



1	An improved method of Newmark analysis for mapping hazards of
2	coseismic landslides
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16 Abstract

17 Coseismic landslides have been responsible for destroyed buildings and structures, dislocated roads 18 and bridges, cut off of pipelines and lifelines, and tens of thousands of deaths. Accurately mapping the 19 hazards of coseismic landslides is an important and challenge work. Newmark's method is widely applied 20 to assess the permanent displacement along a potential slide surface to determine the coseismic responses 21 of the slope. This paper considers the roughness and size effect of the potential slide surface-unloading 22 joint, and then presents an improved method of Newmark analysis for mapping hazard of coseismic 23 landslides. The improved method is verified using data from a case study of the 2014 M_{w} 6.1 (USGS) 24 Ludian earthquake in Yunnan Province, China. The permanent displacement yielded from this method 25 range from 0 to 122 cm. Comparisons are made between the predicted displacements and a comprehensive 26 inventory of landslides triggered by the Ludian earthquake to map the spatial variability using certainty 27 factor model (CFM). Confidence levels of coseismic landslides indicated by certainty factors range from 28 -1 to 0.95. A coseismic landslide hazard map is then produced based on the spatial distribution of the 29 values of certainty factors. Area under the curve analysis is used to draw a comparison between the 30 improved and conventional method of Newmark analysis, revealing the improved performance of the 31 method presented in this paper. Such method can be applied to predict the hazard zone of the region and 32 provide guidelines for making decisions regarding infrastructure development and post-earthquake 33 reconstruction.

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35 *Keywords:* Coseismic landslide; Newmark's method; Barton model; Certainty factor; Hazard Mapping





36 **1. Introduction**

One of the major causes of landslides is recognized as the earthquake. Coseismic landslide hazards have drawn increasing attention in recent years (i.e. Jibson et al., 1998, 2000; Khazai and Sitar, 2004; Qi et al., 2010, 2011, 2012; Chen et al., 2012; Xu et al., 2013; Yuan et al., 2014). In fact, the damage caused by seismically triggered landslides is sometimes more severe than the damage direct from the earthquake (Keefer, 1984). Estimating where is likely to have slope failure under a specific shaking condition plays an important role in regional assessment of coseismic landslides.

43 Pseudostatic analysis formalized by Terzhagi (1950) and finite-element modeling applied by Clough 44 and Chopra (1966) were employed to assess the seismic stability of slopes in early efforts (Jibson, 2011). Newmark (1965) first introduced a relatively simple and practical method, still commonly used, to 45 estimate the coseismic permanent-displacements of slopes (Jibson, 2011). Studies showed that 46 47 Newmark's method yields reasonable and practical results when modeling the dynamic performance of 48 natural slopes (Wilson and Keefer, 1983; Wieczorek et al., 1985; Jibson et al., 1998, 2000; Pradel et al., 49 2005). Recent years, Rathje and Antonakos (2011) present a unified framework for predicting coseismic 50 permanent sliding displacement based on Newmark's method. Chen et al. (2018) used Newmark's method 51 to calculate the minimum accelerations required for coseismic landslides in the affected region of 2014 52 Ludian earthquake. Chen et al. (2019) subsequently developed an easy-operation mapping method to 53 assess coseismic landslide hazard in the quake zone of 2014 Ludian earthquake, with the help of 54 Newmark's method.

55 Such applications generally start from an analysis of the dynamic stability of slopes that is quantified 56 as the critical acceleration. Barton model (Barton, 1973) has been widely used in rock mechanics and





engineering field to predict the shear strength of rock joints, which plays a crucial role in the calculation 57 58 of critical acceleration. However, researches do not pay enough attentions on the shear strength of rock 59 joints during the assessment of coseismic landslides. To better estimate the dynamic stability of slopes, in 60 this paper, we introduce the Barton model (Barton, 1973) into a Newmark analysis to develop an improved 61 modeling method for mapping hazards of coseismic landslides, using data from the 2014 Ludian 62 earthquake in Yunnan Province, Southwestern China. As predictions of coseismic landslides are not only 63 based on exact results, i.e., computed permanent-displacements, but also mingled with unformalized 64 expertise (Shortliffe and Buchanan, 1975), i.e., interpreted landslides, we then present a model of inexact 65 reasoning method, which defies analysis as applications of sets of inference rules that are expressed in the predicate logic (Shortliffe and Buchanan, 1975), to produce a coseismic landslide hazard map. 66

This paper briefly introduces the site characteristics and the spatial distribution of triggered landslides, describes the modeling method used for the analysis of seismic slope stability, then presents the mapping procedure of the confidence level of seismic slope-failure, and finally discusses the results of the seismic hazard assessment and the comparison with a conventional Newmark analysis.

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72 **2. Study area**

The epicenter of the 2014 M_w 6.1 Ludian earthquake is located in the southeastern margin of the Tibetan plateau. A rectangular area lying immediately around the epicenter and containing dense concentrations of induced landslides was chosen for study. Elevation in the study area ranges from 785 m to 3,085 m above the sea. There are three rivers, the Niulanjiang River, the Shaba River and the Longquan River passing through the area. The topography ranges from flat in river valleys to nearly





vertical in the slopes on the side of the rivers. The Niulanjiang River, flowing from southeast (SE) to the
northwest (NW), where according to Chen et al. (2015), incises down to a depth between 1,200 m and
3,300 m, resulting in about 80% of the slopes with angles greater than 40° distributed along the banks.
Predominant geologic units of the study area vary in the era from Proterozoic to Mesozoic, including
dolomite, limestone, shale, sandstone, basalt and slate.

83 A landslide inventory containing 1,416 landslides (Fig. 1) was posed by visual interpretation through comparison between pre-earthquake satellite images from Google Earth (January 30, 2014) and 0.2m-84 85 high-resolution post-earthquake aerial images (August 7, 2014, data provided by Digital Mountain and 86 Remote Sensing Applications Center, Institute of Mountain Hazards and Environment, Chinese Academy 87 of Sciences; Beijing Anxiang Power Technology Co., LTD.). A majority of landslides triggered in this earthquake were shallow flow-like landslides (less than 3 m deep) developing in particularly dense 88 89 concentrations along steeply incised river valleys. The total area of these interpreted landslides was 7.01 km² within a study area of 705 km². A detailed study showed that 846 of the mapped landslides were 90 greater than 1,000 m², occupying 6.74 km² and accounting for 96.1% of the total landslide area, out of 91 which 279 of the mapped landslides were greater than $5,000 \text{ m}^2$, occupying 5.37 km^2 and accounting for 92 93 76.6% of the total landslide area.

