\beta \approx 32°$. The average water depth downstream behind the shock front is 1.532m, and the average velocity is 7.86m s^{-1}. The numerical solution is close to the analytical solution, as shown in Table 1. The output of HM2D and the references, either the water depth or velocity, show good agreement(see Table 1).

Table 1. Comparison between analytical solution and calculation result for oblique jump case

	Angle β	Water depth(m)	Velocity(m s^{-1})	Depth error(%)	Velocity error(%)
Analytical solution	30°	1.49984	7.95308	-	-
HM2D results	32°	1.532	7.86	2.1	1.2
Reference results	30°	1.53	7.9	2.0	0.6
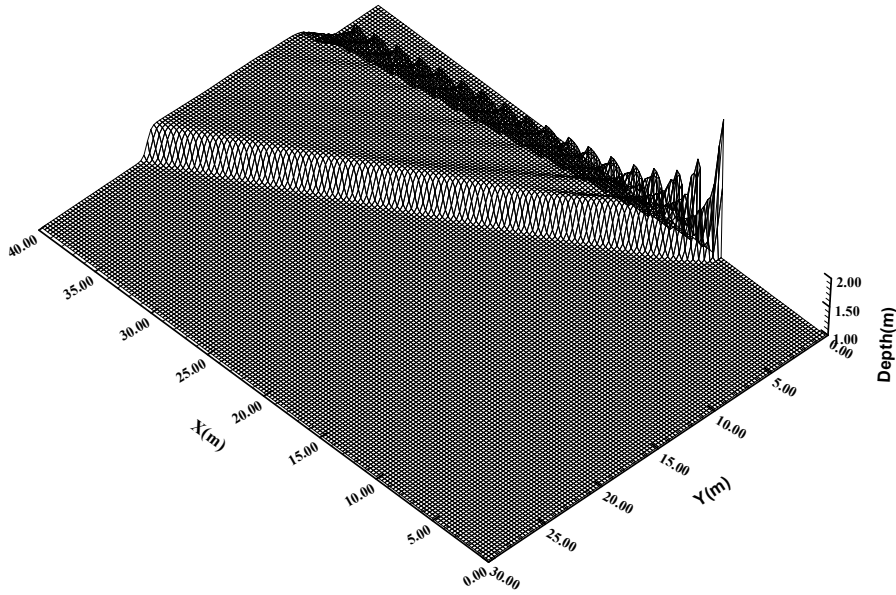
Figure 7. Steady state of water depth of oblique hydraulic jump

3.2   Dam-break over a dry flood plain

235   Dam-break is a classic benchmark problem, which is often used to verify the capability of a numerical scheme in dealing with the dry-wet boundary, and the physical experimental model is easy to conduct. Thus, it is convenient to collect experimental data for comparison with numerical results. The experiment performed by Fraccarollo and Toro (1995) was used to validate the DBCM developed in this study. The model domain is 3m×2m, which is separated into two areas by a dam at $X = 1$m. Initially, the still water with a depth of 0.64m in the reservoir is surrounded by solid walls, while the downstream area is initially dry.

240   The boundaries of the downstream floodplain were all open. A 0.4m wide section in the middle of the dam was breached instantaneously. The numerical model spatial step is $\Delta x = \Delta y = 0.04$m, and roughness coefficient is $n = 0.01$.

Figure 8 shows the water surface elevation at different times. It can be clearly seen that the bore wave propagate toward downstream initiallly. A depression wave travels upstream, which is reflected back at the walls surrounding the reservoir, causing the water surface elevation in the reservoir to oscillate. In Fig.9, a comparison between the measured and the computed

245   data is made, which shows a good agreement. The results are encouraging and the overall trend is well captured.

3.3   Two-Dimensional surface flow over a tilted V-shaped catchment

A two-dimensional surface flow over a tilted V-shaped catchment is simulated (Di Baldassarre et al., 1996; Panday and Huyakorn, 2004). We aim to verify whether the computational domains of the hydrologic and hydraulic models can dynami-
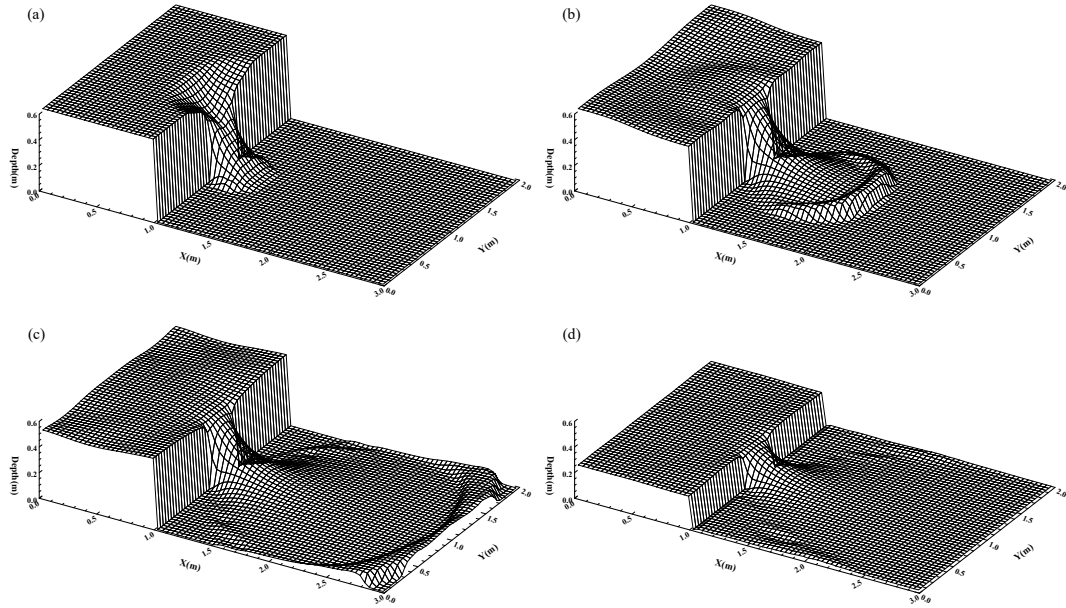
Figure 8. Snapshot of the water elevation for dam-break simulation: a. t=0.1s; b. t=0.5s; c. t=1.1s; d. t=5.0s

cally switch and compare the difference between DBCM, UCM and BCM. As shown in Fig.10, the topography of the example
is depicted.

The computational domain is symmetrically V-shaped, with a pair of symmetrical hillslopes forming a channel at the central
region. The bed slopes are ±0.05 spanwise, and 0.02 streamwise parallel to the channel. The manning coefficient on the
hillslope is 0.015 while it is 0.15 in the main channel. The total simulation time is 180min and the constant rainfall intensity is
10.8 mm h^{-1} for 90 min. Fig.10 shows the detailed dimension and related information of the V-shaped catchment.

Considering the hydrodynamic model provides more details to describe the overland flow than the hydrologic model, the
HM2D and DBCM under the same rainfall conditions were adopted. When water depth is less than 0.005m, the grid is calcu-
lated using the hydrological model, and when water depth is greater than 0.005m the grid is applicable to the hydrodynamic
model. Results are compared with numerical models developed by Di Baldassarre et al. (1996), Panday and Huyakorn (2004).

As shown in Fig.11, the discharge hydrographs obtained by the HM2D and DBCM are compared with other existing models.
The discharge hydrographs show good agreement for the peak discharge. The start periods of discharge rising and receding
limbs simulated by HM2D and DBCM are consistent with those predicted by others. However, discrepancies gradually grow,
and both the HM2D and DBCM slightly under-predict the discharge. Despite this disparity, the overall trend of the hydrographs
indicates that the proposed models are satisfactory.

