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## risk in situations with insufficient data 2 Longxia Qian<sup>1</sup>, Ren Zhang<sup>1,2\*</sup>, Chengzu Bai<sup>1</sup>, Yangjun Wang<sup>1</sup> and Hongrui Wang<sup>3</sup> <sup>1</sup> Institute of Meteorology and Oceanography, National University of Defense Technology, Nanjing, China, 211101 3 <sup>2</sup> Collaborative Innovation Center on Forecast Meteorological Disaster Warning and Assessment, Nanjing 4 University of Information Science & Technology, Nanjing, China, 210044 <sup>3</sup> College of Water Sciences, Beijing Normal University, Key Laboratory for Water and Sediment Sciences, Ministry of Education, Beijing , China, 100875 5 Abstract. In drought years, it is important to have an estimate or prediction of the probability that a water shortage risk will occur to enable risk mitigation. This study 6 developed an improved logistic probability prediction model for water shortage risk in 7 8 situations when there is insufficient data. First, information flow was applied to select water shortage risk factors. Then, the logistic regression model was used to describe 9 10 the relation between water shortage risk and its factors, and an alternative method of parameter estimation (maximum entropy estimation) was proposed in situations 11 12 where insufficient data was available. Water shortage risk probabilities in Beijing 13 were predicted under different inflow scenarios by using the model. There were two main findings of the study. (1) The water shortage risk probability was predicted to be 14 very high in 2020, although this was not the case in some high inflow conditions. (2) 15

An improved logistic probability prediction model for water shortage

16 After using the transferred and reclaimed water, the water shortage risk probability

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- 17 declined under all inflow conditions (59.1% on average), but the water shortage risk
- 18 probability was still high in some low inflow conditions.

Keywords Information flow · Risk factors · Logistic regression model · Maximum entropy estimation · Insufficient data

19

#### 20 1 Introduction

21 Nowadays, water shortages have become a serious problem in many parts of the 22 world due to climate change, heightened demand of water and integrated urbanization, and there is a negative impact on the security and sustainable development of water 23 resources (Giacomelli et al., 2008; Weng et al., 2015; Christodoulou 2011; Wang et al. 24 25 2012; Yang et al. 2015 Qian et al. 2014; Li et al. 2014). Risk is a measure of the 26 probability and severity of adverse effects (Haimes, 2009). It is important to have an estimate or prediction of the probability that a water shortage risk will occur so that 27 effective measures for risk mitigation can be developed, particularly in the case of 28 precipitation deficits (drought). 29

Hashimoto et al. (1982) stated that risk can be described by the probability that a system is in an unsatisfactory state. How to predict or estimate risk probability is still an open issue with no definite solution. Mackenzie (2014) believed that an analyst should first develop a probability distribution over the range of consequences that fully describe the risk of an event. The simulation of probability distribution should be based on a large number of data (Bedford and Cooke, 2001; Giannikopoulou et al., 2015). Unfortunately, a full probabilistic assessment is generally not feasible, because





there is insufficient data to quantify the associated probabilities (Tidwell et al., 2005). 37 38 In some cases, frequency is often used as a substitute for probability in the risk assessment of water resources (Hashimoto et al., 1982; Rajagopalan et al., 2009; 39 Sandoval-Solis et al., 2011), while in other cases, interval-valued probabilities and 40 41 fuzzy probabilities have been proposed to elaborate the concept of an imprecise probability (Karimi and Hüllermeier, 2007). However, these approaches only consider 42 43 the probability of the hazard without consideration of the impact of risk factors. The 44 risk factors include characteristics of hazards and existing conditions of vulnerability 45 that could potentially harm exposed people, property, services and so on (UNISDR, 2009). There are many aspects of vulnerability arising from various physical, social, 46 economic, and environmental factors (Qian et al., 2016; Haimes, 2006; UNISDR, 47 48 2009). Therefore, it has been concluded that modeling risk probability requires a consideration of vulnerability (Haimes, 2006). Although increasing attention has been 49 given to vulnerability assessment (Villagrán, 2006; Plummer, 2012), there have been 50 few studies of the relation between risk probability and water resources vulnerability. 51 52 A water shortage can either occurs or not occur, and therefore water shortage risk is a binary categorical variable. According to statistical theory, a logistic regression 53 model is a nonlinear regression method of studying a binary categorical or 54 multi-categorical variable and its impact factors (Breslow, 1988). Therefore, a logistic 55 56 regression model can be used to describe the relation between water shortage risk and 57 its impact factors. However, the logistic regression model often requires a large

number of observed values of risk (i. e., samples that water shortage risk does or does





