RESPONSE TO REFEREE#1

1) Major revisions should be focused on the discussion of the uncertainties: the length of the synthetic earthquake catalogue and the choices of the parameters. Are 100 earthquakes enough to cover a wide range of scenarios necessary for such a detailed probabilistic analysis for the Tuzla test site? What are we missing? A part from the definitions of the aleatoric and epistemic uncertainties, section 4.4 should present a deeper discussion.

Uncertainties section was re-written in detail and it can be explained why only 100 earthquakes are used, with:” NAFZ generates an earthquake with the recurrence interval of about 250 years beneath the Marmara Sea. Therefore, selecting 100 earthquake scenarios would cover a time period of 100x250 years= 25,000 years which is considered as an adequate catalog duration in this study. However, because of having time dependent probabilistic analyses, this catalog duration is not used for PTHA in this study.”

2) Please re-write the sentence from line 30 to line 34 because it is too long and it is not clear the meaning.

This part was changed with: “The Marmara Sea and the area is one of the most seismically active areas in Turkey. Main active faults of the region pass through under the Marmara Sea. Thus, coastal cities in Marmara region, especially Istanbul which has significant importance in terms of economy, and historical and sociocultural heritage with a population of more than 15 million, is under the threat of high damage due to possible big earthquake and also triggered tsunamis.”

3) At line 39 it is wrong the use of the word “attractive” in this contest, please change or explain.

The region has distinctive characteristics in terms of its complex tectonic structure and high possibility of an earthquake occurrence with the magnitude larger than 7.0 offshore Istanbul mega-city.

4) At line 79 is it “Mw>7″ instead of “M>7” ?

Magnitude type of the expected event is not specified in the reference paper (Ergintav et al.,2014).

5) At line 87 not clear how the small faults generate the tsunami. It is understandable for the submarine failures. Please explain.

In this sentence, several small faults past was chanced with:” E-W trending tectonic deformation along the basin”

6) At line 125 “Grezio et al. 2017” is not in the references.

Paper was added to the reference list.

7) Please keep the acronyms in the text MC (Monte Carlo) and PIF (Prince Island Fault).
Text was modified changing Monte Carlo and Prince Island Fault with their acronyms.

8) Line 226: the sentence “Time dependent probabilistic model is followed for the probability calculations; because, instead of using multi – segment rupture scenarios, only one fault is considered. “ is not clear, please explain it.

This sentence was changed with : “” Time dependent probabilistic model is followed for the probability calculations; because, this probabilistic model allows to consider only one fault instead of using multi – segment rupture scenarios through characteristic earthquake model.”

9) It is better to write parameters and variable using the subscribed mode, for example Tr, Mw, Mo, and so on, because in formula (3) the “2Tr_2t” seems to have 4 variables and not 3.

All the parameters were replaced with subscribed modes in the formulations and text.

10) At line 307 the following sentence should be re-written: “First, graphics are prepared to show general distribution of probability of occurrence with respect to considered tsunami hydrodynamic parameters, which are minimum and maximum water surface elevation and inundation depth”. A possible suggestion is the following: “First, distribution of probability of occurrence of the tsunami hydrodynamic parameters, which are minimum and maximum water surface elevation and inundation depth, are shown”.

This part was changed as recommended.

11) Lines 320-322 in Figure 5, graphics of probabilities of occurrences according to maximum and minimum water surface elevation (maximum water withdraw) and inundation depth for next 50 years are represented, respectively. According to these graphs, tsunami wave heights up to 1 m and withdrawal of the waves around 1 m have approximately 65% probability of occurrence.

The comment regarding this sentence is not clear.

12) Please re-write lines 347-349, they are not clear them. If I understand well your simulation of the worst earthquake case scenario produced the maximum water surface elevation equal to 1.85 m, the minimum water surface elevation (maximum withdraw) equal to 2.16 m and the inundation depth of 4.48 m and the probability of this worst earthquake case scenario is 35% for next 50 years and 60% for next 100 years. In the main text of the paper the residual are not mentioned, please write an explanation there (not only in the captions).

This paragraph was written clearer: “Considering the results of the whole simulations, the worst case earthquake scenario generated tsunami waves with maximum water surface elevation is equal to 1.8 m, minimum water surface elevation (maximum withdraw) is equal to 2.1 m and inundation depth is equal to 1.6 m. The probability of occurrence of this event is 35% for next 50 years and 60% for next 100 years.”
13) Lines 460-464 should be re-written, not clear what the authors intend by “results of the numerical modelling was demonstrated”, “demonstration of results” and “finale outcomes”.

These conclusion remarks are re-written: “Results of this PTHA study was presented in three different ways for the next 50 and 100 years. The first one was the graphs showing the change of probability with the maximum and minimum water surface elevation and inundation depth for different time intervals. Secondly the probabilistic tsunami inundation maps are generated for Tuzla region. Finally, the probability maps of exceedance of 0.3 m wave heights at synthetic gauge points are represented with bar charts.”

14) Figures - Figure 1 is small and the legend is difficult to read. I suggest to use landscape for Figure 1 and to enlarge the legend. Please provide indication for the orange colour dots. - Figure 5 and 6 are difficult to understand, the font of the legend is too small and the red writing cannot be read. - Figure 11 (second panel) can improve the reading using the colour blue or violet for the bar instead of the red.

All the figures are modified regarding to referee comments.
Response to Referee #2

General comments

1. The paper needs major revisions to increase its readability and clarify the adopted methodology (esp. the MC simulations). The title of the paper contains the word “Monte Carlo simulations”. Hence, it is pertinent that the authors include a succinct description of what they mean by the term and how they actually go about utilizing the MC methodology in the context of the paper. For example, any picture showing their sampling of the different parameters (magnitude and depth) would be helpful to the readers to visualize the different scenarios. Thus, in this regard, the current description in Section 2 is inadequate.

Authors appreciate this comment. In fact, explanations for the application of MC simulations have already been revised in Section 2 according to the first referee's comments. We kindly request the referee to reread especially the lines between 175-195 for rephrased explanations.

2. While generating the 100 scenarios for the MC simulations, the PIF fault is defined as a characteristic fault. This crops up in many places in the manuscript. Is this choice because of computational constraints with the simulations or difficulties in applying the MC methodology to multi-segment ruptures or does the seismicity in the PIF does not warrant it? It will be helpful if the authors elaborate on this aspect/choice.

Application of MC simulation technique and the calculation of multi-segment rupture probabilities is a complex problem. Therefore, in this study, only single fault is selected as a source and characteristic model is applied to PTHA as a basic case study. This study can be developed including some connected fault segments to the PIF with static Coulomb stress changes, as mentioned in the manuscript.

Specific comments on the technical content

1. Throughout the paper the tsunami wave height, inundation depth etc. are mentioned as hydrodynamic “parameters”. Since the term parameter is usually used for physical constants in a model, or for independent variables, it is suggested that another word (e.g. quantities) may be used instead.

In literature, the general classification of wave parameters such as velocity, acceleration, height etc. are “hydrodynamic parameters”. Also, there are many examples of using the phrase “tsunami hydrodynamic parameters” in literature (i.e. Brill et al., 2014 https://www.jcronline.org/doi/abs/10.2112/JCOASTRES-D-13-00206.1?journalCode=coas). Therefore, authors would prefer using the term “parameter”.

2. Lines 38-39 – Inclusion of references for studies “regarding the fault mechanisms, ... and triggered tsunamis” will benefit the readers.

Following references are added to the manuscript; Armijo et al., 2002; Armijo et al., 2005; Okay et al., 1999; Le Pichon et al., 2001; Yaltirak 2002; McNeill et al., 2004; Aksu et al., 2000; Imren et al., 2001; Le Pichon et al., 2001; Pondard et al., 2007, Yalçınker et al., 1999; Yalçınker et al., 2002; Aytore et al., 2016 ; Hebert et al., 2005; Altınoğlu et al., 2001; Altınoğlu et al., 2003; Guler et al., 2015; Cankaya et al., 2016; Tufekci et al., 2018; Latcharote et al., 2016

3. Lines 39-40 – Please consider merging or rephrasing the sentence “The region is attractive ... mega-city.” as it seems to be a repetition of facts in lines 34-37.
The sentence was rephrased as: “The region has distinctive characteristics in terms of its complex tectonic structure and high possibility of an earthquake occurrence with the magnitude larger than 7.0 offshore Istanbul mega-city.”