Comparing the hydrographs between the HM2D and DBCM, it can be seen that their rising limb and peak discharges
agree very well. Cosequently, both these hydrodynamic models are used to simualte the overland flows. The difference be-
tween HM2D and DBCM gradually emerges at the receding limb. The HM2D simulates water movement using hydrodynamic
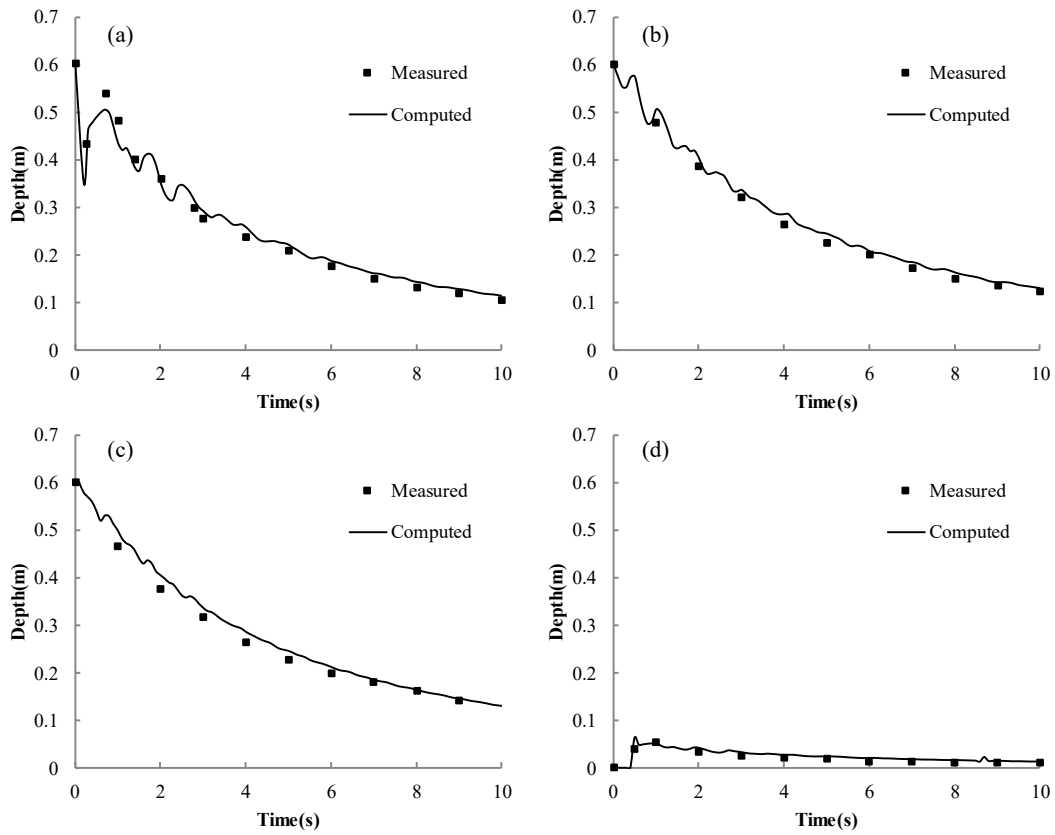
Figure 9. Comparison of water depth variation at four locations: a. x=1m. y=1m; b. x=0.18m, y=1m; c. x=0.48m, y=0.4m; d. x=1.802m, y=1.45m
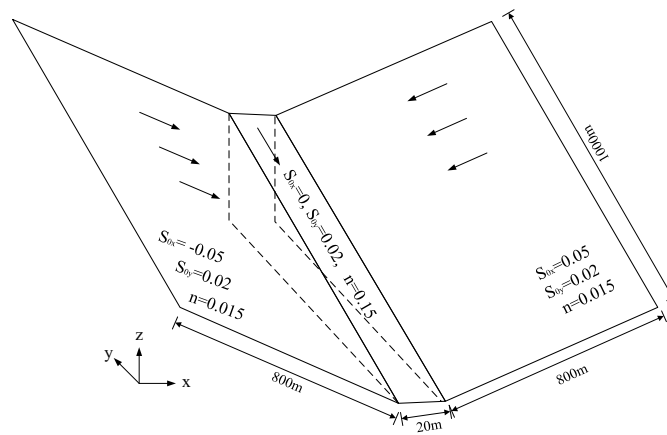
Figure 10. Diagram and dimension of the tilted V-shaped catchment

model(SWE) throughout the computation process, while the DBCM switches from the hydrodynamic model to the hydrologic model(DWE) when the upstream water depth falls below the threshold. Since no time partial derivative terms in the hydrologic model, the velocity at the present is a function of the current water level gradient, and is not equal to the velocity at the previous moment plus the flux term. For this reason, when the DBCM switches from the hydrodynamic model to the hydrologic model, and the velocity calculation approach changes accordingly, then the discharge difference between the HM2D and DBCM emerges. Therefore, the outlet flow is slightly larger, but later slightly smaller, in the DBCM, assuring overall the mass is conserved.
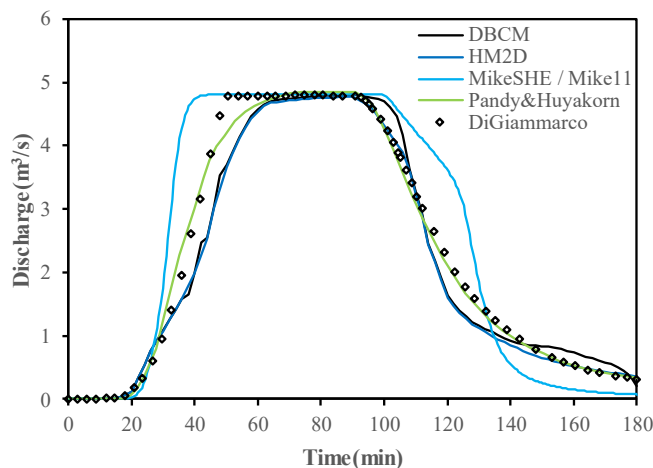
Figure 11. Comparison of discharge hydrographs of the V-shaped catchment

In order to make a detail performance between DBCM and BCM, the coupling model of MIKE SHE and MIKE 11 was used to conduct the comparison with the proposed DBCM. The coupling between MIKE SHE and MIKE 11 is achieved using the line segments termed by river links (Thompson et al., 2004). Water can exchange between MIKE 11 H-points and adjacent MIKE SHE river links and in this way the bidirectional coupling between the two models is realized. The coupling use the overbank spilling option, when water level is over the river bank top elevation, then the overland flow to the river is added to MIKE 11 as lateral inflow. One the contrary, when the water level in the river is higher than that of overland flow, the water from the main river will spill into the MIKE SHE cell and become part of the overland flow. However, the MIKE SHE river links and MIKE 11 H-points are pre-processed before the simulation starting which means they are determined automatically and keep fixed during the simulation, and the flow information between them using the method of interpolation. Besides, MIKE SHE only exchange water volume with the coupled reaches and keep water balance in river links, which is not the case in actual rainfall events for the water exchange should always be dynamical and successive.

Figure 12 shows the comparison of water depth profile(y=500m) between DBCM and MIKE SHE/MIKE11. It can be found that water depth show small difference on the overland slope. Flood propagation is a phenomenon of high-speed movement resulting a drastic change of water depth and velocity. The hydrologic model (DWE, omitting convection term) is insufficient

to describe this movement. However, the water depth near the outlet presents difference of the two models. In the early 30min, the water depth from DBCM was lower than the water depth form MIKE SHE/MIKE11 model. After that till to the end of the simulation, the water depth from DBCM was higher that the water depth from MIKE SHE/MIKE 11 model. The increasing of water depth around the channel leads to strong convective flow, thus the momentum transfer needs to be taken into consideration in order to get reasonable simulation results. However, the momentum transfer is not taken into account in the MIKE SHE/MIKE 11 coupling model.

Flow discharge of the centre channel is shown in Fig.13. It can be found that discharge in the channel obtained by DBCM is much lower than that obtained by MIKE SHE/MIKE 11 coupling model. This is due to the difference of coupling mechanism and flow information exchange. Flow can be only exchange between the finite river links and H-points, and flow from overland can accumulate around the river links which leads to relative increasing of flow discharge. In terms of the DBCM, the flow can exchange water information including both mass and momentum with the dynamical coupling boundary. The coupling mechanism of DBCM shows accordance with natural physical process of flood formation and propagation.