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not occur) and risk factors for parameter estimation. The maximum likelihood 59 60 estimation is often used for parameter estimation; a large number of observed values of riskand risk factors are required (Balakrishnan, 1992). However, the statistical data 61 about risk and its factors are insufficient in China. Therefore, the method of maximum 62 63 likelihood estimation is not applicable when the sample size is small. For this reason, we proposed an improved logistic regression model for predicting water shortage risk 64 65 probability when data is insufficient (i.e. proposing an alternative method of 66 parameter estimation for a logistic regression model when data is insufficient). 67 Moreover, the backward mode is often applied for the selection of sensitive risk factors, but it cannot unravel the cause-effect relation between the water shortage risk 68 and its factors. 69

70 The contributions of our paper are as follows. First, we used a logistic regression model to predict water shortage risk probability. Then, we introduced an information 71 flow (Liang, 2014) for the selection of sensitive risk factors. Compared with the 72 backward mode, it was very easy to determine whether there was a cause and effect 73 74 between the water shortage risk and its factors. Finally, we proposed an alternative method of parameter estimation (maximum entropy estimation) for a logistic 75 regression model in situations with a lack of data. The new method requires only a 76 few data, while maximum likelihood estimation requires a large amount of data. 77

The remainder of the paper is organized as follows. Section 2 presents the principles and structure of the logistic probability prediction model for water shortage risk. Section 3 presents the application of the model and the results of the research and





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81 Section 4 presents some conclusions and proposes future work.

## 82 2 Materials and methods

## 83 2.1 Study area

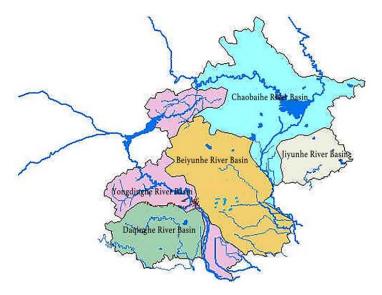
Beijing, China's capital, is located in the northwest of the North China Plain, and 84 85 consists of five river systems from the east to the west (Figure 1). The average annual precipitation is 585 mm. Precipitation in summer accounts for 70% of the total for the 86 87 whole year. Beijing, with a population of more than 20 million, is faced with a severe shortage of water resources. The amount of self-generated water resources is only 88 37.39×10<sup>8</sup> m<sup>3</sup>. The amount of water resources per capita is about 200 m<sup>3</sup>, which is 89 90 about one eighth of the value of water resources per capita for China and one thirtieth of the global value of water resources per capita. 91

The available surface water and groundwater is unable to meet the needs of the city's economic and social development. Some measures, such as the use of transferred and reclaimed water have been put in place to mitigate the water shortage. In 2014, through the South-to-North Water Diversion Project, water was channeled from the Danjiangkou Reservoir in central China's Hebei province to Beijing. Reclaimed water is also essential for Beijing and is mainly used for agricultural irrigation and toilet flushing.





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99 100

Figure 1. Distribution of river system of Beijing

## 101 2.2 Data collection

102 The data used in this paper were obtained from various sources. The inflow and 103 precipitation sequences from 1956 to 2012 were provided by Beijing Hydrological Station. The water demand for 2020 was based on the Beijing City National 104 Comprehensive Plan for Water Resources (Beijing Municipal Development and 105 Reform Commission and Beijing Municipal Bureau of Water Affairs, 2009). The 106 107 water supply sequence for 2020 in the inflow conditions of 1956-2012 was computed 108 by an analysis of the balance between water supply and water demand. The 109 population size and gross domestic product (GDP) from 1979 to 2012 were taken 110 from the Statistical Yearbook 2014 of Beijing City (Statistical Bureau of Beijing City, 2014). The total amount of water resources from 1979 to 2012 were provided by 111 Beijing Hydrological Station. The water use statistics and data regarding the treatment 112 of domestic sewage from 1979 to 2012 were taken from the Statistical Yearbook 2014 113





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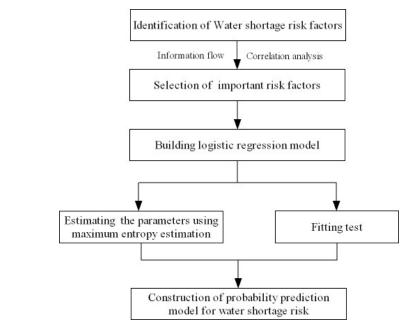
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114 of Beijing City (Statistical Bureau of Beijing City, 2014).