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95 **3. Methodology**

96 3.1 Modeling method

97 In the context of the analysis of the dynamic stability of a slope, Newmark (1965) proposed a 98 permanent-displacement analysis that bridges the gap between simplistic pseudostatic analysis and





99 sophisticated, but generally impractical finite-element modeling (Jibson, 1993). Newmark's method 100 simulates a landslide as a rigid-plastic friction block having a known critical acceleration on an inclined 101 plane (Fig. 2), and then calculates the cumulative permanent displacement of the block as it is subjected 102 to an acceleration-time history of an earthquake. Newmark (1965) showed that the dynamic stability of a 103 slope is related to the critical acceleration of a potential landslide block, and it can be expressed as a 104 simple function of the static factor of safety and the landslide geometry (Jibson et al., 1998, 2000) as 105 below:

$$a_c = (F_S - 1)gsin\alpha \tag{1}$$

106 where a_c is critical acceleration in terms of g, the acceleration due to earth's gravity, F_s is static factor 107 of safety, and α is the angle from the horizontal that the center of the slide block moves when 108 displacement first occurs (Jibson et al., 1998, 2000). For a planar slip surface parallel to the slope, this 109 angle can generally be approximated as the slope angle.

110 Natural slopes often develop a group of shallow unloading joints (Fig. 3) that parallel to the surface 111 due to valley incisions (Gu, 1979; Hoek and Bray, 1981). Studies showed that rock slopes behave as collapsing and sliding failures of shallow unloading joints under strong earthquakes, and 90% of 112 113 coseismic landslides are shallow falls and slides (Harp and Jibson, 1996; Khazai and Sitar, 2003; Dai et 114 al., 2011; Tang et al., 2015). According to Qi et al. (2012), there are two typical kinds of earthquake 115 triggered landslides, i.e., (a) shallow flow-like landslides with depth less than 3 m in general and (b) rock 116 falls that are thrown by the earthquake shaking, usually occurred at the crest of the slope. For both types, 117 the unstable rock blocks are often cut and activated along the rock joints. Therefore, the static factor of 118 safety in terms of the critical acceleration in these conditions is related to the peak shear strength of the





rock joints. For the purpose of regional stable analysis, we use a limit-equilibrium model of an infinite slope (Fig. 2) referring to the simplification of Jibson et al. (1998, 2000) on Newmark's method. On this occasion, the value of the static factor of safety against sliding which is given by the ratio of resisting to driving force is determined by conventional analysis with no consideration of accelerations, expressed as:

$$F_{S} = \frac{Resisting \ force}{Driving \ force} = \frac{\tau L}{mgsin\alpha} = \frac{\tau L}{\gamma Ltsin\alpha} = \frac{\tau}{\gamma tsin\alpha}$$
(2)

123 where τ is peak shear strength of the rock joint, γ is unit weight of the rock mass, and t is the thickness 124 of the failure rock block.

For a Newmark analysis, it has been customary to describe the shear strength of rocks not rock joints in terms of Coulomb's constants for friction and cohesion. However, both are not only stress dependent variables, but also scale dependent (Barton and Choubey, 1977). According to Barton (1973), a more satisfactory empirical relationship for predicting the peak shear strength of a joint can be written as follows:

$$\tau = \sigma_n \tan \left[JRC \log_{10} \left(\frac{JCS}{\sigma_n} \right) + \phi_b \right]$$
(3)

130 where σ_n is effective normal stress, *JRC* is joint roughness coefficient, *JCS* is joint wall compressive 131 strength, ϕ_b is basic friction angle, the angle of frictional sliding resistance between rock joints, which 132 can be obtained from residual shear tests on natural joints (Barton, 1973).

133 The effective normal stress (σ_n) generated by the gravity acting on the rock block is as follows:

$$\sigma_n = \frac{mgcos\alpha}{L} = \frac{\gamma L t cos\alpha}{L} = \gamma t cos\alpha \tag{4}$$





134 Considering the impact of size effect on *JRC* and *JCS*, formulations were developed by Barton and

135 Bandis (1982) and are shown as below:

$$JRC_n = JRC_0 \left(\frac{L_n}{L_0}\right)^{-0.02JRC_0}$$
(5)

$$JCS_n = JCS_0 \left(\frac{L_n}{L_0}\right)^{-0.03JRC_0} \tag{6}$$

- 136 where the nomenclature adopted incorporates the (0) and (n) for laboratory scale and in situ scale values
- 137 respectively.
- Hence the static factor of safety (F_S) of a slope can be written as:

$$F_{S} = \frac{\tau}{\gamma t sin\alpha} = \frac{\sigma_{n} \tan \left[JRC_{n} \log_{10}\left(\frac{JCS_{n}}{\sigma_{n}}\right) + \phi_{b}\right]}{\gamma t sin\alpha}$$
$$= \frac{\gamma t cos\alpha \tan \left[JRC_{n} \log_{10}\left(\frac{JCS_{n}}{\gamma t cos\alpha}\right) + \phi_{b}\right]}{\gamma t sin\alpha}$$
$$= \frac{\tan \left[JRC_{n} \log_{10}\left(\frac{JCS_{n}}{\gamma t cos\alpha}\right) + \phi_{b}\right]}{tan\alpha}$$
(7)

After knowing the slope angle and the static factor of safety, the critical acceleration of a slope can be determined. Once the earthquake acceleration-time history has been selected, those portions of the record lying above the critical acceleration a_c (Fig. 4a) are integrated once to derive a velocity profile (Fig. 4b), which in turn is integrated a second time to obtain the cumulative displacement profile of the block (Fig. 4c), users then judge the dynamic performance of a slope based on the magnitude of the





144 Newmark displacement (Jibson et al., 1998, 2000; Jibson, 2011). The detailed procedure of conducting a

- 145 Newmark analysis with Barton model is discussed in the following sections.
- 146 3.2 Static factor of safety

Considering that the mapped landslides greater than 1,000 m² occupy 96.1% of the total landslide area, 147 148 we selected a 30 m×30 m digital elevation model (DEM), ASTER Global Digital Elevation Model 149 (https://doi.org/10.5067/ASTER/ASTGTM.002, last accessed July 16, 2018) that is capable of facilitating 150 the subsequent hazard analysis. A basic slope algorithm was applied to the DEM to produce a slope map 151 (Fig. 5), where the slope is identified as the steepest downhill descent from the cell to its neighbors 152 (Burrough and McDonell, 1998). The slopes range from greater than 60° in the banks of the Niulanjiang River, the Shaba River and the Longquan River, to less than 20° in moderate and low mountains and hills 153 154 in north and east.

