

Author's Response to the Reviewers

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Spatial Seismic Hazard Variation and Adaptive Sampling of Portfolio Location Uncertainty in Probabilistic Seismic Risk Analysis

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Response to Referee Comment 1

Original Comment: https://editor.copernicus.org/index.php/nhess-2019-110-RC1.pdf?_mdl=msover_md&_jrl=7&_lcm=oc108lcm109w&_acm=get_comm_file&_ms=75583&c=169504&salt=2105809317943394038

Thank you for your helpful review. Please find our answers to each of your comments below:

>> *"This is a quite interesting paper dealing with the Spatial Seismic Hazard Variation and Adaptive Sampling of Portfolio Location Uncertainty in Probabilistic Seismic Risk Analysis. The paper is original, well-written and organized."*

Thank you.

>> *"p. 6 Hazard Model There is need to provide more details on the seismogenic sources introduced in the model."*

We understand that the description of the hazard model was too brief, even though it is not the main topic of our manuscript. In the now updated manuscript, we have therefore improved and extended the corresponding Section 3.1 ("Hazard Model"). We have provided information on the results of the original USGS hazard model, and have described the differences to the original USGS model in more detail. For instance, we have added paragraphs on the modeling of the subduction zone geometry and events on the subduction zone as well as on the ground motion model logic tree. Furthermore, we now show and discuss a hazard map produced using our model.

>> *"p. 6 Write "United States Geological Survey" instead of "United States Geological Service"."*

We corrected the text to "United States Geological Survey".

>> *"p. 6. "Site conditions are based on topographic slope (Wald and Allen, 2007)". But site conditions are also dependent on soil conditions. How do you consider this?"*

We acknowledge that the initial description of our site conditions (or soil classes) was too brief. While they are based on the approach proposed by Wald and Allen (2007), they have also been refined locally to consider areas of soft soil such as river beds. In the updated manuscript, we now describe this.

>> “p. 6. “The CV is the lowest in Kalimantan (< 0.1) due to the absence of any known or modeled crustal faults”. It is hard to follow this statement. Therefore, once more there is need to provide more details on the seismogenic sources introduced in the model.”

We see that it was hard to follow the statement about Kalimantan and have therefore – in addition to elaborating more on the hazard model – extended the corresponding paragraph in Section 3.1. We now explain that only homogenous gridded seismicity is used in this area, and also explain why this is the case.

Response to Referee Comment 2

Original Comment: https://editor.copernicus.org/index.php/nhess-2019-110-RC2.pdf? mdl=msover_md& jrl=7& lcm=oc108lcm109w& acm=get_comm_file& ms=75583&c=169695&salt=15129839991364182583

Thank you for your review and positive feedback.

Response to Referee Comment 3

Original Comment: https://editor.copernicus.org/index.php/nhess-2019-110-RC3.pdf? mdl=msover_md& jrl=7& lcm=oc108lcm109w& acm=get_comm_file& ms=75583&c=170849&salt=5284276181243996975

Thank you for this review and for sharing your view of PSHA. Please find our answer to each of your comments below.

>> [...] I therefore recommend that all such mss, including the present ms by Scheingraber and Käser, should be rejected, unless and until they can refute the criticisms of Mulargia et al (2017). The above recommendation may seem harsh to these authors, as innumerable papers on PSHA or based on PSHA continue to be routinely published. But unless at some point papers on PSHA start to be rejected, they will go on being published forever.

This comment does not refer to the actual content of our paper, but to the method of PSHA in general. The referenced critique is concerned about the theoretical or physical “validity of PSHA”, but we are more interested in the practical benefits the method provides to society.

PSHA – since its first publication by Cornell in 1968 – has been improved in many aspects, especially with regard to its inherent uncertainties. Its benefits are broadly recognized by scientists and practitioners working in PSHA and related fields such as seismic risk analysis and seismic engineering. No better approach has been proposed, which is probably why PSHA continues to be used. To quote the famous statistician George Box: “All models are wrong, but some are useful”.

Having co-authored all of the cited papers, the reviewer Robert Geller is a vehement critic of PSHA. The paper co-authored with Kagan and Jackson from 2012 – and cited to support this critique of PSHA – does in fact not even mention PSHA. It criticizes theories in seismology like “earthquake cycle”, “seismic gap”, and “characteristic earthquake”. We agree on most statements of this opinion paper, but do not see any direct or tangible criticism of the general framework of modern event-based PSHA.

Concerning the two other cited papers (from 2012 and 2017, also co-authored by this reviewer), we again agree with their main points that PSHA cannot provide an accurate measure of hazard, and that it must not be used with blind trust (Quote: “Geoscience consultants feed information into the PSHA machine, the crank is turned, and a seemingly objective number pops out.”). Since we developed our “PSHA machine” ourselves, we are well aware of its weaknesses and dependence on assumptions that sometimes are barely supported by reliable data collected over time scales long enough for certain seismological needs.

One should keep in mind PSHA has its justification exactly in that it can be used to analyze the influence of purely constraint assumptions and quantify the ranges of possible hazard results. The output of PSHA is inherently based on probabilities and therefore it is always possible to find individual examples – as in the suggested papers – that do not nicely fit the model. In any case, abandoning the method entirely and relying only on qualitative judgement does not seem to be a wise recommendation; it is neither practical nor legally viable, because e.g. engineering and financial decisions and regulations require quantitative input.

However, we agree to the argument that the flaws and limits of PSHA and the uncertainties of its results have to be communicated effectively in order to provide a holistic view of risk and avoid “blind trust” in PSHA outputs.

This is precisely why our work is concerned with the computationally efficient treatment of uncertainties in PSHA and PSRA, allowing to analyze the impact of poorly constraint or unknown parameters on risk assessment and to come to an informed decision.

In this paper in particular, we analyze one of these aspects of uncertainty related to seismic risk assessment: insured portfolios often have poor geospatial data quality. We show how the huge uncertainty space can be investigated efficiently by using variance reduction methods, i.e. adaptive sampling strategies instead of simple Monte Carlo simulation. PSHA is just used to get an input parameter for the sampling method we propose for purposes seismic risk analysis, and our method can help to validate PSHA and PSRA more effectively.

We are therefore a bit surprised that Robert Geller did not recognize that our work is actually in line with most of his argument. We assume that our holistic view of PSHA and PSRA was not made clear enough in the abstract and early sections of our original manuscript. To improve this, in our updated manuscript we have added some clear statements about the weaknesses and limits of PSHA and PSRA:

- Page 1, Abstract, Lines 2-4: “The available seismological data is often limited, resulting in many uncertainties and assumptions. The situation is further aggravated by the sometimes poor data quality with regard to insured portfolios.”

- Page 1, Abstract, Lines 16-17: “The results show that the scheme can improve the efficiency of the estimation of loss frequency curves, and may thereby help to spread the treatment and communication of uncertainty in Probabilistic Seismic Risk Analysis.”
- Page 1, Section 1 Introduction, Lines 19-20: “Seismic risk analysis is widely used in academia and industry to model the possible consequences of future earthquake events, but is often associated with poor data quality, resulting in the necessity for many assumptions and a wide range of deep uncertainties (Goda and Ren, 2010). The treatment and communication of uncertainties is highly important for informed decision making and a holistic view of risk (Tesfamariam et al., 2010; Cox, 2012; Bier and Lin, 2013).”
- Page 2, Section 2.1 Probabilistic Seismic Hazard and Risk Analysis, Lines 27-28: “PSRA is based on Probabilistic Seismic Hazard Analysis (PSHA; Cornell, 1968; Senior Seismic Hazard Committee, 1997), which relies on a number of assumptions outlined in the following.”
- Page 23, Section 6 Conclusions, Lines 2-4: “Seismic risk assessment is associated with a large range of deep uncertainties. For example, the exact location of risks is often unknown due to geocoding issues of address information. In order to provide a holistic view of risk and to be able to communicate the effect of uncertainty effectively to decision makers, all model uncertainties need to be treated. Therefore, in this paper we propose [...]”
- Page 25, Section 6 Conclusions, Lines 14-15: “The effect of modeling assumptions and the often poor data quality needs to be investigated further.”

>> 1) This referee’s impression is that PSHA gives ever more unreliable results as the grid is made finer and finer. Notwithstanding the inherent flaws in PSHA, if the regions were made larger and larger the central limit theorem would probably mean the results were more safely usable. Maybe this is like the tradeoff between stability and resolution in inverse theory.

Unfortunately, it is unclear to us to which “grid” this comment refers to. In our paper we are mainly referring to “grid” in the sense of a weighted irregular grid that represents potential locations of insured assets. This concept is explained in our paper and is necessary to spatially distribute insured values given only on administrative geographical zones. This grid is not related to the spatial accuracy of analyzing the seismic ground motion or seismic hazard output. It is also not related to another grid which is typically used to model potential earthquake epicenters within an area source using the method of gridded seismicity. Therefore, we believe this comment comes from a misunderstanding of the term “grid” as it is used in the context of this paper.

>> 2) The quality of the writing is generally good, but there is one typo on page 25. The family name of the first author is “Petersen” not “Mark Petersen.” Ditto for the other coauthors. And in the body of the text this paper needs to be called out as “Petersen et al.,” not “Mark Petersen et al.”

Thanks for pointing this out, we have corrected the typo in the citation of Petersen et al. (2007).

>> Both authors list “Munich Re” as an affiliation on the title page, and the acknowledgements list “Munich Re” as a sponsor. Thus (see line 20 on page 22) the declaration of “no competing interests” is incorrect and must be rewritten. Munich Re sells consulting services and insurance products based on PSRA, and this fact must be appropriately stated in the “competing interests” declaration. [...]

We think that this comment is misleading, as one might conclude that Munich Re potentially profits in any material sense from having provided financial support for this academic research. There was no business-related influence on this paper and there is no financial interest of Munich Re in publishing scientific papers. In fact, Munich Re is highly interested in making academia aware of some of the crucial problems arising in Probabilistic Seismic Risk Assessment (PSRA), as well as in trying to solve them in a way of best scientific practice.

While working on this project, the first author has not been affiliated with Munich Re, but has been a PhD student at Ludwig Maximilian University of Munich and funded by Munich Re. It is the right and duty of a PhD-student to publish scientific results and discuss the applied approaches and findings with the scientific community. Since the first author has not been affiliated with Munich Re while working on this project, we have removed this affiliation and apologize for the confusion this might have caused.

To clarify this and the role of Munich Re in this research, we adjusted the “competing interests” declaration accordingly.

Response to Short Comment 1

Original Comment: https://editor.copernicus.org/index.php/nhess-2019-110-SC1.pdf?_mdl=msover_md&_jrl=7&_lcm=oc108lcm109w&_acm=get_comm_file&_ms=75583&c=169770&salt=6072584531330510715

Thank you for this comment.

We understand that it can be hard to follow the technical details of a highly specialized paper such as this one, in which due to the format we can only provide a concise description of the general methodology of seismic hazard and risk assessment. While we believe that it would clearly be out of scope to explain all details of this scientific area, in our updated manuscript we provide some textbook suggestion for further study for the interested reader at the end of Section 2.1:

Page 3, Section 2.1 Probabilistic Seismic Hazard and Risk Analysis, Lines 18: “For more details on PSHA and PSRA, we refer to the comprehensive textbook of McGuire (2004).”

In addition, Section 3.1 has been almost entirely rewritten to elaborate more on the utilized hazard model.

Spatial Seismic Hazard Variation and Adaptive Sampling of Portfolio Location Uncertainty in Probabilistic Seismic Risk Analysis

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Abstract. Probabilistic Seismic Risk Analysis is widely used in the insurance industry to model the likelihood and severity of losses to insured portfolios by earthquake events. The available seismological data is often limited, resulting in many uncertainties and assumptions. The situation is further aggravated by the sometimes poor data quality with regard to insured portfolios. For example, due to geocoding issues of address information, risk items are often only known to be located within an administrative geographical zone, but precise coordinates remain unknown to the modeler.

In the first part of this paper, we analyze spatial seismic hazard and loss rate variation inside administrative geographical zones in western Indonesia. We find that the variation of hazard can vary strongly not only between different zones, but also between different return periods for a fixed zone. However, the spatial variation of loss rate displays a similar pattern as the variation of hazard, without depending on the return period.

We build upon these results in the second part of this paper. In a recent work, we introduced a framework for stochastic treatment of portfolio location uncertainty. This results in the necessity to simulate ground motion on a high number of sampled geographical coordinates, which typically dominates the computational effort in Probabilistic Seismic Risk Analysis. We therefore propose a novel sampling scheme to improve the efficiency of stochastic portfolio location uncertainty treatment. Depending on risk item properties and measures of spatial loss rate variation, the scheme dynamically adapts the location sample size individually for insured risk items. We analyze the convergence and variance reduction of the scheme empirically. The results show that the scheme can improve the efficiency of the estimation of loss frequency curves, and may thereby help to spread the treatment and communication of uncertainty in Probabilistic Seismic Risk Analysis.

1 Introduction

Seismic risk analysis is widely used in academia and industry to model the possible consequences of future earthquake events, but is often associated with poor data quality, resulting in the necessity for many assumptions and a wide range of deep uncertainties (Goda and Ren, 2010). The treatment and communication of uncertainties is highly important for informed decision making and a holistic view of risk (Tesfamariam et al., 2010; Cox, 2012; Bier and Lin, 2013). In the insurance industry, Probabilistic Seismic Risk Analysis (PSRA) is the means of choice to model the likelihood and severity of losses to

insured portfolios due to earthquake events. In this context precise exposure locations are often unknown, which can have a significant impact on scenario loss as well as on loss frequency curves (Bal et al., 2010; Scheingraber and Käser, 2019).

