An improved method of Newmark analysis for mapping hazards of coseismic landslides

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Abstract

Coseismic landslides have been responsible for destroyed buildings and structures, dislocated roads and bridges, cut off of pipelines and lifelines, and tens of thousands of deaths. Accurately mapping the hazards of coseismic landslides is an important and ~~challenge~~ work. Newmark's method is widely applied to assess the permanent displacement along a potential slide surface to determine the coseismic responses of the slope. This paper considers the roughness and size effect of the potential slide surface-unloading joint, and then presents an improved method of Newmark analysis for mapping hazard of coseismic landslides. The improved method is verified using data from a case study of the 2014 M_w 6.1 (USGS) Ludian earthquake in Yunnan Province, China. The permanent displacement yielded from this method range from 0 to 122 cm. Comparisons are made between the predicted displacements and a comprehensive inventory of landslides triggered by the Ludian earthquake to map the spatial variability using certainty factor model (CFM). Confidence levels of coseismic landslides indicated by certainty factors range from -1 to 0.95. A coseismic landslide hazard map is then produced based on the spatial distribution of the values of certainty factors. Area under the curve analysis is used to draw a comparison between the improved and conventional method of Newmark analysis, revealing the improved performance of the method presented in this paper. Such method can be applied to predict the hazard zone of the region and provide guidelines for making decisions regarding infrastructure development and post-earthquake reconstruction.

Keywords: Coseismic landslide; Newmark's method; Barton model; Certainty factor; Hazard Mapping

1. Introduction

One of the major causes of landslides is recognized as the earthquake. Coseismic landslide hazards have drawn increasing attention in recent years (i.e. Jibson et al., 1998, 2000; Khazai and Sitar, 2004; Qi et al., 2010, 2011, 2012; Chen et al., 2012; Xu et al., 2013; Yuan et al., 2014). In fact, the damage caused by seismically triggered landslides is sometimes more severe than the damage direct from the earthquake (Keefer, 1984). Estimating where is likely to have slope failure under a specific shaking condition plays an important role in regional assessment of coseismic landslides.

Pseudostatic analysis formalized by Terzhagi (1950) and finite-element modeling applied by Clough and Chopra (1966) were employed to assess the seismic stability of slopes in early efforts (Jibson, 2011). Newmark (1965) first introduced a relatively simple and practical method, still commonly used, to estimate the coseismic permanent-displacements of slopes (Jibson, 2011). Studies showed that Newmark's method yields reasonable and practical results when modeling the dynamic performance of natural slopes (Wilson and Keefer, 1983; Wieczorek et al., 1985; Jibson et al., 1998, 2000; Pradel et al., 2005). Recent years, Rathje and Antonakos (2011) present a unified framework for predicting coseismic permanent sliding displacement based on Newmark's method. Chen et al. (2018) used Newmark's method to calculate the minimum accelerations required for coseismic landslides in the affected region of 2014 Ludian earthquake. Chen et al. (2019) subsequently developed an easy-operation mapping method to assess coseismic landslide hazard in the quake zone of 2014 Ludian earthquake, with the help of Newmark's method.

Such applications generally start from an analysis of the dynamic stability of slopes that is quantified as the critical acceleration. Barton model (Barton, 1973) has been widely used in rock mechanics and

57 engineering field to predict the shear strength of rock joints, which plays a crucial role in the calculation

58 of critical acceleration. However, researches do not pay enough attentions on the shear strength of rock

59 joints during the assessment of coseismic landslides. To better estimate the dynamic stability of slopes, in

60 this paper, we introduce the Barton model (Barton, 1973) into a Newmark analysis to develop an improved

61 modeling method for mapping hazards of coseismic landslides, using data from the 2014 Ludian

62 earthquake in Yunnan Province, Southwestern China. As predictions of coseismic landslides are not only

63 based on exact results, i.e., computed permanent-displacements, but also mingled with unformalized

64 expertise (Shortliffe and Buchanan, 1975), i.e., interpreted landslides, we then present a model of inexact

65 reasoning method, which defies analysis as applications of sets of inference rules that are expressed in

66 the predicate logic (Shortliffe and Buchanan, 1975), to produce a coseismic landslide hazard map.

67 This paper briefly introduces the site characteristics and the spatial distribution of triggered

68 landslides, describes the modeling method used for the analysis of seismic slope stability, then presents

69 the mapping procedure of the confidence level of seismic slope-failure, and finally discusses the results

70 of the seismic hazard assessment and the comparison with a conventional Newmark analysis.

71

72 **2. Study area**

73 The epicenter of the 2014 M_w 6.1 Ludian earthquake is located in the southeastern margin of the

74 Tibetan plateau. A rectangular area lying immediately around the epicenter and containing dense

75 concentrations of induced landslides was chosen for study. Elevation in the study area ranges from 785

76 m to 3,085 m above the sea. There are three rivers, the Niulanjiang River, the Shaba River and the

77 Longquan River passing through the area. The topography ranges from flat in river valleys to nearly

vertical in the slopes on the side of the rivers. The Niulanjiang River, flowing from southeast (SE) to the northwest (NW), where according to Chen et al. (2015), incises down to a depth between 1,200 m and 3,300 m, resulting in about 80% of the slopes with angles greater than 40° distributed along the banks. Predominant geologic units of the study area vary ~~in the era~~ from Proterozoic to Mesozoic, including dolomite, limestone, shale, sandstone, basalt and slate.

A landslide inventory containing 1,416 landslides (Fig. 1) was ~~posed~~ by visual interpretation through comparison between pre-earthquake satellite images from Google Earth (January 30, 2014) and 0.2m-high-resolution post-earthquake aerial images (August 7, 2014, data provided by Digital Mountain and Remote Sensing Applications Center, Institute of Mountain Hazards and Environment, Chinese Academy of Sciences; Beijing Anxiang Power Technology Co., LTD.). A majority of landslides triggered in this earthquake were shallow flow-like landslides (less than 3 m deep) developing in particularly dense concentrations along steeply incised river valleys. The total area of these interpreted landslides was 7.01 km^2 within a study area of 705 km^2. A detailed study showed that 846 of the mapped landslides were greater than 1,000 m^2, occupying 6.74 km^2 and accounting for 96.1% of the total landslide area, out of which 279 of the mapped landslides were greater than 5,000 m^2, occupying 5.37 km^2 and accounting for 76.6% of the total landslide area.

3. Methodology

3.1 Modeling method

In the context of the analysis of the dynamic stability of a slope, Newmark (1965) proposed a permanent-displacement analysis that bridges the gap between simplistic pseudostatic analysis and

99   sophisticated, but generally impractical finite-element modeling (Jibson, 1993). Newmark's method

100   simulates a landslide as a rigid-plastic friction block having a known critical acceleration on an inclined

101   plane (Fig. 2), and then calculates the cumulative permanent displacement of the block as it is subjected

102   to an acceleration-time history of an earthquake. Newmark (1965) showed that the dynamic stability of a

103   slope is related to the critical acceleration of a potential landslide block, and it can be expressed as a

104   simple function of the static factor of safety and the landslide geometry (Jibson et al., 1998, 2000) as

105   below:

$$a_c = (F_S - 1)g\sin\alpha \tag{1}$$

106   where a_c is critical acceleration in terms of g, the acceleration due to earth's gravity, F_S is static factor

107   of safety, and α is the angle from the horizontal that the center of the slide block moves when

108   displacement first occurs (Jibson et al., 1998, 2000). For a planar slip surface parallel to the slope, this

109   angle can generally be approximated as the slope angle.

110   Natural slopes often develop a group of shallow unloading joints (Fig. 3) that parallel to the surface

111   due to valley incisions (Gu, 1979; Hoek and Bray, 1981). Studies showed that rock slopes behave as

112   collapsing and sliding failures of shallow unloading joints under strong earthquakes, and 90% of

113   coseismic landslides are shallow falls and slides (Harp and Jibson, 1996; Khazai and Sitar, 2003; Dai et

114   al., 2011; Tang et al., 2015). According to Qi et al. (2012), there are two typical kinds of earthquake

115   triggered landslides, i.e., (a) shallow flow-like landslides with depth less than 3 m in general and (b) rock

116   falls that are thrown by the earthquake shaking, usually occurred at the crest of the slope. For both types,

117   the unstable rock blocks are often cut and activated along the rock joints. Therefore, the static factor of

118   safety in terms of the critical acceleration in these conditions is related to the peak shear strength of the

6

119   rock joints. For the purpose of regional stable analysis, we use a limit-equilibrium model of an infinite

120   slope (Fig. 2) referring to the simplification of Jibson et al. (1998, 2000) on Newmark's method. On this

121   occasion, the value of the static factor of safety against sliding which is given by the ratio of resisting to

122   driving force is determined by conventional analysis with no consideration of accelerations, expressed as:

$$F_S = \frac{Resisting\ force}{Driving\ force} = \frac{\tau L}{mg sin\alpha} = \frac{\tau L}{\gamma L t sin\alpha} = \frac{\tau}{\gamma t sin\alpha} \tag{2}$$

123   where τ is peak shear strength of the rock joint, γ is unit weight of the rock mass, and t is the thickness

124   of the failure rock block.

125   For a Newmark analysis, it has been customary to describe the shear strength of rocks not rock joints

126   in terms of Coulomb's constants for friction and cohesion. However, both are not only stress dependent

127   variables, but also scale dependent (Barton and Choubey, 1977). According to Barton (1973), a more

128   satisfactory empirical relationship for predicting the peak shear strength of a joint can be written as

129   follows:

$$\tau = \sigma_n \tan\left[JRC\ log_{10}\left(\frac{JCS}{\sigma_n}\right) + \phi_b\right] \tag{3}$$

130   where σ_n is effective normal stress, JRC is joint roughness coefficient, JCS is joint wall compressive

131   strength, ϕ_b is basic friction angle, the angle of frictional sliding resistance between rock joints, which

132   can be obtained from residual shear tests on natural joints (Barton, 1973).

133   The effective normal stress (σ_n) generated by the gravity acting on the rock block is as follows:

$$\sigma_n = \frac{mg cos\alpha}{L} = \frac{\gamma L t cos\alpha}{L} = \gamma t cos\alpha \tag{4}$$

134   Considering the impact of size effect on JRC and JCS, formulations were developed by Barton and

135   Bandis (1982) and are shown as below:

$$JRC_n = JRC_0 \left(\frac{L_n}{L_0}\right)^{-0.02JRC_0} \tag{5}$$

$$JCS_n = JCS_0 \left(\frac{L_n}{L_0}\right)^{-0.03JRC_0} \tag{6}$$

136   where the nomenclature adopted incorporates the (0) and (n) for laboratory scale and in situ scale values

137   respectively.