## 115 2.3 Model development

- 116 A flowchart showing the operation of the probability prediction model for water
- 117 shortage risk is given in Figure 2.



- 119 Figure 2. Flowchart showing the operation of the improved probability prediction model for
  - water shortage risk
- 121 As can be seen from Figure 2 the model consists of a determination of water
- shortage risk factors and the construction of a logistic probability prediction model.

## 123 2.3.1 Identification of water shortage risk factors

- 124 Water shortage risk factors include characteristics of hazards and existing conditions
- 125 of water resources vulnerability. Water resources vulnerability is referred to as the
- 126 manifestation of the inherent states (e.g., physical, social, and ecological) of the water
- 127 resources system that causes the system to be liable to a water shortage (Qian et al.,





128	2016). According to the study of Plummer et al. (2012), there are 50 different water
129	vulnerability assessment tools, and the water vulnerability indicators of these tools are
130	quite different. Therefore, a universal standard understanding of water resource
131	vulnerability indicators is difficult to develop. We established the indicators from
132	perspective of hydrological conditions, water resources, water supply and water use.
133	The risk factors are: precipitation (P), water resources per capita $(W_p)$ , water
134	consumption per GDP ( $W_c$ ), satisfactory rate of water demand ( $S_r$ ), and utilization
135	rate of water resources $(U_r)$ , proportion of industrial water use $(IW_p)$ , proportion of
136	agricultural water use $(AW_p)$ , proportion of domestic water use $(DW_p)$ and the
137	treatment rate of domestic sewage $(DS_r)$ . These indicators are defined as follows
138	(Qian et al., 2014):
139	$W_p = \frac{W}{N} \tag{1}$

where W is the total amount of water resources, and N is the population size. 140

141 
$$W_c = \frac{\text{the amount of water use}}{GDP}$$
(2)

142 
$$U_{r} = \frac{W_{ss} + W_{gs}}{W} = \frac{W_{as}}{W}$$
(3)

where  $W_{ss}$  is the surface water supply,  $W_{gs}$  is the groundwater supply, and W is the 143 total amount of water resources. 144

$$DS_r = \frac{DS_t}{DS}$$
(4)

where  $DS_t$  is the amount of sewage treated and DS is the total amount of sewage 146 discharged. 147

$$S_r = \frac{W_{as}}{W_{id}} \tag{5}$$







149 where  $W_{as}$  is the water supply, and  $W_{td}$  is the water demand.

$$IW_p = \frac{IW}{WU} \tag{6}$$

$$AW_p = \frac{AW}{WU} \tag{7}$$

$$DW_p = \frac{DW}{WU} \tag{8}$$

153 where IW is the industrial water use, AW is the agricultural water use, DW is the

154 domestic water use and *WU* is total water use.

## 155 2.3.2 Selection of important risk factors

The purpose of this section was to select some important factors that have a significant impact on water shortage risk. Liang (2014) reported that the cause and effect between two time series can be measured by the time rate of information flowing from one series to the other. Liang proposed a concise formula for causal analysis. The causality is measured by information flow. Therefore, we can use the information inflow to unravel the cause-effect relation between the risk factors and water shortage risk.

163 According to Liang (2014), for series  $X_1$  and  $X_2$ , the rate of information flowing 164 (units: nats per unit time) from the latter to the former is

165 
$$T_{2 \to 1} = \frac{C_{11}C_{12}C_{2,d1} - C_{12}{}^2C_{1,d1}}{C_{11}{}^2C_{22} - C_{11}C_{12}{}^2}$$
(9)

where  $C_{ij}$  is the sample covariance between  $X_i$  and  $X_j$ ,  $C_{i,d_j}$  is the covariance between  $X_i$  and  $X_j^{k}$ , and  $X_j^{k}$  is the difference approximation of  $\frac{dX_j}{dt}$  using the Euler

168 forward scheme.