5. Lines 44-45 – Figure 1 gives a nice overview of the seismicity in the region. In the inset figure inside Figure 1, the labels describing the general tectonic map of Turkey are not clear even after zooming in. Consider either enlarging the inset figure or increasing the fonts of the labels or increasing resolution of the image.

The small figure that shows the tectonic mechanism of Turkey is enlarged.

6. Lines 59-61 – It is not clear why the sentence “Therefore, making ... quite difficult” has been added. Does this difficulty somehow influence the methodology or modelling in the paper?

Conducting a segmentation model for the offshore parts of the NAFZ is quite challenging, which causes the fault dimensions, such as its length and width, to include a sum of error margin. This command is also added to manuscript.

7. Lines 75-78 – Consider splitting the sentence “After the 1999 Izmit ... megacity Istanbul” for increasing readability and clarifying the flow of thought.

This sentence was split into two as, “After the 1999 Izmit event seismic energy along the 150 km long northern part of the NAFZ has been accumulated continuously since 22 May 1766 earthquake. This fault zone extend right next to south of Istanbul beneath the Marmara Sea, and this situation increases the rupture possibility of the PIF and the risk for megacity Istanbul (Stein et al., 1997; Barka 1999; Bohnhoff et al., 2013).”

8. Lines 78-90 – The critical importance of the PIF fault in generating the next earthquake has been brought out nicely in this paragraph. Inclusion of concrete numbers/facts from Ergintav et al. will add strength to the argument.

Some certain numbers are included and the sentences was rephrased as, “Ergintav et al., (2014) also indicated that the PIF segment accumulates stress 15±2 mm/yr and the 3.7m slip deficit has been accumulated since the 1766 events and this makes PIF most likely to generate the next M > 7 earthquake along the Sea of Marmara segment of the NAF.”

9. Line 82 – Please list suitable references related to “studies on historical tsunami records” at the end of the sentence. Would it be possible to replace “majority” by a concrete number?

In the literature, the certain number of the earthquake-related tsunami events is not mentioned. Therefore, authors prefer to use the word “majority”.

10. Line 86-88 – A restructuring of the sentence “The recent one ... tsunami.”, would make this fact more readable.

This sentence has been modified as “The recent one happened after the 17 August 1999 Izmit earthquake and after the earthquake, E-W trending tectonic deformation along the basin and submarine failures generated a tsunami.”

11. Line 91 – Please list suitable references related to “tsunami hazard estimation
studies” at the end of the sentence.

Following references are added “Ozer Sozdinler et al., 2019; Hancilar, 2012; Aytore et al., 2016; Hebert et al., 2005”

12. Lines 93-95 – A rewording of the sentence “When focused on ... normal component”, would make the argument clearer.

This sentence was rephrased as “The 40 km long fault in Eastern Basin of Marmara Sea, with a significant normal component, may generate tsunami wave which can reach maximum 2 m height along the Istanbul coast with locally considerable inundation (Hebert et al., 2005).”

13. Lines 98 – Please list suitable references related to “probabilistic seismic and tsunami hazard analyses” at the end of the sentence.

Following references are added; “Murru et al., 2016; Erdik et al., 2004; Hancilar, 2012”

14. Lines 105-107 – Consider restructuring the sentence “However, probabilistic ... probabilistic studies.”, for better clarity. The readers will benefit more, if the authors can cite a few other reasons as to why a probabilistic hazard assessment is important.

The sentence was changed as “However, probabilistic tsunami hazard assessment is important to calculate the tsunami exposure and risk on human populations and infrastructures since probability calculations consider all possible earthquakes in a fault even they occur with very low probability (Lovholt et al., 2012; Lovhot et al., 2015; Grezio et al., 2017).”

15. Lines 107-109 – The difference of the current work from previous approaches needs to be made clearer here. I found it difficult to lock on to the unique contribution of the paper by reading this.

The statement was changed: “Different from previous probabilistic approaches in Marmara Sea, the probability of earthquake occurrences in one fault segment, PIF, are taken into account for the preparation of high-resolution tsunami inundation maps and distribution of hydrodynamic parameters due to the probability of occurrence of associated earthquakes on PIF determined by MC Simulations.”

17. Lines 127-131 – The sentence “Such studies ... maps” is quite long. Consider splitting it up for clearing the flow of the argument.

This sentence was split into two; “Such kind of studies consider the events that generated by co-seismic sea floor displacement, Seismic Probabilistic Hazard Analysis (SPTHA), but numerous tsunami simulations are required to consider all expected combination of seismic sources. This problem can be solved by applying a simplified event tree approach and a two-stage filtering procedure to reduce the number of required source scenarios without decreasing the quality and accuracy of inundation maps (Lorito et al., 2015).”

18. Line 137 – Please give the expansion of the abbreviation “PSHA”. The word “should” is quite strong. Consider replacing it by a milder alternative or adding a sentence or two to justify its usage.

The word “should be” was changed with “can be”

19. Line 139 – Please clarify the phrase “passive margins”.

The explanation is added.
20. Line 144 – Please list suitable references related to “Paleoseismologic studies” here.

Following references are added: “Ryall et al., 1966; Allen, 1968; Schwartz and Coppersmith, 1984”

21. Line 146-147 – It is not at all clear what the authors intend to convey by the sentence “According to Aki ... seismic cycles”.

The sentence is rephrased as “According to Aki (1984), characteristic earthquake is generated as a result of constancy of barriers to rupture through repeated seismic cycles.”

22. Line 170 – The authors are requested to clarify if they perform “seismic zonation” for this work, or use existing results.

The following explanation is added: “In this study, fault segment model proposed in Ozer Sozdinler et al. (2019) is used and PIF is the only segment for seismic source.”

23. Lines 174-175 – The sentence “Tsunami risk ... local ones”, seems to be a repetition of the previous one. Please consider merging the two sentences.

The following sentence is removed: “Regional PTHA studies can be used as a guide for further local studies to develop of a more effective tsunami warning systems.”.

24. Line 180 – The term “randomly” is quite vague. The authors are requested to situate the term in their context by giving more details about say, the sampling etc..

The term “randomly” changed with depth as “uniformly distributed random numbers in a given interval”

25. Line 182 – It is not clear what is conveyed by “represents the number of iterations randomly done in MC simulations”. The authors can either explain it/cite references as to why 100 seems to be representative of the number of samples.

This part was changed as “Therefore, selecting 100 earthquake scenarios would cover a time period of 100x250 years= 25,000 years which is considered as an adequate catalog duration in this study” regarding to comments of first referee.

26. Line 192 – The authors are requested to verify the range of magnitudes “Mw 6.5-7.1” vis-a-vis the constants given in line 194. It would be better to supply the particular values of a and b (apart from the standard errors and deviations) that have been used to arrive at the range.

The characteristic model assumes that an earthquake releases all of the seismic energy during the fault rupture and the magnitude of the earthquake depends on the dimension of fault (Abrahamson and Bommer, 2005) and PIF zone is assumed that it has potential to generate a characteristic earthquake and rupture the entire fault. Therefore, this fault can generate and event between the Mw 6.5 – 7.1 by rupturing entire fault area every time. Standard errors of a and b value are removed.

27. Lines 206-211 – The authors are requested to clarify what is the range of depths used for generating the scenarios. Is it 5 - 14 km or 10 - 14 km? It would be beneficial to the readers if the ranges of parameters used for the MC simulations were included in Table 1, alongside the other fault parameters.

This sentence was added “Therefore, depth of events vary between 5 to 14 km in MC simulations.”
Authors prefer to keep Table 1 in this way, otherwise the information about depth and magnitude range will be given before the explanation of how they are retrieved.

28. Line 218 – Please list suitable references related to “Brownian passage time (BPT), log-normal or another probability distribution” here.

Following references are added “Matthews et al., 2002; Ellsworth et al., 1999; Davis et al., 1989; Rikitake 1974”

29. Lines 218-220 – The sentence “In this model ... elapsed time.”, needs to be rephrased or split for better readability.
The sentence was rephrased as: “In this model, in addition to the recurrence time of earthquake, variability of the frequency of events and the elapsed time from the last characteristic event are the additional required information and the longer elapsed time causes to increase of probability of an event occurrence (Cramer et al., 2000; Petersen et al., 2007).”