In PSRA, uncertainty is usually taken into account by means of Monte Carlo (MC) simulation (e.g. Pagani et al. 2014; Tyagunov et al. 2014; Foulser-Piggott et al. 2017). This is a computationally intensive process, because the error convergence of MC is relatively slow and a high-dimensional loss integral needs to be evaluated with a sufficient sample size. In PSRA, the hazard component typically dominates the overall model runtime. As a result, stochastic treatment of portfolio location uncertainty can be particularly challenging - ground motion needs to be simulated on a large number of sampled risk locations. On the other hand, a fast model runtime is a key requirement for underwriting purposes in the insurance industry. Methods or sampling schemes to improve the error convergence of MC simulation are known as variance reduction techniques. MC simulation is ubiquitous in many areas of science and engineering and a wide variety of sampling schemes exists. Some well-known ideas are common random numbers and control variates (Yang and Nelson, 1991), importance-, stratified- and hypercube sampling, Quasi Monte Carlo Simulation (QMC) using low-discrepancy sequences, as well as adaptive sampling. The error convergence of different sampling schemes has been investigated for many different types of integrals and application areas (Hess et al., 2006; dos Santos and Beck, 2015). Some work has already been performed on variance reduction for PSHA and PSRA in the form of importance sampling, e.g. preferentially sampling the tails of the magnitude and site ground motion probability distributions (Jayaram and Baker, 2010; Eads et al., 2013). However, to our knowledge so far no study has specifically investigated variance reduction for location uncertainty in PSRA in a modern risk assessment framework. Building on a framework proposed in a recent study, in the present paper we describe a novel variance reduction scheme specifically designed to increase the computational efficiency of stochastic treatment of portfolio location uncertainty in PSRA.

The remainder of this paper is structured as follows. We outline the most important theoretical background in Section 2. Using a seismic risk model of western Indonesia, in Section 3 we explore spatial hazard and loss rate variation inside administrative zones. Based on this, in Section 4 we propose an adaptive location uncertainty sampling scheme and investigate its performance using several test cases in Section 5. In Section 6, we give some recommendations on how to apply the results in practice and conclude with possible future improvements.

2 Background

2.1 Probabilistic Seismic Hazard and Risk Analysis

PSRA is based on Probabilistic Seismic Hazard Analysis (PSHA; Cornell, 1968; Senior Seismic Hazard Committee, 1997), which relies on a number of assumptions outlined in the following. In PSHA, the exceedance rate λ of ground motion level y_0 at a site \mathbf{r}_0 is expressed by the hazard integral

$$\lambda(y_0, \mathbf{r}_0)[y \geq y_0] = \int_V \int_{m_{\min}}^{m_{\max}} P[y \geq y_0 | m, \mathbf{r}, \mathbf{r}_0] \cdot \nu(m, \mathbf{r}) dm d\mathbf{r}, \quad (1)$$

with $\nu(m, \mathbf{r})dmd\mathbf{r}$ the seismic rate density which describes the spatio-temporal distribution of seismic activity, $P[y \geq y_0|m, \mathbf{r}, \mathbf{r}_0]$ the conditional probability of exceeding ground motion y_0 at site \mathbf{r}_0 given a rupture of magnitude m at source location \mathbf{r} , and V the spatial integration volume containing all sources which can cause relevant ground motion at \mathbf{r}_0 . Assuming that the occurrence of earthquake events is a temporal Poisson process, the probability of at least one exceedance of y_0 within time interval t_0 is given by

$$P(y_0, t_0, \bar{\lambda})[y \geq y_0] = 1 - e^{-\bar{\lambda}t_0}, \quad (2)$$

where $\bar{\lambda}$ is the mean annual recurrence rate.

For PSRA in the insurance industry, MC simulation is commonly used to obtain a set of stochastic ground motion fields $\hat{\mathbf{Y}}$ and to then compute the probability that a loss level ι_0 is exceeded as

$$P(\hat{\mathbf{Y}}, \Theta)[\iota \geq \iota_0] = \sum_{i=1}^{n_e} \int_{\iota_0}^{\infty} f_{\iota}(\iota|\hat{\mathbf{Y}}_i, \Theta)d\iota, \quad (3)$$

where $f_{\iota}(\iota|\hat{\mathbf{Y}}_i, \Theta)$ is the loss probability density function for a portfolio Θ given the i th ground motion field $\hat{\mathbf{Y}}_i$. Summing up the contribution of all n_e events yields the total loss exceedance probability. A Probable Maximum Loss (PML) curve, showing loss against mean return period T (with $T = 1/\bar{\lambda}$), can be obtained from the loss exceedance probability curve (Equation 3) using a first order Taylor approximation of Equation 2:

$$T = \frac{t_0}{P(y_0, t_0, \bar{\lambda})[y \geq y_0]}. \quad (4)$$

Here, t_0 is the period of interest (time interval), which is 1 year for most reinsurance contracts.

For more details on PSHA and PSRA, we refer to the comprehensive textbook of McGuire (2004).

2.2 Portfolio Location Uncertainty

- Perhaps surprisingly, in the insurance industry, portfolios frequently lack precise coordinate-based location information. Obtaining this information is often not possible, e.g. because geocoding engines are not used systematically or can not reliably obtain coordinates from the policy address of the insured risk. Especially for large treaty portfolios with thousands or millions of risks, it apparently is simply too much effort for the primary insurer or the insurance broker to obtain and provide this information. Unfortunately, this is also not uncommon for smaller portfolios consisting only of a few hundred high-value risks. However, administrative zones, such as postal codes, can easily be obtained from the insurance policy.

- Exposure uncertainty has previously been identified as an important area of research (Crowley, 2014), and we already introduced a framework for stochastic treatment of location uncertainty in a recent paper (Scheingraber and Käser, 2019). In our framework, locations of risk items without precise coordinate location information are sampled with replacement from a weighted irregular grid inside their corresponding administrative zone. The grid weights are used to preferentially sample locations in areas of assumed high insurance density, e.g. based on population density or on commercial and industrial inventory data depending on the type of risk (Dobson et al., 2000). An example of such a weighted grid is shown in Figure 1.

In MC simulation, the choice of a pseudo-random number generator is of particular importance. In this study we use *MRG32K3a*, a combined multiple recursive generator which efficiently generates random number sequences with low memory requirements and excellent statistical properties (L'Ecuyer, 1999). MRG32K3a supports up to $1.8 \cdot 10^{19}$ statistically independent *substreams*. Each substream has a *period*¹ of $7.6 \cdot 10^{22}$. These properties make MRG32K3a well suited for a large scale parallel MC simulation of seismic risk.

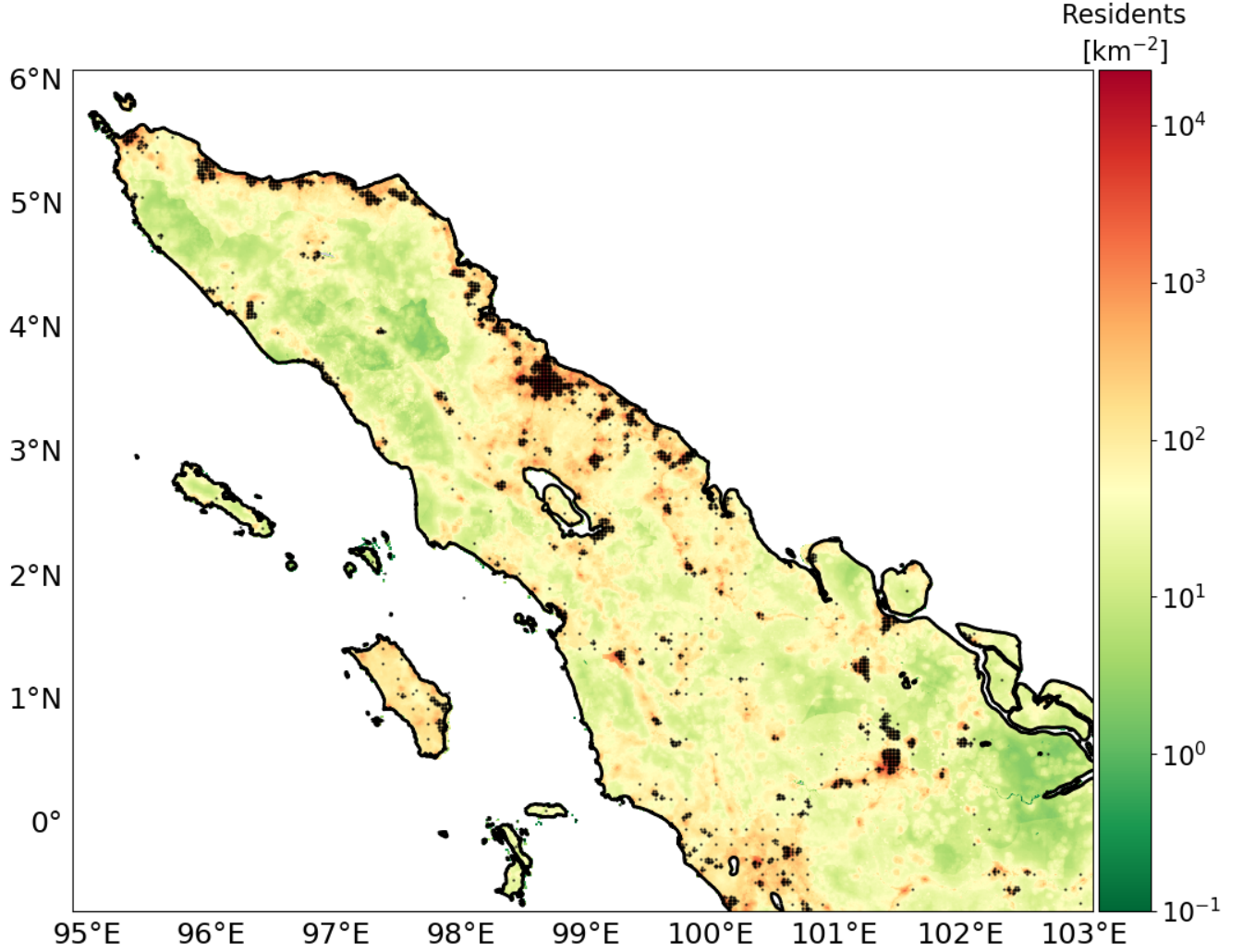


Figure 1. An example of a weighted grid used as an insurance density proxy for the location uncertainty framework. This shows northern Sumatra. Color indicates population density (residents per km^2) as a proxy for insured exposure density. Black markers depict grid points of the weighted grid. The population data in this plot is based on a free dataset (Gaughan et al., 2015).

¹The period of a pseudo-random number generator refers to the minimum length of a generated sequence before the same random numbers are repeated cyclically.

2.3 Evaluation of the Proposed Sampling Scheme

2.3.1 Standard Error

Because MC simulation is a stochastic method, there are no strict error bounds for statistics of interest obtained from a sample of finite size n . The error is therefore usually estimated using the standard deviation of the sampling distribution of the respective statistic, which is referred to as its standard error (E_{SE}). If the sampling distribution is known (e.g. normal), standard errors can often be obtained using a simple closed-form expression (Harding et al., 2014). For the statistics estimated in this study, e.g. PML at a specific return period, we can however not make a valid distribution assumption when taking location uncertainty into account. We therefore use repeated simulation to evaluate the performance of the proposed sampling scheme. The standard error can then be estimated as

$$E_{SE}(\hat{\Phi}_R) = \sqrt{\text{Var}(\hat{\Phi}_R)}, \quad (5)$$

where $\hat{\Phi}_R$ denotes a set of estimations of a statistic obtained from R repeated simulations and $\text{Var}(\cdot)$ the variance operator. The corresponding relative standard error E_{RSE} can be obtained by dividing E_{SE} by the estimated statistic. To estimate confidence intervals of standard errors, we use bootstrapping with the bias-corrected accelerated percentile method (Efron, 1979; Efron and Tibshirani, 1986).

2.3.2 Bias and Convergence Plots

The bias of an estimator $\hat{\theta}$ is defined as

$$\text{Bias}(\hat{\theta}_n) = \mathbb{E}_{\theta}(\hat{\theta}_n) - \theta, \quad (6)$$

where $\hat{\theta}_n = f(x_1, x_2, \dots, x_n)$ is the estimator depending on the n members of the sample and \mathbb{E}_{θ} its expected value. Because deriving the bias analytically is infeasible for a complex numerical simulation such as performed by our framework, we use simple MC² with a large sample size as empirical reference and approximation for θ . In addition we use convergence plots, which are a simple yet powerful method to monitor and verify the results (Robert and Casella, 2004). The values estimated using simple MC and the adaptive variance reduction scheme are plotted against increasing sample size n .

2.3.3 Variance Reduction, Convergence Order and Speedup

To quantify the performance of the proposed scheme at a particular sample size n , we use the following well-known definition of variance reduction VR:

$$\text{VR} = \frac{\sigma_{\text{MC}}^2}{\sigma_{\text{LSS}}^2}, \quad (7)$$

where σ_{MC}^2 is the variance using simple MC and σ_{LSS}^2 the variance using the proposed location sampling scheme (MacKay, 2005; Juneja and Kalra, 2009)

²For simple MC, the strong law of large numbers guarantees an *almost certain* convergence for $n \rightarrow \infty$.

To describe asymptotic error behavior for growing n , we use the big O notation (\mathcal{O} ; Landau, 1909; Knuth, 1976). For example, the error convergence order of simple MC is always $\mathcal{O}(n^{-0.5})$ independent of the dimensionality of the integrand (Papageorgiou, 2003).

To compare the real runtime required by simple MC and the proposed scheme to reach a specific relative standard error level ε_{RSE} , we use the speedup S defined as

$$S = \frac{t_{\text{MC}}}{t_{\text{LSS}}}, \quad (8)$$

where t_{MC} the runtime required by simple MC and t_{LSS} the runtime required by the proposed location sampling scheme.