138   Hence the static factor of safety (F_S) of a slope can be written as:

$$F_S = \frac{\tau}{\gamma t \sin\alpha} = \frac{\sigma_n \tan\left[JRC_n \log_{10}\left(\frac{JCS_n}{\sigma_n}\right) + \phi_b\right]}{\gamma t \sin\alpha}$$

$$= \frac{\gamma t \cos\alpha \tan\left[JRC_n \log_{10}\left(\frac{JCS_n}{\gamma t \cos\alpha}\right) + \phi_b\right]}{\gamma t \sin\alpha}$$

$$= \frac{\tan\left[JRC_n \log_{10}\left(\frac{JCS_n}{\gamma t \cos\alpha}\right) + \phi_b\right]}{\tan\alpha} \tag{7}$$

139   After knowing the slope angle and the static factor of safety, the critical acceleration of a slope can

140   be determined. Once the earthquake acceleration-time history has been selected, those portions of the

141   record lying above the critical acceleration a_c (Fig. 4a) are integrated once to derive a velocity profile

142   (Fig. 4b), which in turn is integrated a second time to obtain the cumulative displacement profile of the

143   block (Fig. 4c), users then judge the dynamic performance of a slope based on the magnitude of the

144 Newmark displacement (Jibson et al., 1998, 2000; Jibson, 2011). The detailed procedure of conducting a

145 Newmark analysis with Barton model is discussed in the following sections.

146 3.2 Static factor of safety

147 Considering that the mapped landslides greater than 1,000 m² occupy 96.1% of the total landslide area,

148 we selected a 30 m×30 m digital elevation model (DEM), ASTER Global Digital Elevation Model

149 (https://doi.org/10.5067/ASTER/ASTGTM.002, last accessed July 16, 2018) that is capable of facilitating

150 the subsequent hazard analysis. A basic slope algorithm was applied to the DEM to produce a slope map

151 (Fig. 5), where the slope is identified as the steepest downhill descent from the cell to its neighbors

152 (Burrough and McDonell, 1998). The slopes range from greater than 60° in the banks of the Niulanjiang

153 River, the Shaba River and the Longquan River, to less than 20° in moderate and low mountains and hills

154 in north and east.

155 For some slope steeper than 60°, few blocks can stay on that steep sliding surface, and the calculated

156 F_S will be nearly zero in this case. Actually, the unstable blocks have already failed, and further sliding

157 will occur along a failure plane inside the slope, and the angle (α) of the inclination of the failure plane

158 will be $45°+\frac{\phi_b}{2}$. Therefore, we assigned an angle (α) of $45°+\frac{\phi_b}{2}$ to those slopes more than 60° to avoid a

159 too low F_S in Newmark analysis.

160 Digital geologic map from China Geological Survey (GCS) was rasterized at 30 m grid spacing for

161 assigning material properties throughout the study area. According to the literature researches, we found

162 that JRC_0 and JCS_0 depend strongly on the lithology (Coulson, 1972; Barton and Choubey, 1977;

163 Bandis et al., 1983; Priest, 1993; Bilgin and Pasamehmetoglu, 1990; Singh et al., 2012 Alejano et al.,

164   2012, 2014; Giusepone, 2014; Yong et al., 2018). Representative values of γ, JRC_0, JCS_0 and ϕ_b

165   assigned to each rock type exposed in the area can normally be estimated with the help of the test data

166   listed in Table 1. The selected values were near the middle of the ranges represented in the references.

167   These JRC_0 and JCS_0 are considered in laboratory scale, for the length of 100 mm as L_0. For each grid

168   cell in regional analysis, L_n, the length of engineering dimension, can generally be set as a ten-fold range

169   of L_0, because the value of JRC_n/JRC_0 (JCS_n/JCS_0) is almost constant when the value of L_n/L_0

170   greater than 10 (Bandis et al., 1981). The values of JRC_n and JCS_n, then, are calculated by inserting

171   values from JRC_0, JCS_0, L_0, and L_n into Eq. (5) and Eq. (6). Fig. 6a and Fig. 6b show the spatial

172   distribution of JRC_n and JCS_n respectively. The basic-friction-angle (ϕ_b) map and unit weight (γ) map

173   are shown as Fig. 7 and Fig. 8 respectively.

174   For simplicity, the thickness of the modeled block t was taken to be 3 m, which reflects the typical

175   slope failures of the Ludian earthquake. The static factor-of-safety map was produced by combing these

176   data layers (α, JRC_n, JCS_n, ϕ_b, and γ) in Eq. (7). In the initial iteration of the calculation, grid cells in

177   steep areas with static factors of safety less than 1 indicate that the slopes are statically unstable, but do

178   not necessarily mean that the slopes are moving under the earthquake shaking. In this condition, to avoid

179   conservative results, we did not increase the strengths of rock types having statically unstable cells, either,

180   adjust strengths of other rock types to preserve the relative strength differences between rock types (Jibson

181   et al., 1998, 2000). Instead we assigned a minimal static factor of safety as 1.01, merely above limit

182   equilibrium (Jibson et al., 1998, 2000), to these slopes, to avoid a negative value of the critical acceleration

183   a_c. According to Keefer (1984), most landslides triggered by earthquakes occur with a slope of 5° at least.

184   Static factors of safety resulting from slopes less than 5° were very high, and these slopes that were

10

185 ~~impossible to have failures~~ under the Ludian earthquake did not produce a statistically significant sample

186 ~~to the~~ analysis. Therefore, slopes less than 5° were not analyzed during the second iteration. After the

187 adjustment, the static factors of safety ranged from 1.0 to 17.4, as shown in Fig. 9.

188 3.3 Critical acceleration

189 According to Newmark (1965), a pseudostatic analysis in terms of the static factor of safety and the

190 slope angle was employed to calculate the critical acceleration of a potential landslide. The critical-

191 acceleration map (Fig. 10) was produced by combining the static factor of safety and the slope angle in

192 Eq. (1).

193 The critical acceleration that results in a static factor of safety of 1.0 and initiates a sliding of a slope in

194 a limit-equilibrium analysis is derived from the intrinsic slope properties (topography and lithology),

195 regardless which ground shaking is given. Therefore, the critical-acceleration map indicates the

196 susceptibility of the coseismic landslides (Jibson et al., 1998, 2000). The calculated critical accelerations

197 range from almost zero in areas that are more susceptible to coseismic landslides, to 14.0 g in areas with

198 lower susceptibility.

199 3.4 Shake map

200 There are 23 strong-motion stations within 100 km of the Ludian earthquake epicenter (Fig. 11).

201 Each station record includes three components of the peak ground acceleration (PGA), in south-north

202 direction, east-west direction and up-down direction respectively, as listed in Table 2 (The data set is

203 provided by China Earthquake Data Center, http://data.earthquake.cn, last accessed June 16, 2016). We

204 calculated the average PGA of the two horizontal components of each strong-motion recording, and then

205 plotted a contour map (Fig. 12) using an Inverse Distance Weighted (IDW) interpolation algorithm. ~~This~~

206 ~~method assumes that the variable of the average~~ *PGA* ~~being mapped decreases in influence with distance~~

207 ~~from its sampled location.~~ ~~Inverse Distance Weighted (IDW) interpolation~~ determines cell values using a

208 linearly weighted combination of a set of sample stations (Watson and Philip, 1985)~~. The~~ weight ~~is a~~

209 ~~function of inverse~~ distance. In addition, considering that input stations far away from the epicenter

210 location where the prediction is being made may have poor or no spatial correlation, we eliminated the

211 input stations out of 100 km from the calculation.

212 3.5 Newmark displacement

213   In a real landslide hazard case, it is impossible to conduct a rigorous Newmark analysis when

214 accelerometer records are unavailable. It is also impractical and time consuming to produce a

215 displacement in each cell during the regional analysis. Therefore, empirical regressions (Ambraseys and

216 Menu, 1988; Bray and Travasarou, 2007; Jibson, 2007; Saygili and Rathje, 2008; Rathje and Saygili,

217 2009; Hsieh and Lee, 2011) were proposed to estimate Newmark displacement as a function of the critical

218 acceleration and peak ground acceleration or Arias intensity. Among those empirical estimations, Rathje

219 and Saygili (2009) developed a vector model for displacement in terms of the critical acceleration (a_c),

220 peak ground acceleration (PGA) and moment magnitude (M_w) based on analysis of over 2,000 strong

221 motions.

$$lnD = 4.89 - 4.85 \left(\frac{a_c}{PGA}\right) - 19.64 \left(\frac{a_c}{PGA}\right)^2 + 42.49 \left(\frac{a_c}{PGA}\right)^3 - 29.06 \left(\frac{a_c}{PGA}\right)^4$$

$$+0.72\ln(PGA) + 0.89(M_w - 6) \tag{8}$$

222 where D is predicted displacement in units of cm, a_c and PGA are in units of g.

223   This model is a preferred displacement model at a specific site where acceleration-time recordings are

224   not available. ~~The~~ incorporating multiple ground motion parameters in the analysis typically results in

225   less variability in the prediction of displacement (Rathje and Saygili, 2009).

226   The Newmark displacement (Fig. 13) in each cell was calculated by combing corresponding values

227   of the critical acceleration, peak ground acceleration and moment magnitude in Eq (8). Predicted

228   displacements range from 0 cm to 122 cm.

229   3.6 Certainty factor and coseismic landslide hazard map

230   According to Jibson et al. (1998, 2000), predicted displacements provide an index of seismic

231   performance of slopes, larger predicted displacements relate to greater incidence of slope failures. But the

232   displacements do not correspond directly to measurable slope movements in the field. To produce a

233   coseismic landslide hazard map, we chose a model of inexact reasoning, the certainty factor model (CFM),

234   which was created by Shortliffe and Buchanan (1975) and improved by Hecherman (1986), to explore

235   the relationship between the landslide occurrences and the predicted displacements. The CFM was created

236   as a numerical method, which was initially used by MYCIN, a backward chaining expert system in

237   medicine (Shortliffe and Buchanan, 1975), for managing uncertainty in a rule-based system. In this model,

238   the certainty factor CF represents the net confidence in a hypothesis H based on the evidence E

239   (Hecherman, 1986). Certainty factors range between -1 and 1. A CF with a value of -1 means total lack

240   of confidence, whereas a CF with a value of 1 means total confidence. Values greater than 0 favor the

241   hypothesis while values less than 0 favor the negation of the hypothesis. According to Hecherman (1986),

242   there is a probabilistic interpretation for CF shown as below:

$$CF = \begin{cases} \dfrac{p(H|E) - p(H)}{p(H|E)[1 - p(H)]}, & p(H|E) > p(H) \\[4mm] \dfrac{p(H|E) - p(H)}{p(H)[1 - p(H|E)]}, & p(H|E) < p(H) \end{cases} \tag{9}$$

where CF is the certainty factor, $p(H|E)$ denotes the conditional probability for the case of a posterior hypothesis that relies on evidence, the posterior probability, and $p(H)$ is the prior probability before any evidence is known. In the displacement analysis, $p(H|E)$ was defined as the proportion of the landslide area within a specific displacement area while $p(H)$ was defined as the proportion of the landslide area within the entire study area excluding the slopes less than 5°. In this way, values of CF represent the confidence level of coseismic landslides. Positive values correspond to an increase in confidence level in a slope failure while negative quantities correspond to a decrease in confidence level. Greater positive values indicate higher confidence level of coseismic landslides.