The spatial variability of the flow depth, velocity and flux at 90 min and 120min are shown in Fig.14 and Fig.15.For the DBCM, the main difference between the governing equations used by the hydrologic model and hydrodynamic model is that the flux term is not calculated in the former, meanwhile the latter needs to calculate the convection term. The non-inundation region and inundation region can be determined by whether the flux term is generated during the calculation process. When t=90min, the rain stops, the water depth reaches its peak value and the flow information is determined by the hydrodynamic model over the whole domain. At t=120min, the water continues to flow to the outlet and the water volume near the upstream region decreases, but a small amount of water still exists. No flux is calculated while velocity computation continues. Obviously, a sharp division line separating the domain arises at this moment.

For the DBCM, the coupling boundary between DWE and SWE is time-dependent. Fig.16 shows the evolvement of the coupling boundary. During the first 90min, rainfall keeps constant over the whole catchment and water depth arises in a short period. As a result, the water depth in most part of the domain is above the depth threshold and SWE was implemented in these regions. However, 90min later, the rainfall stops and no extra water flow into the domain. Then, the water depth begins to decrease. Once the depth is lower than the depth threshold, the grid cell use DWE to determine the discharge as well as water depth and the coupling boundary shrinks (see Fig.16). The evolution of coupling boundary is consistent with the flux analysis stated above. It is well known that solving the SWE costs numerous computational resources and time, which limits its application, especially for large scale simulation. In terms of this small scale V-shaped catchment, the simulation performance between the SWE, DBCM and DWE was conducted. Fig.17 shows the result and the simulation time was used by the SWE(100%). It can be seen that both the DBCM and DWE need less simulation time compared to SWE, for DWE nearly 15% simulation time saved. Whereas, the DBCM alters the SWE and DWE according to the local flow information. Compared with SWE, the simulation time of DBCM was only slightly lower than the SWE due to that in the early half simulation time in this V-shaped catchment most of the flow information is calculated by the SWE as discussed in the above section (Fig.16).
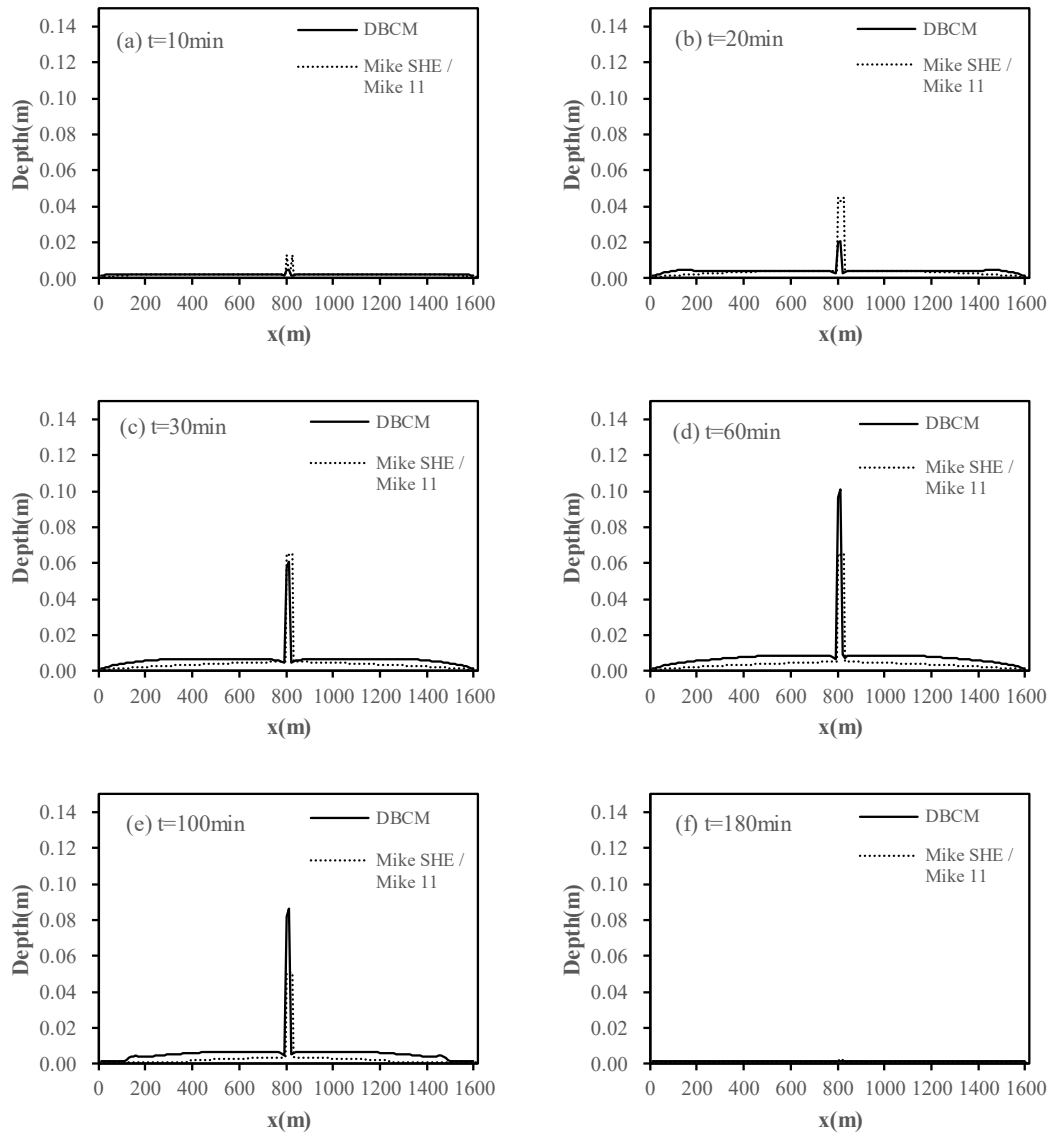
Figure 12. Comparison of water depth profile between DBCM and MIKE SHE/MIKE 11 at the downstream catchment (y=500m)
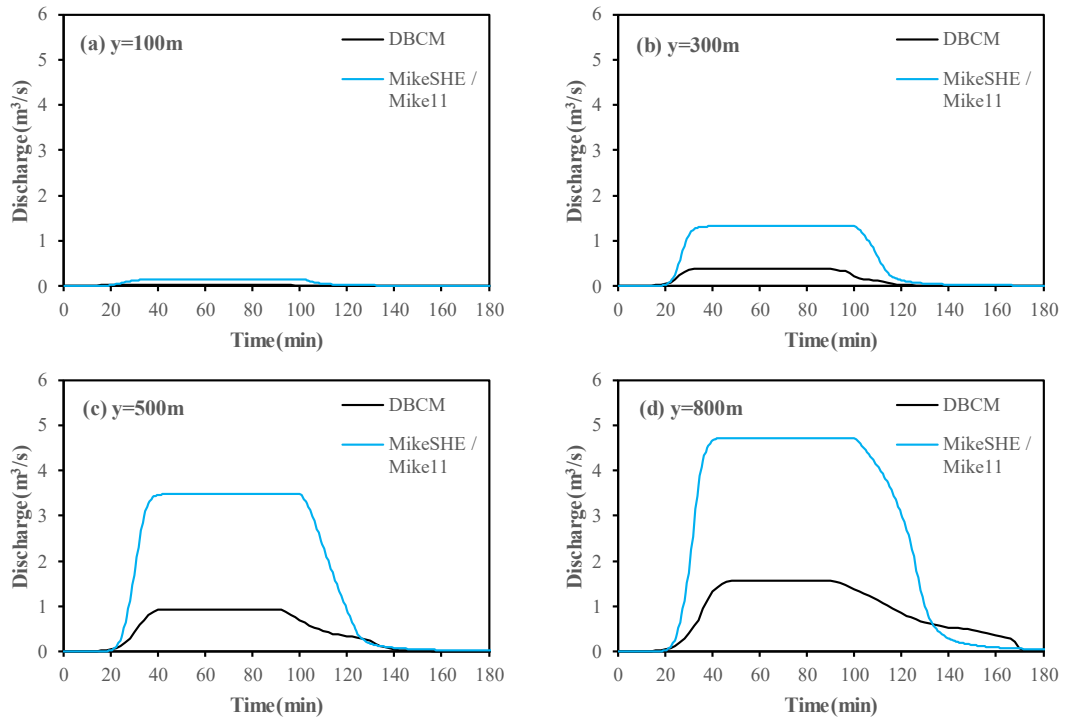
Figure 13. Discharge processes in the centre channel
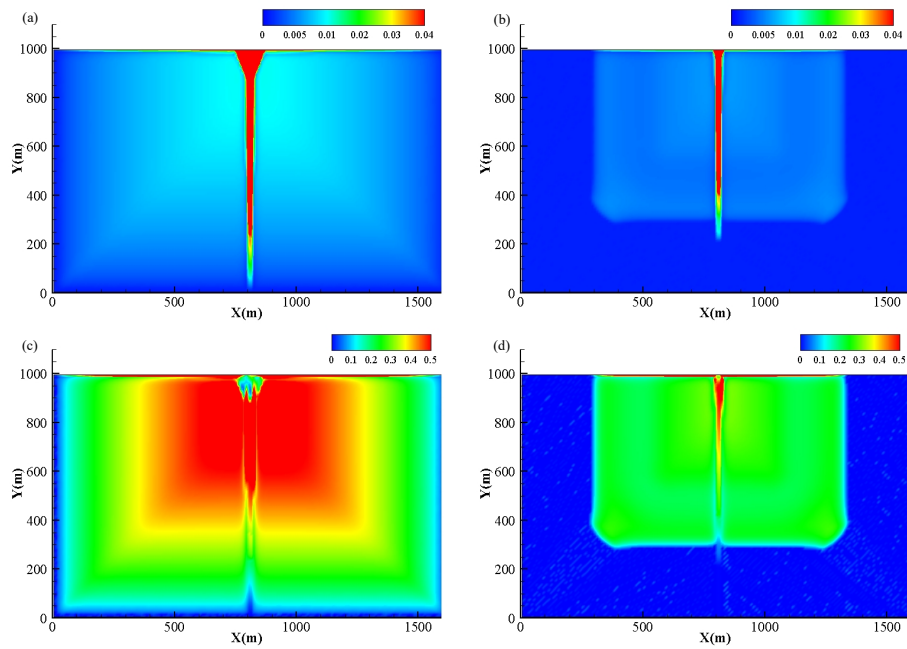
Figure 14. Water depth and velocity distribution at 90min(a and c) and 120min(b and d)
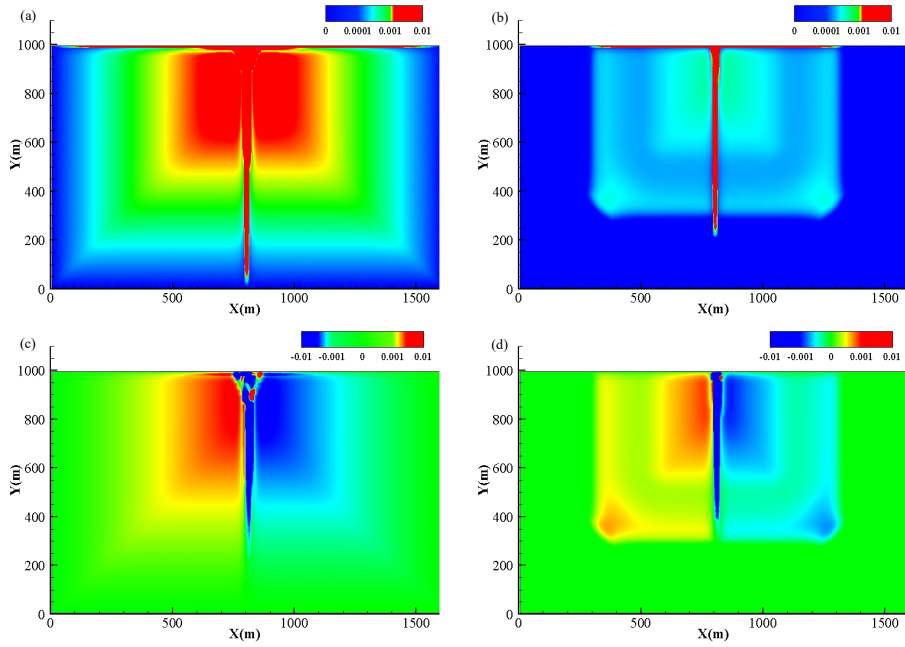
Figure 15. Flux distributions of in X and Y direction at 90min(a and c) and 120min(b and d)
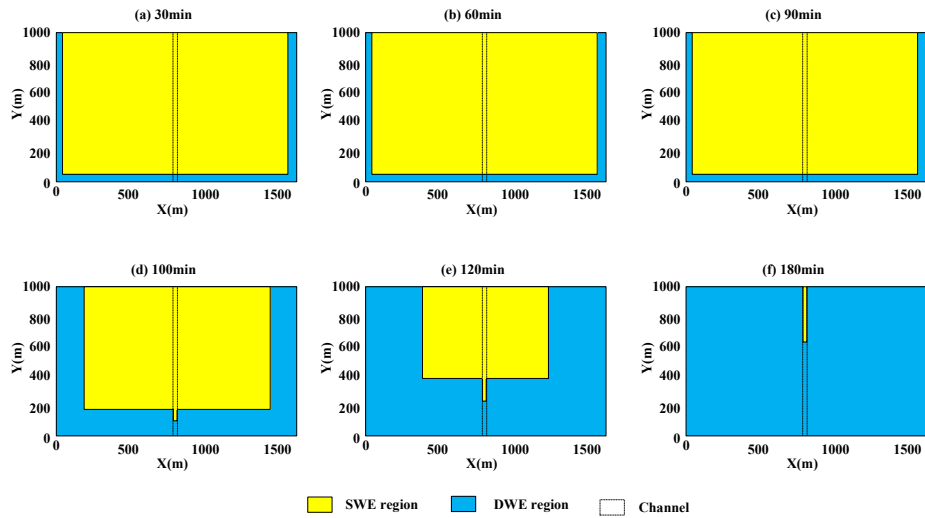
Figure 16. Evolvement of coupling boundary
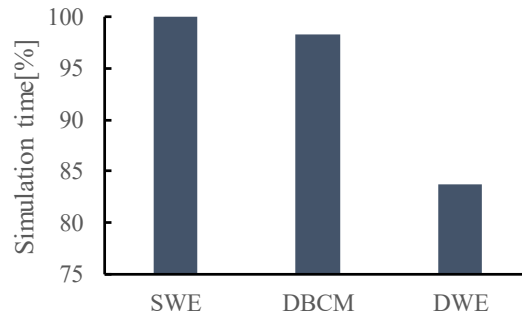
Figure 17. Comparison of water depth profile in the channel outlet