2.4 Generation of Synthetic Portfolios

In this work, we use synthetic portfolios in western Indonesia modeled after real-world counterparts in terms of spatial distribution of risk items as well as value distribution among risk items.

2.4.1 Value Distribution

The total sum insured (TSI) is kept constant for all portfolios:

$$\text{TSI} = \text{const.} = 1 \cdot 10^6. \quad (9)$$

However, the TSI is distributed among a varying number of risk items (portfolio size). For this study, we use portfolio sizes n_r of 1, 10, 20, 50, 100, 1000 and 10000 risk items.

The value distribution observed in many real residential portfolios can be approximated well by a randomly perturbed flat value distribution:

$$\text{VI}_{\text{flat},i}^* = \frac{\text{TSI}}{n_r} \cdot X_i, \quad (10)$$

$$\text{VI}_{\text{flat},i} = \frac{\text{TSI}}{\sum_{i=1}^{n_r} \text{VI}_{\text{flat},i}^*} \cdot \text{VI}_{\text{flat},i}^*. \quad (11)$$

$\text{VI}_{\text{flat},i}$ (“value insured”) is the value assigned to the i th risk item and n_r denotes the number of risk items. X_i is a uniform random number in the interval $[1 - p, 1 + p]$, where p is a perturbation factor set to 0.2, which is consistent with the characteristics of many real portfolios. Equation 11 normalizes the n_r randomly perturbed insured values to ensure $\sum_{i=1}^{n_r} \text{VI}_{\text{flat},i} = \text{TSI}$.

2.4.2 Geographical Distribution

For each portfolio size, we created a set of 6 portfolios with an increasing fraction of unknown coordinates: 0%, 20%, 40%, 60%, 80%, and 100% of the risk items have unknown coordinates and are only known on the basis of their administrative zone (Indonesian provinces, or regencies and cities, see Section 3).

The geographical distribution of the exposure locations follows the weighted irregular grid described in Section 2.2. For each portfolio size, a portfolio with 0% unknown coordinates is initially created by choosing exposure locations from the irregular



Table 1. Ground motion models and corresponding weights used by the hazard model for different tectonic region types.

Tectonic Region Type	Ground Motion Model	Weight
Active Shallow Crust	Boore and Atkinson (2008)	1/3
	Campbell and Bozorgnia (2008)	1/3
	Chiou and Youngs (2008)	1/3
Stable Continental Crust	Toro et al. (1997)	1
Subduction Interface	Zhao et al. (2006)	2/3
	Youngs et al. (1997)	1/3
Subduction Intraslab	Atkinson and Boore (2003)	1

grid according to the grid point weights. For the other portfolios with the same number of risk items but a higher fraction of unknown coordinates, coordinate-based location information is then removed stepwise from the initial portfolio. In each step, 20% of the risk items are randomly selected for the removal of coordinates until all risk items have unknown coordinates.

3 Case Study: Spatial Seismic Hazard Variation in Western Indonesia

5 3.1 Hazard Model



For this study, we use a custom seismic risk model based on the South-East Asia hazard model by Petersen et al. (2007) of the United States Geological Survey (USGS). Site conditions or soil classes are based on topographic slope (Wald and Allen, 2007), but have been refined locally to consider areas of soft soil, such as river beds. The geometry of the Sumatra subduction zone has been improved over the original USGS model. It is a complex representation of the fault geometry based on the *Slab* 1.0 model (Hayes et al., 2012), which provides three-dimensional data of the subduction. To generate finite geometry patches for individual events on the complex fault, we use a rupture floating mechanism similar to the implementation of OpenQuake (Pagani et al., 2014), a free and open-source seismic hazard and risk software developed as part of the Global Earthquake Model initiative (Crowley et al., 2013).

In order to reduce the computational effort of the hazard model, we have simplified the logic tree of the ground motion model for all tectonic regions types. This allowed to thoroughly analyze the performance of the proposed sampling scheme for a larger set of insurance portfolios and sampling scheme parameters, while retaining overall accordance with the hazard of the original model. Table 1 gives an overview of the selected ground motion models and their weights.

Figure 2 shows the resulting seismic hazard map for an exceedance probability of 10% in 50 years. Assuming a temporal Poisson distribution, this probability equals an average return period of 475 years, which is used for most seismic hazard maps and by the engineering community for the design of building codes. The depicted area is comprised of the islands

of Sumatra, Java, and Kalimantan (the Indonesian sector on the island of Borneo). The hazard results of our model are in general agreement with results obtained using the original USGS South-East Asia model (Petersen et al., 2007) or third-party implementations such as by the Global Earthquake Model (GEM) initiative evaluated using the OpenQuake engine³. Slight differences are caused by the inclusion of site conditions, simplified ground motion model logic tree, different source parameterization, improved subduction geometry representation, and slightly modified seismicity rates based on the latest ISC-GEM Global Instrumental Earthquake Catalogue (Storchak et al., 2013) and Global Historical Earthquake Catalogue⁴.

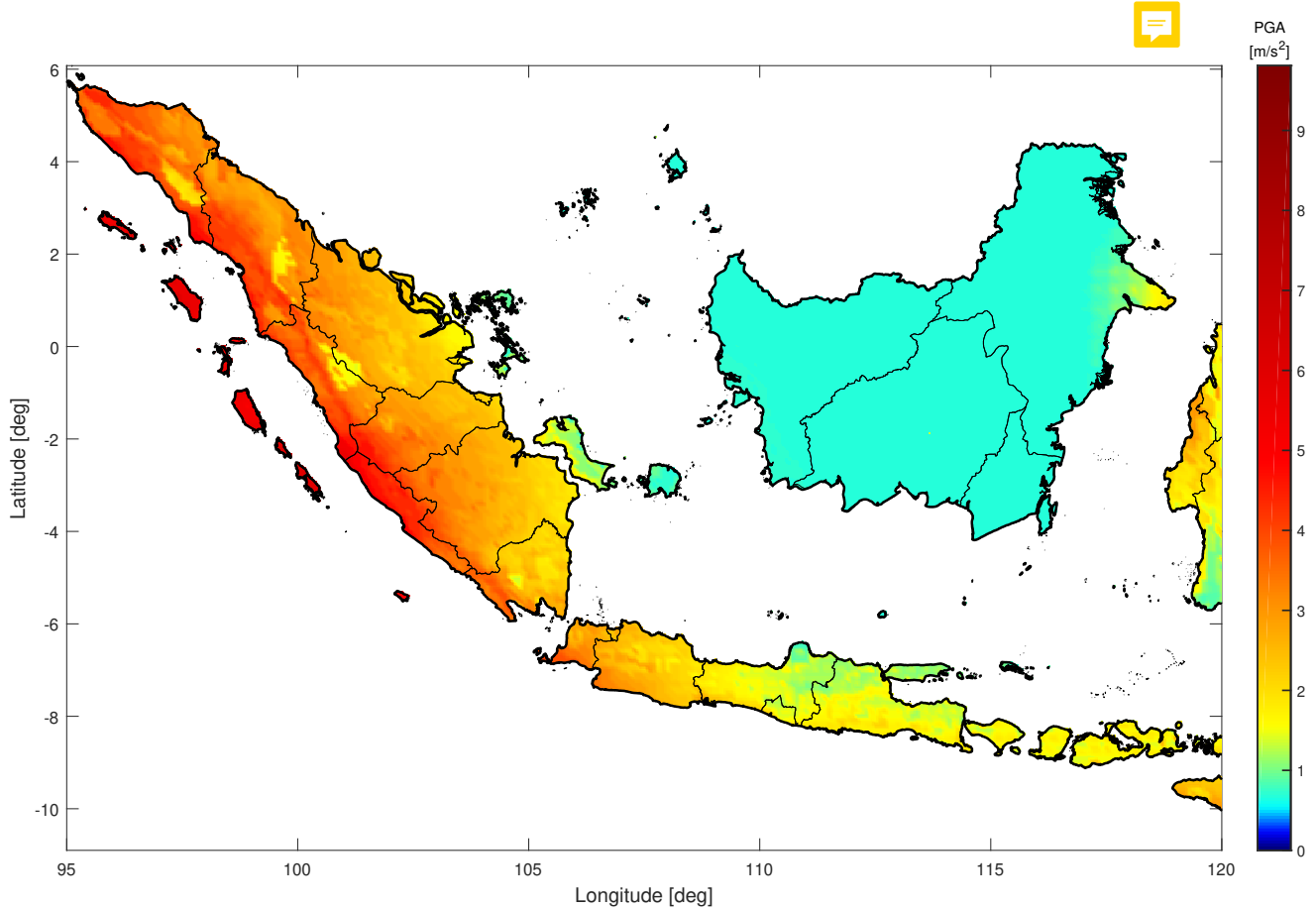


Figure 2. Seismic hazard in western Indonesia, as obtained using our hazard model. Color shows the level of Peak Ground Acceleration (PGA, in ms^{-2}) that is predicted to be exceeded at an average return period of 475 years.

On the island of Sumatra, the effect of the Sumatra fault zone is clearly visible and seismic hazard is strong. The seismic hazard of Java is highest in the western area of the island, around the city of Jakarta. The hazard levels decrease towards the

³See https://hazardwiki.openquake.org/sea2007_intro for results obtained using OpenQuake.

⁴See <http://www.emidius.eu/GEH/>.

east. On Kalimantan, there are no known or modeled seismic crustal faults. Therefore, only a low level of spatially homogenous distributed gridded seismicity is used in this area, resulting in low hazard.

The hazard model and results are described in more detail in a recent paper (Scheingraber and Käser, 2019).

3.2 Spatial Seismic Hazard Variation

- 5 For this analysis, we compute seismic hazard on a regular grid using a resolution of 0.3° . We investigate the coefficient of variation (CV) of hazard inside administrative geographical zones for different levels of resolution, corresponding to provinces and regencies or cities in Indonesia. The CV is defined as

$$CV = \frac{\sigma}{\mu}, \quad (12)$$

where σ is the standard deviation and μ the mean.

10 3.2.1 Dependence on Resolution Level of Geographical Zones

- Figure 3 shows the CV of peak ground acceleration with an exceedance probability of 10% in 50 years per province in Indonesia. There is a noticeable decrease of the CV from west to east. The subduction modeled by the complex fault and the Sumatra Fault Zone (SFZ) result in the highest CV on Sumatra (most values 0.2 - 0.3). The CV is also relatively high on Java (around 0.15). The CV is the lowest in Kalimantan (< 0.1) due to the absence of any known or modeled crustal faults. As only
- 15 gridded seismicity is used in this area, the hazard variation is very small. Furthermore, zones with a large extent perpendicular to the SFZ show a larger CV than zones with a smaller extent along the direction of the steepest hazard gradient. An example of this are the provinces of *Jambi* and *Bengkulu* in Figure 3. Arguably, location uncertainty is more important in *Jambi* than in *Bengkulu*.

- Figure 4 shows the CV per regency or city for the same exceedance probability. Due to the smaller spatial extent of the
- 20 administrative zones, the CV is in general lower at this more granular resolution of administrative geographical zones. Another observation is that the influence of individual seismo-tectonic features emerges; the CV is higher in the vicinity of modeled faults. While the Sumatra subduction only has a weak influence, the SFZ has a pronounced effect. Near the SFZ, the CV has values of about 0.1 - 0.2. Perpendicular to the SFZ, the CV quickly drops below 0.1.

- In general, the CV is highest in zones close to modeled faults of shallow depths, as they result in a higher spatial hazard
- 25 gradient than compared to areas where hazard is dominated by rather regularly distributed gridded seismicity. A reasonable assumption is that location uncertainty can be particularly high in such zones.