For some slope steeper than 60°, few blocks can stay on that steep sliding surface, and the calculated F_S will be nearly zero in this case. Actually, the unstable blocks have already failed, and further sliding will occur along a failure plane inside the slope, and the angle (α) of the inclination of the failure plane will be $45^{\circ} + \frac{\phi_b}{2}$. Therefore, we assigned an angle (α) of $45^{\circ} + \frac{\phi_b}{2}$ to those slopes more than 60° to avoid a too low F_S in Newmark analysis.

Digital geologic map from China Geological Survey (GCS) was rasterized at 30 m grid spacing for assigning material properties throughout the study area. According to the literature researches, we found that JRC_0 and JCS_0 depend strongly on the lithology (Coulson, 1972; Barton and Choubey, 1977; Bandis et al., 1983; Priest, 1993; Bilgin and Pasamehmetoglu, 1990; Singh et al., 2012 Alejano et al., 2012, 2014; Giusepone, 2014; Yong et al., 2018). Representative values of γ , JRC_0 , JCS_0 and ϕ_b





165 assigned to each rock type exposed in the area can normally be estimated with the help of the test data 166 listed in Table 1. The selected values were near the middle of the ranges represented in the references. 167 These JRC_0 and JCS_0 are considered in laboratory scale, for the length of 100 mm as L_0 . For each grid cell in regional analysis, L_n , the length of engineering dimension, can generally be set as a ten-fold range 168 169 of L_0 , because the value of JRC_n/JRC_0 (JCS_n/JCS_0) is almost constant when the value of L_n/L_0 greater than 10 (Bandis et al., 1981). The values of JRC_n and JCS_n , then, are calculated by inserting 170 171 values from JRC_0 , JCS_0 , L_0 , and L_n into Eq. (5) and Eq. (6). Fig. 6a and Fig. 6b show the spatial distribution of JRC_n and JCS_n respectively. The basic-friction-angle (ϕ_b) map and unit weight (γ) map 172 173 are shown as Fig. 7 and Fig. 8 respectively.

174 For simplicity, the thickness of the modeled block t was taken to be 3 m, which reflects the typical 175 slope failures of the Ludian earthquake. The static factor-of-safety map was produced by combing these data layers (α , JRC_n, JCS_n, ϕ_b , and γ) in Eq. (7). In the initial iteration of the calculation, grid cells in 176 steep areas with static factors of safety less than 1 indicate that the slopes are statically unstable, but do 177 178 not necessarily mean that the slopes are moving under the earthquake shaking. In this condition, to avoid 179 conservative results, we did not increase the strengths of rock types having statically unstable cells, either, 180 adjust strengths of other rock types to preserve the relative strength differences between rock types (Jibson 181 et al., 1998, 2000). Instead we assigned a minimal static factor of safety as 1.01, merely above limit 182 equilibrium (Jibson et al., 1998, 2000), to these slopes, to avoid a negative value of the critical acceleration a_c . According to Keefer (1984), most landslides triggered by earthquakes occur with a slope of 5° at least. 183 Static factors of safety resulting from slopes less than 5° were very high, and these slopes that were 184 185 impossible to have failures under the Ludian earthquake did not produce a statistically significant sample





186 to the analysis. Therefore, slopes less than 5° were not analyzed during the second iteration. After the

adjustment, the static factors of safety ranged from 1.0 to 17.4, as shown in Fig. 9.

188 3.3 Critical acceleration

According to Newmark (1965), a pseudostatic analysis in terms of the static factor of safety and the slope angle was employed to calculate the critical acceleration of a potential landslide. The criticalacceleration map (Fig. 10) was produced by combining the static factor of safety and the slope angle in Eq. (1).

The critical acceleration that results in a static factor of safety of 1.0 and initiates a sliding of a slope in a limit-equilibrium analysis is derived from the intrinsic slope properties (topography and lithology), regardless which ground shaking is given. Therefore, the critical-acceleration map indicates the susceptibility of the coseismic landslides (Jibson et al., 1998, 2000). The calculated critical accelerations range from almost zero in areas that are more susceptible to coseismic landslides, to 14.0 g in areas with lower susceptibility.

199 3.4 Shake map

There are 23 strong-motion stations within 100 km of the Ludian earthquake epicenter (Fig. 11). Each station record includes three components of the peak ground acceleration (*PGA*), in south-north direction, east-west direction and up-down direction respectively, as listed in Table 2 (The data set is provided by China Earthquake Data Center, <u>http://data.earthquake.cn</u>, last accessed June 16, 2016). We calculated the average *PGA* of the two horizontal components of each strong-motion recording, and then plotted a contour map (Fig. 12) using an Inverse Distance Weighted (IDW) interpolation algorithm. This method assumes that the variable of the average *PGA* being mapped decreases in influence with distance





from its sampled location. Inverse Distance Weighted (IDW) interpolation determines cell values using a linearly weighted combination of a set of sample stations (Watson and Philip, 1985). The weight is a function of inverse distance. In addition, considering that input stations far away from the epicenter location where the prediction is being made may have poor or no spatial correlation, we eliminated the input stations out of 100 km from the calculation.