Given this definition, we could produce a coseismic landslide hazard map in terms of certainty factors. First, displacement cells in every 1 cm were grouped into bins, such that all cells having displacements between 0 cm and 1 cm were grouped into the first bin; those having displacements between 1 cm and 2 cm were grouped into the second bin, and so on. The displacements were grouped into 123 bins, from 0 cm to 122 cm. Later, we calculated the proportion of cells occupied by landslide area in each bin. This proportion was considered the posterior probability of each bin as defined. The prior probability calculated by dividing the entire landslide area by the entire study area is same in each bin. Finally, values of CF were computed in each bin by using Eq. (9) to combine corresponding values of the posterior probability and prior probability. Certainty factors range from -1 to 0.95. Values of CF indicate the

14

260 confidence level of landslide occurrence of each bin in the study area and provide the basis for producing

261 a coseismic landslide hazard map.

262   As shown in the hazard map for the Ludian earthquake (Fig. 14), most of the actual triggered landslides

263 lie in the higher confidence-level areas with CF values greater than 0.60. The interpreted landslides are

264 covered on the map to demonstrate the good fit for predicted confidence levels of coseismic landslides.

265

266 **4. Results and Discussion**

267   The predicted displacements represent the cumulative sliding displacements for a given

268 acceleration-time history. Based on the statistically significant sizes of the area of each displacement,

269 ~~displacements~~ less than 60 cm, which is around the middle of the displacement range, occupy about 80%

270 of the study area, while displacements greater than 80 cm occupy a very small area. Jibson et al. (1998,

271 2000) supposed that shallow falls and slides in brittle, weakly cemented materials would fail at a relatively

272 small displacement, while slumps and block slides in more compliant materials would likely fail at a

273 larger displacement. That is to say, the study area is more susceptible to rock falls and shallow, disrupted

274 slides that fail at a relatively small displacement, while the study area is with a lower probability subjected

275 to coherent, deep-seated slides that would fail at a larger displacement. Indeed, the majority of landslides

276 triggered by the Ludian earthquake were shallow, disrupted slides and rock falls (Zhou et al., 2016).

277 Although few catastrophic rock avalanches, such as the Hongshiyan landslide (Chang et al., 2017),

278 occurred in the field, they did not produce statistically significant samples that could meaningfully

279 contribute to the model, which was consistent with the statistic results as discussed previously. Therefore,

the model should relate well to typical kinds of earthquake-induced landslides in the study area, meanwhile demonstrate its potential utility to predict the probability of other types of landslides.

For each CF-value area, the proportion of area occupied by landslide area was plotted as a dot in Fig. 15. The data was fitted by a piecewise function, which was derived from Eq. (9). Different from a Weibull curve (1939) through statistical regression, whose shape would probably be different in different regions (Jibson et al., 1998, 2000), the piecewise function of CF value and the proportion of landslide area can be derived from Eq. (9). This method is more universal. From the curve shown in Fig. 15, when the value of CF is reaching 1.0 (total confidence), the proportion of landslide area is trending to monotonically increase, which means the confidence level of a slope failure is growing and a landslide would probably occur. Such a procedure is consistent with the interpretation of the certainty factor theory. Therefore, the CFM demonstrates the capability of its representation and predicting approach for a probabilistic hazard analysis of coseismic landslides.

When fitting the results of shear tests using Coulomb's linear relation, the shear strengths vary widely from high normal stress in laboratory to low normal stress in the field (Barton, 1973). We introduced Barton model into the Newmark analysis to reduce the variability of shear strengths in terms of Coulomb's constants. And we considered the impact of scale effects by using Eq. (5) and Eq. (6), which helps to prevent Newmark's method from underestimating the shear strength of geologic units in a regional analysis. In addition, for Barton model, the joint roughness coefficient (JRC) could be estimated from tilt tests or from matching of Barton joint standard roughness profiles that were regarded by the International Society for Rock Mechanics (ISRM, 1978), while the joint wall compressive strength (JCS) could be estimated by Schmidt hammer index tests. These tests are helpful to make a quick estimate of the shear

301 strength in situ, which could facilitate ~~using~~ Newmark's method in an emergency hazard and risk

302 assessment after an earthquake.

303   It is difficult for a statically stable slope to fail under an earthquake. Earthquakes usually make statically

304 unstable slopes or slopes on the boundary fail. For this reason, it is important to truthfully characterize

305 the shear strengths of slopes. Shear strengths assigned to the geologic units ~~were~~ from results of hundreds

306 of shear tests ~~from~~ the references. We assigned the original shear strengths to the geologic units other than

307 increasing strengths to make statically unstable cells stable as Jibson et al. (1998, 200) did, which ~~will~~

308 change the statically stable level of the whole area, especially the slopes on the boundary at first. In

309 addition, we considered size effect of the potential slide surface, ~~this~~ would yield lower F_S, ~~which~~ in turn,

310 ~~yield~~ higher displacement. However, the actual inventory of landslides was used to calibrate the predicted

311 displacements, and the confidence levels indicated by certainty factors fit well ~~of~~ the spatial distribution

312 of coseismic landslides as shown in the hazard map (Fig. 14).

313   We also ran a conventional Newmark analysis using assigned strengths, such as internal friction angle

314 (φ) and cohesion (c) as shown in Table 2. Predicted displacements calculated by the conventional

315 Newmark analysis range from 0 cm to 121 cm, compared with 0 cm to 122 cm by the new method

316 described in the paper. Fig. 16 shows the hazard map produced using the conventional Newmark analysis.

317 The CFs range from -1 to 0.94, almost the same as results from the new method above. However, there

318 are big differences along the Shaba River and upstream of the Niulanjiang River from these two methods.

319 By comparing Fig. 14 with Fig. 16, we can see that confidence levels from the new method fit better than

320 that of the conventional method, especially near upstream of the Niulanjiang River. The area under the

321 curve (AUC) analysis was employed to compare performances of both methods. To create an AUC plot,

322   the cumulative area of CFs within each interval of calculated values from the maximum to the minimum

323   was determined as a proportion of the total study area (x-axis) and plotted against the proportion of

324   cumulative landslides falling within those CFs (y-axis) (Miles and Keefer, 2009). The area under the

325   curve is calculated as an index to conduct comparison across both methods. A value of 0.5 indicates

326   performance that is no better than random guessing and 1.0 indicates perfect performance (Miles and

327   Keefer, 2009). Fig. 17 shows the results of the AUC analysis for both methods. The calculated AUC value

328   for the new method is 0.58, while the value for the conventional Newmark's method is 0.53. That is to

329   say, the new method introduced in this paper yields better results, and it is actually an improvement over

330   the conventional way of Newmark analysis.

331

332   **5. Conclusion**

333   Newmark's method is a useful, physically based model to estimate the seismic stability of natural slopes.

334   Mapping procedure of data from the 2014 Ludian earthquake shows the feasibility of a Newmark analysis

335   combined with Barton' shear strength criterion. Such method provides practical applications in regional

336   seismic hazard assessment. We also consider the size effect of shear strength parameters, such as the joint

337   roughness coefficient (JRC) and the joint wall compressive strength (JCS) in a regional analysis. Moreover,

338   the linkage of Newmark displacements to certainty factor model improves the utility of Newmark's

339   method to predict the hazard of coseismic landslides. Finally, results of the AUC analysis indicate that the

340   new method has higher reliability than a conventional Newmark's method.

341

342   **Acknowledgements**

346

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480

481   **Figure Captions**

482   **Fig. 1.** Map of the study area showing interpreted landslides.

483   **Fig. 2.** Conceptual sliding-block model of a Newmark analysis.

484   **Fig. 3.** A schematic diagram showing shadow unloading joints in the slope.

485   **Fig. 4.** Demonstration of the Newmark-analysis algorithm (adapted from Wilson and Keefer, 1983; Jibson

486   et al., 1998, 2000)

487   **Fig. 5.** Slope map derived from the DEM of the study area.

488   **Fig. 6.** (a) JRC_n component and (b) JCS_n component of shear strength assigned to rock types in the

489   study area.

490   **Fig. 7.** Basic-friction-angle (ϕ_b) component of shear strength assigned to rock types in the study area.

491   **Fig. 8.** Unit weight (γ) assigned to rock types in the study area.

492   **Fig. 9.** Static factor-of-safety map of the study area.

493   **Fig. 10.** Map showing critical accelerations in the study area.

494   **Fig. 11.** Locations of strong-motion stations.

495   **Fig. 12.** Contour map of peak ground acceleration (PGA) produced by the Ludian earthquake in the

496   study area. PGA values shown are in g.

497   **Fig. 13.** Map showing predicted displacements in the study area.

498   **Fig. 14.** Map showing confidence levels of coseismic landslides in the Ludian earthquake using method

499   introduced in this paper. Confidence levels are portrayed in terms of values of CF.

500   **Fig. 15.** Proportion of the area of landslides lying in each CF-value area. A dot shows the proportion of

501   landslide area within an area of CF value; the red line is the fitting curve of the data using second order

502   exponential growth function.

503   **Fig. 16.** Map showing confidence levels of coseismic landslides in the Ludian earthquake using a

504   conventional Newmark analysis. Confidence levels are portrayed in terms of values of CF.

505   **Fig. 17.** Area under the curve plots for comparing the new method with a conventional Newmark's

506   method.

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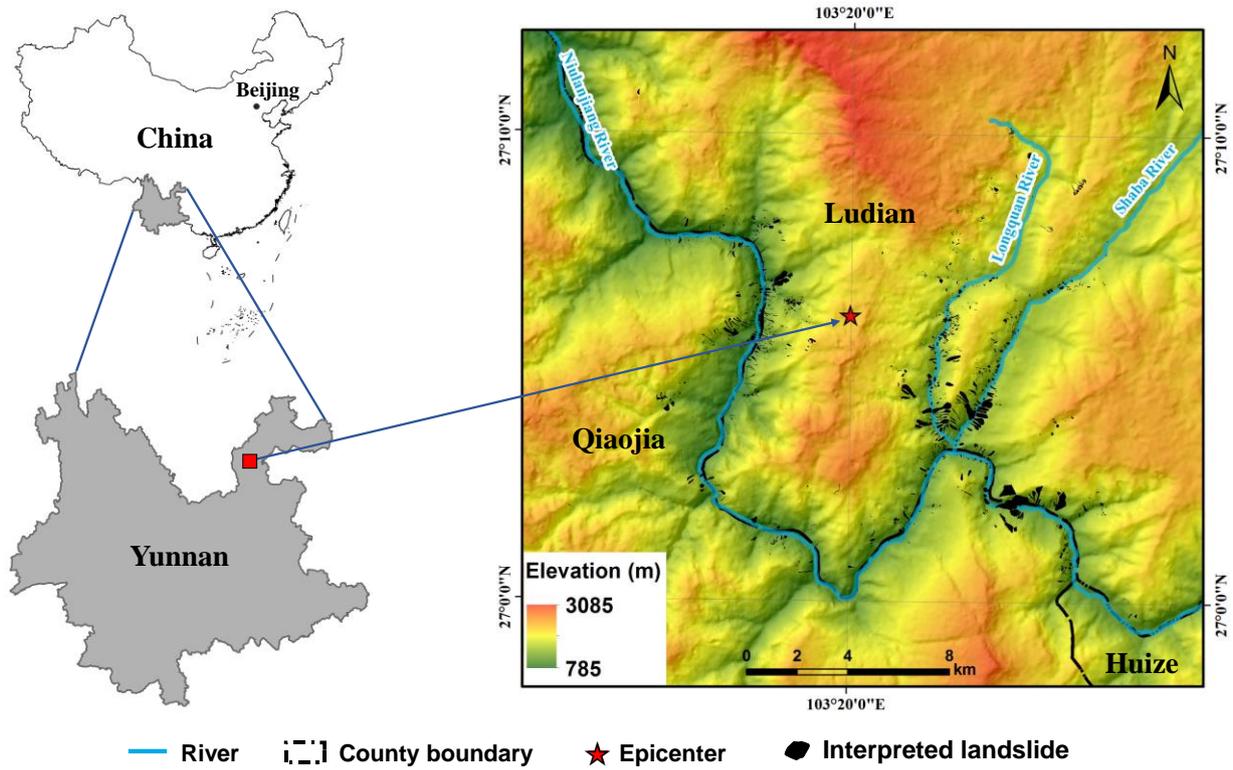
Fig. 1. Map of the study area showing ~~interpreted~~ landslides.