3.2.2 Dependence on Return Period

- Analysis of the CV across different return periods for individual zones revealed a similar pattern for most administrative zones. The CV is small for short return periods, and reaches a relatively stable level above a certain return period. An example of
- 30 this behavior is shown in Figure 5 for the province of *Jambi*. However, the CV does not show this pattern in all administrative

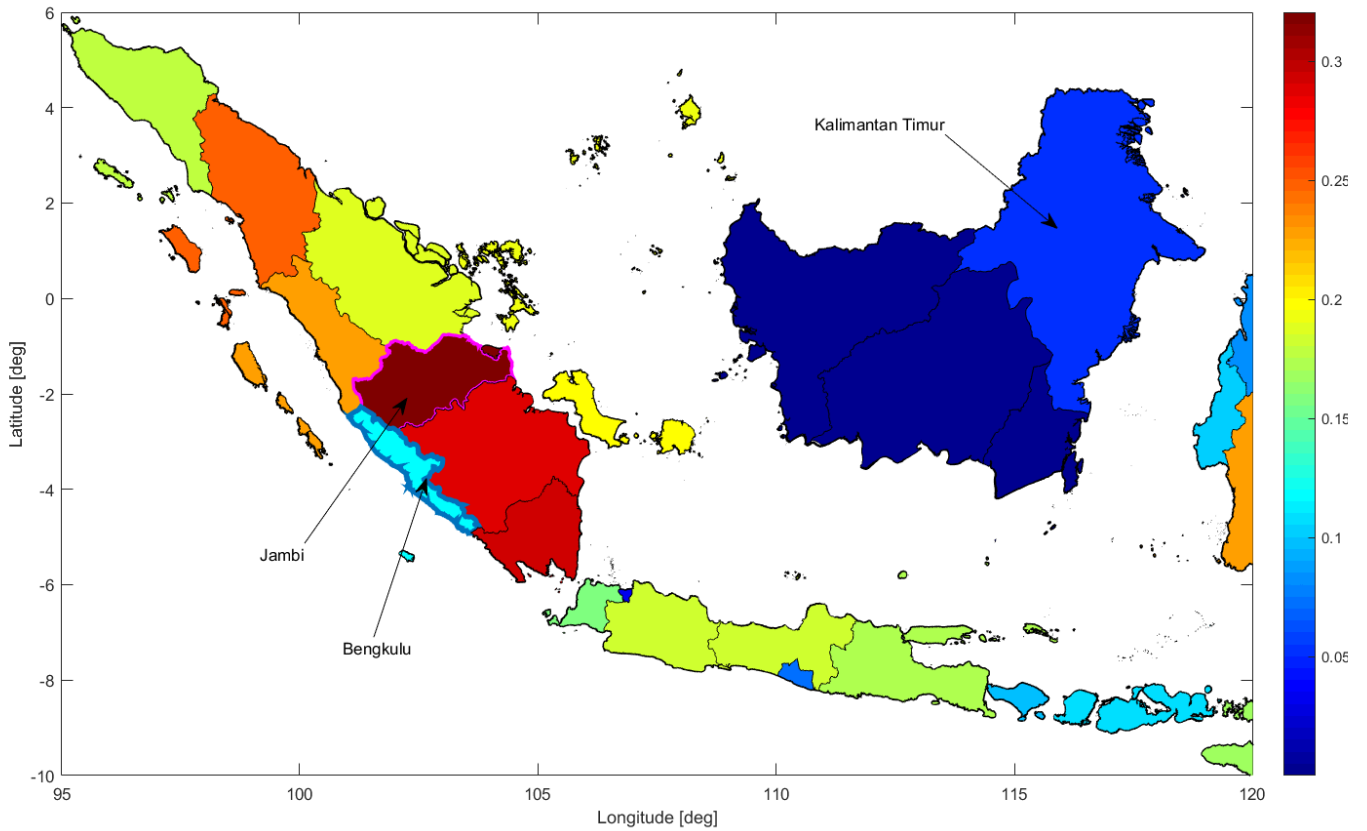


Figure 3. Coefficient of Variation (CV) of Peak Ground Acceleration (PGA) with an exceedance probability of 10% in 50 years inside provinces in western Indonesia. Color denotes the CV. Note how the CV is higher in provinces that have a large extent perpendicular to the Sumatra Fault Zone, such as *Jambi* (outlined in pink color), than in provinces with a small extent in that direction, such as *Bengkulu* (outlined in blue).

zones. For some zones, especially at the level of regencies and cities, we could not determine a range of return periods for which the CV is roughly constant, as for example in the province of *Kalimantan Timur* shown in Figure 6.

3.3 Loss Rate Variation

The variability of the CV over return periods for certain zones makes it difficult to choose a general return period suitable for assessing the spatial variation of hazard inside a zone. To avoid the subjectivity introduced by a manual decision process for a suitable return period, we use the CV of the loss rate per zone, as it considers all return periods. Figure 7 shows the CV of the loss rate for Indonesian provinces. The overall pattern agrees with the pattern of the spatial hazard variation in Figure 3, but the range of values is much higher, from about 0.1 to 0.9.

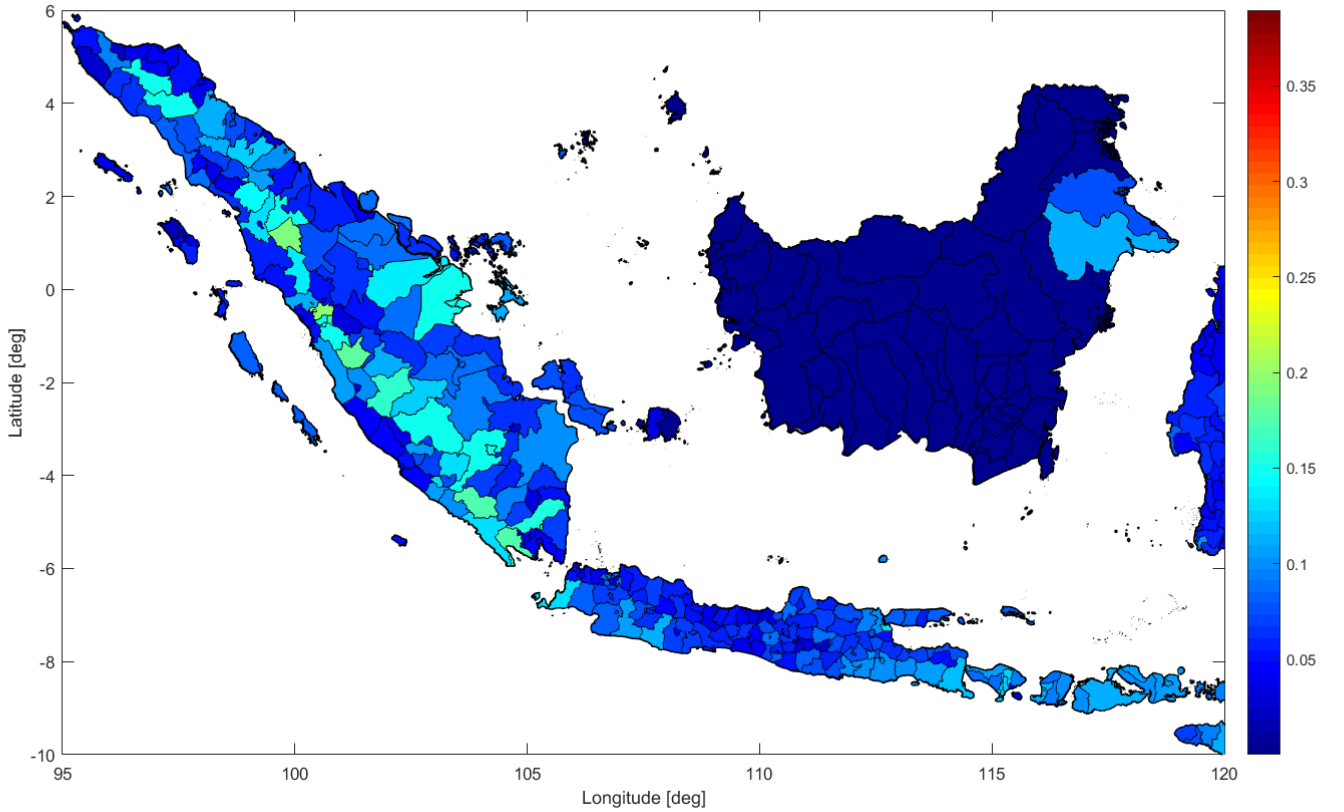


Figure 4. Coefficient of Variation (CV) of Peak Ground Acceleration (PGA) with an exceedance probability of 10% in 50 years inside regencies and cities in western Indonesia. Color denotes the CV. At this geographical resolution the CV is lower than for provinces (see Figure 3), and the influence of individual seismo-tectonic features, such as the Sumatra fault zone, becomes apparent.

4 A Framework for Adaptive Sampling of Portfolio Location Uncertainty

To increase efficiency, in our framework ground motion is jointly simulated on all unique locations of all sampled location sets. Since the computation of hazard dominates the overall runtime of PSRA, it is worthwhile to explore possibilities to distribute the number of locations on which hazard is computed in a smart way among risk items. To this end, we introduce three sampling

5 criteria to determine the location sample size individually per risk item. A large location sample size is used for risk items for which at all three criteria indicate that location uncertainty has a strong influence. If any of the three criteria predicts that location uncertainty has a lesser effect, a smaller sample size is used. In this way, more computational effort is invested where it is important and a better estimation of the PML curve associated with a lower variance is obtained for a given number of used hazard locations. To not add noticeable overhead to the calculation, a key requirement is that all criteria can be evaluated

10 very efficiently. To keep the computational overhead small, another design goal is that the framework is adaptive in a sense that it depends directly on properties of the portfolio and a precalculated hazard variability (see Section 3), but does not require

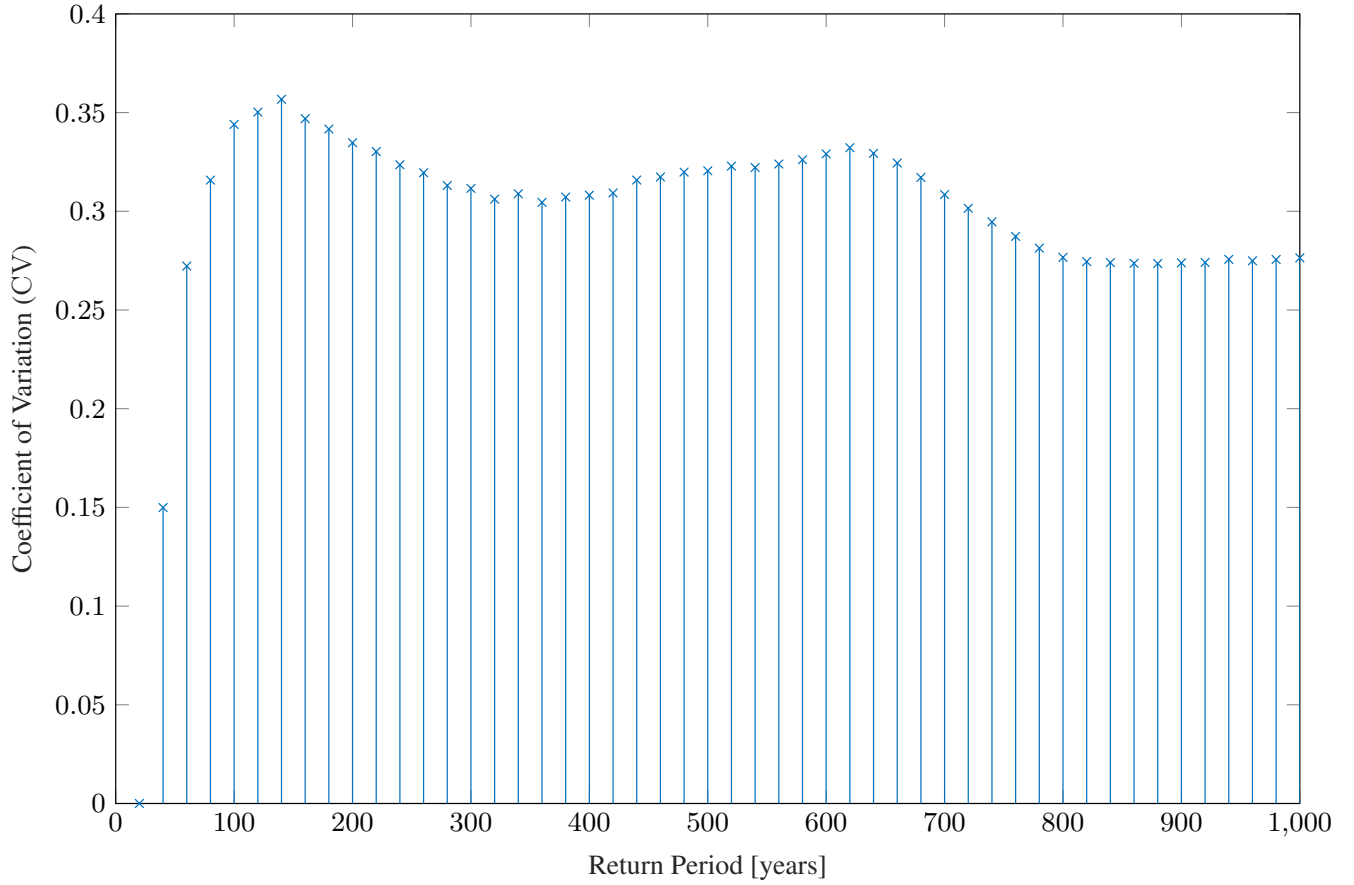


Figure 5. Coefficient of variation (CV) of ground motion predicted to be exceeded at various return periods for the *Jambi* province (see Figure 3). The CV remains quite stable over a large range of return periods.

on-the-fly integral presampling such as used by some general purpose adaptive variance reduction schemes (Press and Farrar, 1990; Jadach, 2003).

4.1 Risk Location Index Mapping Table

We store an array containing all unique geographical locations on which ground motion is simulated, and another array storing the sampled location indices per risk item. Table 2 illustrates the concept. Each column of the table corresponds to a location set representing a valid realization of location uncertainty for the entire portfolio. To combine unequal sample sizes for risk items without introducing bias due to overemphasis of a subset of a sample, we restrict the sample size to powers of two. The full sample can then be repeated in the mapping table.