30. Lines 221-224 – It is not clear what the authors mean to convey by this paragraph. Is this relevant to the application of the method used in this work?
The following sentence is added “Therefore, this model is suitable for calculating the probability of occurrence of an earthquake on a single fault.”

31. Lines 228-232 – This paragraph is a repetition of lines 70-74 and should be deleted.

It was deleted.

32. Line 236 – The authors can share the reasons for adopting the simplification: “earthquake releases all energy loaded on the fault and then starts the new failure cycle.”. Is it because of lack of earthquake cycling models with residual energy or perhaps, due to incompatibility with the BPT model?

The sentence is rephrased as: “A characteristic event occur when the load-state process reaches to the failure threshold; an earthquake releases all energy loaded on the fault and then starts the new failure cycle.”

33. Lines 247-249 – The authors are suggested to cite a reference for the definition of Tr so that interested readers may look into it.

The following reference is added “Ren and Zhang, 2013”

34. Lines 269-270 – The linear version of the SW equations is usually faster than the non-linear version, needs lesser memory and is accurate in deep water where nonlinear effects may be neglected. Thus, the reasons given by the authors here are not convincing. A NSW model is, of course, a better model than the linear case because it models the physics better. The authors can supply a sentence or two as to why the use of NSW is attractive in this work.

There is typo in this sentence, thanks the referee for the correction. It was corrected as Linear shallow water equations.

35. Line 274 – The authors have used Okada equations for calculating deformation due to the fault. A figure of the PIF segmentation (maybe in Figure 2, left figure) portraying one of the scenarios from the 100 cases would be helpful to visualize the fault.

The figure is added to manuscript as Figure 5.
36. Lines 279-280 – Accurate coastal bathymetry is crucial for accuracy in highresolution simulations near the coast. The authors can clarify the source for the bathymetry-topography data at 3m resolution. Is it simply the downscaled version of 30m ASTER and 900m GEBCO data? Or is it another, local dataset? Also, when merging the different bathymetry datasets, a common problem is the fixing of the coastline. How do the authors decide the coastlines between GEBCO and ASTER, as well as the digitized coastline from ArcGIS(?)? A few sentences describing their adopted methodology would be appropriate.

The explanation for bathymetry-topography data was added.

37. Line 292 & Figure 4 – The ratio 1 : 3 has been employed here for scaling of consecutive mesh resolutions for simulation. Is there a similar guideline for appropriate spacing between the different nested grids? In Figure 4, the nesting rectangles for 3m, 9m, and 27m are bunched together on their right (eastern) sides. This would create a sharp gradient of mesh resolution from 3m to 27m in that region. The authors can comment on the possible repercussions due to this on the results. Although the nested domains seem like they are located very close to each other, this is just because of map resolution. In fact, there are enough number of grid nodes between two consecutive domains in order to have stable calculations in NAMIDANCE. Besides, it doesn’t cause stability problem to have even only one grid node between two domains.

38. Lines 323-325 – The authors make a good point about the importance of the minimum wave height in terms of stranding of ships. A citation/past example would make this point even better.

The example of 20th July 2017 Bodrum-Kos earthquake and tsunami (Yalçınler et al., 2017) is added.

39. Lines 348,471 – The inundation depth calculated in worst case earthquake scenario is given as “4.48m”. I am unable to find this number in Figures 5 or 6. The authors can clarify this. Also, should it be “2.16m” or -2.16m, as is written in line 471?

The inundation depth should be 1.6m instead of 4.48. Therefore, it was changed with 1.6m.

40. Line 352 – I was very interested in the hazard of small amplitude waves dragging people. A citation would be relevant for readers (like me) who would want to dig more into this aspect.

The following reference is added; “Jonkman and Penning-Rowsell, 2008”

41. Line 363 - Do the authors mean “mean (average) inundation depth values” or mean (average) probability values? It would be more clarifying to include a step-by-step/point-by-point procedure of calculating the exceedance probabilities from the 100 MC simulations.

The calculations steps are explained gradually as suggested.

42. Lines 434-444 - This discussion of uncertainties does not shed enough light on the results. As such, it is better positioned in the methodology section (maybe? before line 233/discussion of BPT model). Otherwise, the authors can expand this section a bit more with concrete connections to the numbers in the numerical results.

The discussion of uncertainties has already extended according to comments of the first referee.
Probabilistic Tsunami Hazard Analysis For Tuzla Test Site Using Monte Carlo Simulations

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Abstract. In this study, time-dependent probabilistic tsunami hazard analysis (PTHA) is performed for Tuzla, Istanbul in the Sea of Marmara, Turkey, using various earthquake scenarios of Prince Island Fault (PIF) within next 50 and 100 years. Monte Carlo (MC) simulation technique is used to generate a synthetic earthquake catalogue, which includes earthquakes having moment magnitudes between Mw 6.5 and 7.1. This interval defines the minimum and maximum magnitudes for the fault in the case of entire fault rupture, which depends on the characteristic fault model. Based on this catalogue, probability of occurrence and associated tsunami wave heights are calculated for each event. The study associates the probabilistic approach with tsunami numerical modelling. Tsunami numerical code NAMI DANCE was used for tsunami simulations. According to the results of the analysis, distribution of probability of occurrence corresponding to tsunami hydrodynamic parameters are represented. Maximum positive and negative wave amplitudes show that tsunami wave heights up to 1 m have 65% probability of exceedance for next 50 years and this value increases by 85% in Tuzla region for the next 100 years. Inundation depth also exceeds 1m in the region with probabilities of occurrence of 60% and 80% for the next 50 and 100 years, respectively. Moreover, probabilistic inundation maps are generated to investigate inundated zones and the amount of water penetrated inland. Probability of exceedance of 0.3 m wave height ranges between 10% and 75% according to these probabilistic inundation maps and the maximum inundation distance calculated among entire earthquake catalogue is 60 m in this test site. Furthermore, synthetic gauge points are selected along the western coast of the Istanbul by including Tuzla coasts. Tuzla is one of the area, that show high probability exceedance of 0.3 m wave height, which is around 90%, for the next 50 years while this probability reaches up to more than 95% for the next 100 years.

1 Introduction

Marmara Region, especially highly populated cities along the coasts of the Marmara Sea, is the heart of Turkish economy in terms of having great number of industrial facilities in largest capacity and potential, refineries, ports and harbors. The Marmara Sea and the area is one of the most seismically active areas in Turkey. Main active faults of the region pass through the...
Marmara Sea. Thus, coastal cities in Marmara region, especially Istanbul, which has significant importance in terms of economy, and historical and sociocultural heritage with a population of more than 15 million, is under the threat of high damage due to possible big earthquake and also triggered tsunamis. Recent studies and evaluation of earthquake recurrence periods revealed that there is a high possibility of having an earthquake with magnitude larger than $M_{w} > 7.0$ in PIF. According to Ambraseys (2002), the latest earthquake on this fault system occurred in 1766 and since that time, this fault has been accumulating huge amount of energy. According to Parsons (2004), the probability of occurrence of $M>7$ earthquake beneath the Marmara Sea was estimated to be 35-70% in the following 30 years. The region has distinctive characteristics in terms of its complex tectonic structure and high possibility of an earthquake occurrence with the magnitude larger than 7.0 offshore Istanbul mega-city. Therefore, there has been a wide range of studies in Marmara Sea region regarding the fault mechanisms, seismic activities, earthquakes and triggered tsunamis (Armijo et al., 2002; Armijo et al., 2005; Okay et al., 1999; Le Pichon et al., 2001; Yaltirak 2002; McNeill et al., 2004; Aksu et al., 2000; Imren et al., 2001; Pondard et al., 2007; Yalçiner et al., 1999; Yalçiner et al., 2000; Yalçiner et al., 2002; Aytore et al., 2016; Hebert et al., 2005; Altunok et al., 2001; Altunok et al., 2003; Guler et al., 2015; Cankaya et al., 2016; Tufekci et al., 2018; Latcharote et al., 2016).