4 DBCM implemented to a natural watershed

The proposed DBCM was implemented to a natural watershed for flood risk assessment, that is, Helin town of Longxi River in Chongqing City, China. The Longxi river basin is located in the eastern region of Chongqing(see Fig.18), which is a first-class tributary of the Yangtze River. It is about 221km long with a catchment area about 3280km^2. The overall terrain gradually goes down from northeast to southwest, consistent with the trend of the main channel. Most of the central and southwest areas are relatively flat, and the east and west areas are mountainous, a typical topography of a trough sandwiched by two mountains. The average annual rainfall in the basin is 1192.4mm, which is prone to heavy rain in summer, and the flood spreads rapidly to the central district due to the topographic feature. The selected catchment, Helin town, located in the northeast of the Longxi river basin, was chosen as a case study for investigating the surface flow phenomena using the DBCM. The administrative location and DEM information of Helin town is shown in Fig.18.
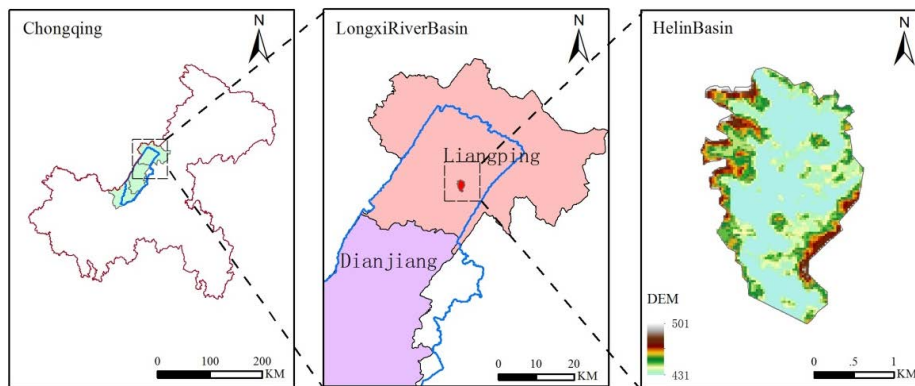
Figure 18. Location of Helin town. Chongqing City(left), Longxi river basin (middle), Helin basin(right)

The river section in Helin basin is a typical mountainous river. The upper part of the river has a steep slope, while the middle and lower reaches are relatively gentle. At present, no flood protection works exist on the river banks along the main

channel. The terrain along the river is relatively plain, and farmlands widely distribute around the main stream, resulting in the poor ability to resist flood disasters. Once heavy rainfall occurs and flow overtops the river banks, the residential area and

335   farmland along the river will be inundated. Floods in Helin town are always caused by heavy rainstorms, and the flood season is consistent with the rainstorm season which lasts from April to September. Heavy rainstorms and flood often occur during this period.