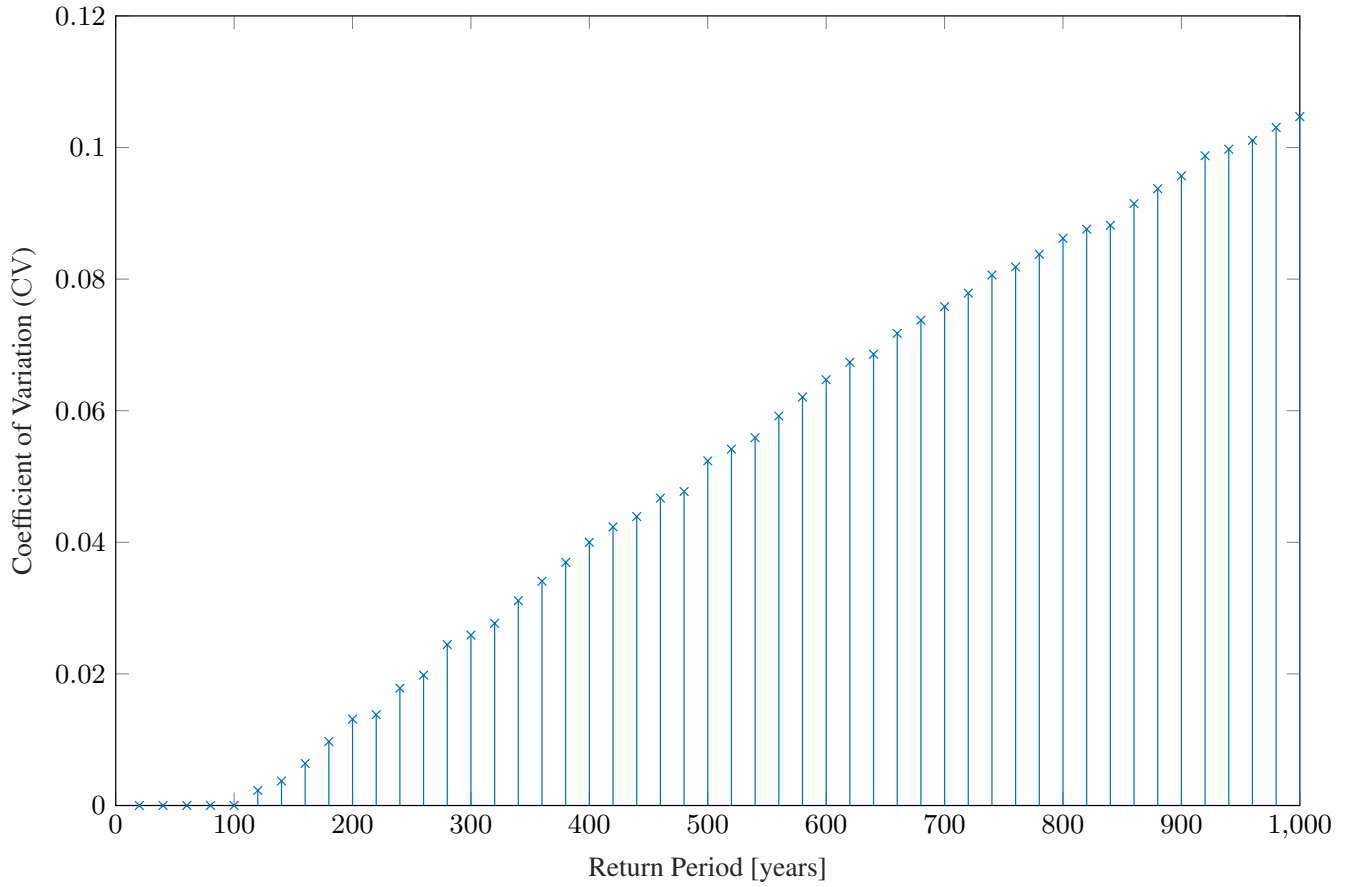


Figure 6. Coefficient of variation (CV) of ground motion predicted to be exceeded at various return periods for the *Kalimantan Timur* province (see Figure 3). In this case, it is not possible to determine a range of return periods for which the CV remains in a stable range.

Table 2. Risk Location Index Mapping Table. Rows correspond to individual risk items, showing sampled grid point indices. Each column represents a possible spatial distribution of the portfolio. Risk item 1 has the maximum location sample size of $n_{\max} = 4$, but risk items 2 and 3 only have a sample size of 2 and 1, respectively.

Risk Item Index	Sample Size	Sample 1	Sample 2	Sample 3	Sample 4
1	4	43	13	31	51
2	2	23	18	23	18
3	1	51	51	51	51

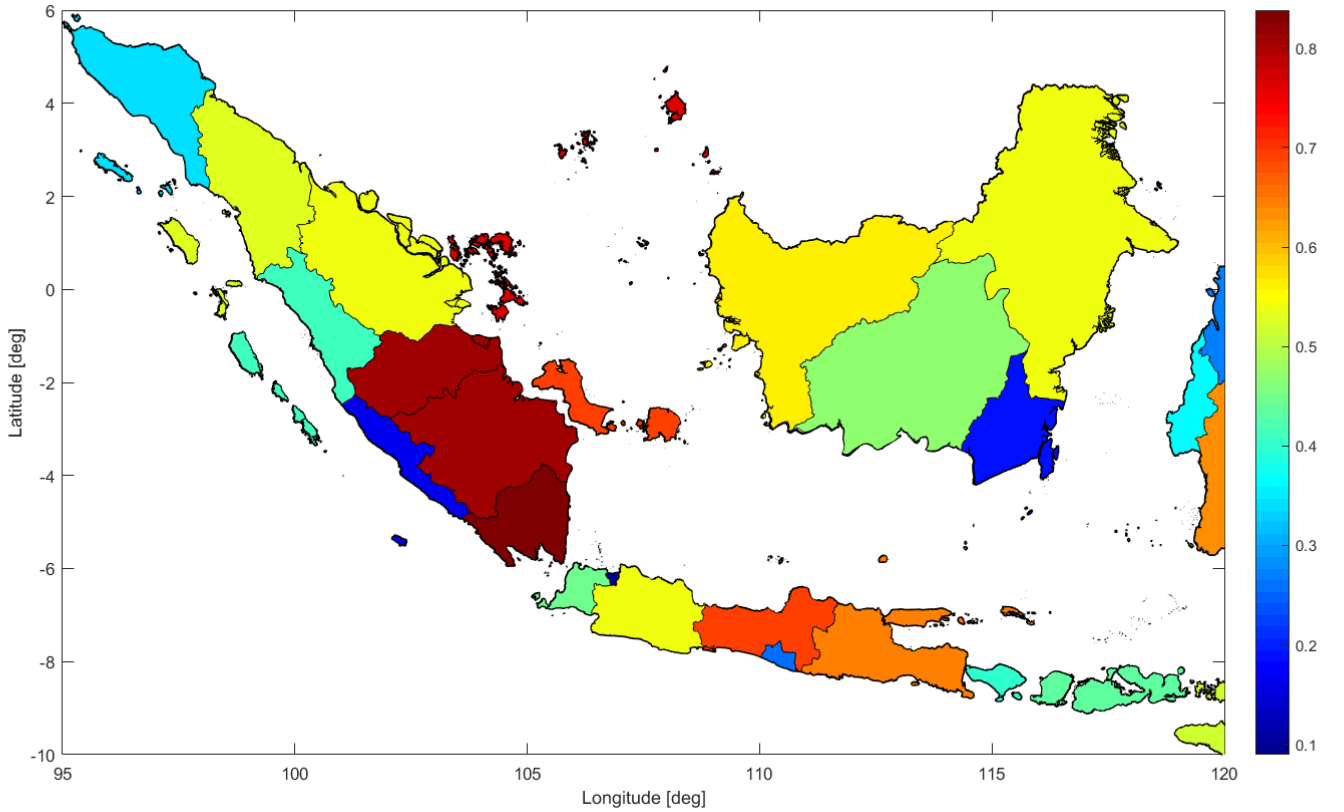


Figure 7. Coefficient of variation (CV) of the loss rate inside provinces in western Indonesia. Color denotes the CV.

4.2 Criterion I: Coefficient of Variation of Loss Rate

The first criterion is based on the CV of loss rate within a zone (see Section 3), hereafter denoted by CV_z . The values of CV_z can be precomputed for all administrative geographical zones, and therefore the evaluation of this criterion can be implemented in a very efficient manner.

- 5 The number of samples n_L due to criterion I is defined piecewise:

$$n_L^* = \begin{cases} 1, & \text{if } CV_z \leq t_l, \\ \frac{n_{\max}-1}{t_u-t_l} \cdot CV_z + 1, & \text{if } CV_z \in (t_l, t_u), \\ n_{\max}, & \text{if } CV_z \geq t_u. \end{cases} \quad (13)$$

Here, t_l and t_u are lower and upper threshold values. n_{\max} represents the maximum used sample size. We round n_L^* up to the next higher power of two to obtain the final n_L . The criterion is shown in Figure 8 for the example $t_l = 0.1$, $t_u = 0.4$ and $n_{\max} = 16$. In our final implementation, t_l and t_u are chosen adaptively as empirical quantiles of the CV distribution ($CV_{0.4}$

for t_l and $CV_{0.6}$ for t_u , i.e. the 40% and 60% percentiles) of the loss rate of all administrative zones of a model (see Section 3), which was found to be a reasonable choice for our test cases with the aid of an extensive parameter study (see Section 5.1).

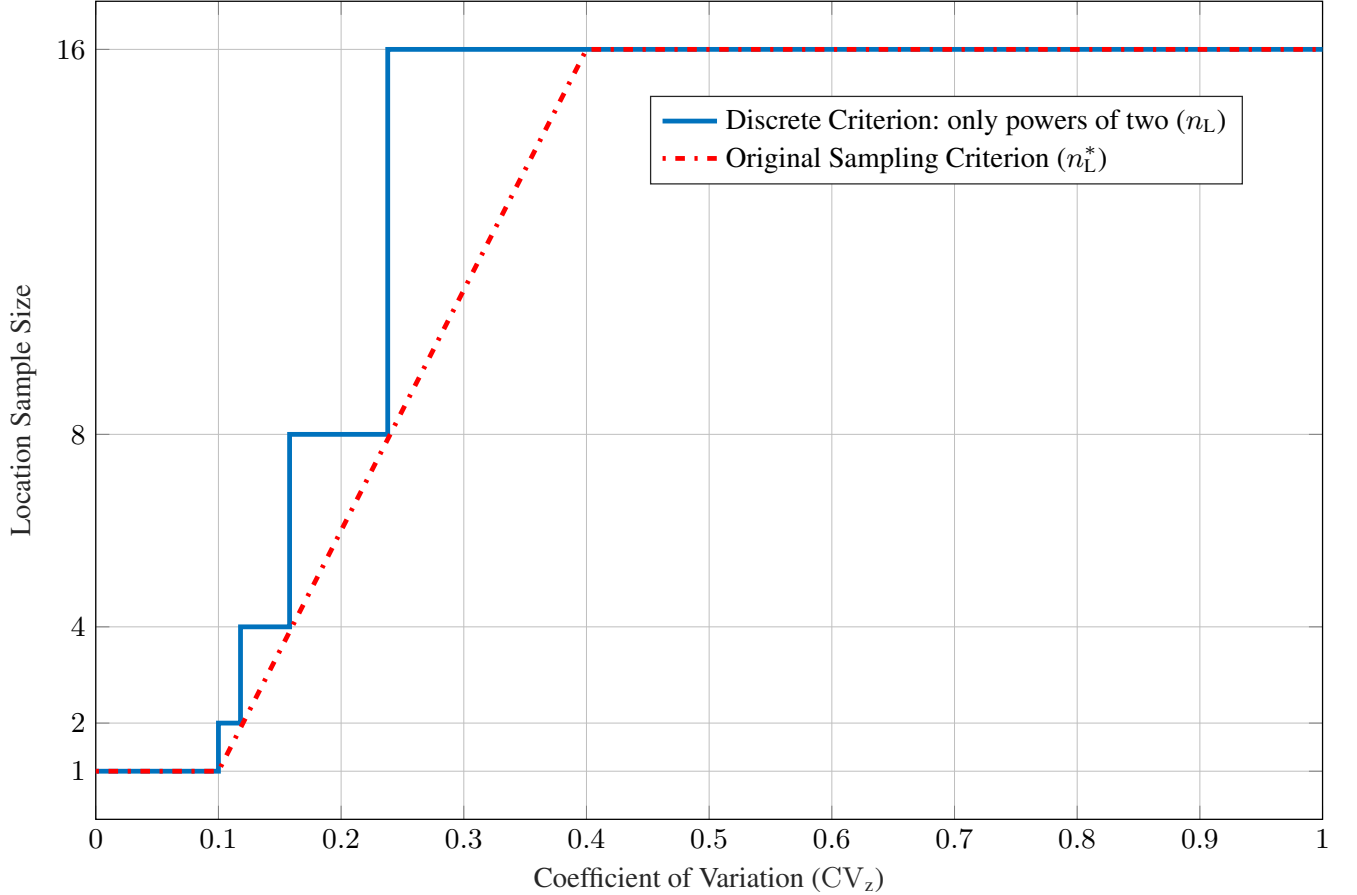


Figure 8. Criterion I: Number of samples per zone depending on coefficient of variation. The discrete realization of the criterion (limited to powers of two) is shown in blue, while the red line represents the theoretical linear behavior.

4.3 Criterion II: Number of Risk Items

The second criterion involves two steps. The first step defines a maximum sample size for the entire portfolio depending on the total number of risk items n_r in the portfolio and a threshold t_p as

$$n_R^\dagger = \begin{cases} -\frac{n_{\max}-1}{\log(t_p-1)} \cdot \log(n_r-1) + n_{\max}, & \text{if } n_r < t_p, \\ 1, & \text{if } n_r \geq t_p, \end{cases} \quad (14)$$

which is then used to obtain a maximum sample size per zone, depending on the number of risk items in a zone n_z and a threshold t_z :

$$n_R^* = \begin{cases} -\frac{n_R^\dagger - 1}{t_z - 1} \cdot (n_z - 1) + n_R^\dagger, & \text{if } n_z < t_z, \\ 1, & \text{if } n_z \geq t_z. \end{cases} \quad (15)$$

We round n_R^* up to the next higher power of two to obtain the final n_R . Figures 9 and 10 illustrate this criterion for $t_p = 10000$, $t_z = 100$ and $n_{\max} = 16$. In this study, t_p is chosen to be 10000 and t_z is set adaptively to equal the number of grid points of the weighted location uncertainty sampling grid (see Section 2.2) inside each administrative zone. The design of this criterion is based on the results of a previous study, in which we systematically investigated the effect of location uncertainty and loss aggregation due to spatial clustering of risk items for a large range of different portfolios. It was found that location uncertainty typically has a neglectable effect for very large portfolios and a roughly flat value distribution (Scheingraber and Käser, 2019).