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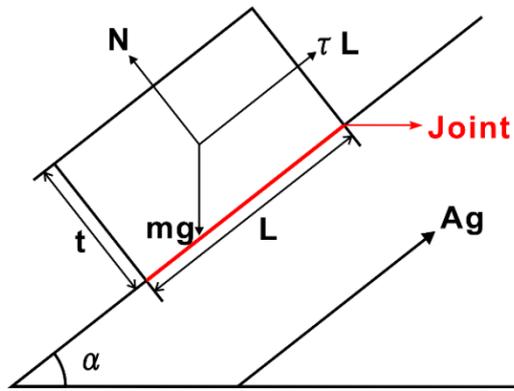
Fig. 2. Conceptual sliding-block model of a Newmark analysis. The potential landslide is modeled as a rigid-plastic block resting on an inclined plane at an angle (α) from the horizontal (Jibson et al., 1998, 2000). The base of the block is subjected to an earthquake ground acceleration that is denoted by Ag.

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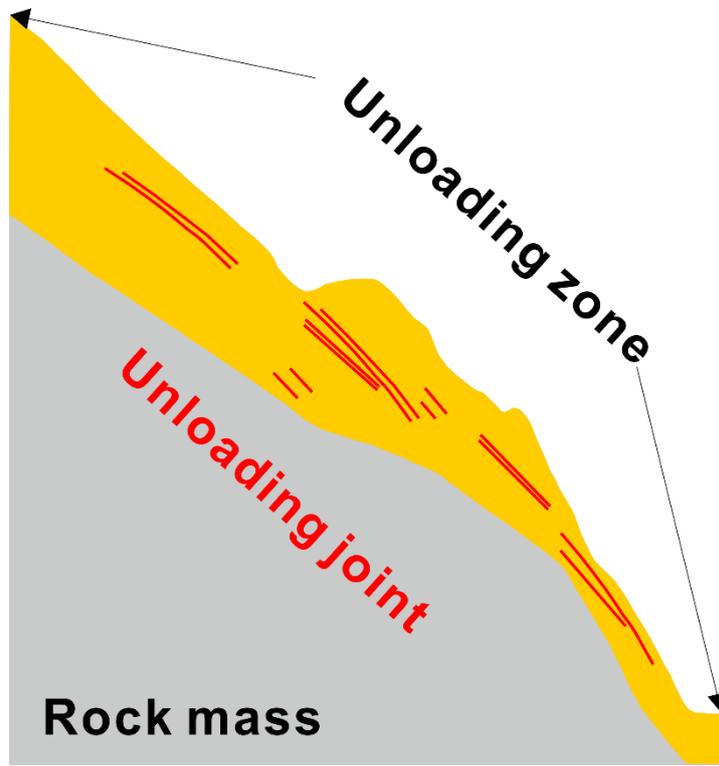
Fig. 3. A schematic diagram showing shallow unloading joints in the slope.

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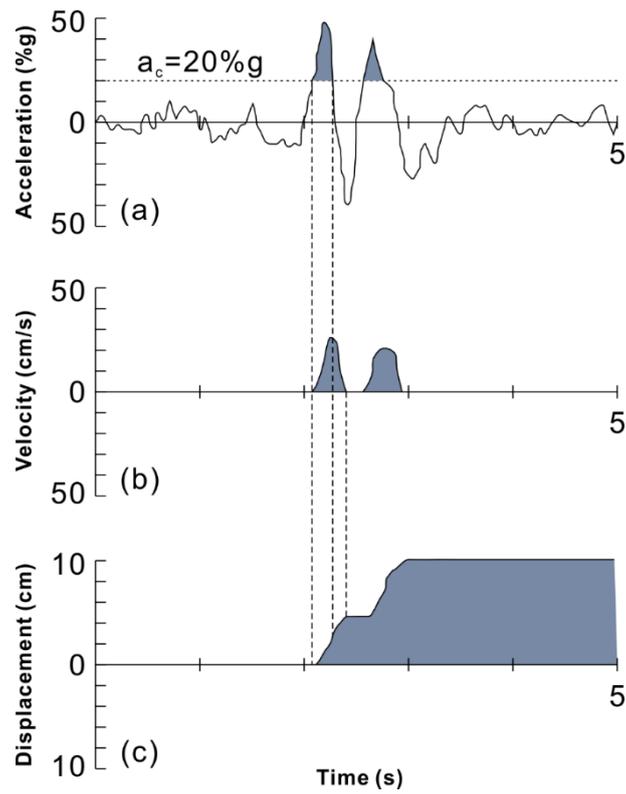
Fig. 4. Demonstration of the Newmark-analysis algorithm (adapted from Wilson and Keefer, 1983; Jibson et al., 1998, 2000): (a) Acceleration-time history with critical acceleration (horizontal dotted line) of 20%g superimposed. (b) Velocity of block versus time. (c) Displacement of block versus time.
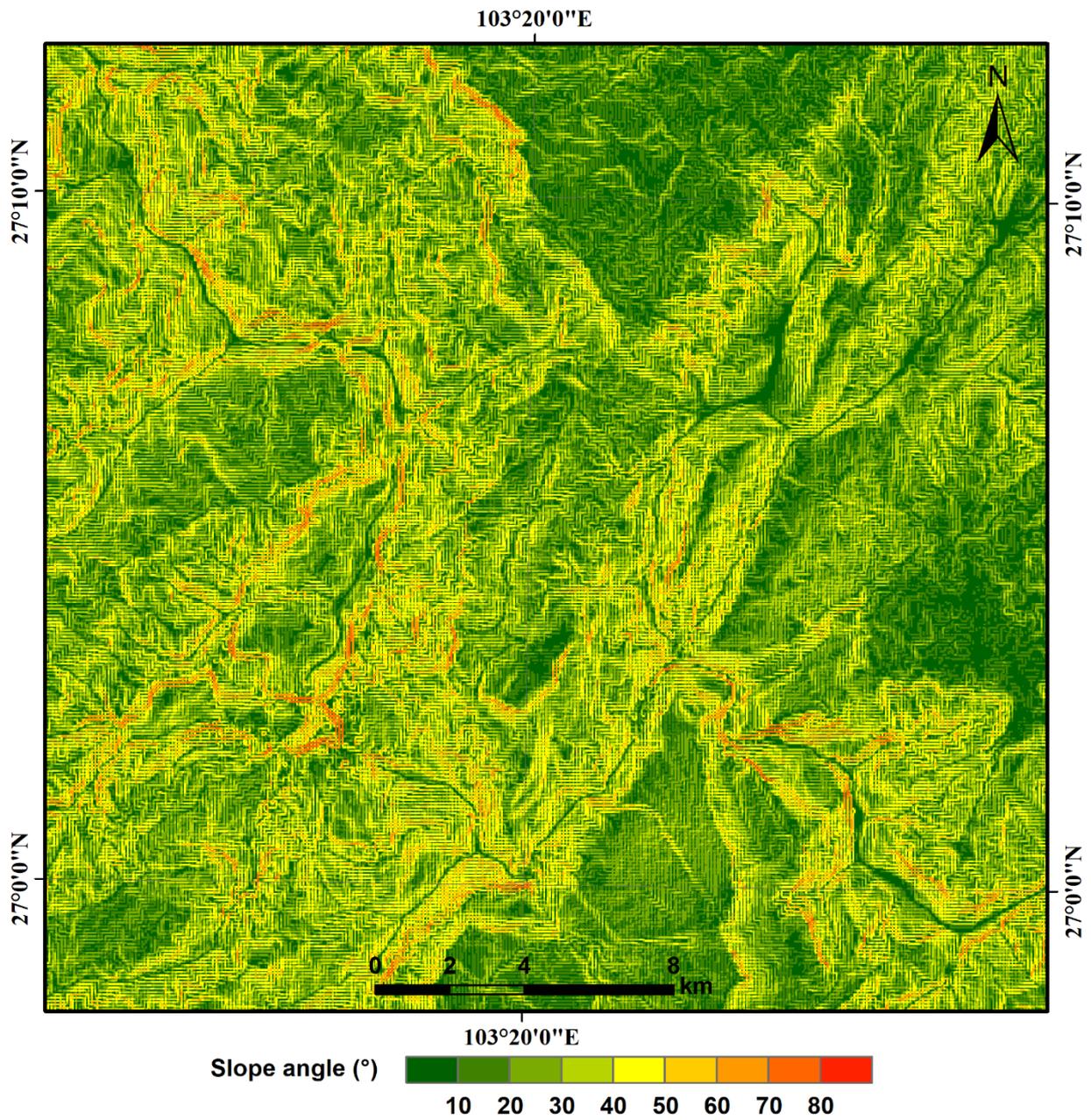
Fig. 5. Slope map derived from the DEM of the study area.
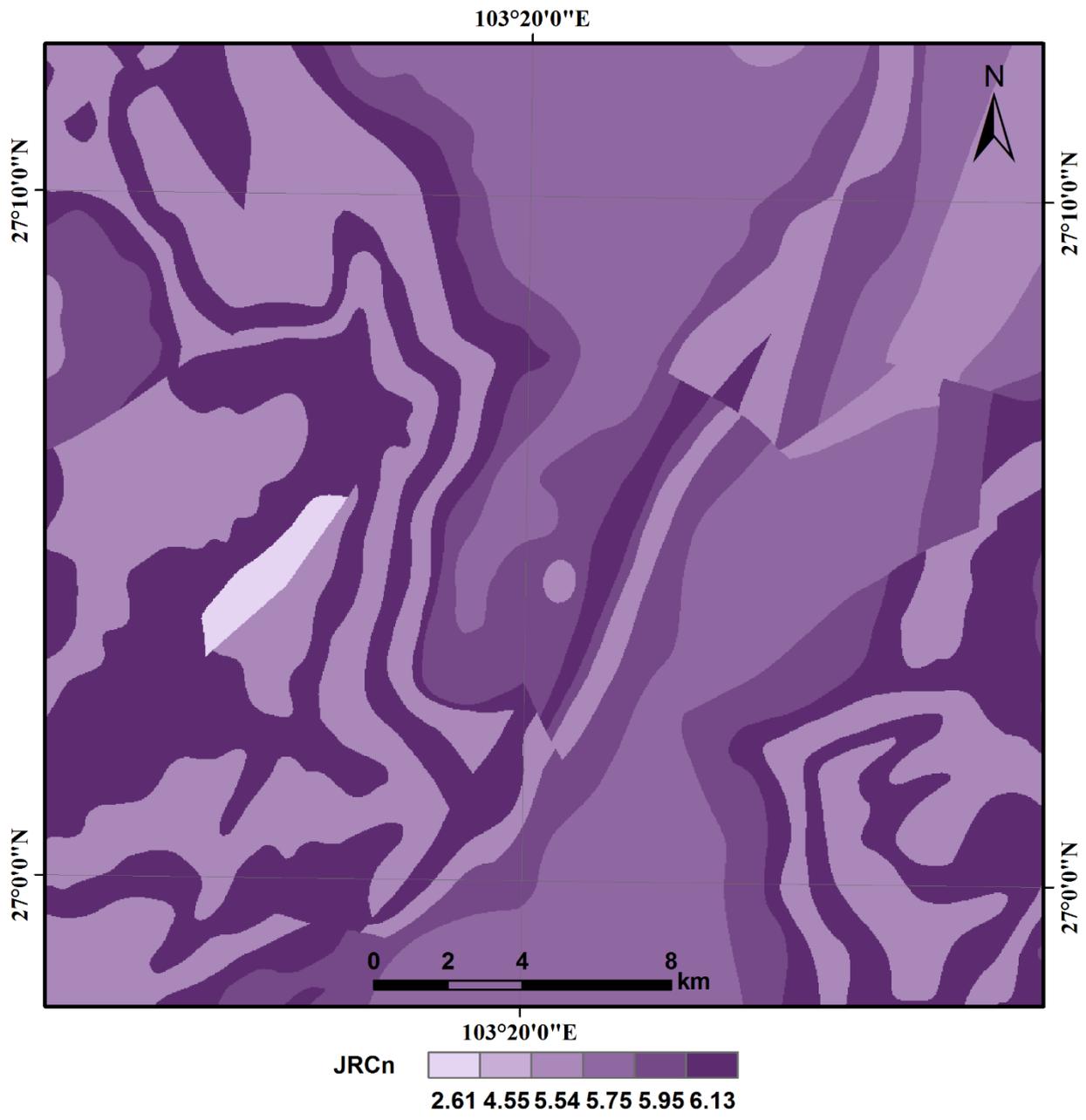
(a)
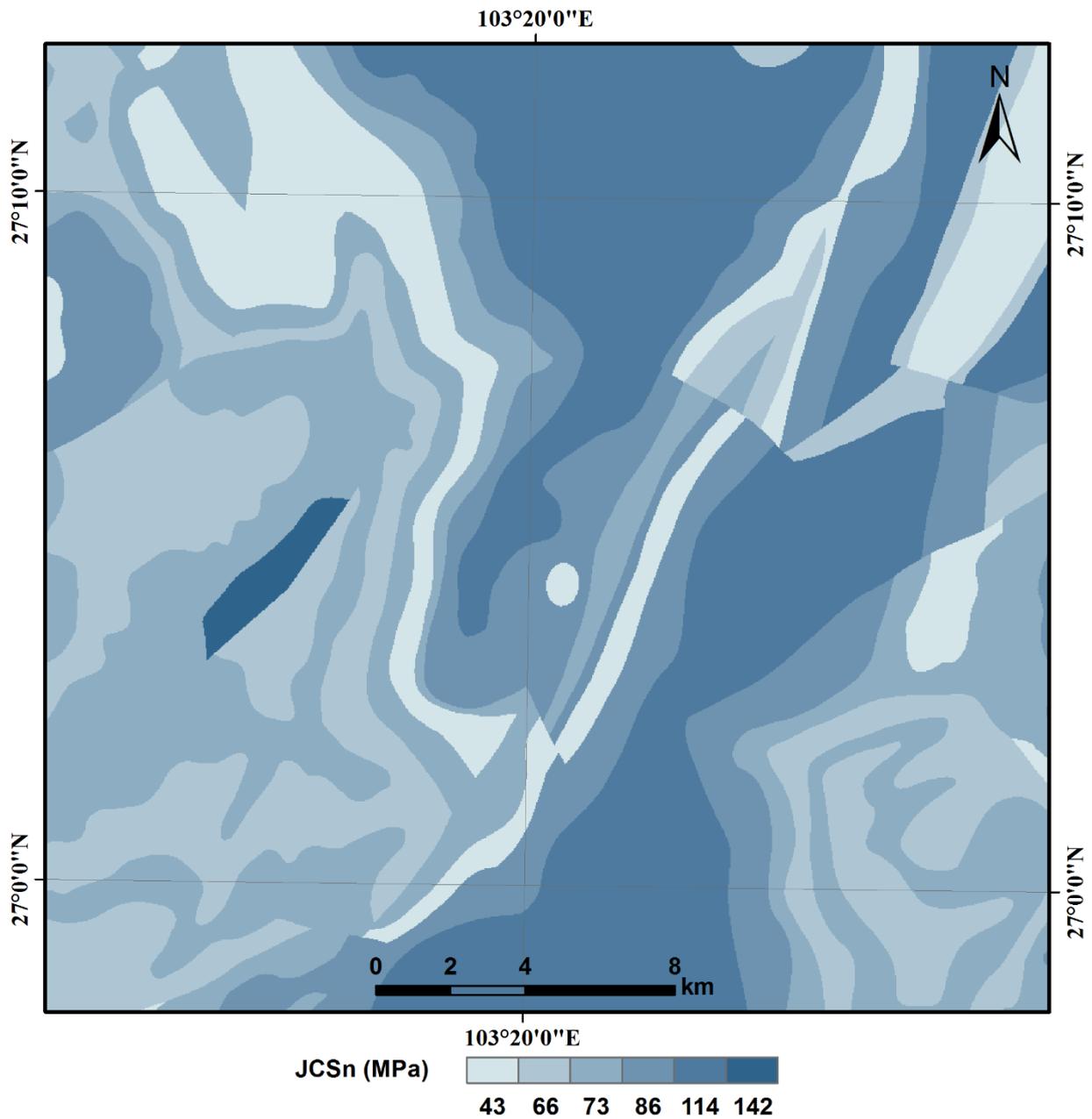
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530   (b)