The input datasets for the DBCM include the DEM, the LULC(land use and land cover) and soil type as shown in Fig.18 and Fig.19. DEM data were obtained from the GDEMV2 database with a spatial resolution of 30m. The DEM was resampled

340   according to field survey datasets of the channel section in order to obtain fine resolution topography. Four main kinds of land use types involves in the Helin basin: urban, forest, farmland and water. Besides, several soil types with small proportion have been consolidated into the categories with large proportion. Soil properties determine the infiltration rate, which further affects the surface runoff. The parameters, such as roughness and soil moisture content, are extracted from the data provided by local administrative sectors. The LULC data are processed by remote sensing interpretation tools using the satellite image. The soil data are processed by SWAT, Soil-Plant-Air-Water (SPAW) model using the Harmonized World Soil Database (HWSD).
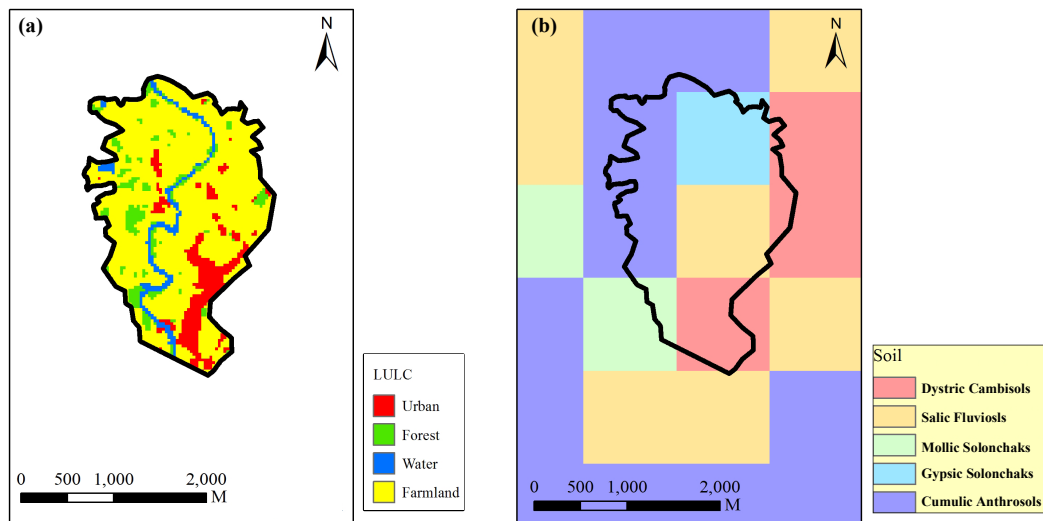
Figure 19. LULC and Soil of Helin basin

345

The DBCM was applied to simulate the rainfall runoff process in the Helin town and was compared with a UCM composed of SWAT(as the hydrologic model). The SWAT was calibrated by the design storm and hydrographs (flood return period of 1%) in the Helin town outlet. The selected coefficients and parameters of rainfall and flood event are listed in Table 3 and Table 4. The calibration results are shown in Fig.20. It can be seen clearly that the flooding process calculated by the SWAT model

350   is very similar to the design flood, with similar flood peak flow and fluctuation process. At the beginning of the simulation, because of the soil infiltration, no surface runoff although the rainfall exists for a short time. However, when the soil saturated, the discharge curve climbs rapidly which is consistent with the rainfall intensity. The simulation result reflects the storm runoff

production process affected by the combination of precipitation process and infiltration process. The hydrographs show good agreement with the design flood, demonstrating that results from the SWAT are reliable for the hydrodynamic model. Once being calibrated, the hydrographs generated by the SWAT at different locations were extracted and applied as inflow boundary conditions for hydrodynamic models. Two simulation scenarios were designed, as shown in Table 2.

Table 2. Simulation scenarios

Case	Model	Boundary condition	Descriptions
A	HM2D	Helin outflow as inflow BC	SWE
B	DBCM	Helin inlet flow	Coupling DWE and SWE

Table 3. Rainfall parameters (Cs: coefficient of skewness; Cv: coefficient of variation; P: flood recurrence period)

Duration(h)	Mean value(mm)	Cv	Cs/Cv	P(%)			
				1.0	2.0	5.0	10.0
6	81.7	0.5	3.5	**224**	197	162	137
24	112	0.48	3.5	**297**	263	218	183

Table 4. Peak discharge at Helin outlet for different flood frequency

P(%)	**1.0**	2.0	5.0	10	20	50
Discharge(m^3 s^{-1})	**2280**	1920	1470	1150	831	433

The results obtained in Case A and Case B are compared to investigate the capability of the DBCM. Fig.21 depicts the maximum water depth distribution. The inundation region has expanded significantly in Case B. Not only the lowland areas, but the hillsides also have been inundated. Even though Case A adopted the simulated outlet hydrographs larger than that Case B, the runoff failed to inundate the hillside because of the topographic feature. The red cycle in Fig.21 indicates the urban area. Water depth was extracted for each case. Due to the lack of measured data, field survey and historical records have to be used as reference data to verify the model outputs. Several problems involved in the current river topographic conditions: both sides of the river are flat, with a lot of farmland and some villages distributed along the main river. No embankments or bank protection works have been built along the river. All of these problems lead to a low flood control capacity. As local residents recall, in 2017, the flood covered the middle of the trees along the river bank, equivalent to at least 3m water depth. In terms of the urban area, according to the historic record, the rainstorm in 12 August 1998 caused a flash flood that made the local streets and airports inundated with a water depth of 1.0m and 1.4m respectively. All villages and towns around Helin town catchment were submerged with water depth exceeding 0.5m on average. In Case B, this phenomenon was simulated and it was found that the maximum water depth in urban areas was more than 0.6m, in accord with the historic data. But no water emerged in Case A, although the Helin outlet flow is utilized as inflow discharge, greater than that of Case B, as shown in Fig.22. Referring to
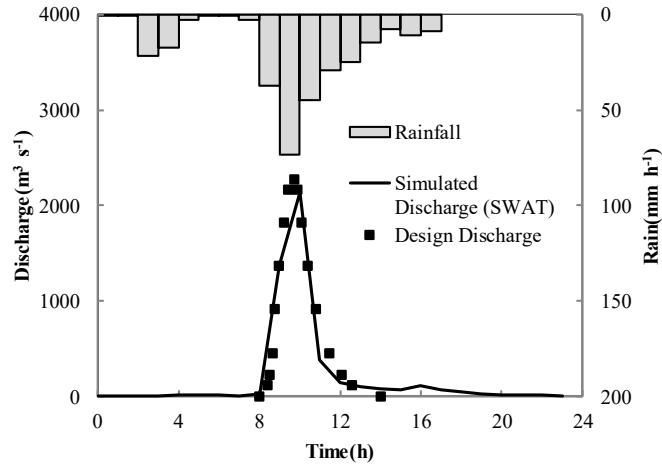
Figure 20. Design rain and flood with calculated flow in Helin basin outlet(1%)