212 3.5 Newmark displacement

213 In a real landslide hazard case, it is impossible to conduct a rigorous Newmark analysis when 214 accelerometer records are unavailable. It is also impractical and time consuming to produce a 215 displacement in each cell during the regional analysis. Therefore, empirical regressions (Ambraseys and 216 Menu, 1988; Bray and Travasarou, 2007; Jibson, 2007; Saygili and Rathje, 2008; Rathje and Saygili, 217 2009; Hsieh and Lee, 2011) were proposed to estimate Newmark displacement as a function of the critical 218 acceleration and peak ground acceleration or Arias intensity. Among those empirical estimations, Rathje 219 and Saygili (2009) developed a vector model for displacement in terms of the critical acceleration (a_c) , 220 peak ground acceleration (PGA) and moment magnitude (M_w) based on analysis of over 2,000 strong 221 motions.

$$lnD = 4.89 - 4.85 \left(\frac{a_c}{PGA}\right) - 19.64 \left(\frac{a_c}{PGA}\right)^2 + 42.49 \left(\frac{a_c}{PGA}\right)^3 - 29.06 \left(\frac{a_c}{PGA}\right)^4 + 0.72\ln\left(PGA\right) + 0.89(M_w - 6)$$
(8)

222 where D is predicted displacement in units of cm, a_c and PGA are in units of g.





This model is a preferred displacement model at a specific site where acceleration-time recordings are not available. The incorporating multiple ground motion parameters in the analysis typically results in less variability in the prediction of displacement (Rathje and Saygili, 2009).

The Newmark displacement (Fig. 13) in each cell was calculated by combing corresponding values of the critical acceleration, peak ground acceleration and moment magnitude in Eq (8). Predicted displacements range from 0 cm to 122 cm.

229 3.6 Certainty factor and coseismic landslide hazard map

230 According to Jibson et al. (1998, 2000), predicted displacements provide an index of seismic 231 performance of slopes, larger predicted displacements relate to greater incidence of slope failures. But the 232 displacements do not correspond directly to measurable slope movements in the field. To produce a coseismic landslide hazard map, we chose a model of inexact reasoning, the certainty factor model (CFM), 233 234 which was created by Shortliffe and Buchanan (1975) and improved by Hecherman (1986), to explore 235 the relationship between the landslide occurrences and the predicted displacements. The CFM was created 236 as a numerical method, which was initially used by MYCIN, a backward chaining expert system in 237 medicine (Shortliffe and Buchanan, 1975), for managing uncertainty in a rule-based system. In this model, 238 the certainty factor CF represents the net confidence in a hypothesis H based on the evidence E 239 (Hecherman, 1986). Certainty factors range between -1 and 1. A CF with a value of -1 means total lack 240 of confidence, whereas a CF with a value of 1 means total confidence. Values greater than 0 favor the 241 hypothesis while values less than 0 favor the negation of the hypothesis. According to Hecherman (1986), 242 there is a probabilistic interpretation for *CF* shown as below:





$$CF = \begin{cases} \frac{p(H|E) - p(H)}{p(H|E)[1 - p(H)]}, & p(H|E) > p(H) \\ \frac{p(H|E) - p(H)}{p(H)[1 - p(H|E)]}, & p(H|E) < p(H) \end{cases}$$
(9)

where CF is the certainty factor, p(H|E) denotes the conditional probability for the case of a posterior 243 244 hypothesis that relies on evidence, the posterior probability, and p(H) is the prior probability before any evidence is known. In the displacement analysis, p(H|E) was defined as the proportion of the landslide 245 246 area within a specific displacement area while p(H) was defined as the proportion of the landslide area within the entire study area excluding the slopes less than 5°. In this way, values of CF represent the 247 248 confidence level of coseismic landslides. Positive values correspond to an increase in confidence level in 249 a slope failure while negative quantities correspond to a decrease in confidence level. Greater positive 250 values indicate higher confidence level of coseismic landslides.

251 Given this definition, we could produce a coseismic landslide hazard map in terms of certainty factors. 252 First, displacement cells in every 1 cm were grouped into bins, such that all cells having displacements 253 between 0 cm and 1 cm were grouped into the first bin; those having displacements between 1 cm and 2 254 cm were grouped into the second bin, and so on. The displacements were grouped into 123 bins, from 0 255 cm to 122 cm. Later, we calculated the proportion of cells occupied by landslide area in each bin. This 256 proportion was considered the posterior probability of each bin as defined. The prior probability 257 calculated by dividing the entire landslide area by the entire study area is same in each bin. Finally, values 258 of CF were computed in each bin by using Eq. (9) to combine corresponding values of the posterior 259 probability and prior probability. Certainty factors range from -1 to 0.95. Values of CF indicate the





260 confidence level of landslide occurrence of each bin in the study area and provide the basis for producing261 a coseismic landslide hazard map.

As shown in the hazard map for the Ludian earthquake (Fig. 14), most of the actual triggered landslides lie in the higher confidence-level areas with *CF* values greater than 0.60. The interpreted landslides are covered on the map to demonstrate the good fit for predicted confidence levels of coseismic landslides.

265

4. Results and Discussion

267 The predicted displacements represent the cumulative sliding displacements for a given acceleration-time history. Based on the statistically significant sizes of the area of each displacement, 268 269 displacements less than 60 cm, which is around the middle of the displacement range, occupy about 80% 270 of the study area, while displacements greater than 80 cm occupy a very small area. Jibson et al. (1998, 271 2000) supposed that shallow falls and slides in brittle, weakly cemented materials would fail at a relatively 272 small displacement, while slumps and block slides in more compliant materials would likely fail at a 273 larger displacement. That is to say, the study area is more susceptible to rock falls and shallow, disrupted 274 slides that fail at a relatively small displacement, while the study area is with a lower probability subjected 275 to coherent, deep-seated slides that would fail at a larger displacement. Indeed, the majority of landslides 276 triggered by the Ludian earthquake were shallow, disrupted slides and rock falls (Zhou et al., 2016). 277 Although few catastrophic rock avalanches, such as the Hongshiyan landslide (Chang et al., 2017), 278 occurred in the field, they did not produce statistically significant samples that could meaningfully 279 contribute to the model, which was consistent with the statistic results as discussed previously. Therefore,





the model should relate well to typical kinds of earthquake-induced landslides in the study area, meanwhile demonstrate its potential utility to predict the probability of other types of landslides.

282 For each *CF*-value area, the proportion of area occupied by landslide area was plotted as a dot in 283 Fig. 15. The data was fitted by a piecewise function, which was derived from Eq. (9). Different from a 284 Weibull curve (1939) through statistical regression, whose shape would probably be different in different 285 regions (Jibson et al., 1998, 2000), the piecewise function of CF value and the proportion of landslide area can be derived from Eq. (9). This method is more universal. From the curve shown in Fig. 15, when 286 287 the value of CF is reaching 1.0 (total confidence), the proportion of landslide area is trending to 288 monotonically increase, which means the confidence level of a slope failure is growing and a landslide 289 would probably occur. Such a procedure is consistent with the interpretation of the certainty factor theory. 290 Therefore, the CFM demonstrates the capability of its representation and predicting approach for a 291 probabilistic hazard analysis of coseismic landslides.