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169 
$$\mathbf{X}_{j,n} = \frac{X_{j,n+k} - X_{j,n}}{k\Delta t}$$
(10)

According to Liang (2014), with  $k \ge 1$ , for a general time series k = 1 would be suitable. If  $T_{2\rightarrow 1} = 0$  or the absolute value of  $T_{2\rightarrow 1}$  is less than 0.01,  $X_2$  does not cause  $X_1$ , otherwise it is causal. A positive  $T_{2\rightarrow 1}$  means that  $X_2$  functions to make  $X_1$ more uncertain, while a negative value means that  $X_2$  tends to stabilize  $X_1$ . Liang (2015) proposed a method of normalizing the causality between time series and the range of value for  $T_{2\rightarrow 1}$  is 0 and 1.

## 176 2.3.3 Correlation analysis of selected risk factors

177 In theory, a probability prediction model requires variables to be mutually 178 independent. Therefore, it is necessary to perform a correlation analysis. Because all 179 of the factors are continuous variables, Pearson correlation coefficients are often 180 applied. If the absolute correlation coefficient is greater than 0.5, there is a significant 181 correlation between two factors.

# 182 2.4 Risk probability prediction model using maximum entropy 183 estimation

A logistic regression model is a nonlinear regression method of studying a binary categorical or multi-categorical variable and its impact factors. Because a water shortage either occurs or does not occur, water shortage risk belongs to a binary categorical variable. Therefore, we can use a logistic regression model to simulate the relation between water shortage risk and its factors. Suppose the risk factors are  $\{x_{ij} (i = 1, 2, L, n; j = 1, 2, L, m)\}$ , where  $x_{ij}$  denotes the value of the *jth* factor in





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190 the *ith* year. The risk sequence is  $\{y_i (i = 1, 2, L, n)\}$ , 191 where  $y_i = \begin{cases} 0, water shortage risk does not occur \\ 1, water shortagerisk occurs \end{cases}$ , and is the observed value of the ith

- 192 year.
- 193  $p_i = p(y_i = 1 | x_{ij} (j = 1, 2, L, m))$  is the conditional probability when  $y_i = 1$  under
- 194 the conditions of  $x_{ij}$  (i = 1, 2, L, n; j = 1, 2, L, m). The logistic regression model is

195 
$$p_i = \frac{1}{1 + e^{-(\alpha + \beta_1 x_{i1} + \beta_2 x_{i2} + K + \beta_m x_{im})}}$$
(11)

196 where  $\alpha, \beta_1, \beta_2, L$ ,  $\beta_m$  are the estimated parameters. The parameters are often 197 determined by a maximum likelihood estimation. The log likelihood equation of 198 computing  $\alpha, \beta_1, \beta_2, L$ ,  $\beta_m$  is as follows:

$$\begin{cases} \frac{\partial L}{\partial \alpha} = \sum_{i=1}^{n} \left[ y_{i} - \frac{\exp\left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right)}{1 + \exp\left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right)} \right] = 0 \\ \frac{\partial L}{\partial \beta_{j}} = \sum_{i=1}^{n} \left[ y_{i} - \frac{\exp\left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right)}{1 + \exp\left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right)} x_{ij} \right] = 0 \quad j = 1, 2, L, m \end{cases}$$
(12)

199

According to Eq. (12), a large number of observed values of risk  $(y_i (i = 1, 2, L, n))$  and its factors are required for parameter estimation. Unfortunately, the correlated samples between risk and its controlling factors are insufficient. It is therefore far better to estimate the parameters. In this case, the maximum likelihood estimation is not applicable for parameter estimation. An alternative approach for parameter estimation is therefore required.