10 4.4 Criterion III: Value Distribution

The third criterion depends on the relative insured values of risk items (“sum insured”, SI). Risk items are sorted with respect to their SI, and the index of their sorted order I_r is used along with a threshold index t_i to determine the maximum sample size per risk item:

$$n_V^* = \begin{cases} -\frac{n_{\max} - 1}{t_i - 1} \cdot (I_r - 1) + n_{\max}, & \text{if } I_r < t_i, \\ 1, & \text{if } I_r \geq t_i. \end{cases} \quad (16)$$

15 We round n_V^* up to the next higher power of two to obtain the final n_V . Figure 11 illustrates this criterion for $t_i = 6$ and $n_{\max} = 16$. In this study, for t_i we adaptively set the index of the first risk item which has a SI higher than the mean of all risk items.

4.5 Combination of Criteria

The final sample size for a specific risk item is then given by the minimum of the three criteria:

$$20 \quad n = \min\{n_L, n_R, n_V\}. \quad (17)$$

The rationale behind this decision is that any of the criteria can separately predict that a particular risk item has a low impact on loss uncertainty. For example, if a risk item with an unknown coordinate has a low insured value, it has a relatively low impact on loss uncertainty even if the variation of hazard or loss rate within the corresponding administrative zone is high, and thus a small location uncertainty sample size can be used. Vice versa, the impact of location uncertainty is limited if a risk item with an unknown coordinate has a high insured value but the hazard within the corresponding administrative zone is relatively flat. Furthermore, loss uncertainty is also limited if a portfolio contains a very high number of total risk items or the number of risk items belonging to an administrative zone is high compared to the number of grid points within this zone.

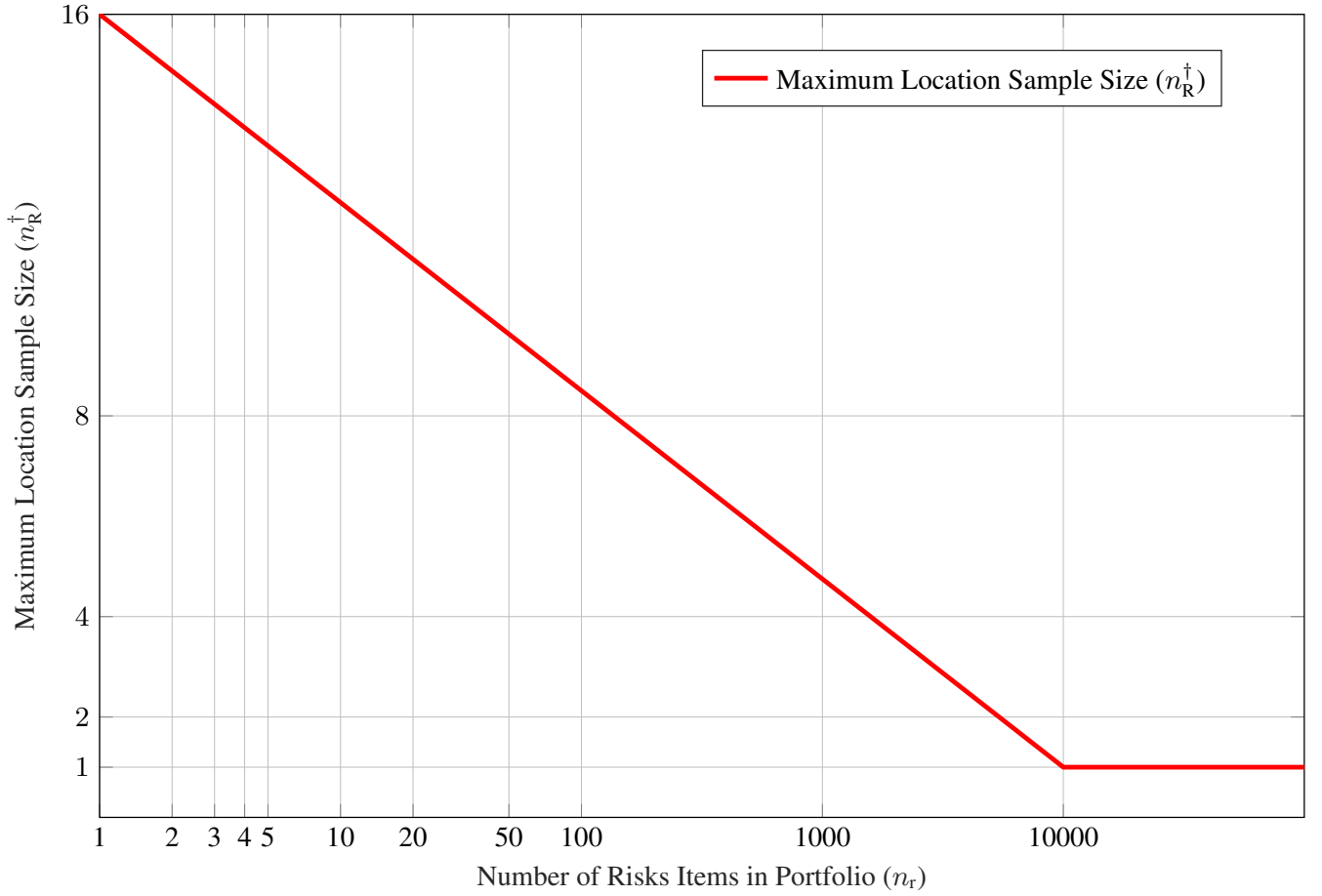


Figure 9. Criterion II.a: Number of samples per zone depending on the number of risk items in the portfolio. Note that we do not round up to the next higher power of two, since this plot illustrates Equation 14, which is an intermediate step.

5 Results

In this section, the variance reduction and speedup obtained with the proposed adaptive location uncertainty sampling scheme is analyzed using the western Indonesia hazard model described in Section 3.1 in conjunction with a vulnerability model for regional building stock composition. To this end, loss frequency curves are computed for the synthetic portfolios described in Section 2.4 with simple MC as well as the adaptive scheme. The convergence and relative standard errors are evaluated against the number of unique hazard locations used for the loss calculation by either approach and the associated required runtime is compared.

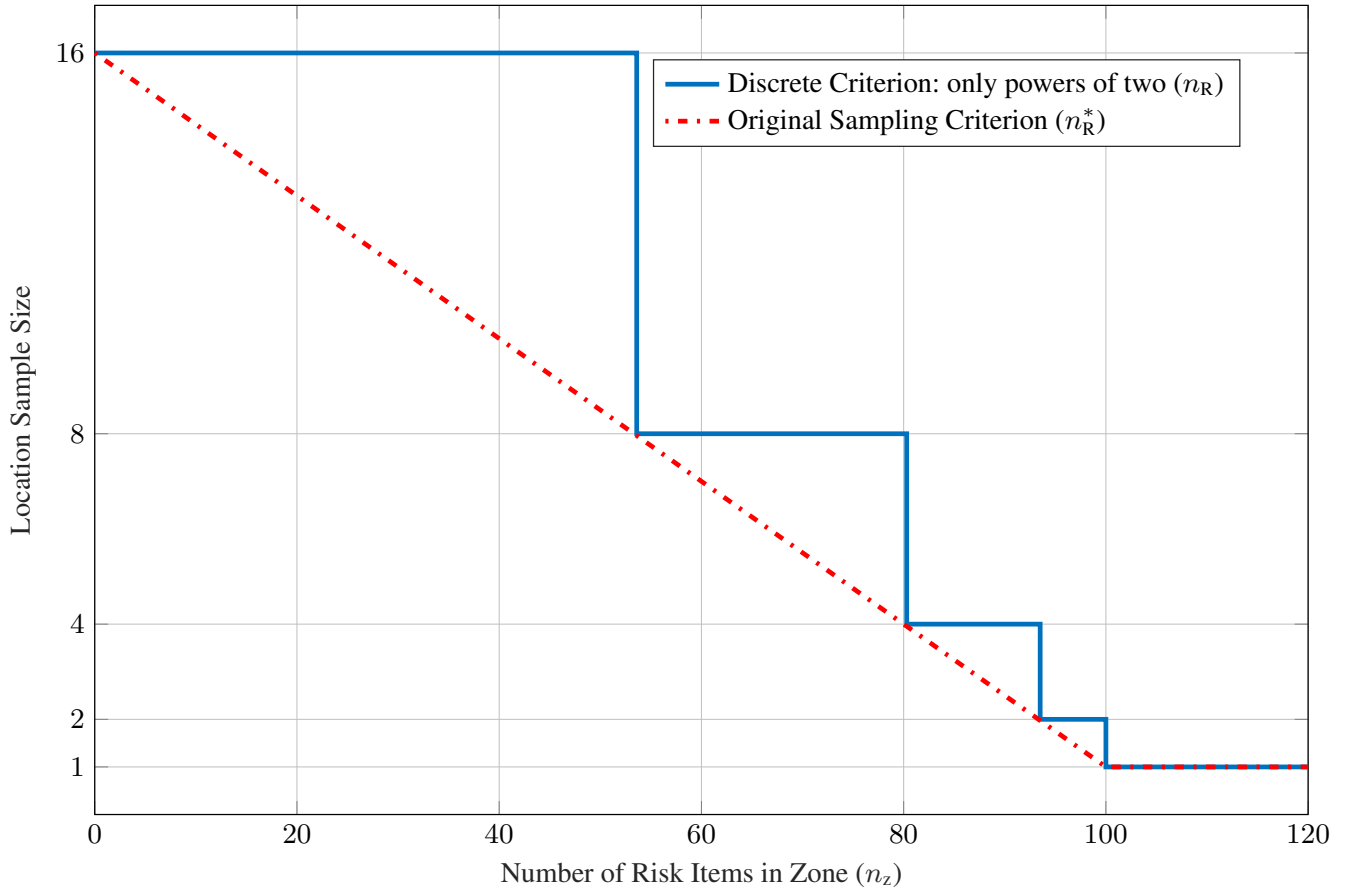


Figure 10. Criterion II.b: Maximum number of samples per zone depending on the number of risk items in an administrative zone. The discrete realization of the criterion (limited to powers of two) is shown in blue, while the red line represents the theoretical linear behavior.

5.1 Spatial Variation Parameter Study

We first analyze the performance of the adaptive sampling scheme for different values of the lower (t_l) and upper (t_u) threshold parameters for the spatial variation of loss rate in an administrative zone in comparison to simple sampling. In simple MC, all risk items get the same location uncertainty sample size n_{\max} and there is not restriction to powers of two. For this parameter study, we use values of $n_{\max} = 32, 64, 96, 128, 160, 192, 224, 256$ in order to obtain a smooth curve with a high number of support points.

For the adaptive variance reduction scheme, the sample size is restricted to powers of two and is determined for each risk item individually - potentially smaller than the maximum allowed location uncertainty sample size n_{\max} (see Section 4 and Table 2). Since the sample size varies between risk items, for a meaningful comparison with simple MC it is necessary to use a measure of the total effort spend for the treatment of location uncertainty of all risk items. We use the total number of unique

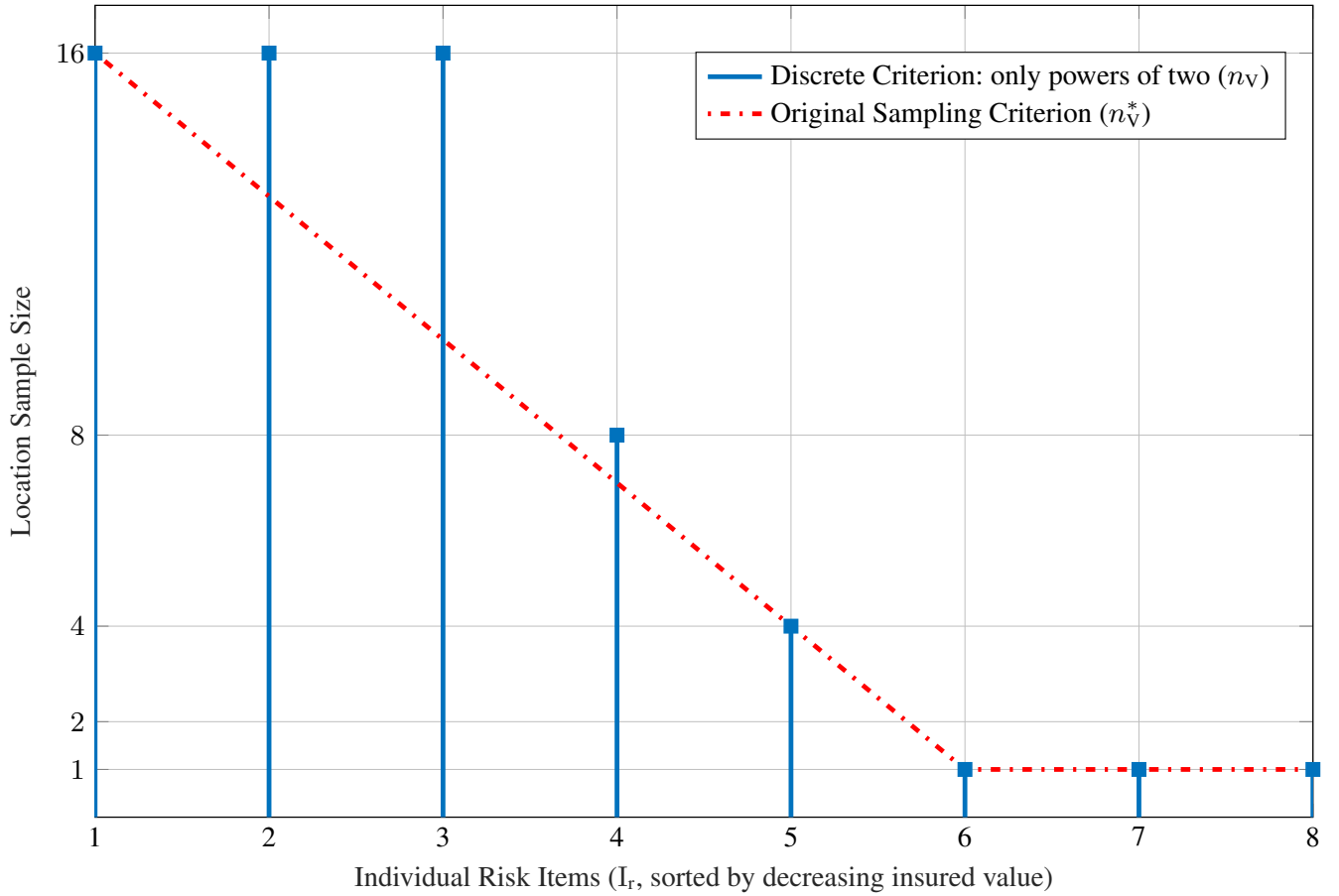


Figure 11. Criterion III: Number of samples per zone depending on the insured values of the risk items. The discrete realization of the criterion (limited to powers of two) is shown in blue, while the red line represents the theoretical linear behavior.

hazard locations (n_{hazard}) and the runtime spent for the computation of hazard (t_{hazard}). While for simple MC all risk items get the maximum sample size n_{max} , the adaptive location sampling scheme reduces the sample size for risk items for which location uncertainty likely has a smaller influence. This means that the adaptive location sampling scheme results in a smaller n_{hazard} than simple MC for the same portfolio and n_{max} . Therefore, in order to obtain a comparable values for n_{hazard} , a larger maximum sample size n_{max} has to be employed for the adaptive scheme than for simple MC. Here, we use $n_{\text{max}} = 2^i$ with $i = 5, 6, \dots, 8$.