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532   study area.

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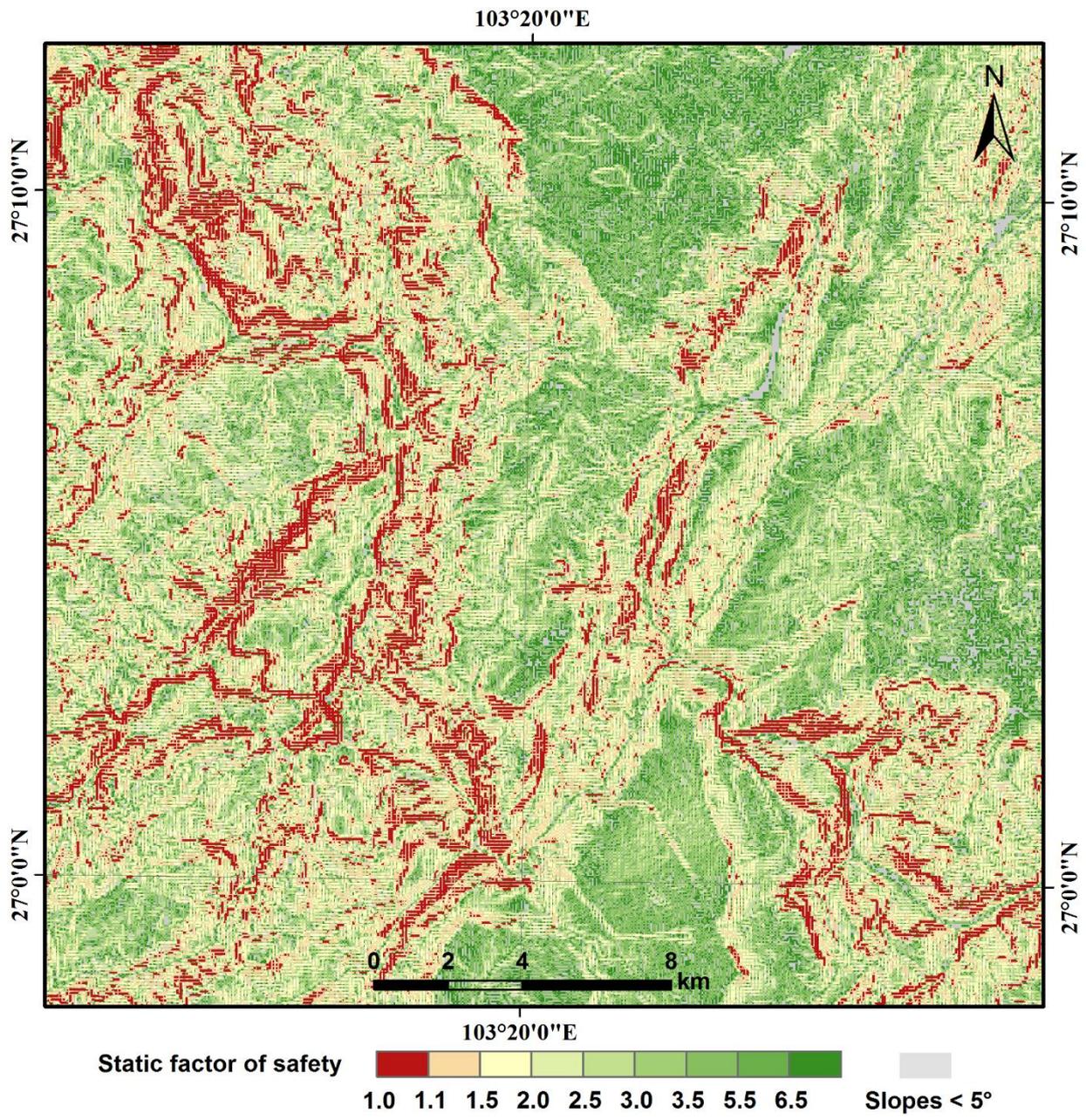
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Fig. 9. Static factor-of-safety map of the study area.
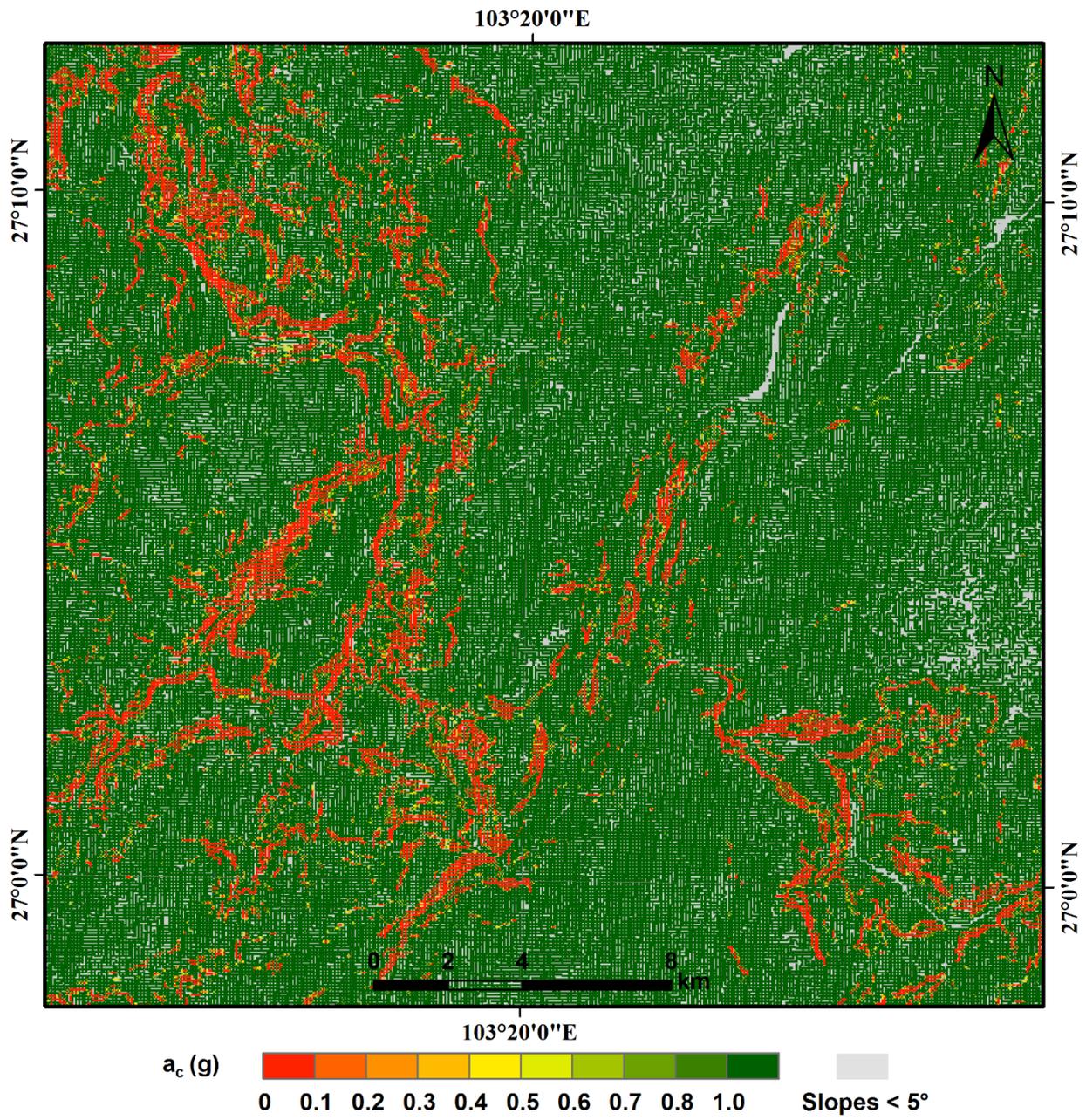
Fig. 10. Map showing critical accelerations in the study area.