The North Anatolian Fault Zone (NAFZ) controls the great part of the seismic activity in the Marmara Sea region. The fault zone sets apart Anatolia (Asian part of Turkey) and Eurasia due to the northward migration of Arabian Plate in the east and southward rollback of the Hellenic subduction zone in the west as seen in Fig. 1 (Armijo et al., 1999; Flerit et al., 2004; Le Pichon et al., 2015).
Figure 1: Seismicity map of the Marmara region and general tectonic map of the Turkey on the top – left. In the seismicity map, the size of the circle's changes with magnitude of the earthquakes and the color of the circles defines the depth change of the earthquakes. Red lines show the known active faults (Modified from Emre et al., 2013) in the region and white square is the area with the PIF. In the general tectonic map of Turkey, red arrows show the direction of the plate motion, black lines show the active faults in the region (Modified from Emre et al., 2013) and red rectangular shows the Marmara region (created using The Generic Mapping Tools, Version 5.4.1).
The Marmara Sea region is a transition zone between the strike-slip regime of the NAFZ and the extension regime of the Aegean Sea area (on the top – left of Fig 1). The northern branch of the NAFZ forms a major transtensional NW-SE right bend under the Sea of Marmara at Çınarcık trough (Murru et al., 2016). The fault trace is attached to the complex Central Marmara and Tekirdağ pull-apart basins, before joining the NE-SW striking Ganos fault on land by following the northern margin of the Marmara Sea. Finally, the fault exits into the Aegean Sea by way of Saros Gulf (Wong et al., 1995; Armijo et al., 1999; Armijo et al., 2002; Okay et al., 1999; Le Pichon et al., 2001; Yalçınkaya 2002; McNeill et al., 2004). The fault trace beneath the Marmara Sea is not directly observable. Therefore, making a segmentation model for the offshore parts of the NAFZ is quite challenging, which causes the fault dimensions, such as its length and width, to include a sum of error margin (Aksu et al., 2000; Imren et al., 2001; Le Pichon et al., 2001; Armijo et al., 2002; Armijo et al., 2005; Pondard et al., 2007).

The current right-lateral slip rate along the NAFZ is about 25 mm/yr (Meade et al., 2002; Reilinger et al., 2006). In the western side, the motion between the Anatolia and Eurasia plates is accommodated across the Marmara region by ~ 19 mm/yr of right-lateral slip and 8 mm/yr of extension (Flerit et al., 2003; Flerit et al., 2004). Slip rates of the main Marmara fault range between 17-28 mm/yr (Le Pichon et al., 2003; Reilinger et al., 2006). On the other hand, Hergert and Heidbach (2010) suggests that the right-lateral slip rate on the main Marmara fault is between 12.8-17.8 mm/yr due to slip partitioning and internal deformation.

The right-lateral slip rate for the PIF and Çınarcık basin is 15±2 mm/yr and in addition to this, the fault has 6±2 mm/yr of extension (Ergintav et al., 2014).

The main characteristic of the NAFZ is having earthquakes systematically propagated westward and historical records show that, northern strand of the NAFZ generates an earthquake with the recurrence interval of about 250 years beneath the Marmara Sea and the latest event occurred in 1766 (Ambraseys, 2002, Bohnhoff et al., 2013). This event caused the rupture of the 58 km long northern part of NAFZ from İzmit to Tekirdağ (Ambraseys and Finkel, 1995; Ambraseys and Jackson, 2000).

However, the earthquake that happened on 2 September 1754 can be considered as the latest characteristic event for the PIF segment and it caused the rupture of a 36 km long fault segment (Ambraseys and Jackson, 2000). The NAFZ has experienced two M>7 earthquakes in August 1912 Ganos and August 1999 İzmit earthquakes recently. After the 1999 İzmit event, seismic energy along the 150 km long northern part of the NAFZ has been accumulating continuously since 22 May 1766 earthquake. This fault zone extends right next to south of Istanbul beneath the Marmara Sea, and this situation increases the rupture possibility of the PIF and the risk for megacity Istanbul (Stein et al., 1997; Barka 1999; Bohnhoff et al., 2013). Ergintav et al., (2014) also indicated that the PIF segment accumulates stress 15±2 mm/yr and the 3.7m slip deficit has been accumulating since the 1766 events and this makes PIF, most likely to generate the next M>7 earthquake along the Sea of Marmara segment of the NAF.

Beside these seismic activities in the region, studies on the historical tsunami records show that 35 tsunami events happened between BC 330 and 1999 in the Marmara Sea region and the majority of them are earthquake-related tsunami events (Altınok et al., 2011; Yalçınkaya et al., 2002). The 1509 earthquake, with an estimated magnitude around 8.0, is one of the examples for these events. This earthquake triggered a tsunami and the tsunami waves inundated along Istanbul coasts, reaching the city walls and around 4000–5000 people died in the city (Ambraseys and Finkel, 1995). The 1894 earthquake is also one of the...
important events that happened in the Marmara Sea. The earthquake triggered a tsunami and the sea inundated 200 m in Istanbul (Altinok et al., 2011). The recent one happened after the 17 August 1999 İzmit earthquake and after the earthquake, E-W trending tectonic deformation along the basin and submarine failures generated a tsunami. The International Tsunami Survey Team (Yalçın et al., 1999; Yalçın et al., 2000) investigated the region and they observed 2.66 m run-up along the coast from Tütüncülik to Hereke and 2.9 m run-up at Değirmendere (Yalçın et al., 2002).

Several tsunami hazard estimation studies (Ozer Sozdinler et al., 2019; Hancilar, 2012; Aytore et al., 2016; Hebert et al., 2005) were also conducted in the region. These tsunami analyses were mostly performed in deterministic manner using various earthquake scenarios depending on the combinations of different fault parameters without considering probability of occurrences. The 40 km long fault in Eastern Basin of Marmara Sea, with a significant normal component, may generate tsunami wave which can reach maximum 2 m height along the Istanbul coast with locally considerable inundation (Hebert et al., 2005). The rupture of Yalova Fault, PIF or Central Marmara Fault can also cause a serious damage along the coast of Istanbul. Tsunami wave heights can reach 4.8 m and can penetrate 340 m inwards from the coast in Haydarpaşa Port (Aytore et al., 2016).

A few probabilistic seismic and tsunami hazard analyses (Murru et al., 2016; Erdik et al., 2004; Hancilar, 2012) were also done in this region. Seismic hazard maps were prepared in the Marmara Sea region by describing fault segments and peak ground accelerations with the periods corresponding to 10% and 2% probabilities of exceedance in 50 years (Erdik et al., 2004). Besides that, tsunami inundation maps are prepared based on probabilistic and deterministic analyses by depending on these segmentations (Hancilar, 2012). Time-dependent and time-independent earthquake ruptures are also estimated in the Marmara Sea region for the next 30 years (Murru et al., 2016). These previous studies have been conducted for entire Marmara Sea region and therefore they give general and rough information about probability of occurrence in the region without focusing on any specific region in high resolution. However, probabilistic tsunami hazard assessment is important to calculate the tsunami exposure and risk on human populations and infrastructures, since probability calculations consider all possible earthquakes in a fault even if they occur with very low probability (Lovholt et al., 2012; Lovholt et al., 2015; Grezio et al., 2017). The results of probabilistic studies should be considered when decision makers design coastal zones and structures, especially critical ones. Different from previous probabilistic approaches in the Marmara Sea, the probability of earthquake occurrences in one fault segment PIF are taken into account for the preparation of high-resolution tsunami inundation maps and distribution of hydrodynamic parameters due to the probability of occurrence of associated earthquakes on PIF determined by Monte Carlo Simulations.