292 When fitting the results of shear tests using Coulomb's linear relation, the shear strengths vary widely from high normal stress in laboratory to low normal stress in the field (Barton, 1973). We introduced 293 294 Barton model into the Newmark analysis to reduce the variability of shear strengths in terms of Coulomb's 295 constants. And we considered the impact of scale effects by using Eq. (5) and Eq. (6), which helps to 296 prevent Newmark's method from underestimating the shear strength of geologic units in a regional 297 analysis. In addition, for Barton model, the joint roughness coefficient (*IRC*) could be estimated from tilt 298 tests or from matching of Barton joint standard roughness profiles that were regarded by the International 299 Society for Rock Mechanics (ISRM, 1978), while the joint wall compressive strength (ICS) could be 300 estimated by Schmidt hammer index tests. These tests are helpful to make a quick estimate of the shear





301 strength in situ, which could facilitate using Newmark's method in an emergency hazard and risk
302 assessment after an earthquake.

303 It is difficult for a statically stable slope to fail under an earthquake. Earthquakes usually make statically 304 unstable slopes or slopes on the boundary fail. For this reason, it is important to truthfully characterize 305 the shear strengths of slopes. Shear strengths assigned to the geologic units were from results of hundreds 306 of shear tests from the references. We assigned the original shear strengths to the geologic units other than 307 increasing strengths to make statically unstable cells stable as Jibson et al. (1998, 200) did, which will 308 change the statically stable level of the whole area, especially the slopes on the boundary at first. In addition, we considered size effect of the potential slide surface, this would yield lower F_{s} , which, in turn, 309 310 yield higher displacement. However, the actual inventory of landslides was used to calibrate the predicted 311 displacements, and the confidence levels indicated by certainty factors fit well of the spatial distribution 312 of coseismic landslides as shown in the hazard map (Fig. 14).

313 We also ran a conventional Newmark analysis using assigned strengths, such as internal friction angle 314 (ϕ) and cohesion (c) as shown in Table 2. Predicted displacements calculated by the conventional 315 Newmark analysis range from 0 cm to 121 cm, compared with 0 cm to 122 cm by the new method 316 described in the paper. Fig. 16 shows the hazard map produced using the conventional Newmark analysis. 317 The CFs range from -1 to 0.94, almost the same as results from the new method above. However, there 318 are big differences along the Shaba River and upstream of the Niulanjiang River from these two methods. 319 By comparing Fig. 14 with Fig. 16, we can see that confidence levels from the new method fit better than 320 that of the conventional method, especially near upstream of the Niulanjiang River. The area under the 321 curve (AUC) analysis was employed to compare performances of both methods. To create an AUC plot,





the cumulative area of *CF*s within each interval of calculated values from the maximum to the minimum 322 323 was determined as a proportion of the total study area (x-axis) and plotted against the proportion of 324 cumulative landslides falling within those CF_{s} (y-axis) (Miles and Keefer, 2009). The area under the curve is calculated as an index to conduct comparison across both methods. A value of 0.5 indicates 325 326 performance that is no better than random guessing and 1.0 indicates perfect performance (Miles and 327 Keefer, 2009). Fig. 17 shows the results of the AUC analysis for both methods. The calculated AUC value 328 for the new method is 0.58, while the value for the conventional Newmark's method is 0.53. That is to 329 say, the new method introduced in this paper yields better results, and it is actually an improvement over 330 the conventional way of Newmark analysis.

331

5. Conclusion

333 Newmark's method is a useful, physically based model to estimate the seismic stability of natural slopes. 334 Mapping procedure of data from the 2014 Ludian earthquake shows the feasibility of a Newmark analysis 335 combined with Barton' shear strength criterion. Such method provides practical applications in regional 336 seismic hazard assessment. We also consider the size effect of shear strength parameters, such as the joint 337 roughness coefficient (IRC) and the joint wall compressive strength (ICS) in a regional analysis. Moreover, 338 the linkage of Newmark displacements to certainty factor model improves the utility of Newmark's method to predict the hazard of coseismic landslides. Finally, results of the AUC analysis indicate that the 339 340 new method has higher reliability than a conventional Newmark's method.

341

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- 346





347 References

- 348 Alejano, L. R., González, J. and Muralha, J.: Comparison of different techniques of tilt testing and basic
- friction angle variability assessment. Rock mechanics and rock engineering 45(6), 1023-1035, 2012.
- Alejano, L. R., Perucho, Á., Olalla, C. and Jiménez, R.: Rock engineering and rock mechanics: structures
 in and on rock masses. CRC Press, Boca Raton, Florida, 615-1148, 2014.
- 352 Ambraseys, N. N. and Menu, J. M.: Earthquake-induced ground displacements. Earthquake engineering
- and structural dynamics 16(7), 985-1006, 1988.
- Bandis, S., Lumsden, A. C. and Barton, N. R.: Experimental studies of scale effects on the shear behaviour
 of rock joints. International Journal of Rock Mechanics and Mining Sciences & Geomechanics
 Abstracts 18(1), 1-21, 1981.
- 357 Bandis, S. C., Lumsden, A. C. and Barton, N. R.: Fundamentals of rock joint deformation. International
- Journal of Rock Mechanics and Mining Sciences & Geomechanics Abstracts 20(6), 249-268, 1983.
- Barton, N.: Review of a new shear-strength criterion for rock joints. Engineering geology 7(4), 287-332,
- 360 1973.
- 361 Barton, N. and Bandis, S.: Effects of block size on the shear behavior of jointed rock. Keynote Lecture in
- 362 the 23rd US Symposium on Rock Mechanics (USRMS). American Rock Mechanics Association,
- 363 Berkeley, California, 739-760, 1982.
- Barton, N. and Choubey, V.: The shear strength of rock joints in theory and practice. Rock mechanics
 10(1-2), 1-54, 1977.
- 366 Bilgin, H. A. and Pasamehmetoglu, A. G.: Shear behaviour of shale joints under heat in direct shear. In
- Barton N. and Stephansson O. (Eds.), Rock joints. CRC Press, Rotterdam, 179-183, 1990.