206 Thus, we proposed a new parameter estimation method based on the maximum





- 207 entropy principle. The new method is named after maximum entropy estimation. The
- 208 new method does not require the observed values of risk, and it requires only some
- 209 observed values of the factors. Its principle is as follows.
- 210 For an observation, we can define its entropy to evaluate its degree of uncertainty.
- 211 According to Jones and Jones (2000), the entropy of the ith observation of water
- 212 shortage risk is

$$H(p_{i}) = -C\left[P_{i}\ln P_{i} + (1-P_{i})\ln(1-P_{i})\right]$$

$$= -C\left[P_{i}\ln\left(\frac{P_{i}}{1-P_{i}}\right) + \ln(1-P_{i})\right]$$

$$= -C\left\{\frac{\left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right)}{1 + \exp\left[-\left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right)\right]} - \ln\left(1 + \exp\left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right)\right)\right\}$$
(13)

where C is a positive value and  $p_i = p(y_i = 1 | x_{ij} (j = 1, 2, L, m))$  is the 214 conditional probability when the conditions 215 under of  $y_i$ =1  $x_{ii}$  (i = 1, 2, L, n; j = 1, 2, L, m). According to the maximum entropy principle, if the 216 217 values of  $H(P_i)$  reaches a maximum, the optimal parameters are obtained (Jones and Jones, 2000). The reasons for obtaining a solution based on the maximum entropy 218 principle are as follows. ① It conforms to the principle of entropy increase, which 219 states that the entropy of an isolated system tends to reach a maximum. 2 It accords 220 with the principle that the solution should be in line with the sample/data and the least 221 hypotheses must be constructed regarding the unknown parts when the data is 222 insufficient. ③ It fits the maximum multiplicity principle. The multiplicity of a state 223 refers to the number of possible ways in which a system can evolve to that state. The 224





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- 225 maximum multiplicity principle states that the greater the multiplicity of a state, the
- 226 larger the possibility that a system is in this state.

## 227 2.4.1 Parameter estimation

228 Based on the analysis above, an optimization model can be constructed as follows:

229 
$$\max H_{i} = -C \left\{ \frac{\left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right)}{1 + \exp\left[-\left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right)\right]} - \ln\left(1 + \exp\left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right)\right) \right\}$$
(14)

- 230 According to the extreme theory of multivariate function (Khuri 2003), we can
- 231 obtain

$$232 \quad \begin{cases} \frac{\partial H_{i}}{\partial \alpha} = \frac{\left\{1 + \exp\left[-\left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right)\right]\right\} + \left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right) \cdot \exp\left[-\left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right)\right] \\ \frac{\partial H_{i}}{\partial \alpha} = \frac{\left\{1 + \exp\left[-\left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right)\right]\right\}^{2}}{\left\{1 + \exp\left[-\left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right)\right]\right\}^{2}} \\ \frac{\partial H_{i}}{\partial \beta_{j}} = \frac{x_{ij} \cdot \left\{1 + \exp\left[-\left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right)\right]\right\} + x_{ij} \cdot \left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right) \cdot \exp\left[-\left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right)\right]}{\left\{1 + \exp\left[-\left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right)\right]\right\}^{2}} \\ \frac{\partial H_{i}}{\partial \beta_{j}} = \frac{x_{ij} \cdot \left\{1 + \exp\left[-\left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right)\right]\right\} + x_{ij} \cdot \left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right) \cdot \exp\left[-\left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right)\right]} \\ \frac{\partial H_{i}}{\partial \beta_{j}} = \frac{x_{ij} \cdot \left\{1 + \exp\left[-\left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right)\right]\right\} + x_{ij} \cdot \left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right) \cdot \exp\left[-\left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right)\right]} \\ \frac{\partial H_{i}}{\partial \beta_{j}} = \frac{x_{ij} \cdot \left\{1 + \exp\left[-\left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right)\right]\right\} + x_{ij} \cdot \left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right) \cdot \exp\left[-\left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right)\right]} \\ \frac{\partial H_{i}}{\partial \beta_{j}} = \frac{x_{ij} \cdot \left\{1 + \exp\left[-\left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right)\right\} + x_{ij} \cdot \left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right) \cdot \exp\left[-\left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right)\right]} \\ \frac{\partial H_{i}}{\partial \beta_{j}} = \frac{x_{ij} \cdot \left\{1 + \exp\left[-\left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right)\right\} + x_{ij} \cdot \left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right) - \exp\left[-\left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right)\right]} \\ \frac{\partial H_{i}}{\partial \beta_{j}} = \frac{x_{ij} \cdot \left\{1 + \exp\left[-\left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right)\right\} + x_{ij} \cdot \left\{1 + \exp\left[-\left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right)\right\right\} - \exp\left[-\left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right)\right] - \exp\left[-\left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right)\right]} \\ \frac{\partial H_{i}}{\partial \beta_{j}} = \frac{x_{ij} \cdot \left\{1 + \exp\left[-\left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right)\right\} - \exp\left[-\left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right)\right]} - \exp\left[-\left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right)\right] - \exp\left[-\left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right)\right] - \exp\left[-\left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right)\right]} - \exp\left[-\left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right)\right] - \exp\left[-\left(\alpha + \sum_{j=1}^{m} \beta_{j} x_{ij}\right)\right]$$