This PTHA study depends on the fully characteristic fault model and the main purpose is to perform PTHA for selected test site. Tuzla test site is one of the coastal districts of Istanbul and located on the southernmost part of the city (Fig 2). The region includes several residential areas, but the most critical point about the region is that Tuzla has the biggest shipyard area not only in the Marmara Sea but also in Turkey (Fig 3). In this study we mainly focused on this region because it is about 20 km away from the PIF and therefore has high risk of both earthquake and tsunami damage.
Figure 2: The Marmara Sea Region, Tuzla Test Site and the Location of PIF Segment which is used in the analysis like a straight line (created using ArcMap Version 10.5).
Figure 3: Some Important Locations at Tuzla Domain (a) Northern part of the Tuzla domain. (b) Southern part of the Tuzla Domain. (c) Tuzla Shipyard (created using ArcMap Version 10.5).
Probabilistic tsunami hazard analysis (PTHA), as it is recently becoming a widely used procedure for coastal zones, is performed for Tuzla region, Istanbul. This method has been applied for various tsunami sources, such as earthquakes, landslides, volcanic activities, etc., in various scales, local, regional, and global (Grezio et al., 2017). For the earthquake generated tsunamis, the method is generally adapted from seismic hazard assessment methods (González et al., 2009). Such kind of studies consider the events that are generated by co-seismic sea floor displacement. Seismic Probabilistic Hazard Analysis (SPTHA), but numerous tsunami simulations are required to consider all expected combination of seismic sources. This problem can be solved by applying a simplified event tree approach and a two-stage filtering procedure to reduce the number of required source scenarios without decreasing the quality and accuracy of inundation maps (Lorito et al., 2015). The earthquake source itself is very uncertain and the investigation of this uncertainty can be done by building an event tree instead of using logic tree and hazard integrals (Selva et al., 2016). Logic tree approach can be applied to generation of tsunami hazard curves to decrease the uncertainties by including branches, which are the combination of tsunami sources, magnitude distribution of characteristic tsunamigenic earthquakes, their recurrence interval, and tsunami height estimation procedure based on a numerical simulation (Annaka et al., 2007). For regional studies, hazard curves can be generated by empirical analysis using available tsunami run-up data. However, if such data is not available, Monte Carlo simulations, a computational based method widely used in probabilistic seismic hazard analysis (PSHA), can be considered as a primary method to generate tsunami hazard curves (Geist and Parsons, 2006; Horspool et al., 2014). Submarine landslides, on the other hand, are the major tsunami source for passive margins, which are the transition zone between oceanic and continental lithosphere that is not an active plate boundary, and they have been included in PTHA methodologies (Geist and Lynett, 2014). Probabilistic studies are also applied to develop multi-hazard loss estimation methodology for coastal regions that are exposed to cascading shaking-tsunami hazards due to offshore mega-thrust subduction earthquakes (Goda and Risi, 2018).

In this study, characteristic earthquake model is used to estimate the earthquake recurrence on PIF. Paleoseismicologic studies (Ryall et al., 1966; Allen, 1968; Schwartz and Coppersmith, 1984) suggest that an individual fault tends to generate characteristic earthquakes having a very narrow range of magnitudes. These individual faults have a different frequency distribution than the log linear Gutenberg-Richter frequency-magnitude relationship (Aki, 1984; Schwartz and Coppersmith, 1984; Youngs and Coppersmith, 1985). According to Aki (1984), characteristic earthquake is generated as a result of constancy of barriers to rupture through repeated seismic cycles. PIF is fully characteristic and a characteristic earthquake will rupture entire fault as a whole and release the entire energy. Therefore, while performing Monte Carlo simulations, area of the fault and fault parameters (strike, dip and rake angles) are used as constants referring to the outcomes of EU 7th Frame Project MARSITE (Ozer Sozdinler et al., 2019). One of the work packages of this project aimed to define the geometry of the possible tsunamigenic faults in the Marmara Sea and 30 different earthquake scenarios with the different rupture combinations of 32 possible fault segments. Based on these 30 different earthquake scenarios, tsunami numerical modelling is performed. The definition of fault segments depends on extensive review of the
As a result of this review, each fault segment is defined as a rectangular area with hypothetical uniform slip. According to the results of the project, the fault parameters of the PIF, are given in Table 1. The 3D Fault configuration given by Armijo et al., 2002, which explains fault segmentation in the region depending on morphology, geology and long-term displacement fields, also fits with the PIF parameters that are used in the project. These parameters are used as constants in this study while assessing probability of occurrence of each earthquake to allow entire fault rupture at different depths with different magnitudes.

<table>
<thead>
<tr>
<th>Fault Length (km)</th>
<th>Fault Width (km)</th>
<th>Strike</th>
<th>Dip</th>
<th>Rake</th>
</tr>
</thead>
<tbody>
<tr>
<td>33.5</td>
<td>14</td>
<td>119</td>
<td>80</td>
<td>210</td>
</tr>
</tbody>
</table>

Table 1: The area and the focal mechanism of the PIF zone. These are the constant parameters during the MC simulation application.

MC simulation technique is generally applied to generate earthquake catalogue of a given length of time. In this technique, a list of earthquakes can be generated using the frequency-magnitude relationship for each seismic source (Zolfaghari, 2015). Seismic zonation should be done by considering regions that have relatively homogeneous earthquake activity and faulting regimes (Sørensen et al., 2012). In this study, fault segment model proposed in Ozer Sozdinler et al., 2019 is used and PIF is the only segment for seismic source. After that, tsunami numerical modelling is performed for each event of this synthetic catalogue and tsunami hydrodynamic parameters, mainly maximum wave heights, inundation depth, current velocities, as well as tsunami inundation zones are estimated. Tsunami risk assessment will serve the best for the needs of societies when associate regional studies with the local ones (Sørensen et al., 2012).

MC simulation technique allows generating a list of earthquakes based on a frequency-magnitude relationship. This technique depends on a uniformly distributed source model and it provides equal chance to each earthquake source. As a result, synthetic earthquake catalogue will have uniformly random distributed earthquake sources (Zolfaghari, 2015). Using MC simulation, a synthetic earthquake catalogue is generated by selecting earthquake magnitude and depth as uniformly distributed random numbers in a given interval and using area and directivity of the fault as a constant variable (Table 1). We performed MC simulations 100 times for having 100 different earthquake scenarios. The number of earthquakes in the catalog is selected as a reasonable number, which represents the number of iterations randomly done in MC simulations for having a synthetic earthquake scenario. As mentioned earlier, NAFZ generates an earthquake with the recurrence interval of about 250 years beneath the Marmara Sea. Therefore, selecting 100 earthquake scenarios would cover a time period of 100x250 years=25,000 years which is considered as an adequate catalog duration in this study. However, because of having time dependent...
Earthquake magnitude is one of the parameters randomly selected by the MC technique. Based on a characteristic earthquake model, individual faults tend to rupture entire fault when a large earthquake occurred. This model assumes that characteristic earthquake releases all of the seismic energy during the fault rupture and the magnitude of the earthquake depends on the dimension of fault (Abrahamson and Bommer, 2005).

As mentioned previously, only the PIF is considered as earthquake source with approximately 34 km in length and 14 km in width (Ozer Sozdinler et al., 2019; Karabulut et al., 2002). This fault zone is assumed that it has potential to generate a characteristic earthquake and rupture the entire fault. According to Wells and Coppersmith (1994) scaling relation between fault area and magnitude (Eq. 1), this fault can generate a characteristic earthquake with the magnitude varying between $M_w = 6.5 - 7.1$

$$M_w = a + b \times \log (L \times W)$$  

(1)

In this equation, $a$ and $b$ are coefficient, which are 4.33 and 0.09 respectively, $L$ is fault length and $W$ is the fault width. Displacement on the fault surface calculations are done, for each randomly selected magnitude, using the formulation of Aki (1966),

$$D = \frac{M_w}{\mu A} = \frac{10^{(M_w+6.07)/1.5}}{\mu A}$$  

(2)

where $D$ is displacement on the fault surface, $M_w$ is moment magnitude, $\mu$ is the shear modulus ($\mu=30$ GPa), and $A$ is the fault area.

Seismogenic thickness and the location of the earthquake is another important parameter required for earthquake and tsunami source. At first, the PIF zone is accepted as fully characteristic and an earthquake should rupture the entire fault area. Therefore, it is assumed that if the rupture starts at the center of the fault and continues in both directions, the fault will rupture entirely. For this reason, the locations of the earthquakes are accepted as the midpoint of PIF zone for each earthquake scenario (Ozer Sozdinler et al., 2019).

For the seismogenic thickness, the seismic activity of the northern segment of NAFZ starts at the depth of 5 km (Karabulut et al., 2003). The bottom of the seismogenic thickness can be determined based on the after-shock activity of the 17 August 1999 Izmit Earthquake. The earthquakes on the northern scarp of the Çınarcık basin are observed between the depths of 5 and 14 km. The mechanism of events between the depth of 5 and 10 km shows the behavior of normal faulting. On the other hand, strike-slip mechanism dominates the depths below 10 km to 14 km. As a result, seismic activity can be observed between the depths of 5-14 km and fault plane solutions show normal and strike-slip mechanisms in this area (Karabulut et al., 2002). Therefore, depth of events vary between 5 to 14 km in MC simulations. In time-independent earthquake occurrence models, probability of an event occurrence follows a Poisson distribution in a given certain period of time. Therefore, the result of this model does not vary in time. However, probability of an earthquake occurrence is based on the time that has passed since the occurrence of last event and it follows a Brownian passage time (BPT), log-normal or another probability distribution (Matthews et al., 2002; Ellsworth et al., 1999; Davis et al., 1989; Rikitake 1974). In this model, in addition to the recurrence
In this equation, $C_{long}$ can be obtained using the formulation of Kanamori (2004) and the moment rate of the fault ($\mu$) and the long recurrence interval of earthquakes ($R_s$) was taken as 0.5 in this study (Parsons, 2004). The mean probability of an event occurrence increases with the elapsed time. This parameter, which is known as the parameter defining how much an expected characteristic earthquake occurs much an expected characteristic earthquake occurs, is moment magnitude ($M_w$), long-term slip rate in mm/yr and A is the fault area.