- 368 Bray, J. D. and Travasarou, T.: Simplified procedure for estimating earthquake-induced deviatoric slope
- displacements. Journal of geotechnical and geoenvironmental engineering 133(4), 381-92, 2007.
- 370 Burrough, P. A. and McDonnell, R. A.: Principles of geographical information systems (2nd Edition).
- 371 Oxford University Press, New York, 190, 1998.
- 372 Chang, Z. F., Chang, H., Yang, S. Y., Chen, G. and Li, J. L.: Characteristics and formation mechanism of
- 373 large rock avalanches triggered by the Ludian Ms6.5 earthquake at Hongshiyan and Ganjiazhai.
- 374 Seismology and Geology 39(5), 1030-1047, 2017 (in Chinese with English abstract).
- Chen, X. L., Ran, H. L. and Yang, W. T.: Evaluation of factors controlling large earthquake-induced
 landslides by the Wenchuan earthquake. Natural Hazards and Earth System Sciences, 12(12), 36453657, 2012.
- 378 Chen, X. L., Zhou, Q. and Liu, C. G.: Distribution pattern of coseismic landslides triggered by the 2014
- Ludian, Yunnan, China Mw6.1 earthquake: special controlling conditions of local topography.
 Landslides 12(6), 1159-1168, 2015.
- 381 Chen, X. L., Liu, C. G., Wang, M. M. and Zhou, Q.: Causes of unusual distribution of coseismic landslides
- triggered by the Mw 6.1 2014 Ludian, Yunnan, China earthquake. Journal of Asian Earth Sciences 159,
 17-23, 2018.
- Chen, X. L., Liu, C. G. and Wang, M. M.: A method for quick assessment of earthquake-triggered
 landslide hazards: a case study of the Mw6. 1 2014 Ludian, China earthquake. Bulletin of Engineering
 Geology and the Environment 78(4), 2449-2458, 2019.
- 387 Clough, R. W. and Chopra, A. K.: Earthquake stress analysis in earth dams. ASCE Journal of the
- 388 Engineering Mechanics Division 92, 197-211, 1966.





- Coulson, J.H.: Shear strength of flat surfaces in rock. In Cording, E. J. (Ed.), Stability of Rock Slopes.
 13th Symposium on Rock Mechanics, Urbana, Illinois, 77-105, 1972.
- 391 Dai, F. C., Xu, C., Yao, X., Xu, L., Tu, X. B. and Gong, Q. M.: Spatial distribution of landslides triggered
- by the 2008 Ms 8.0 Wenchuan earthquake, China. Journal of Asian Earth Sciences 40(4), 883-895,
 2011.
- Geological Engineering Handbook Editorial Committee: Geological Engineering Handbook. China
 Architecture & Building Press, Beijing, 2018 (in Chinese).
- 396 Giusepone, F. and da Silva, L. A. A.: Hoek & Brown and Barton & Bandis Criteria Applied to a Planar
- 397 Sliding at a Dolomite Mine in Gandarela Synclinal. In ISRM Conference on Rock Mechanics for
- 398 Natural Resources and Infrastructure-SBMR 2014. International Society for Rock Mechanics, 2014.
- 399 Gu, D. Z.: Engineering geomechanics of rock mass. Science Press, Beijing, China, 1979 (in Chinese).
- Harp, E. L. and Jibson, R. W.: Landslides triggered by the 1994 Northridge, California, earthquake.
 Bulletin of the Seismological Society of America 86(1B), S319-S332, 1996.
- 402 Heckerman, D.: Probabilistic interpretations for MYCIN's certainty factors. In Kanal, L. N. and Lemmer,
- 403 J. F. (Eds), Machine Intelligence and Pattern Recognition 4, North-Holland, 167-196, 1986.
- 404 Hsieh, S. Y. and Lee, C. T.: Empirical estimation of the Newmark displacement from the Arias intensity
- 405 and critical acceleration. Engineering Geology 122(1-2), 34-42, 2011.
- 406 Hoek, E. and Bray, J. D.: Rock slope engineering. CRC Press, 1981.
- 407 ISRM (International Society for Rock Mechanics): Suggested Methods for the Quantitative Description
- 408 of Discontinuities in Rock Masses. International Journal of Rock Mechanics and Mining Sciences &
- 409 Geomechanics Abstracts 15, 319-368, 1978.





- Jibson, R. W.: Predicting earthquake-induced landslide displacements using Newmark's sliding block
 analysis. Transportation research record 1411, 9-17, 1993.
- Jibson, R. W.: Methods for assessing the stability of slopes during earthquakes-A retrospective.
 Engineering Geology, 122(1-2), 43-50, 2011.
- Jibson, R. W.: Regression models for estimating coseismic landslide displacement. Engineering Geology
 91(2), 209-218, 2007.
- 416 Jibson, R. W., Harp, E. L. and Michael, J. A.: A method for producing digital probabilistic seismic
- 417 landslide hazard maps: an example from the Los Angeles, California, area. US Geological Survey.
 418 Open-File Rep. 98-113. 17 pp., 1998.
- Jibson, R. W., Harp, E. L. and Michael, J. A.: A method for producing digital probabilistic seismic
 landslide hazard maps. Engineering Geology 58(3-4), 271-289, 2000.
- Keefer, D. K.: Landslides caused by earthquakes. Geological Society of America Bulletin 95(4), 406-421,
 1984.
- 423 Khazai, B. and Sitar, N.: Evaluation of factors controlling earthquake-induced landslides caused by Chi-
- 424 Chi earthquake and comparison with the Northridge and Loma Prieta events. Engineering geology
 425 71(1-2), 79-95, 2004.
- 426 Miles, S. B. and Keefer, D. K.: Evaluation of CAMEL-comprehensive areal model of earthquake-induced
 427 landslides. Engineering Geology 104(1-2), 1-15, 2009.
- 428 NASA/METI/AIST/Japan Spacesystems and U.S./Japan ASTER Science Team: ASTER Global Digital
- 429 Elevation Model version 2. NASA EOSDIS Land Processes DAAC, https://doi:
- 430 10.5067/ASTER/ASTGTM.002 (last accessed July 16, 2018), 2009.