For each sample size, the spatial variation threshold parameters are varied over the distribution of CV values, picking quantiles in constant steps of 0.2. The lower threshold t_l is varied from $CV_{0.0}$ to $CV_{0.8}$, and the upper threshold t_u from $CV_{0.2}$

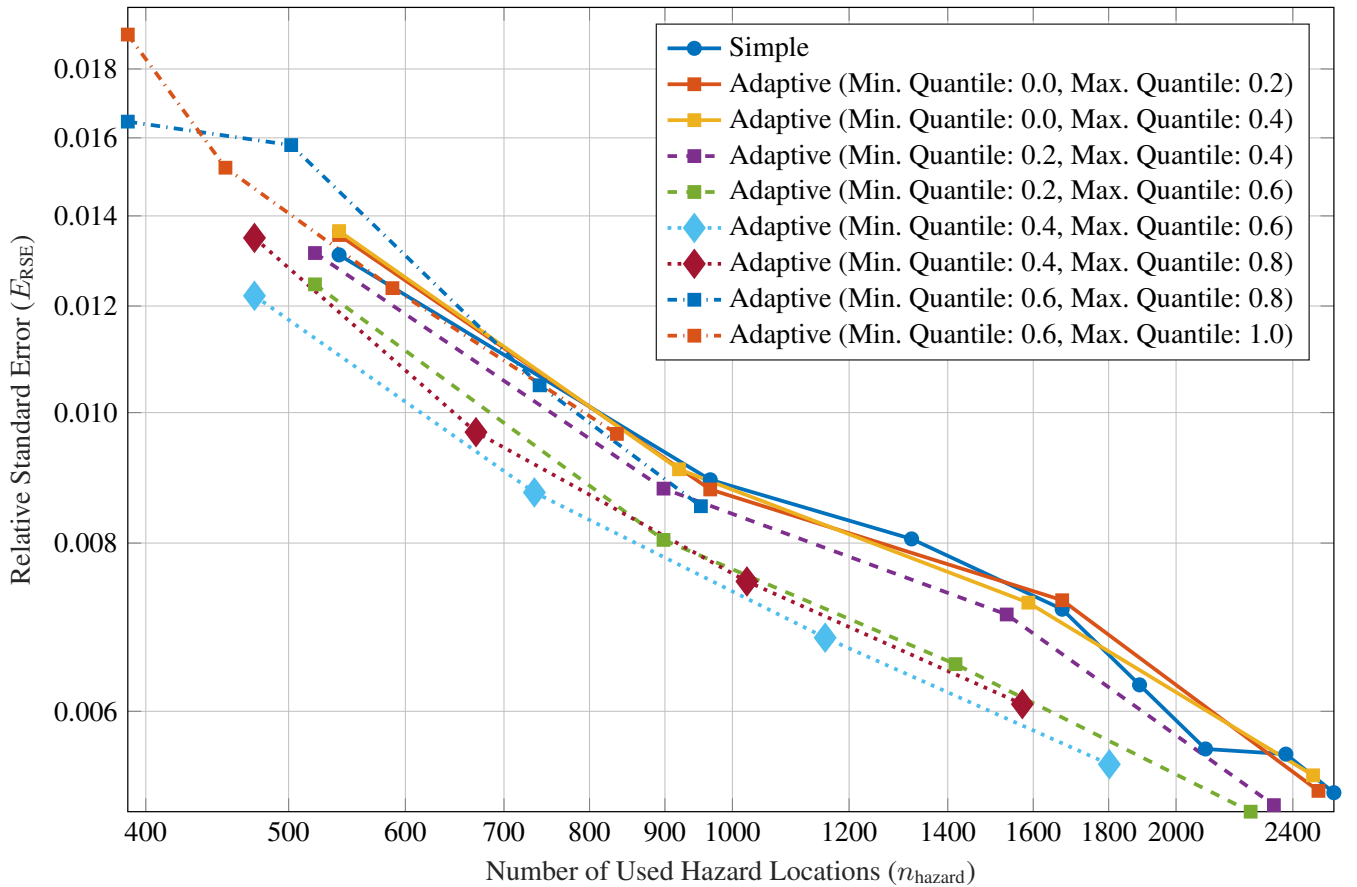


Figure 12. Results of a systematic parameter study with the goal of finding good values for the lower threshold (t_l) and upper threshold (t_u) parameters of Criterion I of the adaptive location uncertainty sampling scheme (see Section 4), based on the distribution of the Coefficient of Variation (CV) of loss rate in administrative zones. This shows a logarithmic plot of relative standard error (E_{RSE}) of Probable Maximum Loss (PML) at a return period of 100 years against the number of used hazard locations (n_{hazard}) for a portfolio of 20 risk items with 100% unknown coordinates. Color indicates different combinations for the threshold parameters t_l and t_u . Quantiles of the CV distribution around $t_l \in [CV_{0.2}; CV_{0.4}]$ in combination with $t_u \in [CV_{0.6}; CV_{0.8}]$ work best.

to $CV_{1.0}$. For each combination of t_l and t_u , $R = 20$ repeated simulations were performed for each sample size to estimate the respective relative standard error E_{RSE} .

In general, for our test cases the scheme works well around $t_l \in [CV_{0.2}; CV_{0.4}]$ in combination with $t_u \in [CV_{0.6}; CV_{0.8}]$. For example, for a portfolio of 20 risk items and 100% unknown coordinates, Figure 12 shows a logarithmic plot of the relative standard error E_{RSE} of PML at a return period of 100 years against the number of used hazard locations n_{hazard} for some combinations of t_l and t_u . The error curves for all combinations of t_l and t_u have the same slope as the curve for simple MC and thus the same convergence order of $\mathcal{O}(n^{-0.5})$. For certain combinations, the error curve is below the curve for simple

MC, meaning that in these cases the scheme successfully reduces the variance of the estimation and therefore the associated standard error.

For the final implementation, we used $t_l = CV_{0.4}$ and $t_u = CV_{0.6}$, which performed best in this parameter study.

5.2 Performance of the Final Implementation

- 5 We now evaluate the performance of the final implementation of the adaptive scheme, checking if it results in any unwanted systematic bias and investigating variance reduction and speedup for the calculation of PML for different portfolios.

5.2.1 Convergence and Bias

Figures 13 and 14 show convergence plots of PML at 100 years return period against the number of used hazard locations n_{hazard} for portfolios with $n_r = 10$ and $n_r = 100$ risk items, respectively. The left plots depict the results for portfolios with 60% unknown coordinates, the right plots the results for portfolios with 100% unknown coordinates. Simple sampling is shown in blue, the adaptive scheme in red. For all portfolios, the sample size n was varied as $n = 2^i$ with $i = 3, 4, \dots, 9$. For each sample size and both sampling schemes $R = 20$ repeated simulations are shown as semi-transparent circles, with solid lines highlighting one individual repetition.

15 The results show that empirically the adaptive scheme converges to the same result as simple MC for our test cases, meaning that the scheme does not result in any systematic bias. It is also apparent that for a given number of used hazard locations n_{hazard} , the relative PML values obtained with the adaptive scheme scatter less than those estimated with simple MC.

5.2.2 Variance Reduction and Speedup

For the same portfolios as analyzed in the previous section, Figure 15 shows logarithmic plots of the relative standard error E_{RSE} obtained from $R = 20$ repeated simulations against the number of used hazard locations n_{hazard} . Vertical bars depict upper 95% confidence intervals estimated using bootstrapping with 1000 resamples. Simple MC is again shown in blue, the variance reduction sampling scheme in red. While the observed error convergence order of the adaptive scheme remains the same as for simple MC (i.e. $\mathcal{O}(n^{-0.5})$, compare Section 5.1), the error curves are below those for simple MC for all portfolios.

25 The variance reduction quotient (VR, the ratio of the variances of the estimations obtained using simple MC and the adaptive scheme, see Equation 7) varies between portfolios with different number of risk items and fractions of unknown coordinates, but generally increases with growing n_{hazard} . For example, for the portfolio with 10 risk items and 60% unknown coordinates, VR is about 6.2 at $n_{\text{hazard}} = 10^2$ and increases to 13.2 at $n_{\text{hazard}} = 10^3$. For the portfolio with 10 risk items and 100% unknown coordinates, $VR \approx 1.8$ at $n_{\text{hazard}} = 10^2$ and 2.2 at $n_{\text{hazard}} = 10^3$. For the portfolios with 100 risk items, the situation is similar. For 60% unknown coordinates, $VR \approx 2.4$ at $n_{\text{hazard}} = 10^3$ and 3.7 at $n_{\text{hazard}} = 10^4$. For 100% unknown coordinates, $VR \approx 1.7$ at $n_{\text{hazard}} = 10^3$ and 3.0 at $n_{\text{hazard}} = 10^4$.

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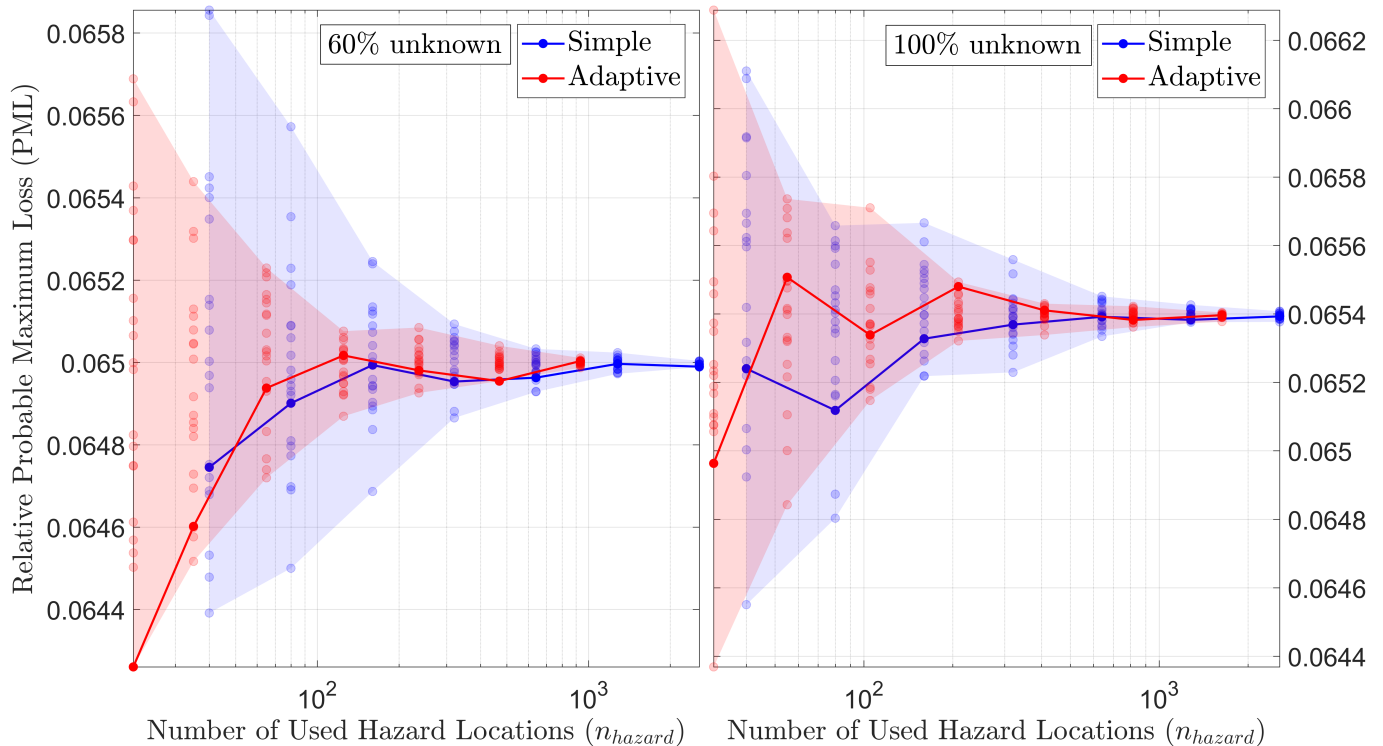


Figure 13. Convergence plots showing relative Probable Maximum Loss (PML) at a return period of 100 years against the number of used hazard locations n_{hazard} for portfolios of $n_r = 10$ risk items with 60% (left plot) and 100% (right plot) unknown coordinates using simple MC (shown in blue) as well as the adaptive scheme (shown in red). Semi-transparent circles depict $R = 20$ repeated simulations for each sample size, solid lines highlight one repetition. The transparently shaded background shows the entire range for each sampling scheme. The plots show that the adaptive scheme scatters less and converges faster to the same result as simple sampling.