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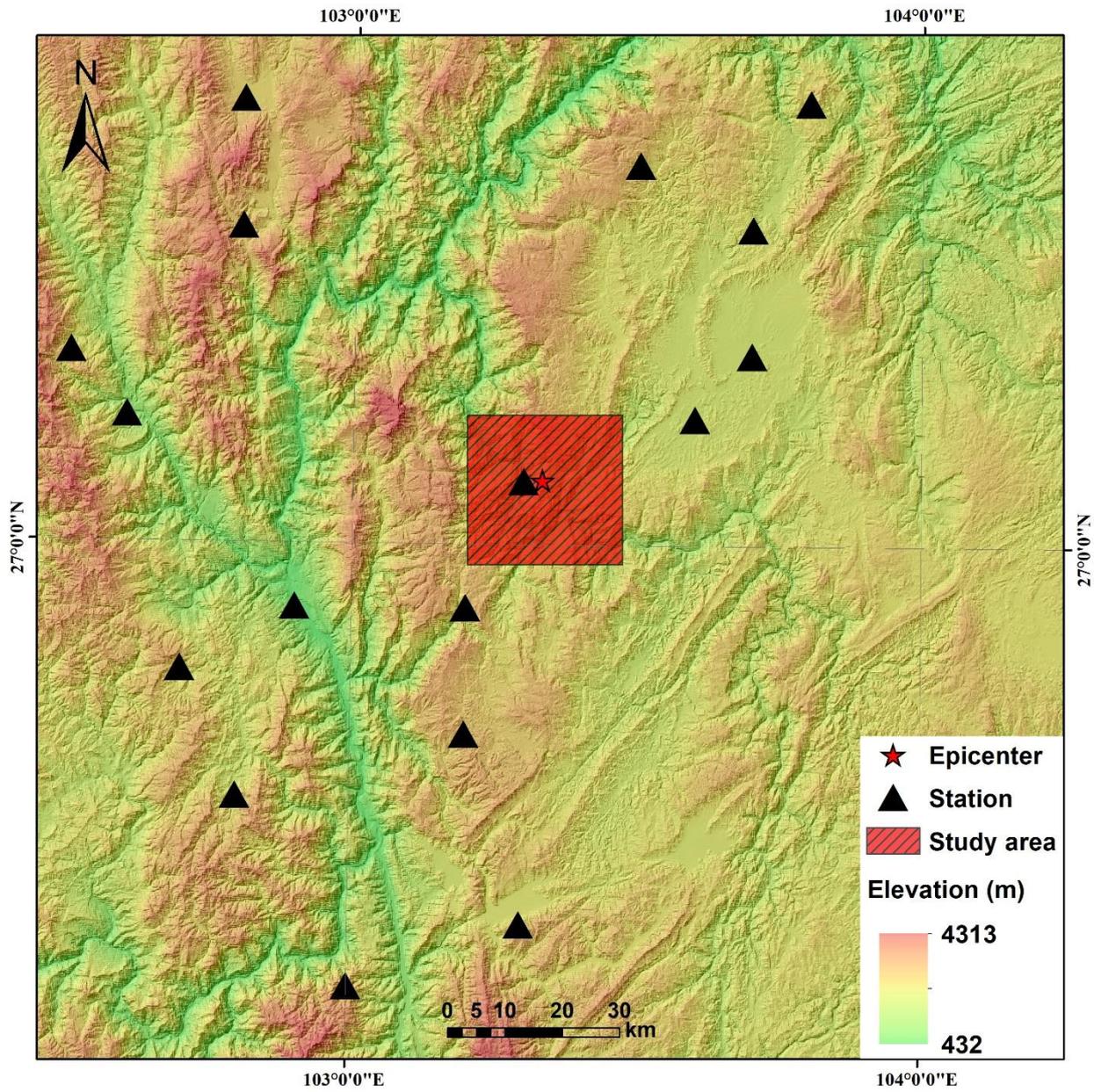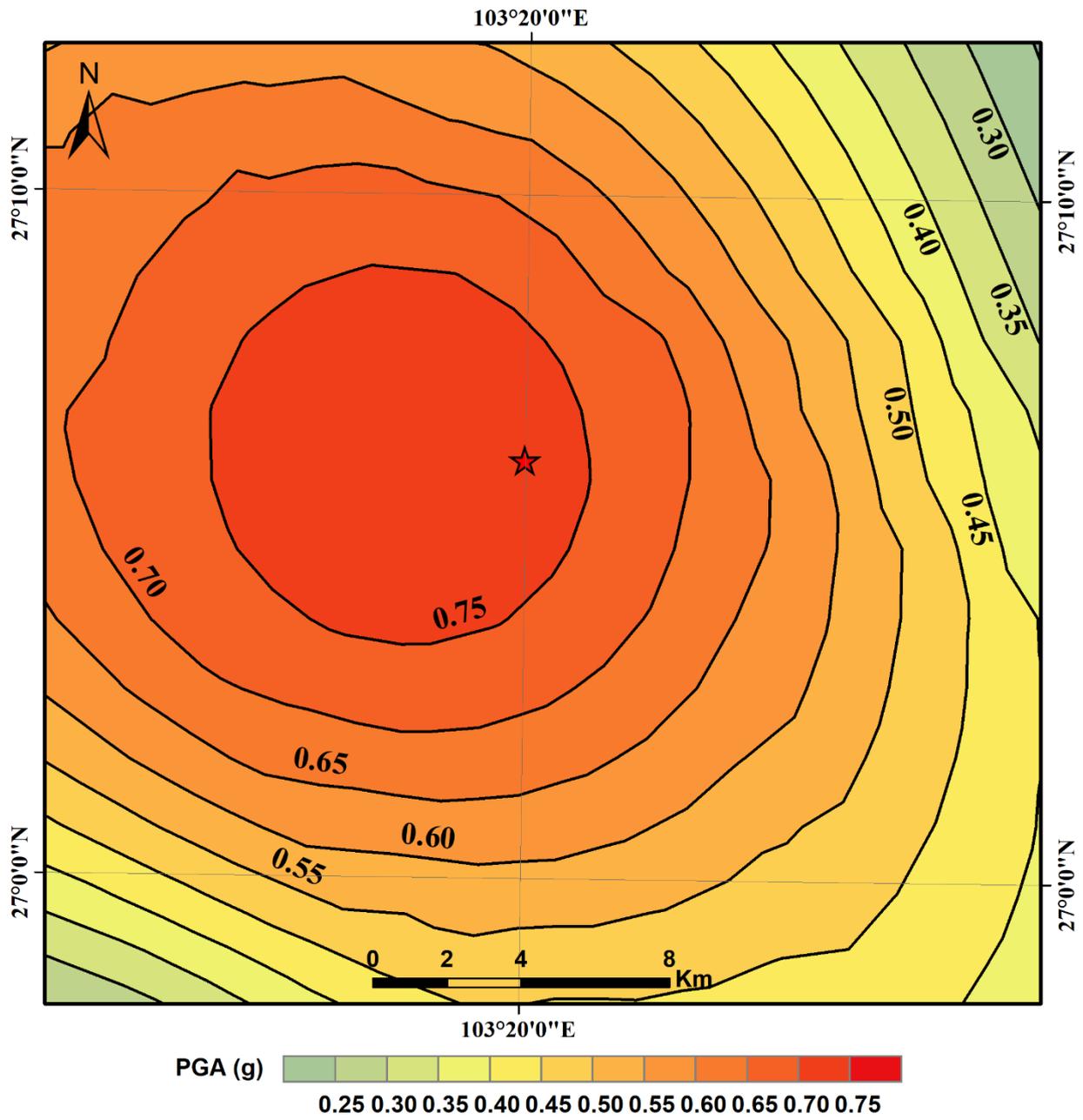
547   **Fig. 11.** Locations of strong-motion stations.