- 431 Newmark, N. M.: Effects of earthquakes on dams and embankments. Geotechnique 15(2), 139-160, 1965.
- 432 Pradel, D., Smith, P. M., Stewart, J. P. and Raad, G.: Case history of landslide movement during the
- 433 Northridge earthquake. Journal of Geotechnical and Geoenvironmental Engineering 131(11), 1360434 1369, 2005.
- 435 Priest, S. D.: Discontinuity analysis for rock engineering. Springer Science & Business Media, B.V.,
 436 Dordrecht, 320, 2012.
- Qi, S. W., Xu, Q., Lan, H. X., Zhang, B. and Liu, J. Y.: Spatial distribution analysis of landslides triggered
 by 2008.5.12 Wenchuan Earthquake, China, Engineering Geology 116 (1-2), 95~108, 2010.
- Qi, S. W., Xu, Q., Zhang, B., Zhou, Y. D., Lan, H. X. and Li, L. H.: Source characteristics of long runout
 rock avalanches triggered by the 2008 Wenchuan earthquake, China, Journal of Asian Earth Sciences
 40 (4), 896~906, 2011.
- Qi, S. W., Yan, C. G. and Liu, C. L.: Two typical types of earthquake triggered landslides and their
 mechanisms. In Landslides and Engineered Slopes: Protecting Society through Improved
 Understanding, ISBN 978-0-415-63303-1, 2012.
- Rathje, E. M. and Antonakos, G.: A unified model for predicting earthquake-induced sliding
 displacements of rigid and flexible slopes. Engineering Geology 122(1-2), 51-60, 2011.
- Rathje, E. M. and Saygili, G.: Probabilistic assessment of earthquake-induced sliding displacements of
 natural slopes. Bulletin of the New Zealand Society for Earthquake Engineering 42(1), 18-27, 2009.
- 449 Saygili, G. and Rathje, E. M.: Empirical predictive models for earthquake-induced sliding displacements
- 450 of slopes. Journal of Geotechnical and Geoenvironmental Engineering 134(6), 790-803, 2008.





- 451 Shortliffe, E. H. and Buchanan, B. G.: A model of inexact reasoning in medicine. Mathematical
 452 Biosciences 23, 351-379, 1975.
- 453 Singh, T. N., Kainthola, A. and Venkatesh, A.: Correlation between point load index and uniaxial
- 454 compressive strength for different rock types. Rock Mechanics and Rock Engineering 45(2), 259-264,
 455 2012.
- 456 Tang, C., Ma, G., Chang, M., Li, W., Zhang, D., Jia, T. and Zhou, Z.: Landslides triggered by the 20 April
- 457 2013 Lushan earthquake, Sichuan Province, China. Engineering Geology 187, 45-55, 2015.
- 458 Terzhagi, K.: Mechanism of landslides. In Paige, S. (Ed.), Application of Geology to Engineering Practice
- 459 (Berkey Volume). Geological Society of America, New York, NY, 83-123, 1950.
- Watson, D. F. and Philip, G. M.: A Refinement of Inverse Distance Weighted Interpolation. Geoprocessing
 2, 315–327, 1985.
- Weibull, W.: In: A Statistical Theory of the Strength of Materials. Ingenioersvetenskaps-akademien,
 Handlingar, Stockholm, p., 151, 1939.
- 464 Wieczorek, G. F., Wilson, R. C. and Harp, E. L.: Map showing slope stability during earthquakes in San
- 465 Mateo County, California. U.S. Geological Survey Miscellaneous Investigations Map I-1257-E, scale
 466 1:62,500, 1985.
- 467 Wilson, R. C. and Keefer, D. K.: Dynamic analysis of a slope failure from the 6 August 1979 Coyote
- Lake, California, earthquake. Bulletin of the Seismological Society of America 73(3), 863-877, 1983.
- 469 Xu, C., Xu, X., Zhou, B., amd Yu, G.: Revisions of the M 8.0 Wenchuan earthquake seismic intensity
- 470 map based on co-seismic landslide abundance. Natural Hazards, 69(3), 1459-1476, 2013.





- 471 Yong, R., Ye, J., Liang, Q. F., Huang, M. and Du, S. G.: Estimation of the joint roughness coefficient
- 472 (JRC) of rock joints by vector similarity measures. Bulletin of Engineering Geology and the
- 473 Environment 77, 735-749, 2018.
- 474 Yuan, R. M., Tang, C. L., Hu, J. C., and Xu, X. W.: Mechanism of the Donghekou landslide triggered by
- the 2008 Wenchuan earthquake revealed by discrete element modeling. Natural Hazards and Earth
- 476 System Sciences, 14(5), 1195-1205, 2014.
- 477 Zhou, S. H., Chen, G. Q. and Fang, L. G.: Distribution pattern of landslides triggered by the 2014 Ludian
- 478 earthquake of China: Implications for regional threshold topography and the seismogenic fault
 479 identification. ISPRS International Journal of Geo-Information 5(4), 46, 2016.





481 Figure Captions

- 482 **Fig. 1.** Map of the study area showing interpreted landslides.
- 483 Fig. 2. Conceptual sliding-block model of a Newmark analysis.
- 484 **Fig. 3.** A schematic diagram showing shadow unloading joints in the slope.
- 485 Fig. 4. Demonstration of the Newmark-analysis algorithm (adapted from Wilson and Keefer, 1983; Jibson
- 486 et al., 1998, 2000)
- 487 **Fig. 5.** Slope map derived from the DEM of the study area.
- 488 Fig. 6. (a) JRC_n component and (b) JCS_n component of shear strength assigned to rock types in the
- 489 study area.
- 490 Fig. 7. Basic-friction-angle (ϕ_b) component of shear strength assigned to rock types in the study area.
- 491 **Fig. 8.** Unit weight (γ) assigned to rock types in the study area.
- 492 **Fig. 9.** Static factor-of-safety map of the study area.
- 493 **Fig. 10.** Map showing critical accelerations in the study area.
- 494 **Fig. 11.** Locations of strong-motion stations.
- 495 **Fig. 12.** Contour map of peak ground acceleration (*PGA*) produced by the Ludian earthquake in the
- 496 study area. PGA values shown are in g.
- 497 **Fig. 13.** Map showing predicted displacements in the study area.
- 498 Fig. 14. Map showing confidence levels of coseismic landslides in the Ludian earthquake using method
- 499 introduced in this paper. Confidence levels are portrayed in terms of values of CF.