The optimal estimation  $\alpha, \beta_i (j = 1, 2, L, m)$  can be obtained by solving Eq. (15). Numerical approaches are often used to obtain an approximate solution of Eq. (15) rather than its exact solution. Therefore, we made use of the optimization function of Matlab to estimate the parameters, i.e., the fminsearch function. If there are n observations, there are  $n H_i (i = 1, 2, L, n)$ . It is impossible to find the parameters that make all the  $H_i (i = 1, 2, L, n)$  reach the maximum value. According to the maximum entropy principle, the greater the entropy is, the larger the uncertainty of an





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- observation is. Therefore, the maximum value of the sequences  $\{H_i, i = 1, 2, L_i, n\}$  was
- taken as the objective function of the optimization model.

## 242 2.4.2 Goodness-of-fit test

- 243 According to Brown (1982), a goodness-of-fit test should be made for evaluating the
- 244 fitting effect of the logistic regression model and its ability to identify water shortage
- risk. In this study, the Kolmogorov-Smirnov Test (K-S) test and Pearson  $\chi^2$  test are

246 used.

## 247 2.4.2.1 K-S test (t)

- A K-S test is often applied as a fitting test. It can be used to test the ability of the model to identify water shortage risk. The value of K-S is between 0 and 1; the greater the value is, the better the logistic model is. The idea is as follows.
- Let  $F_{n1}(x)$  be the cumulative probability distribution of the samples that do not encounter a water shortage.  $F_{n2}(x)$  is the cumulative probability distribution of the samples that encounter a water shortage. A two independent samples test is then applied to compare whether the empirical distribution functions of two samples are the same. The test is as follows:

256 
$$H_0: F_{n1}(x) = F_{n2}(x) \quad H_1: F_{n1}(x) \neq F_{n2}(x) \quad (16)$$

257 The value of K-S is:

258  $K - S = \max \left| F_{n1}(x) - F_{n2}(x) \right|$ (17)

When  $N \rightarrow \infty$ , the cumulative distribution curve and probability density curve of two samples can be obtained. The value of K-S is the maximum value of the cumulative distribution functions. When the value of K-S is greater than 0.35, the





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- 262 logistic regression model is applicable. The international classification standard of the
- 263 logistic model is shown in Table 1 (Brown, 1982).

264	
201	

Table 1. The international classification standard of the logistic model

K-S	The effect of the model
<0.2	Bad
0.2~0.4	General
0.4~0.5	Good
0.5~0.6	Better
0.6~0.75	Very good
0.75~1	Perfect

#### 265

## 266 **2.4.2.2** *Pearson* $\chi^2$ *test*

- 267 The test is as follows:
- 268  $H_0$ : the fitting is good  $H_1$ : the fitting is bad (18)

269 The expression of the  $\chi^2$  statistic is as follows.

270 
$$\chi^{2} = \sum_{j=1}^{l} \frac{\left(O_{j} - E_{j}\right)^{2}}{E_{j}}$$
(19)

where j = 1, 2, L, l, l is the number of covariant types,  $O_j$  is the observed frequency of the *jth* covariant type, and  $E_j$  is the predicted frequency of the *jth* covariant type. The degree of freedom is the difference between the number of covariant types and parameters.

#### 275 **3 Results and discussion**





- 276 In this section, a logistic probability prediction model for water shortage risk is
- 277 constructed and discussed, and the risk probability in 2020 in Beijing is predicted
- using the proposed model.

## 279 **3.1** Construction of the Logistic probability prediction model

- A sequence of risk factors were obtained for the period from 1979 to 2012, and were computed based on Eqs. (1)~(8). The risk sequence  $\{y_i (i = 1, 2, L, 34)\}$  from 1979 to 2012 was obtained as follows. According to Qian and Zhang et al. (2016), a water supply is deemed inadequate if the supply is less than the demand, leading to a water shortage in the water supply system.  $y_i = \begin{cases} 0, water shortage does not occur \\ 1, water shortage occurs \end{cases}$ .
- 285 Therefore, there are only 34-year data.