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Fig. 12. Contour map of peak ground acceleration (*PGA*) produced by the Ludian earthquake in the study area. *PGA* values shown are in *g*.
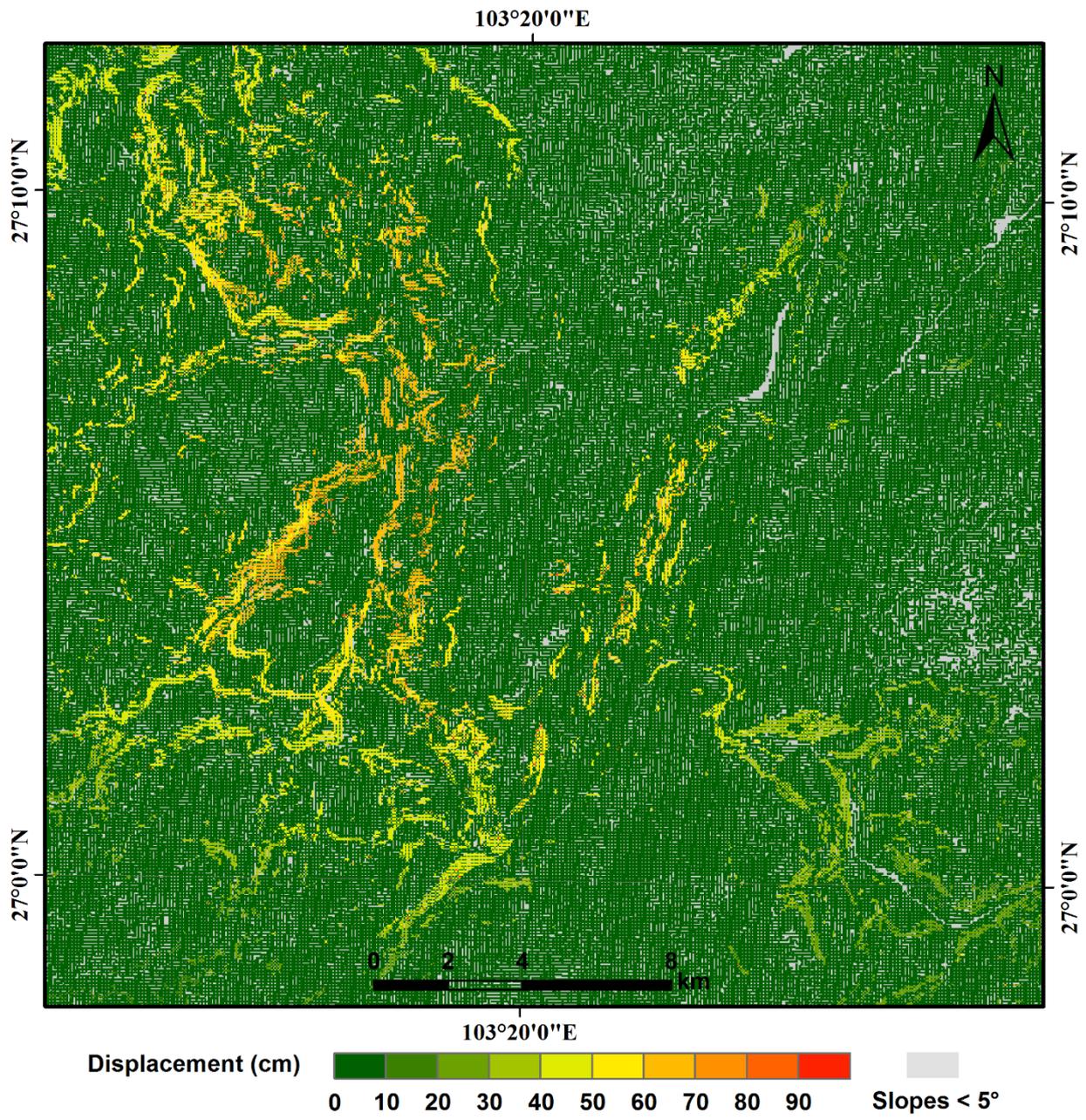
Fig. 13. Map showing predicted displacements in the study area.
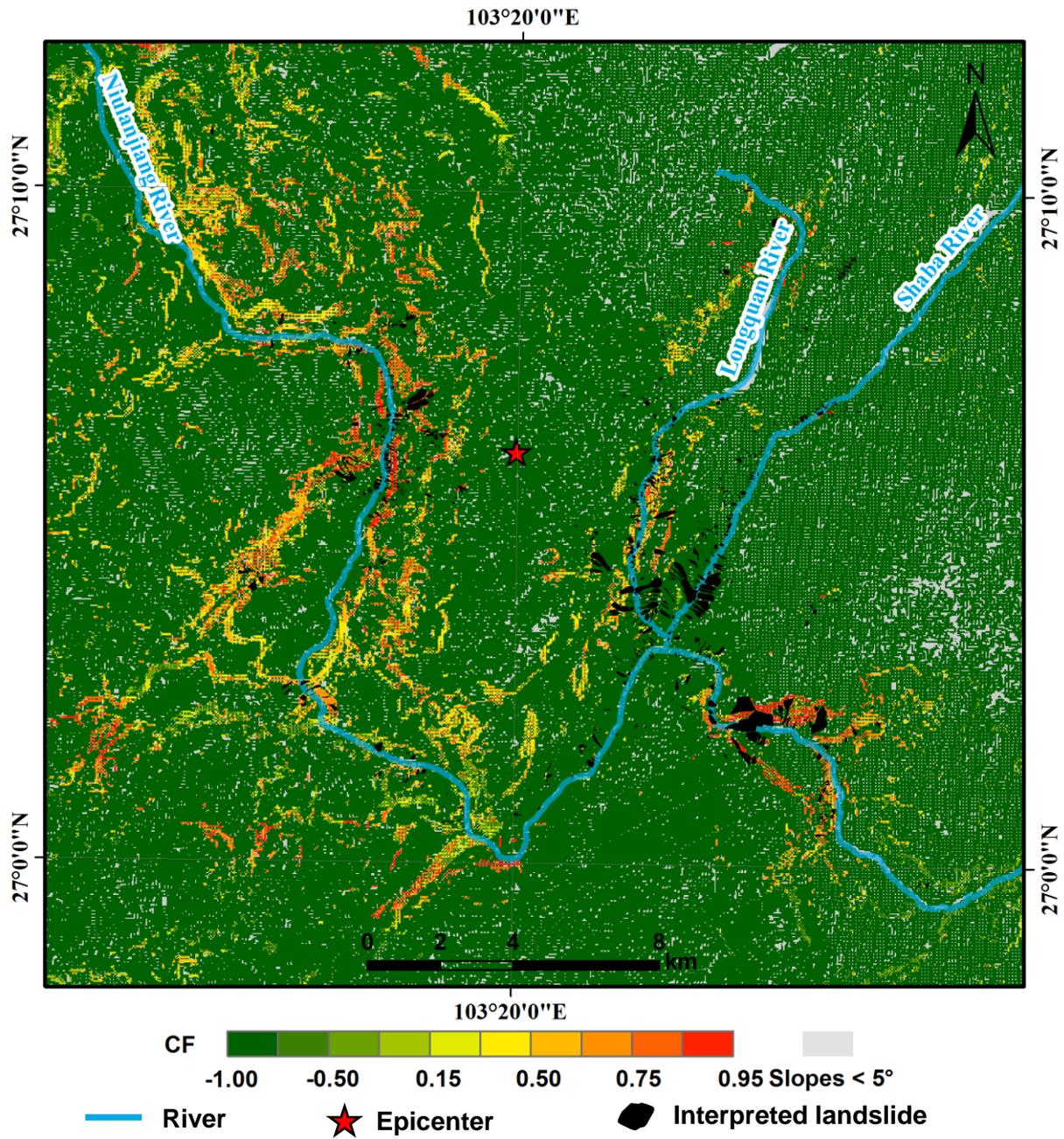
**Fig. 14.** Map showing confidence levels of coseismic landslides in the Ludian earthquake using method introduced in this paper. Confidence levels are portrayed in terms of values of *CF*.

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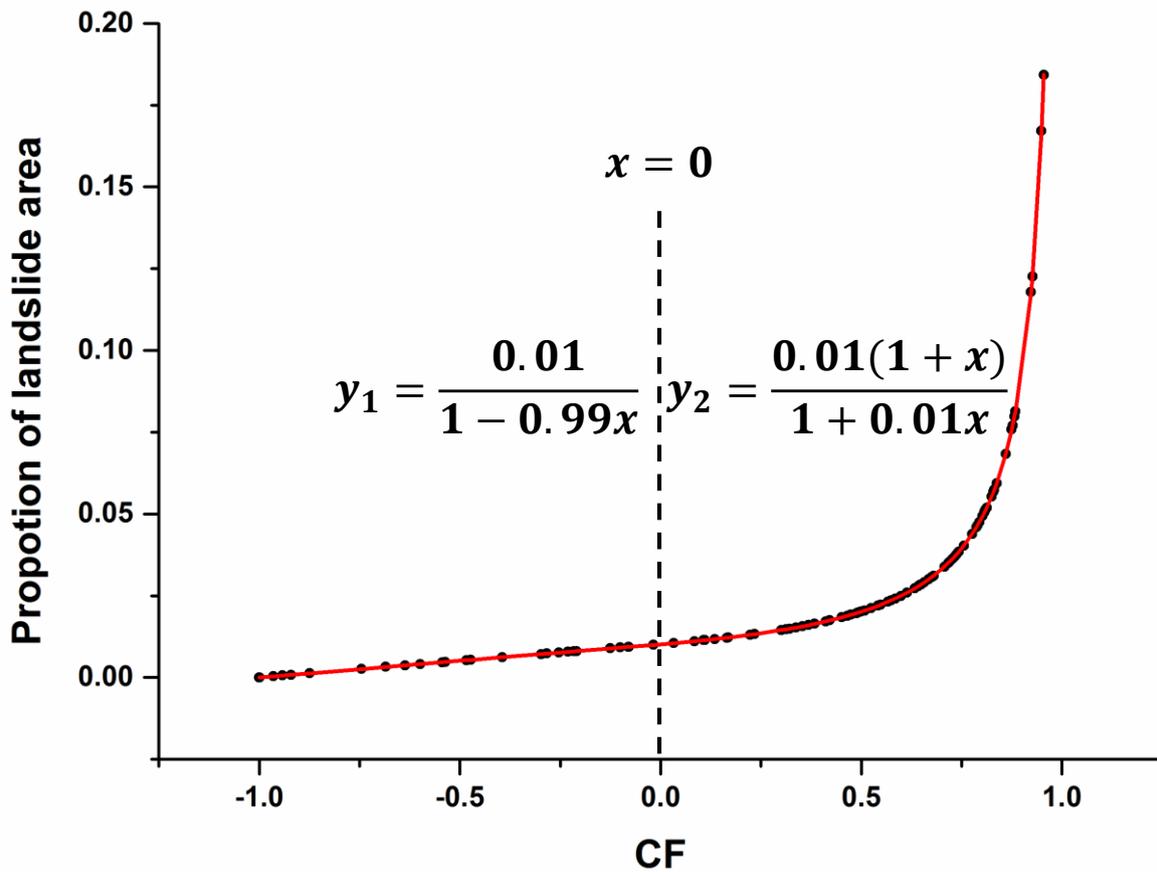
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Fig. 15. Proportion of the area of landslides lying in each CF-value area. A dot shows the proportion of landslide area within an area of CF value; the red line is the fitting curve of the data using second order exponential growth function.