Calculation of probability in multi – segment ruptures and more complicated models includes Gutenberg Richter magnitude – frequency relationship (Gutenberg and Richter, 1944). The application of time – dependent models based on characteristic earthquake model, which assumes all large events occurring along a particular fault segment would have similar magnitudes, rupture area and average displacements (Schwartz and Coppersmith, 1984). Therefore, this model is suitable for calculating the probability of occurrence of an earthquake on a single fault.

It should be noted that, in this study, PIF is considered as the only source for the earthquake and tsunami. Time dependent probabilistic model is followed for the probability calculations; because, this probabilistic model allows to consider only one fault instead of using multi – segment rupture scenarios through characteristic earthquake model.

In the time-dependent approach, Brownian passage time (BPT) probability model is used to obtain the recurrence time probability of the earthquake in the fault segment. This model does not show significant difference with the log – normal distribution except for consideration of very long elapsed times from the last characteristic event (Petersen et al., 2007). A characteristic event occur when the load-state process reaches to the failure threshold, an earthquake releases all energy loaded on the fault and then starts the new failure cycle. The time interval between consecutive earthquakes shows a Brownian passage time distribution and that can be useful to forecast long term seismic events by generating a time – dependent model (Matthews et al., 2002). The Working Group on California Earthquake Probabilities (1999) and the Earthquake Research Committee (2001) have already implemented this time – dependent approach to the San Francisco Bay and Japan, respectively, for the prediction of long-term events (Petersen et al., 2007). This model depends on the time period passed since the last characteristic event and recurrence time of the earthquake. The probability density function for BPT model (Matthews et al., 2002) is given by,

$$f(t; T_r, \alpha) = \left(2\pi\alpha^2 t^3\right)^{1/2} \exp\left(-\frac{(t-T_r)^2}{2\alpha^2 t^3}\right)$$

(3)

where $t$ is the elapsed time from the last characteristic event and $\alpha$ is the aperiodicity (also known as the coefficient of variation). Aperiodicity defines the regularity of the expected characteristic earthquakes on the fault and varies between the 0.3 and 0.7. This parameter, which is known as the parameter defining how much an expected characteristic earthquake occurs regularly or irregularly on any fault segment (Murru et al., 2016), was taken as 0.5 in this study (Parsons, 2004). The mean recurrence interval of earthquakes ($T_r$) can be defined as the ratio between the mean moment of repeating earthquakes (seismic moment) and the long-term moment accumulation rate on the fault (moment rate) (Ren and Zhang, 2013). Seismic moment can be obtained using the formulation of Kanamori (2004) and the moment rate of the fault is calculated from fault area and long-term slip rate of the fault (WGCEP 2003).

$$T_r = \frac{M_0}{\mu V A} = \frac{10^{(M_w+6.07)/1.5}}{\mu V A}$$

(4)

In this equation, $M_w$ is moment magnitude, $\mu$ is the shear modulus, $V$ is long-term slip rate in mm/yr and A is the fault area.
The moment magnitude value in Eq. (4) was selected randomly using Monte Carlo simulations. Thus, seismic moment \( M_w \) and the mean recurrence time \( T_r \) were calculated for each earthquake scenario. Long term slip rate is also selected as 17 mm/yr for this equation (Ergintav et al., 2014).

Probability of the earthquake occurrence on the fault is calculated based on the probability density function approach. The probability of occurrence of an event in the next \( \Delta T \) years, given that it has not occurred in the last \( t \) years is given by (Erđik et al., 2004),

\[
P(t, \Delta T) = \frac{\int_{t}^{t+\Delta T} f(t) \, dt}{\int_{0}^{\infty} f(t) \, dt}
\]

In this case, probability of a characteristic earthquake was calculated using \( \Delta T \) as 50 and 100 years.

### 3 Tsunami Numerical Modelling

Tsunami simulations are performed for each earthquake in synthetic catalogue using tsunami numerical model NAMI DANCE (NAMI DANCE, 2011). The code is the user-friendly version of TUNAMI-N2 (Imamura et al., 2001) developed in C++ language, which computes all fundamental parameters of tsunami motion in shallow water and in the inundation zone. It uses explicit numerical solution of shallow water wave equations with finite-difference technique and allows for better understanding of the effect of the tsunami waves (Shuto et al., 1990; Imamura, 1989). NAMI DANCE can solve both Linear and Nonlinear Shallow Water Equations with selected coordinate system (Cartesian or spherical) and calculates the tsunami motion. Linear Shallow Water (LSW) equations are preferable in deep water because of reasonable computer time and memory and calculates the results in acceptable error limit (Insel, 2009). NAMI DANCE is validated and verified using NOAA standards and criteria for tsunami currents and inundation (Synolakis et al., 2007; Synolakis et al., 2008). The numerical solutions of NAMI DANCE are also tested, validated and verified against analytical solutions, laboratory measurements and field observations (NTHMP, 2015; Lynett et al., 2017; Velioglu, 2009).

NAMI DANCE calculates tsunami generation using Okada (1985) equations. In this study, water surface distribution of tsunami source (initial wave amplitude) are calculated with this method for 100 earthquakes of the synthetic earthquake catalogue prepared by Monte Carlo simulations. As an example, Figure 5 shows the initial water surface calculated due to one of 100 tsunami sources generated by MC simulations (Fig 5).

Before starting tsunami simulations, the necessary inputs should be prepared precisely in order to obtain reliable results. Bathymetry - topography data is one of the most important input in NAMI DANCE that significantly effects the reliability of results especially in shallow water zone due to the nature of NSW Equations. NAMI DANCE can make nested analyses under the condition that grid size of study domains have a certain 1:3 ratio between each other. Therefore, we generated four nested domains having the coarsest grid size as 81 m and the finest grid size as 3 m with 1:3 ratio in GIS environment. Bathymetric data for the biggest domain is the combination of 30 arc second resolution General Bathymetric Chart of the Oceans (GEBCO) and data produced by navigational charts in shallow zones. Topographic data, on the other hand, contains the high resolution, which is obtained from the Department of Housing and Urban Development of Istanbul Metropolitan Municipality, Digital
Elevation Model (DEM) and vector data with resolution 5m and 1m, respectively. The bathymetry-topography data in the smaller domains is the downscaled version of the 81m grid sized bathymetry-topography data, however high resolution digitized coastline, and sea and land structures are also included to the data to generate 3m grid sized smallest domain (Fig 4).

Synthetic gauge point file is another required input of the NAMI DANCE. In addition to the calculation of principal tsunami hydrodynamic parameters, program can also calculate the change of water level, current velocity and flow depth over time in every gauge point. Therefore, various gauge points are selected along the coast of nested domains, near shore and offshore and close to some critical structures on land.

During the inundation of tsunami waves, current velocity is an important tsunami parameter in land and sea, especially in ports and bays. Strong current velocities may cause dragging offshore or landing of sea vessels inland. This parameter as well as tsunami wave amplitude, inundation depth and Froude number can be calculated by NAMI DANCE. However, in this study, the results are represented based on only the probability of exceedance of threshold values for water surface elevation and inundation depth.

NAMI DANCE can make nested analyses under the condition that grid size of study domains have a certain 1:3 ratio between each other. Therefore, we generated four nested domains having the coarsest grid size as 81 m and the finest grid size as 3 m with 1:3 ratio in GIS environment. Coarser data includes multi-beam bathymetric measurements and 900m grid sized GEBCO data in the sea and 30m grid sized ASTER data on land. Coastline, and sea and land structures are also digitized in GIS environment and included in 3m grid sized high resolution bathymetry-topography data in the smallest domain (Fig 4).