## 286 3.1.1 Determination of water resources vulnerability indicators

Based on the risk factors sequences from 1979 into 2012 (Table 2) and the method of normalized information inflow (Liang, 2015), the values of normalized information flow from the factors to risk are shown in Table 3. According to the normalized information flow results (Table 3), the value of the normalized information flow from  $AW_p$  to water shortage risk is only 0.0031, and it is very little. It was concluded that the  $AW_p$  does not result in a water shortage risk. Therefore,  $AW_p$  was removed as risk factors.

2	9	4

Table 2. The values of the risk factors and risk from 1979 to 2012

Year	<i>W</i> <sub>c</sub>			<i>P</i> (mm)	$DS_r(\%)$	$AW_p$	$DW_p$	$IW_p$	$S_r$	Risk
	(m <sup>3</sup> per CNY)	(m <sup>3</sup> per capita)								
1979	0.36	426.15	1.12	652.00	10.20	0.56	0.10	0.33	0.71	0
1980	0.36	287.52	1.94	387.30	9.40	0.63	0.10	0.27	0.41	1





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1981	0.35	261.10	2.00	433.50	10.80	0.66	0.09	0.25 0.40	1
1982	0.30	391.44	1.29	585.10	10.90	0.61	0.10	0.29 0.62	1
1983	0.26	365.26	1.37	465.50	10.20	0.66	0.10	0.24 0.58	1
1984	0.18	407.36	1.02	442.10	10.00	0.55	0.10	0.36 0.79	0
1985	0.12	387.36	0.83	611.20	10.00	0.32	0.14	0.54 0.96	0
1986	0.13	262.94	1.35	560.30	8.90	0.53	0.20	0.27 0.59	1
1987	0.09	369.25	0.80	662.60	7.70	0.31	0.23	0.45 1.00	0
1988	0.10	369.27	1.08	594.70	7.40	0.52	0.15	0.33 0.74	0
1989	0.10	200.47	2.07	479.50	6.60	0.55	0.14	0.31 0.39	1
1990	0.08	330.20	1.15	662.40	7.30	0.53	0.17	0.30 0.70	0
1991	0.07	386.56	0.99	662.70	6.60	0.54	0.18	0.28 0.80	0
1992	0.07	203.63	2.07	500.00	1.20	0.43	0.24	0.33 0.39	1
1993	0.05	176.89	2.30	424.30	3.10	0.45	0.21	0.34 0.35	1
1994	0.04	403.73	1.01	727.70	9.60	0.46	0.23	0.32 0.79	0
1995	0.03	242.51	1.48	608.90	19.40	0.43	0.26	0.31 0.54	1
1996	0.02	364.22	0.87	669.40	21.20	0.47	0.23	0.29 0.92	0
1997	0.02	179.44	1.81	419.00	22.00	0.45	0.28	0.28 0.44	1
1998	0.02	302.67	1.07	687.40	22.50	0.43	0.30	0.27 0.75	0
1999	0.02	113.11	2.93	384.70	25.00	0.44	0.30	0.25 0.27	1
2000	0.01	123.64	2.40	446.60	39.40	0.41	0.33	0.26 0.33	1
2001	0.01	138.62	2.03	462.00	42.00	0.45	0.32	0.24 0.39	1
2002	0.01	113.13	2.15	413.00	45.00	0.45	0.34	0.22 0.37	1
2003	0.01	126.34	1.84	453.00	50.10	0.39	0.38	0.23 0.41	1
2004	0.01	143.36	1.52	539.00	53.90	0.39	0.39	0.22 0.50	1
2005	0.00	150.85	1.27	468.00	62.40	0.38	0.42	0.20 0.54	1
2006	0.00	154.97	1.14	448.00	73.80	0.37	0.45	0.18 0.57	1
2007	0.00	145.74	1.13	499.00	76.20	0.36	0.48	0.17 0.55	1
2008	0.00	201.77	0.74	638.00	78.90	0.34	0.51	0.15 0.78	0
2009	0.00	124.22	1.08	448.00	80.29	0.34	0.52	0.15 0.49	1
2010	0.00	117.64	0.99	524.00	81.00	0.32	0.42	0.14 0.52	1
2011	0.00	132.81	0.88	552.00	81.70	0.30	0.43	0.14 0.60	1
2012	0.00	190.89	0.58	708.00	83.00	0.26	0.45	0.14 0.88	0

295

According to Liang (2014), a positive value of the information flow means that the factor makes water shortage risk more uncertain, while a negative value means that the indicator tends to stabilize water shortage risk. Therefore, all the factors tend to make water shortage risk more uncertain. Furthermore, the impact of P,  $W_p$ ,





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## 300 $W_c$ are very significant.