local topography, the main reason for this issue is that the urban areas locate in a higher position, between riverbed and hillside, hence the upwelling movement of water in rivers is easily blocked due to local terrain. Nevertheless, the urban area will be submerged by uphill surface flow, even though the river flow has been obstructed. It can be seen that the computed results of Case B by the DBCM are closer to the practical situation.
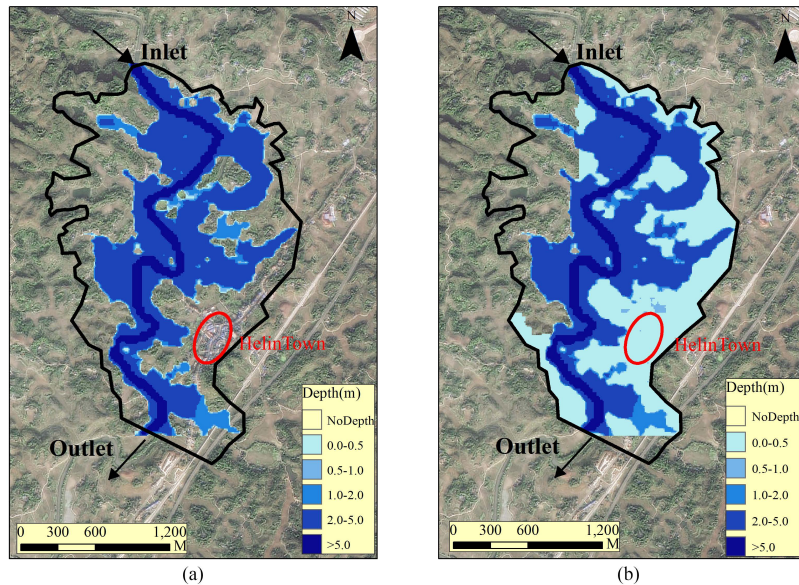
Figure 21. Comparison of maximum depth, (a)case A, (b)case B. Red circle denotes location of Helin town(Satellite imagery base map was obtain from Google Earth)

375   In DBCM, the coupling boundary is time-dependent, and the grid cells on each side solve different model (whether DWE or SWE). The water depth threshold (0.01m) is used to distinguish the two models in this case. Flux calculation was only conducted within SWE cells, since there is no need of flux information for DWE cells. As shown in Fig.24, the rainfall stopped 17h later, and then the surface flow on the slope gradually decreased. However, a small amount of water is still left within the sloping area where the grid cells information was solved by DWE. Thus, even though the flux calculation has stopped, flow
380   velocity still exists in most part of the slope areas. The low-lying area on the northeast corner, due to the obstruction of the terrain, cannot be flooded in Case A. However, using the DBCM, the confluence of the surrounding slope accumulated to the local area and form a small range of flooded area.

Figure 23 shows the evolvement of coupling boundary of the DBCM in Case B. In the early 8h, rainfall intensity was small (see Fig.19), and most amount of the runoff were infiltrated to underground. Thus, the surface flow were determined by SWE
385   with the upstream inflow. After that, rainfall began to increase, and runoff started to generate surface flow using the DWE. The region of SWE continued to extend until the inundation area reached a maximum value. And then, the area began to shrink with the receding of rainfall.
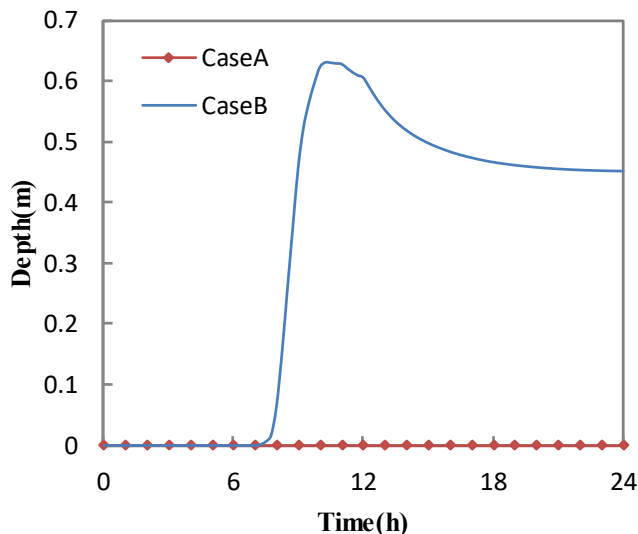
Figure 22. Comparison of water depth variation

5   Conclusions

A dynamic bidirectional coupling model (DBCM) for surface flow inundation simulation has been developed. In DBCM, the
390   runoff production is depicted by the hydrologic model through the rainfall-runoff process, while the hydrodynamic model is used to simulate the flood propagation processes. The characteristic wave theory is applied to determine the coupling boundary between the hydrologic and hydrodynamic computational domains.