Figure 4: Nested domains for tsunami numerical modelling. Red rectangles show the limits of these domains. Grid size of these domains have a certain 1:3 ratio between each other (created using ArcMap Version 10.5).
4 Results and Discussion

In this study, tsunami hydrodynamic parameters are calculated in both coarsest domain (whole Marmara Sea) and finest domain (Tuzla region). The main parameters focused in this study are the tsunami wave heights and inundation depths and the results are shown in the terms of probability of exceedance of threshold wave height and inundation depth values within the next 50 and 100 years. The situation for the next 500 years is not considered because the return period of the fault rupture is about 250 years, which means this fault generates at least one earthquake within the next 500 years. In other words, probability of exceedance for the next 500 years will be about 99%.

We present the results of the PTHA for Tuzla test site in terms of three different visualization categories for the next 50 and 100 years. First, distribution of probability of occurrence of the tsunami hydrodynamic parameters, which are minimum and maximum water surface elevation and inundation depth, are shown. Second, tsunami inundation maps that show probability of exceedance of 0.3 m inundation depth for different time periods are generated for Tuzla region in order to observe flooded areas and their probabilities clearly. And finally, the probability map of exceedance of 0.3 m wave heights at synthetic gauge points are represented as bar charts.

4.1 Probability of Exceedance for Entire Synthetic Earthquake Catalogue

The graphics are generated to demonstrate the probabilities of occurrences corresponding to the minimum and maximum water surface elevations and inundation depth calculated from tsunami sources of each earthquake in synthetic earthquake catalogue. It should be noted that in case of having same magnitude of earthquakes in two different earthquake scenarios of the catalogue,
the probability of occurrences of these scenarios would be the same. However, since they would have different focal depths, the tsunami initial wave height calculated by Okada (1985) will be different, which results in the calculation of different hydrodynamic parameters. As a result, the graphs show different maximum water surface elevations having the same probability of occurrences.

In Figure 6, graphics of probabilities of occurrences according to maximum and minimum water surface elevation (maximum water withdraw) and inundation depth for next 50 years are represented, respectively. According to these graphs, tsunami wave heights up to 1 m and withdrawal of the waves around 1 m have approximately 65\% ± 15 probability of occurrence. Tuzla region includes various shipyards, ports and other important facilities. Therefore, probability of the withdrawal of the water is as important as maximum water surface elevation. 1 m height of wave withdrawal may cause the ships to be stranded at the ports and results in extreme financial losses as observed in the 20\textsuperscript{th} July 2017 Bodrum-Kos earthquake and tsunami (Yalciner et al., 2017). The probability for having 1 m inundation depth, on the other hand, can be predicted as about 60\% ± 10. Residual probability with respect to the fitted curve for each data point is demonstrated right after the percentage of probability with ± sign.
Figure 6: Probabilities of Exceedance Corresponding to Maximum Water Surface Elevation, Minimum Water Surface Elevation and Inundation Depth for the next 50 years. Black dots represent the probability of exceedance of tsunami hydrodynamic parameter for each event in the catalog. Blue line is the best fit curve to the data and dashed blue line is the 95% confidence boundary of the fitted curve. Residual of the fit is represented for each probability curve.

The situation for next 100-years (Fig 7) obviously shows that probability of occurrences would increase with time. The probability of exceedance of 1 m water surface elevation and 1 m wave withdrawal reaches up to 85% ±10. Probability of exceedance of inundation depth also changes significantly. The probability of exceedance of 1 m inundation depth is found around 80% ±10.
Considering the results of the whole simulation, the worst case earthquake scenario generated tsunami waves with maximum water surface elevation equal to 1.8 m, minimum water surface elevation (maximum withdraw) equal to -2.1 m and inundation depth equal to 1.6 m. The probability of occurrence of this event is 35% for next 50 years and 60% for next 100 years.

4.2 Probabilistic Tsunami Inundation Maps for Tuzla Test Site

Inundation maps of Tuzla domain are also prepared for the next 50 and 100-years in GIS environment. Even if inundation depth is in the order of few centimeters, it can lead to dragging of people in coastal regions due to the high current velocities of the waves (Jonkman and Penning-Rowsell, 2008). Therefore, these inundation maps have a great significance to understand the flooded areas in study domain and the amount of water penetrated inland.

Generation of inundation maps are based on the probability of exceedance of 0.3 m inundation depth. There are several studies in literature proving both experimentally and numerically that tsunami waves with the order of 0.3 m height have a potential to collapse a human body (Jonkman and Penning-Rowsell, 2008; Takagi et al., 2016). For this reason, only the earthquake scenarios that generated inundation depths larger than or equal to 0.3 m threshold value are considered.

- Inundation depth files, which is one of the outputs of the NAMI DANCE, are used for the calculation.
- The inundation depth values at each grid node are replaced with the probability of occurrence of the respective earthquake scenario. We repeated this procedure for all earthquake scenarios, which has inundation depths larger than or equal to 0.3 m threshold.

The mean (average) probability of occurrence is calculated at each grid node. Thus, the spatial distribution of probability of exceedance of 0.3 m inundation depth in inundation zone is obtained for a specific time interval (Fig 8).

Figure 8 shows the inundation maps of Tuzla shipyard for the next 50 and 100-years. Most of the area in Tuzla shipyard region have probability of exceedance between 10% and 20% for both of the next 50 and 100 years. However, some places in the northern and southern part of the area and inside the bay show larger than 75% probability of inundation within the next 100 years. Maximum inundation distance is observed as around 60 m in the test site.
Figure 8: Probabilistic Tsunami Inundation Maps for Tuzla Study Domain representing the Probability of Exceedance of 0.3 m Inundation Depth within the Next 50 and 100 Years. Change of colors from green to red represents the increasing probability of exceedance (created using ArcMap Version 10.5).

In Figure 8, probabilistic inundation maps of one of the most important facilities in the study region are represented for the next 50 and 100 years. The area has high potential to be exposed to tsunami waves with probability larger than 50% for the next 50 years. In 100 years, this probability increases and varies between 75% and 90%. No significant inundation zone is observed along the coast of the seawall and the peninsula. This may be due to the high ground elevation of these zones. Tsunami waves are inundated up to 45 m inside the small bay. This inundation distance could cause severe damage to shipyard and other constructions if corresponding current velocities are also significant.
Figure 9: Probabilistic Tsunami Inundation Maps of Northern Part of Tuzla Study Domain representing the Probability of Exceedance of 0.3 m Inundation Depth for the Next 50 and 100 Years. Change of colors from green to red represents the increasing probability of exceedance (created using ArcMap Version 10.5).

In the next figure (10), the southern part of the Tuzla shipyard is seen according to probabilities of inundation for the next 50 and 100 years. Very limited area in the coastal zone is inundated with the probability between 30% and 50% within the next 50 years. The probability reduces up to 10% at some inner locations from the coastline. For 100-year recurrence time, the situation is almost the same. Only minor parts of the region at the south approaches up to 75% - 90% probability of exceedance of 0.3 m inundation depth threshold. The maximum inundation distance is calculated about 60 m. The inundated region does not include any important facility or structure and the effect of the tsunami will be minimal. The inundation distance decreases to 10 m at the other parts of the region.
Figure 10: Probabilistic Tsunami Inundation Maps for the Southern Part of Tuzla Study Domain representing the Probability of Exceedance of 0.3 m Inundation Depth for the Next 50 and 100 Years. Change of colors from green to red represents the increasing probability of exceedance (created using ArcMap Version 10.5).

The region indicated in Fig 11 is located inside the bay and includes a large part of the shipyard area. This area includes lots of large and small piers and ship construction facilities. The situation is more or less the same with the previous region (Fig 10). Probability of having larger than 0.3 m inundation depth changes between 30% and 50% within the next 50 years, while only a few places show 75% - 90% probability for the next 100 years along the coast. Moreover, maximum inundation distance is calculated as 25 m for this zone. Even if the probability of inundation is low, these zones should be taken into consideration before constructing a new structure.
Figure 1 shows Probabilistic Tsunami Inundation Maps of Shipyard Area in Tuzla Study Domain representing the Probability of Exceedance of 0.3 m Inundation Depth for the Next 50 and 100 Years. Change of colors from green to red represents the increasing probability of exceedance (created using ArcMap Version 10.5).

4.3 Synthetic Gauges

Finally, the probability of exceedance of 0.3 m wave heights at synthetic gauge points are presented by bar charts to consider the near shore effect of tsunami waves along the western coast of Istanbul. Because of the closeness to the fault zone, the southeast coasts of the city are under the threat of the significant tsunami damage. Similar with the method applied during the preparation of probabilistic inundation maps, the earthquake scenarios with wave heights at synthetic gauge points larger than or equal to 0.3 m are selected and replaced with the probability of each scenario according to wave heights and after that the average probabilities at each synthetic gauge point are obtained accordingly.