The obtained variance reduction partially leads to a speedup of the computational runtime to reach a specific relative standard error level ε_{RSE} . Table 3 shows the speedup S of the scheme to reach relative standard error levels of $\varepsilon_{\text{RSE}} = 10^{-4}$ and $\varepsilon_{\text{RSE}} = 10^{-5}$ for the same portfolios. Depending on the portfolio, the scheme achieves a speedup between 8% and 35% to reach $\varepsilon_{\text{RSE}} = 10^{-4}$, and between between 6% and 37% to reach $\varepsilon_{\text{RSE}} = 10^{-5}$. Note that we obtained these speedup values using a

5 highly optimized seismic hazard and risk analysis framework. We suspect that the scheme can result in a significantly higher speedup for less optimized code, especially if the hazard simulation is not vectorized but contains a loop over locations.

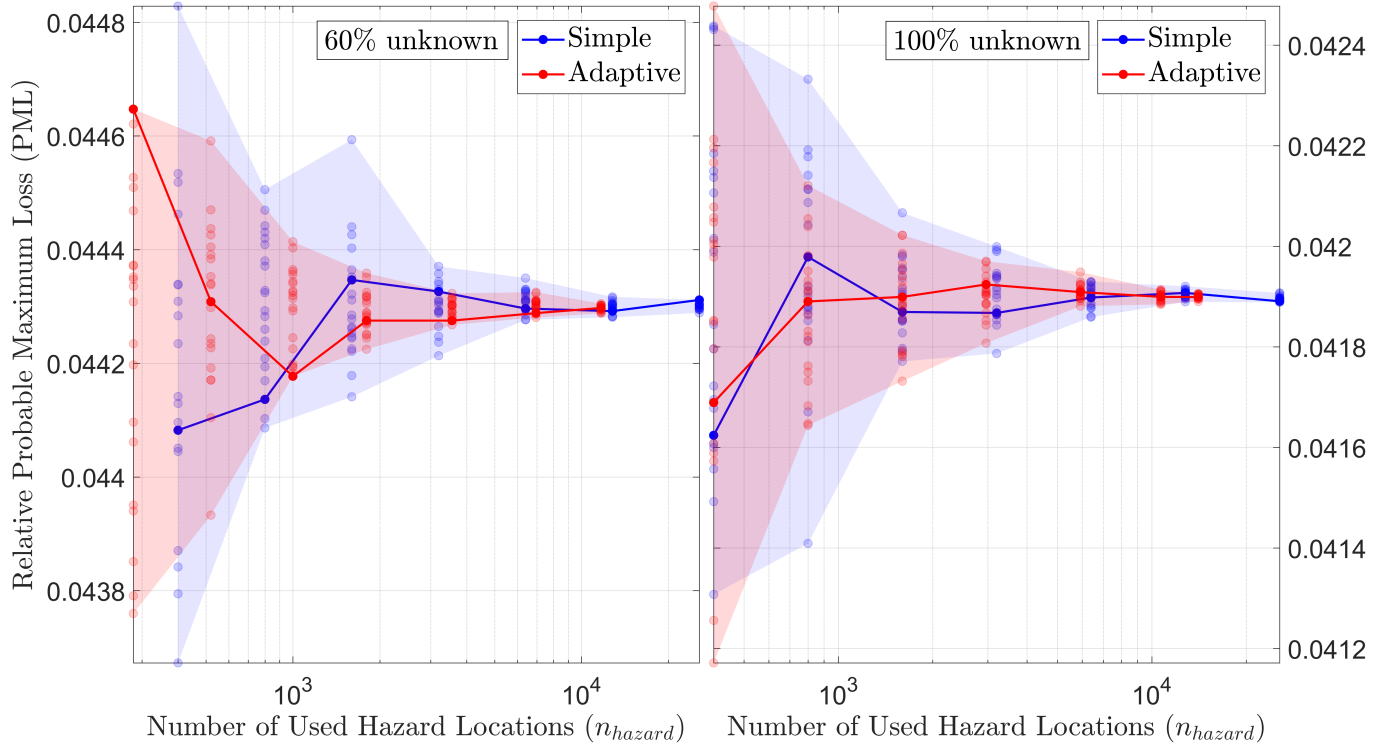


Figure 14. Convergence plots showing relative Probable Maximum Loss (PML) at a return period of 100 years against the number of used hazard locations n_{hazard} for portfolios of $n_r = 100$ risk items with 60% (left plot) and 100% (right plot) unknown coordinates using simple MC (shown in blue) as well as the adaptive scheme (shown in red). Semi-transparent circles depict $R = 20$ repeated simulations for each sample size, solid lines highlight one repetition. The transparently shaded background shows the entire range for each sampling scheme. The plots show that the adaptive scheme scatters less and converges faster to the same result as simple sampling.

6 Conclusions

Seismic risk assessment is associated with a large range of deep uncertainties. For example, the exact location of risks is often unknown due to geocoding issues of address information. In order to provide a holistic view of risk and to be able to communicate the effect of uncertainty effectively to decision makers, all model uncertainties need to be treated. Therefore, in this

- 5 paper we propose a novel adaptive sampling strategy to efficiently treat this location uncertainty using a seismic hazard and risk model for western Indonesia. The adaptive scheme considers three criteria to decide how often an unknown risk coordinate has to be sampled within a known administrative zone: (1) the loss rate variation within the zone, (2) the number of risks within the zone, and (3) the individual value of the risk. As the variation of hazard can vary quite strong not only between different administrative geographical zones, but also between different return periods, we use the spatial variation of loss rate which

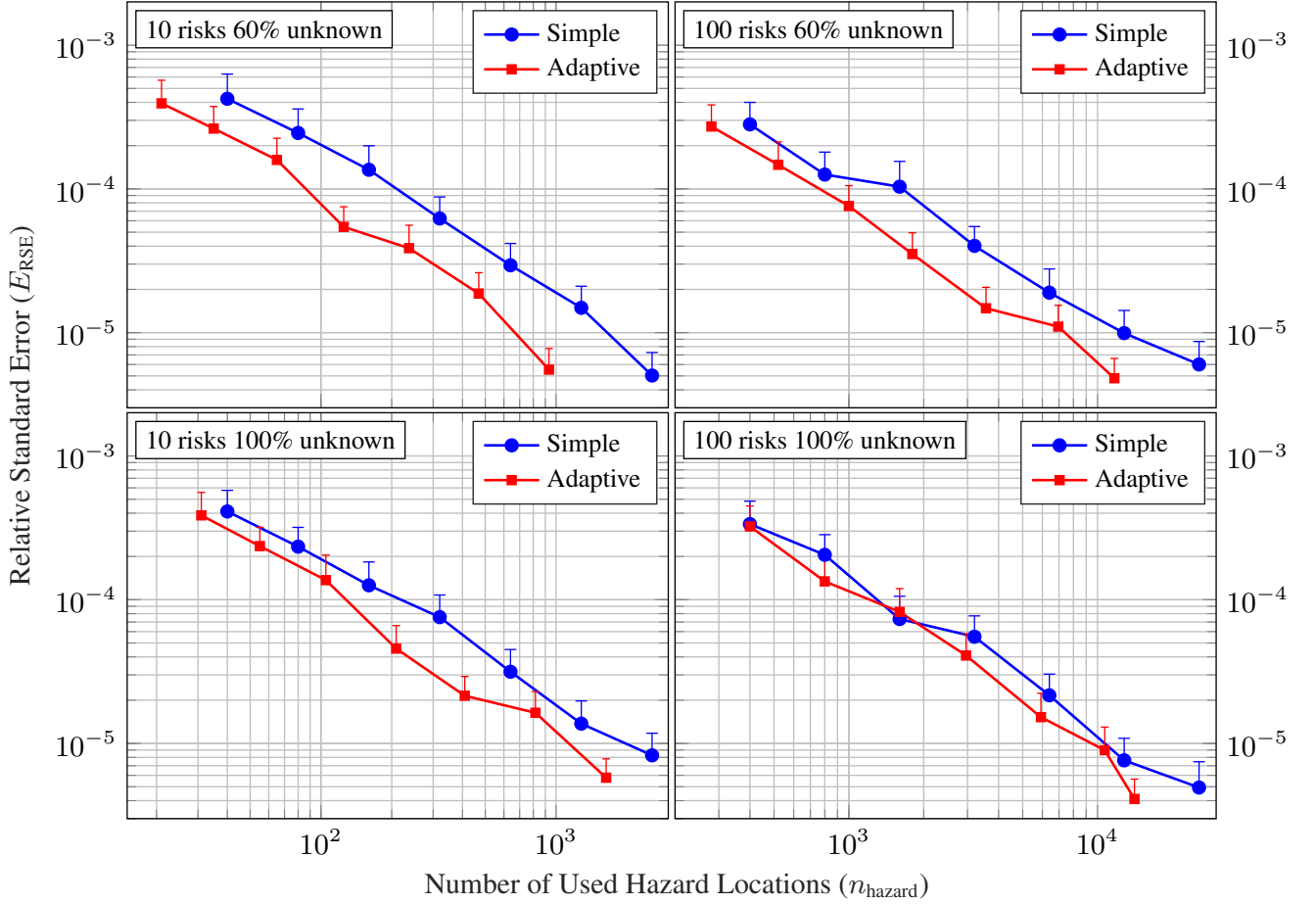


Figure 15. Logarithmic plot of relative standard errors E_{RSE} of Probable Maximum Loss (PML) at a return period of 100 years against the total number of used hazard locations n_{hazard} for different portfolios with $n_r = 10$ (left plots) and $n_r = 100$ (right plots) risk items and 60% (upper plots) and 100% (lower plots) unknown coordinates. Simple MC is shown in blue, the adaptive variance reduction scheme in red. All E_{RSE} have been obtained from $R = 20$ repeated simulations, vertical error bars depict upper 95% confidence intervals estimated using bootstrapping with 1000 resamples.

Table 3. Mean runtime speedup and standard errors ($S \pm E_{SE}$) of the hazard computation achieved by the adaptive location uncertainty sampling scheme in comparison to simple sampling to obtain relative standard error levels of $\varepsilon_{RSE} = 10^{-4}$ and $\varepsilon_{RSE} = 10^{-5}$, estimated from $R = 20$ repeated simulations. Depending on the portfolio and ε_{RSE} , the mean speedup ranges from 6% to 37%.

Portfolio	Speedup (S)	
	$\varepsilon_{RSE} = 10^{-4}$	$\varepsilon_{RSE} = 10^{-5}$
10 risk items, 60% unknown coordinates	1.24 ± 0.09	1.14 ± 0.04
10 risk items, 100% unknown coordinates	1.35 ± 0.06	1.37 ± 0.09
100 risk items, 60% unknown coordinates	1.08 ± 0.04	1.06 ± 0.03
100 risk items, 100% unknown coordinates	1.09 ± 0.03	1.08 ± 0.02

displays a similar pattern as the variation of hazard, but is independent of the return period. Furthermore, the total number of risks in the corresponding administrative zone, as well as the value (importance) of the risk with respect to the entire portfolio are considered by the adaptive scheme.

5 We investigated the performance of the scheme for a large range of sample sizes using different synthetic portfolios of different levels of unknown risk locations. We have found that the scheme successfully reduces the expected error, i.e. it reaches the same error levels as simple Monte Carlo with less samples of potential risk locations. This results in lower memory requirements and a moderate but appreciable runtime speedup to reach a desired level of reliability when computing loss frequency curves - a critical measure of risk in the insurance industry. The scheme helps to obtain a holistic view of risk including the associated uncertainties, and could also be applied to other natural perils, such as probabilistic wind and flood models. This should help to avoid blind trust in probabilistic risk assessment.

While the proposed scheme already successfully reduces the variance of loss frequency curve estimations, future improvements in the treatment of uncertainty in PSRA are conceivable and necessary. The effect of modeling assumptions and the often poor data quality needs to be investigated further. The computation might become yet more efficient by the application of variance reduction techniques to other uncertainties, for example in the ground motion and vulnerability models. Moreover, it would be essential to investigate the relative importance of location uncertainty in comparison to these other uncertainty types.

Code and data availability. The hazard model used for this work is based on the publicly available United States Geological Survey (USGS) South-East Asia seismic hazard model by Petersen et al. (2007), as described in Section 3.1. The seismic risk model and analysis software used for this work is proprietary and not publicly available.

Author contributions. CS implemented the location uncertainty sampling schema, analyzed the seismic hazard variation and sampling schema performance, and wrote the paper. MK conceptualized the sampling methodology, provided guidance for the analysis and for writing the paper, and revised the paper.



5 *Competing interests.* This work has been supported by a scholarship provided by Munich Re to the first author, who has worked on the project in the course of his doctoral studies at Ludwig Maximilian University of Munich. The second author works as senior seismic risk modeler at Munich Re and is a professor at Ludwig Maximilian University of Munich. Munich Re sells reinsurance products and services based on PSHA and PSRA and therefore has a high interest in modeling the inherent uncertainties within these methods, but did not influence the results of this study in any way.

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