(a) t=1h **(b) t=6h** **(c) t=9h**

(d) t=12h **(e) t=18h** **(f) t=24h**

SWE region DWE region Dry region
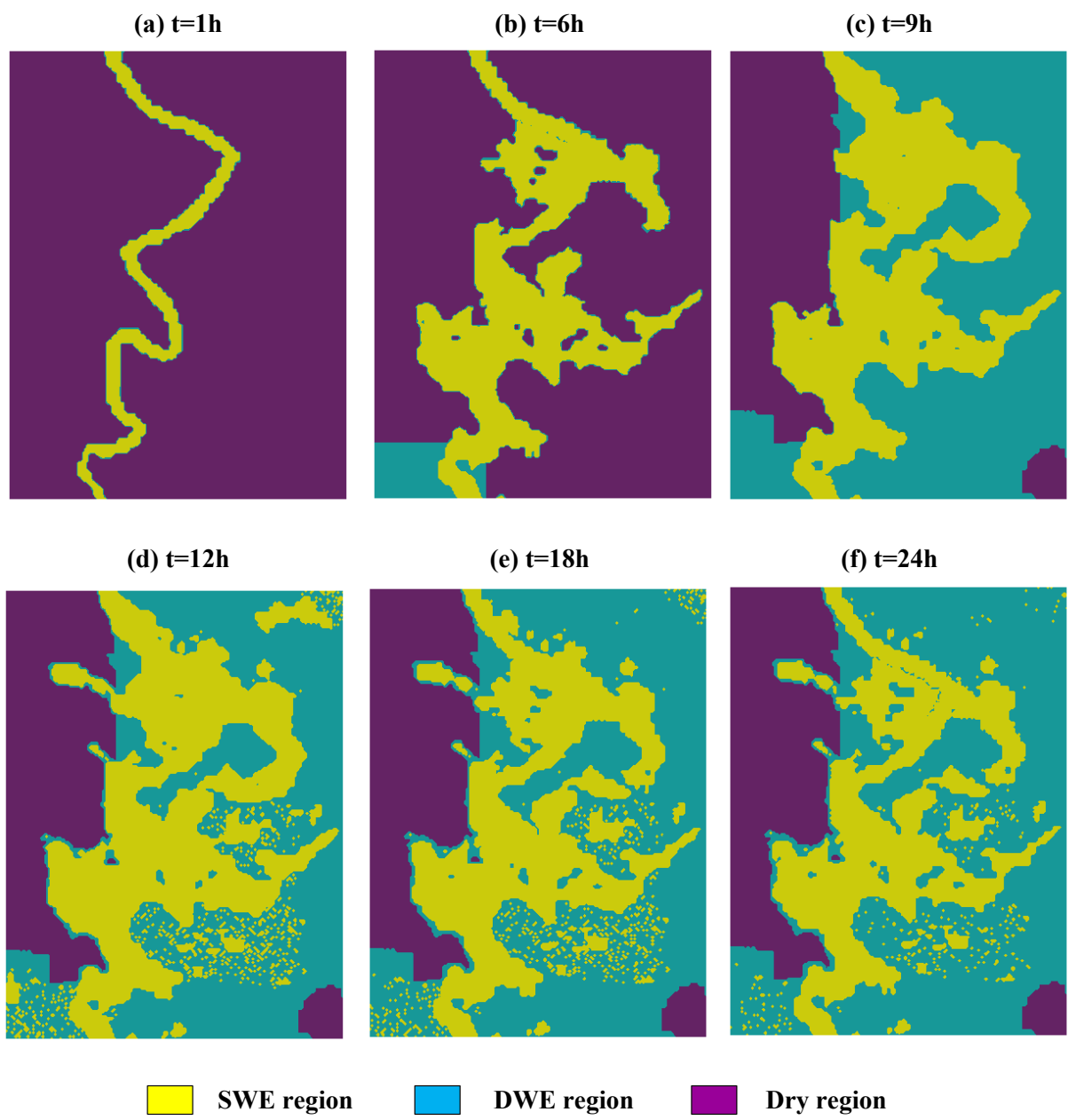
Figure 23. Evolvement of coupling boundary
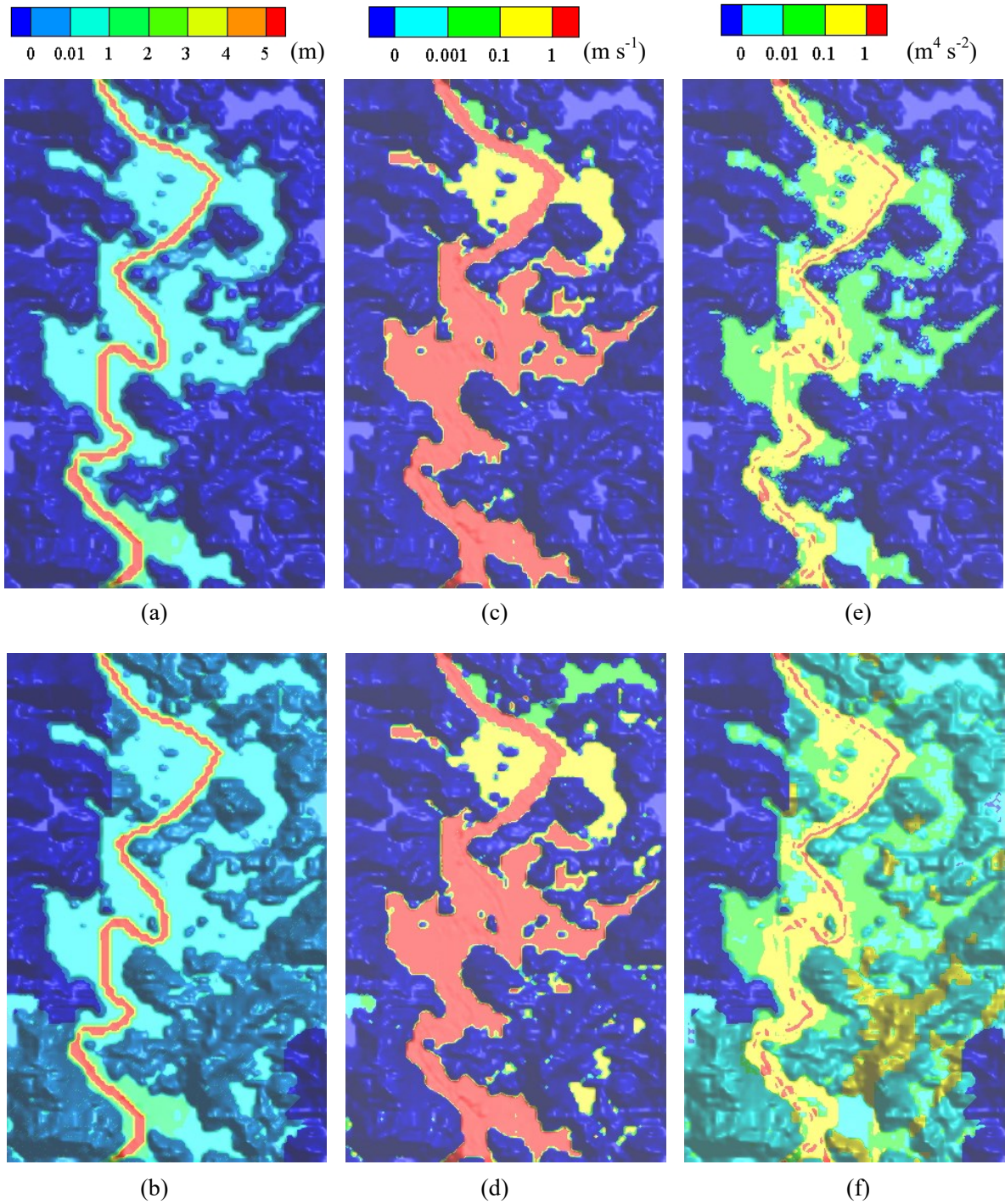
Figure 24. Simulation results at t=17h, (a) and (b) are water depth(m) for case A and case B,(c) and (d) are velocity(m s^{-1}) for case A and case B, (e) and (f) are flux term(m^4 s^{-}2) for case A and case B

The DBCM can dynamically alter the coupling boundary position to determine the non-inundation and inundation regions, which takes into account both of mass and momentum exchange on the coupling boundary. The hydrologic and hydrodynamic models are solved simultaneously. The coupling approach in DBCM shows more approximation to the natural physical process of flood formation and propagation, which has the potential to improve the accuracy of flood prediction.

The main advantages of the proposed DBCM are three folds:(1) flow discharge at the coupling boundary is determined based on the characteristic wave theory. Solution of hydrologic model and hydrodynamic model on each side of the coupling boundary are solved according to characteristic wave analysis and slope gradient analysis, respectively. (2) The discharge obtained on the coupling boundary takes into account both of mass and momentum transfer between the hydrologic model and hydrodynamic model, and flow information on both sides of the coupling boundary can be reflected.(3) the coupling boundary is time-dependent, and the computational domain of inundation and non-inundation regions varies according to the flow state throughout the calculation process, which is more aligned with natural rainfall and flood propagation conditions. The benchmark tests show that the DBCM is capable of accurately simulating the hydrologic and hydrodynamic response to rainfall events in various catchments. The DBCM gains a good agreement with the analytical solution, and realizes the dynamic switching between the hydrologic and hydrodynamic models in simulating surface flows, which is hardly achieved by former methods. The DBCM also succeeds in predicting the inundation regions in real flood events with more reasonable results when compared to the BCM.

However, the DBCM in present study only accounts for precipitation and infiltration among the various physical processes of the hydrological cycle. Besides, a uniform rainfall station data were adopted in the present DBCM, which limits its application to relatively small-scale catchment simulation. Thus, further study involving other physical processes, such as evapotranspiration, interception, and snow melt .etc. as well as distributed rainfall datasets processing, need to be implemented to the DBCM in order to make it suitable for more general application and complicate case study or practice.

Data availability. Model simulation and calibration data as well as codes are available upon request from the corresponding author. Digital elevation model data are provided by the Geospatial Data Cloud at http://www.gscloud.cn. The data sets of Soil Properties and Land cover are provided by Cold and Arid Regions Sciences Data Center at Lanzhou (http://westdc.westgis.ac.cn).The Satellite imagery base map of Helin town was obtained from Google earth Pro.

Author contributions. YWY designed the methodology and carried out the investigation with cooperation from all co-authors. QZ provided the original model input data. The study was supervised by CBJ. YWY prepared the first draft of the manuscript, which was then revised and improved by the co-authors.

Competing interests. The authors declare that they have no conflict of interest.

Acknowledgements. This study was supported by the National Science Foundation of China (No. 51679121) and National Key Research and Development Program of China(NO. 2016YFC0502204).

References

425 Ata, R., Pavan, S., Khelladi, S., and Toro, E. F.: A Weighted Average Flux (WAF) scheme applied to shallow water equations for real-life applications, Advances in Water Resources, 62, 155–172, 2013.

Bates, P. D. and De Roo, A. P. J.: A simple raster-based model for flood inundation simulation, Journal of Hydrology, 236, 54–77, 2000.

Bouilloud, L., Chancibault, K., Vincendon, B., Ducrocq, V., Habets, F., Saulnier, G. M., Anquetin, S., Martin, E., and Noilhan, J.: Coupling the ISBA Land Surface Model and the TOPMODEL Hydrological Model for Mediterranean Flash-Flood Forecasting: Description,
430   Calibration, and Validation, Journal of Hydrometeorology, 11, 315–333, 2010.