Figure 1 demonstrates the probability of exceedance of 0.3m wave height at synthetic gauge points, which are about 350 m distant to each other, along the western coast of the Istanbul within the next 50 and 100 years. The probability is increasing while color scale chances from green to purple. According to this figure, minimum probability of exceedance is shown as 75% at some points. Except for a few of 228 synthetic gauge points, all points have larger than 90% probability of exceedance of
0.3 m wave height within the next 50-years time scale.
This condition is very serious since there are so many residential areas and important spots such as ports and recreational facilities in this region. The minimum probability of occurrence, which can generate tsunami waves with at least 0.3 m wave heights, reaches up to 90% for the next 100-year time period. However, 95% probability of exceedance of 0.3 m wave height dominates the region for this time scale.
Figure 1: Probability of Exceedance of 0.3 m Tsunami Wave Height within the next 50 and 100 years at Synthetic Gauge Points (yellow rectangles show the Tuzla study domain, change of colors from purple to green on the bars represents the decreasing probability of exceedance (created using ArcMap Version 10.5).

4.4 Uncertainties

PTHA studies include some uncertainties because of the nature of rare occurrence of large events. Quantification of these uncertainties generally includes mixture of empirical analyses and subjective judgment.

Uncertainties of PTHA can be divided into two as aleatory and epistemic variability. Aleatoric uncertainty is the natural randomness of the physical process. Including more data in the analyses does not contribute to reduce the aleatoric uncertainty. However, knowledge about the modelling process may decrease this unpredictability. The occurrence time of the earthquake is one of the most fundamental aleatory variables in PTHA. This parameter is generally assumed a time-independent variable. However, in this study we used time-dependent probability model which reduces the uncertainty on this parameter. Mechanism of the source is considered as another aleatory variable for PTHA studies. The great number of the earthquakes all round the world occur at well-defined plate boundaries. However, some unidentified low active intraplate faults exist, which are recently contained in PTHA studies (Selva et al., 2016). Moreover, the fault volume, which is used in scaling relations to calculate the
source magnitude, is another aleatory term. Although homogenous slip distribution is a common implementation in PTHA, slip distribution of large events do not show homogenous behavior. Therefore, definition of asperities on the fault is another aleatory variable which should be considered. Tsunami numerical modelling, itself, is also another aleatory variable since, they do not show correlation with real observations, which are more variable than earthquake scenarios incorporated in PTHA (Grezio et al., 2017). The aleatory variable affects the results because it is incorporated directly into the hazard calculations (Abrahamson and Bommer, 2005).

Epistemic uncertainty, on the other hand, consists of the lack of knowledge of the physical process and data. Segmentation of fault system is one of the epistemic variables since, it is not certain where the rupture will be generated, and which segments will be triggered. In addition, there are many different scaling relations, which cause another epistemic uncertainty, between the fault area and magnitude. It is also important for tsunami generation whether the fault rupture reaches to the surface or not. Thus, updip and downdip limits of the fault rupture can be considered as another epistemic variable (Grezio et al., 2017).

Accurate probability distributions of input cannot be known. For example, assuming that probability of occurrence of an event follows Poisson distribution. However, return periods of events do not simply fit to this distribution (Gonzalez et al., 2013). Unlike aleatory one, epistemic uncertainty can be decreased when more information is available (Godinho, 2007). Different techniques, such as logic tree, Bayesian method etc., have been developed to reduce these uncertainties.

In this study, probabilistic model is established based on the characteristic fault model of PIF, which is a segment of NAF one of the best studied fault zones in the world. It is also assumed that the entire fault area is ruptured, reached to the surface and generated a homogenous slip for each event. The maximum magnitude range of the fault is calculated with Wells and Coppersmith (1994) scaling relation. All these assumptions naturally include uncertainties which are naturally reflected to this PTHA study. Besides, MC simulation itself also includes uncertainty as being performed hundred times to create synthetic earthquake scenarios. The effect of uncertainty in aperiodicity parameter is also existing and can be reduced by including different parameters to MC simulation. Therefore, the tsunami hydrodynamic parameters associated with the probability of occurrence of the corresponding scenario preserve the same uncertainty.

5 Conclusion

In this study, time-dependent PTHA is performed in Tuzla region, Istanbul for the purpose of understanding the probability of having tsunami inundation after the PIF rupture. The study combines tsunami numerical modelling with probabilistic approach, which is modified by probabilistic seismic hazard analysis. Probability calculations have been done based on the time-dependent BPT model, which depends on the time period passed since the last characteristic event and the recurrence time of earthquake. After that, synthetic earthquake catalogue is generated using MC simulation technique and tsunami numerical modelling was performed depending on this earthquake catalogue using NAMI DANCE code in GPU environment.

Results of this PTHA study was presented in three different ways for the next 50 and 100 years. The first one was the graphs showing the change of probability with the maximum and minimum water surface elevation and inundation depth for different time intervals. Secondly, the probabilistic tsunami inundation maps are generated for Tuzla region. Finally, the probability maps of exceedance of 0.3 m wave heights at synthetic gauge points are represented with bar charts.
The main results of this study can be summarized as follows:

- According to the distribution of probability with respect to tsunami hydrodynamic parameters, the probability of exceedance of 1 m maximum positive and negative water surface elevation is 65% within next 50 years. The probability for 1 m inundation depth is 60%.

- Considering probabilities for next 100 years, 85% probability of exceedance of 1 m was calculated. For 1 m inundation depth, probability of exceedance is obtained about 80%.

- As a result of the whole simulations, 1.8 m, -2.1 m and 1.6 m were calculated for maximum and minimum water surface elevation and inundation depth, respectively with the probability of 35% for the next 50 years, 60% for next 100 years.

- Inundation maps, indicate that inundation of tsunami waves that are equal to or larger than 0.3 m have probability mostly higher than 10% and 20% for the next 50 years and 100 years, respectively. The probability of occurrence of 0.3 m inundation depth was calculated as maximum 75% for the next 100 years. Maximum inundation distance is calculated as 60 m and observed in the southern part of the finest 3m grid-sized study area.

- Probabilistic results for the exceedance of 0.3 m wave height at synthetic gauge points demonstrate that only few of them have a probability between 75% - 85%, however several points have more than 90% probability for the next 50 years. Probability of exceedance increases by more than 95% for the next 100 years.

The tsunami impact of the PIF rupture along the Tuzla coast is very important as proposed with the results of this study. However, as further steps of this study, PTHA can be done for the other critical test sites along the Marmara Sea that are close to the PIF segment. Besides, it is also advantageous to consider the other fault segments, having their various rupture combinations and complex rupture probabilities in Marmara Sea as further studies. Previously in the framework of the MARSite project, tsunami arrival times and maximum wave amplitudes are calculated along the coast of the Marmara Sea using different earthquake scenarios and a tsunami scenario database was obtained in deterministic approach (Ozer Sozdinler et al., 2019). Results of this study show that, arrival time of tsunami waves is very short in Marmara Sea for most of the scenarios which complicates the tsunami early warning operations and evacuation actions. However, due to the short arrival times of first tsunami waves along Marmara coast, the tsunami inundation scenario databases would be of great importance in such conditions. It would be the best option for the decision makers and civil protection authorities to have the inundation maps prepared also in probabilistic approach in order to realize the possibility of exceedance of selected threshold inundation depth for certain critical coastal locations.

This study shows a methodology for PTHA with time – dependent probabilistic model using only one fault (PIF) as earthquake and tsunami source. Furthermore, this study can be developed including some connected faults to the PIF in both time – dependent and time - independent probability calculations and Brownian passage time (BPT) probability can be combined with static Coulomb stress changes on the faults. Brownian passage time (BPT) model can also be improved by including different aperiodicity parameters. The probability of occurrence of earthquakes is the main focus of this study to perform tsunami hazard analyses. However, submarine landslides are other critical important sources for tsunami generation in
Marmara Sea. Probabilities of sliding areas and the sliding volumes can be considered in the analyses. Submarine landslide generated tsunamis can be coupled with the earthquake triggered tsunamis in order to obtain integrated PTHA in the Marmara Sea.

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