- 500 Fig. 15. Proportion of the area of landslides lying in each *CF*-value area. A dot shows the proportion of
- 501 landslide area within an area of *CF* value; the red line is the fitting curve of the data using second order
- 502 exponential growth function.
- 503 Fig. 16. Map showing confidence levels of coseismic landslides in the Ludian earthquake using a
- 504 conventional Newmark analysis. Confidence levels are portrayed in terms of values of CF.
- 505 Fig. 17. Area under the curve plots for comparing the new method with a conventional Newmark's
- 506 method.
- 507







508

509 Fig. 1. Map of the study area showing interpreted landslides.







511

512 **Fig. 2.** Conceptual sliding-block model of a Newmark analysis. The potential landslide is modeled as a 513 rigid-plastic block resting on an inclined plane at an angle (α) from the horizontal (Jibson et al., 1998, 514 2000). The base of the block is subjected to an earthquake ground acceleration that is denoted by *Ag*.







516

517 Fig. 3. A schematic diagram showing shallow unloading joints in the slope.







519

Fig. 4. Demonstration of the Newmark-analysis algorithm (adapted from Wilson and Keefer, 1983; Jibson
et al., 1998, 2000): (a) Acceleration-time history with critical acceleration (horizontal dotted line) of 20%g
superimposed. (b) Velocity of block versus time. (c) Displacement of block versus time.







525 **Fig. 5.** Slope map derived from the DEM of the study area.

526







528

527

(a)



529





Fig. 6. (a) JRC_n component and (b) JCS_n component of shear strength assigned to rock types in the study area.







534 **Fig. 7.** Basic-friction-angle (ϕ_b) component of shear strength assigned to rock types in the study area.

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536









540 **Fig. 9.** Static factor-of-safety map of the study area.

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543 **Fig. 10.** Map showing critical accelerations in the study area.

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545

546 **Fig. 11.** Locations of strong-motion stations.

549 Fig. 12. Contour map of peak ground acceleration (*PGA*) produced by the Ludian earthquake in the
550 study area. *PGA* values shown are in *g*.

551

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Fig. 14. Map showing confidence levels of coseismic landslides in the Ludian earthquake using methodintroduced in this paper. Confidence levels are portrayed in terms of values of *CF*.

558

Fig. 15. Proportion of the area of landslides lying in each CF-value area. A dot shows the proportion of landslide area within an area of CF value; the red line is the fitting curve of the data using second order exponential growth function.

Fig. 16. Map showing confidence levels of coseismic landslides in the Ludian earthquake using a
conventional Newmark analysis. Confidence levels are portrayed in terms of values of *CF*.

566

Fig. 17. Area under the curve plots for comparing the new method with a conventional Newmark'smethod.

570

571 Table Captions

- 572 **Table 1.** Shear strengths assigned to rock types in the study area.
- 573 **Table 2.** Station records included three components of the peak ground acceleration.

575 **Table 1**

576 Shear strengths assigned to rock types in the study area.

Rock type	γ (kN/m ³)	ϕ_b	JCS ₀ (MPa)	JRC ₀	φ	c (kPa)	References
				9.5	43°	35	Singh et al., 2012
Dolomite	25.9	32°	140				Giusepone, 2014
							Alejano et al., 2014
			160	9	45°	30	Bandis et al., 1983
Limestone	21.5	37°					Singh et al., 2012
							Yong et al., 2018
	24.9		75	8	27°	16	Barton and Choubey, 1977
Shale		27°					Bilgin and Pasamehmetoglu,
							1990
	23.5			6	42°	24	Coulson, 1972
Sandstone		35°	100				Bandis et al., 1983
							Priest, 1993
							Coulson, 1972
Basalt	27.9	38°	205	8.5	50°	40	Barton and Choubey, 1977
							Alejano et al., 2014
	26.5	30°	175	3	40°	11	Coulson, 1972
							Barton and Choubey, 1977
Slate							Bandis et al., 1983
							Alejano et al., 2012
							Yong et al., 2018

577 Internal friction angle (φ), cohesion (*c*) and unit weight (γ) are derived from Geological Engineering 578 Handbook (Geological Engineering Handbook Editorial Committee, 2018)

580 **Table 2**

581 Station records included three components of the peak ground acceleration.

No.	Station	Epicentral distance (km)	EW (g)	NS (g)	UD (g)	Average of horizontal components (g)
1	Longtoushan 1	8.114	0.5141	0.9679	0.7193	0.7410
2	Longtoushan 2	8.3	0.9685	0.7203	0.5147	0.8444
3	Qianchang	18.6	0.1490	0.1432	0.0539	0.1461
4	Ciyuan	32.6	0.0468	0.0457	0.0265	0.0463
5	Mashu	38.5	0.1380	0.1361	0.0663	0.1370
6	Qiaojia	43	0.0253	0.0210	0.0135	0.0232
7	Zhaotong 1	47.4	0.0096	0.0152	0.0065	0.0124
8	Zhaotong 2	47.671	0.0065	0.0096	0.0088	0.0081
9	Huidongxijie	63.3	0.0123	0.0128	0.0037	0.0126
10	Maolin	64.4	0.0251	0.0184	0.0111	0.0217
11	Yongshanmaolin	65.647	0.0111	0.0252	0.0184	0.0182
12	Jingan	66.2	0.0103	0.0122	0.0062	0.0113
13	Butuotuojue	66.8	0.0118	0.0173	0.0079	0.0146
14	Zhaotongjingan	67.392	0.0062	0.0103	0.0122	0.0083
15	Huidongqianxin	67.4	0.0224	0.0223	0.0067	0.0224
16	Ningnansongxin	69.2	0.0062	0.0081	0.0032	0.0071
17	Pugebaishui	76	0.0152	0.0149	0.0066	0.0151
18	Huize	76.5	0.0164	0.0182	0.0090	0.0173
19	Pugediban	81.2	0.0186	0.0127	0.0046	0.0156
20	Butuodiban	83.7	0.0024	0.0021	0.0024	0.0023
21	Tuobuka	85.2	0.0168	0.0168	0.0136	0.0168

22	Pugeyangwo	91.4	0.0066	0.0069	0.0022	0.0068
23	Daguan	91.8	0.0043	0.0035	0.0027	0.0039