Bradbrook, K.: JFLOW: a multiscale two-dimensional dynamic flood model, Water and Environment Journal, 20, 79–86, 2006.

Bradbrook, K., Lane, S., Waller, S., and Bates, P.: Two dimensional diffusion wave modelling of flood inundation using a simplified channel representation, International Journal of River Basin Management, 2, 211–223, 2004.

Bravo, J. M., Allasia, D., Paz, A. R., Collischonn, W., and Tucci, C. E. M.: Coupled Hydrologic-Hydraulic Modeling of the Upper Paraguay
435   River Basin, Journal of Hydrologic Engineering, 17, 635–646, 2012.

Chen, A. S., Evans, B., Djordjević, S., and Savić, D. A.: A coarse-grid approach to representing building blockage effects in 2D urban flood modelling, Journal of Hydrology, 426-427, 1–16, 2012.

Choi, C. C. and Mantilla, R.: Development and Analysis of GIS Tools for the Automatic Implementation of 1D Hydraulic Models Coupled with Distributed Hydrological Models, Journal of Hydrologic Engineering, 20, 06015 005, 2015.

440 Di Baldassarre, G., Giammarco, P., Todini, E., and Lamberti, P.: A conservative finite elements approach to overland flow: the control volume finite element formulation, Journal of Hydrology, 175, 267–291, 1996.

Fraccarollo, L. and Toro, E. F.: Experimental and numerical assessment of the shallow water model for two-dimensional dam-break type problems, Journal of hydraulic research, 33, 843–864, 1995.

Godunov, S. K.: A finite difference method for the computation of discontinuous solutions of the equations of fluid dynamics, Sbornik:
445   Mathematics, 47, 357–393, 1959.

Grimaldi, S., Petroselli, A., Arcangeletti, E., and Nardi, F.: Flood mapping in ungauged basins using fully continuous hydrologic–hydraulic modeling, Journal of Hydrology, 487, 39–47, 2013.

Hdeib, R., Abdallah, C., Colin, F., Brocca, L., and Moussa, R.: Constraining coupled hydrological-hydraulic flood model by past storm events and post-event measurements in data-sparse regions, Journal of Hydrology, 565, 160–176, 2018.

450 Hsu, M. H., Chen, S. H., and Chang, T. J.: Inundation simulation for urban drainage basin with storm sewer system, Journal of Hydrology, 234, 21–37, 2000.

Laganier, O., Ayral, P. A., Salze, D., and Sauvagnargues, S.: A coupling of hydrologic and hydraulic models appropriate for the fast floods of the Gardon River basin (France), Nat. Hazards Earth Syst. Sci., 14, 2899–2920, nHESS, 2014.

Leandro, J., Chen, A. S., and Schumann, A.: A 2D parallel diffusive wave model for floodplain inundation with variable time step (P-DWave),
455   Journal of Hydrology, 517, 250–259, 2014.

Lerat, J., Perrin, C., Andréassian, V., Loumagne, C., and Ribstein, P.: Towards robust methods to couple lumped rainfall–runoff models and hydraulic models: A sensitivity analysis on the Illinois River, Journal of Hydrology, pp. 123–135, 2012.

Li, D., Bou-Zeid, E., Baeck, M. L., Jessup, S., and Smith, J. A.: Modeling Land Surface Processes and Heavy Rainfall in Urban Environments: Sensitivity to Urban Surface Representations, Journal of Hydrometeorology, 14, 1098–1118, 2013.

460   Li, D., Malyshev, S., and Shevliakova, E.: Exploring historical and future urban climate in the Earth System Modeling framework: 1. Model development and evaluation, Journal of Advances in Modeling Earth Systems, 8, 917–935, 2016.

Liang, D., Lin, B., and Falconer, R. A.: Simulation of rapidly varying flow using an efficient TVD–MacCormack scheme, International journal for numerical methods in fluids, 53, 811–826, 2007.

Liu, G., Schwartz, F. W., Tseng, K.-H., and Shum, C. K.: Discharge and water-depth estimates for ungauged rivers: Combining hydrologic,
465   hydraulic, and inverse modeling with stage and water-area measurements from satellites, Water Resources Research, 51, 6017–6035, 2015.

McMillan, H. K. and Brasington, J.: End-to-end flood risk assessment: A coupled model cascade with uncertainty estimation, Water Resources Research, 44, 2008.

Montanari, M., Hostache, R., Matgen, P., Schumann, G., Pfister, L., and Hoffmann, L.: Calibration and sequential updating of a coupled hydrologic-hydraulic model using remote sensing-derived water stages, Hydrology and Earth System Sciences, 13, 367–380, 2009.

470   Osti, R. P.: Strengthening Flood Risk Management Policy and Practice in the People's Republic of China: Lessons Learned from the 2016 Yangtze River Floods, Working papers, 2017.

Panday, S. and Huyakorn, P. S.: A fully coupled physically-based spatially-distributed model for evaluating surface/subsurface flow, Advances in water Resources, 27, 361–382, 2004.

Patro, S., Chatterjee, C., Mohanty, S., Singh, R., and Raghuwanshi, N. S.: Flood inundation modeling using MIKE FLOOD and remote
475   sensing data, Journal of the Indian Society of Remote Sensing, 37, 107–118, 2009.

Rallison, R. E. and Miller, N.: Past, present, and future SCS runoff procedure, in: Rainfall-runoff relationship/proceedings, International Symposium on Rainfall-Runoff Modeling held May 18-21, 1981 at Mississippi State University, Mississippi State, Mississippi, USA/edited by VP Singh, Rainfall-runoff relationship/proceedings, International Symposium on Rainfall-Runoff Modeling held May 18-21, 1981 at Mississippi State University, Mississippi State, Mississippi, USA/edited by VP Singh, Littleton, Colo.: Water Resources Publications,
480   1982.

Rawls, W. J., Brakensiek, D. L., and Miller, N.: Green-ampt Infiltration Parameters from Soils Data, Journal of Hydraulic Engineering, 109, 62–70, 1983.

Rayburg, S. and Thoms, M.: A coupled hydraulic–hydrologic modelling approach to deriving a water balance model for a complex floodplain wetland system, Hydrology Research, 40, 364–379, 2009.

485   Rogers, B., Fujihara, M., and Borthwick, A. G.: Adaptive Q-tree Godunov-type scheme for shallow water equations, International Journal for Numerical Methods in Fluids, 35, 247–280, 2001.

Singh, J., Altinakar, M. S., and Ding, Y.: Numerical Modeling of Rainfall-Generated Overland Flow Using Nonlinear Shallow-Water Equations, Journal of Hydrologic Engineering, 20, 04014 089, 2015.

Thompson, J. R.: Simulation of Wetland Water-Level Manipulation Using Coupled Hydrological/Hydraulic Modeling, Physical Geography,
490   25, 39–67, 2004.

Thompson, J. R., Sørenson, H. R., Gavin, H., and Refsgaard, A.: Application of the coupled MIKE SHE/MIKE 11 modelling system to a lowland wet grassland in southeast England, Journal of Hydrology, 293, 151–179, 2004.

Toro, E. F.: Shock-capturing methods for free-surface shallow flows, John Wiley, 2001.

Viero, D. P., Peruzzo, P., Carniello, L., and Defina, A.: Integrated mathematical modeling of hydrological and hydrodynamic response to
495   rainfall events in rural lowland catchments, Water Resources Research, 50, 5941–5957, 2014.

Yu, C. and Duan, J.: Two-Dimensional Hydrodynamic Model for Surface-Flow Routing, Journal of Hydraulic Engineering, 140, 04014 045, 2014a.

Yu, C. and Duan, J.: Simulation of Surface Runoff Using Hydrodynamic Model, Journal of Hydrologic Engineering, 22, 04017006, 2017.

Yu, C. and Duan, J. G.: High resolution numerical schemes for solving kinematic wave equation, Journal of Hydrology, 519, 823–832, 2014b.

500   Zhu, Z., Oberg, N., Morales, V. M., Quijano, J. C., Landry, B. J., and Garcia, M. H.: Integrated urban hydrologic and hydraulic modelling in Chicago, Illinois, Environmental Modelling & Software, 77, 63–70, 2016.