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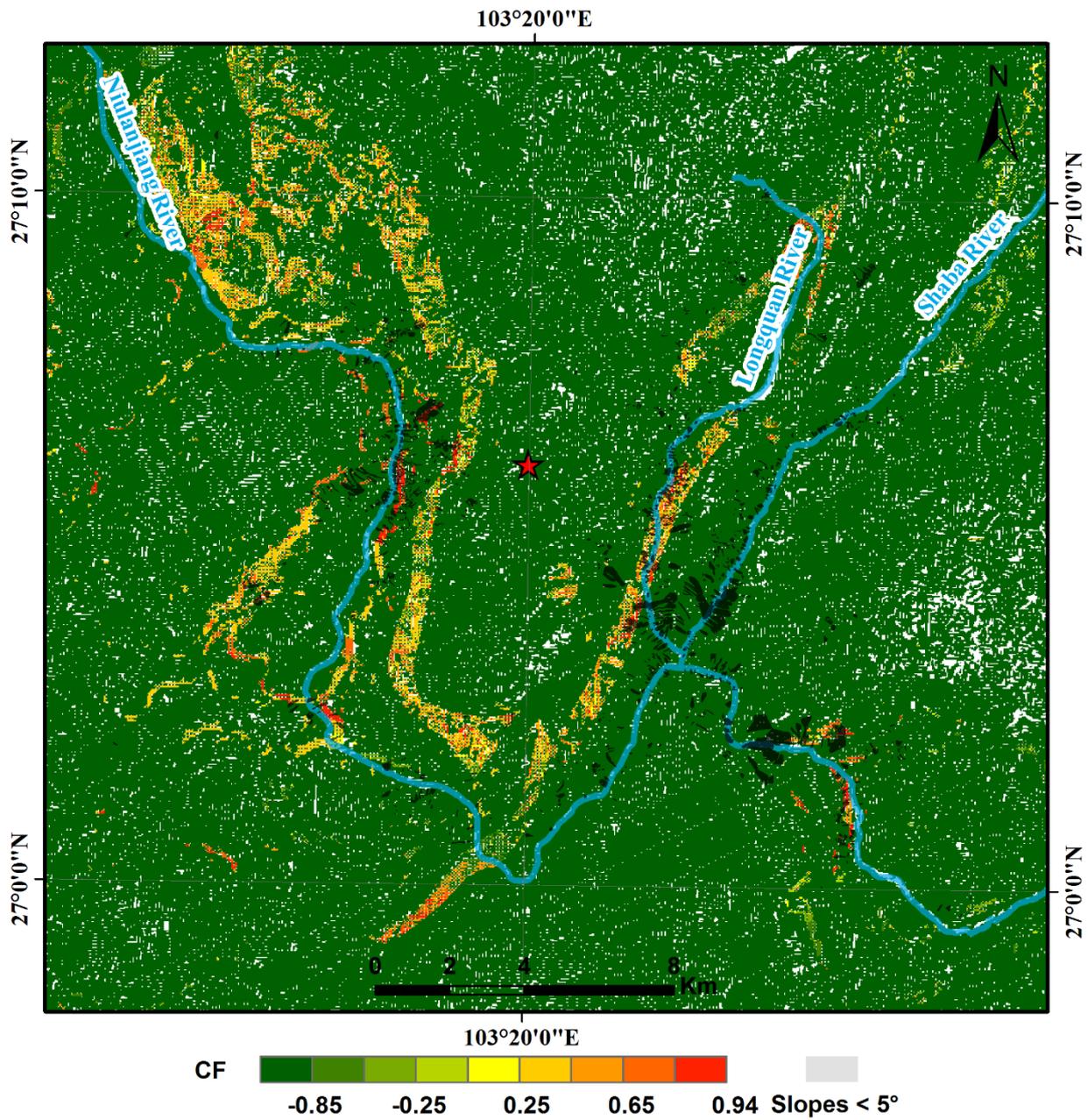
Fig. 16. Map showing confidence levels of coseismic landslides in the Ludian earthquake using a conventional Newmark analysis. Confidence levels are portrayed in terms of values of *CF*.

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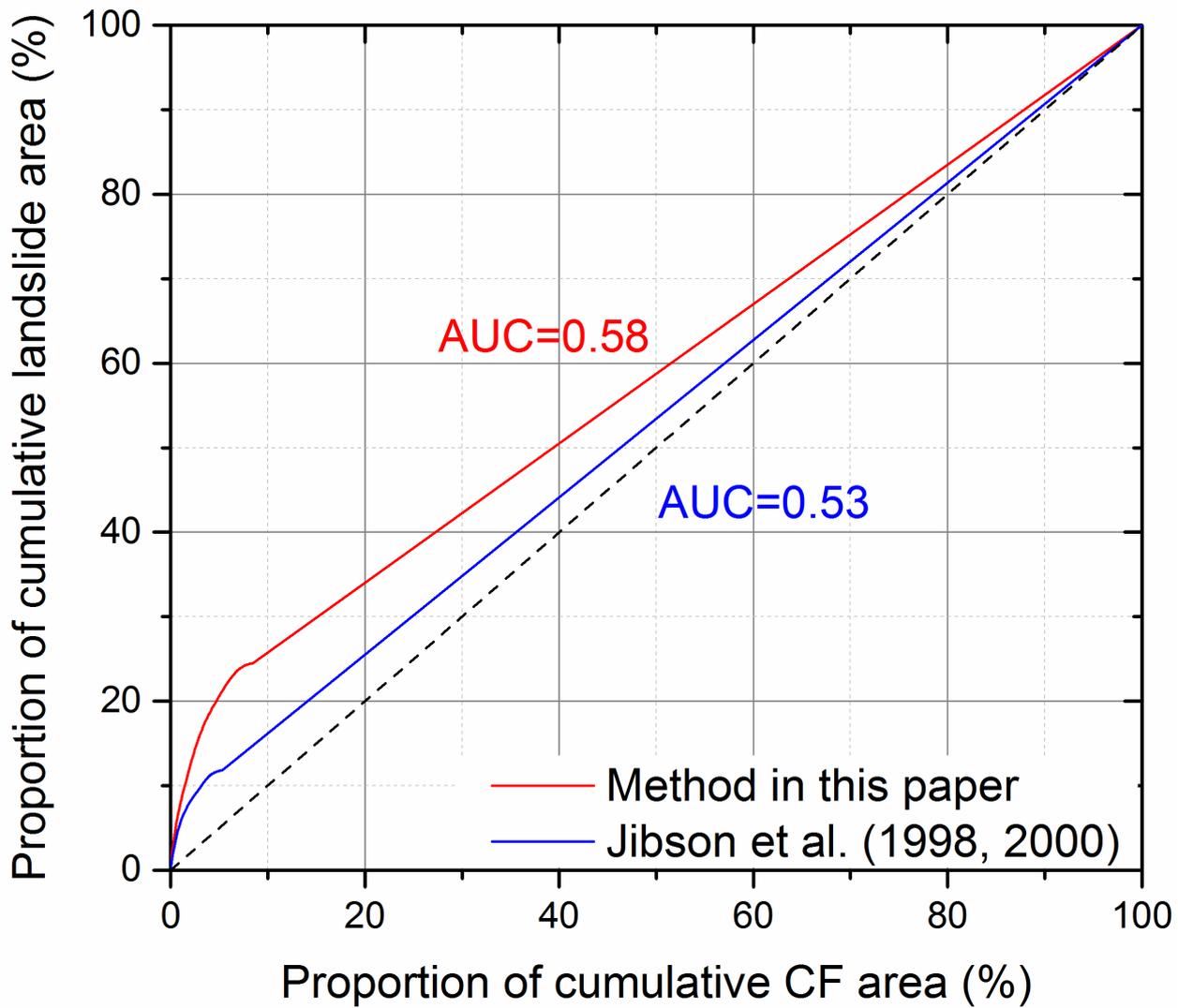
Fig. 17. Area under the curve plots for comparing the new method with a conventional Newmark's method.

576   **Table Captions**

577   **Table 1.** Shear strengths assigned to rock types in the study area.

578   **Table 2.** Station records included three components of the peak ground acceleration.

579

580

581 **Table 1**

582 Shear strengths assigned to rock types in the study area.

Rock type	γ (kN/m^3)	ϕ_b	JCS_0 (MPa)	JRC_0	φ	c (kPa)	References
Dolomite	25.9	32°	140	9.5	43°	35	Singh et al., 2012 Giusepone, 2014 Alejano et al., 2014
Limestone	21.5	37°	160	9	45°	30	Bandis et al., 1983 Singh et al., 2012 Yong et al., 2018
Shale	24.9	27°	75	8	27°	16	Barton and Choubey, 1977 Bilgin and Pasamehmetoglu, 1990 Coulson, 1972
Sandstone	23.5	35°	100	6	42°	24	Bandis et al., 1983 Priest, 1993 Coulson, 1972
Basalt	27.9	38°	205	8.5	50°	40	Barton and Choubey, 1977 Alejano et al., 2014 Coulson, 1972
Slate	26.5	30°	175	3	40°	11	Barton and Choubey, 1977 Bandis et al., 1983 Alejano et al., 2012 Yong et al., 2018

583 Internal friction angle (φ), cohesion (c) and unit weight (γ) are derived from Geological Engineering

584 Handbook (Geological Engineering Handbook Editorial Committee, 2018)

585

586   **Table 2**

587   Station records included three components of the peak ground acceleration.

No.	Station	Epicentral distance (km)	EW (g)	NS (g)	UD (g)	Average of horizontal components (g)
1	Longtoushan 1	8.114	0.5141	0.9679	0.7193	0.7410
2	Longtoushan 2	8.3	0.9685	0.7203	0.5147	0.8444
3	Qianchang	18.6	0.1490	0.1432	0.0539	0.1461
4	Ciyuan	32.6	0.0468	0.0457	0.0265	0.0463
5	Mashu	38.5	0.1380	0.1361	0.0663	0.1370
6	Qiaojia	43	0.0253	0.0210	0.0135	0.0232
7	Zhaotong 1	47.4	0.0096	0.0152	0.0065	0.0124
8	Zhaotong 2	47.671	0.0065	0.0096	0.0088	0.0081
9	Huidongxijie	63.3	0.0123	0.0128	0.0037	0.0126
10	Maolin	64.4	0.0251	0.0184	0.0111	0.0217
11	Yongshanmaolin	65.647	0.0111	0.0252	0.0184	0.0182
12	Jingan	66.2	0.0103	0.0122	0.0062	0.0113
13	Butuotuojue	66.8	0.0118	0.0173	0.0079	0.0146
14	Zhaotongjingan	67.392	0.0062	0.0103	0.0122	0.0083
15	Huidongqianxin	67.4	0.0224	0.0223	0.0067	0.0224
16	Ningnansongxin	69.2	0.0062	0.0081	0.0032	0.0071
17	Pugebaishui	76	0.0152	0.0149	0.0066	0.0151
18	Huize	76.5	0.0164	0.0182	0.0090	0.0173
19	Pugediban	81.2	0.0186	0.0127	0.0046	0.0156
20	Butuodiban	83.7	0.0024	0.0021	0.0024	0.0023

21	Tuobuka	85.2	0.0168	0.0168	0.0136	0.0168
22	Pugeyangwo	91.4	0.0066	0.0069	0.0022	0.0068
23	Daguan	91.8	0.0043	0.0035	0.0027	0.0039

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589