301

#### Table 3. The values of information flow from the factors to water shortage risk

Factors	Information flow
W <sub>c</sub>	0.3560
$W_p$	0.4823
$U_r$	0.3109
Р	0.1575
$DS_r$	0.2413
$IW_p$	0.1320
$AW_p$	0.0031
S <sub>r</sub>	0.1247
$DW_p$	0.1164

302

303 A correlation analysis was performed on the remaining factors. The values of the

304 Pearson correlation coefficients are shown in Table 4.

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		<u></u>
0	υ	2

Table 4. Pearson correlation coefficients for the relations between various factors

Pearson correlation	W	$W_p$	U <sub>r</sub>	n	$DS_r$	$DW_p$	ΠW	C
coefficients	$W_{c}$			Р	$DS_r$		$IW_p$	$S_r$
W <sub>c</sub>	1	0.603	0.047	-0.066	-0.559	0.354	-0.780	0.047
$W_p$	0.603	1	-0.455	0.571	-0.682	0.654	-0.753	0.696
$U_r$	0.047	-0.455	1	-0.723	-0.268	0.026	-0.157	-0.869
Р	0.066	0.571	-0.723	1	-0.100	0.219	-0.064	-0.820





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$DS_r$	-0.559	-0.682	-0.268	-0.100	1	-0.802	0.902	-0.087
$DW_p$	0.354	0.654	0.026	0.219	-0.802	1	-0.715	0.354
$IW_p$	-0.780	-0.753	-0.157	-0.064	0.920	-0.715	1	-0.013
S <sub>r</sub>	0.047	0.696	-0.869	0.820	-0.087	0.354	-0.013	1

Based on the results in Tables 3 and 4,  $AW_p$ ,  $S_r$ ,  $IW_p$ , and  $DW_p$  were

removed as risk factors. Therefore, the selected factors for logistic regression model were  $W_c$ ,  $W_p$ ,  $U_r$ , P and  $DS_r$ .

## 309 3.1.2 Construction of the logistic risk probability predication model

The data for the risk and selected factors  $(W_c, W_p, U_r, P \text{ and } DS_r)$  from 1979 to 2012 (Table 2) are used to construct the logistic risk predication probability model. Because there is only 34 samples, it is impossible to estimate the parameters by the maximum likelihood estimation. Substituting the sequences of  $W_c, W_p, U_r, P$  and  $DS_r$ from 1979 to 2012 (Table 2) into Eq. (14), the values of parameters obtained by maximum entropy estimation can be obtained. The estimated values for  $\alpha, \beta_1, \beta_2, L, \beta_5$  are 61.6386, 0.004, -0.1262, -12.4077, -0.012 and -29.0963.

Therefore, the logistic regression model based on the maximum entropyestimation is as follows:

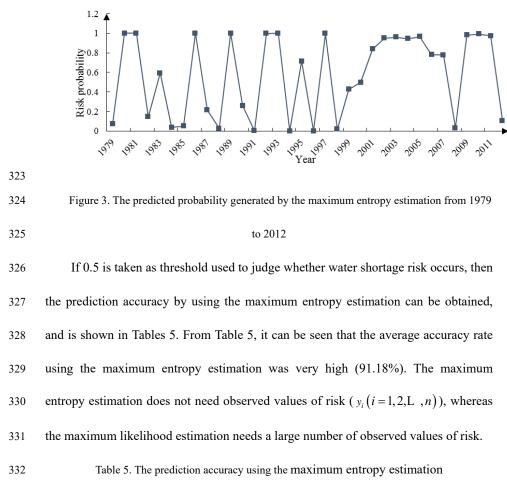
319 
$$Predicted \ probability = \frac{1}{1 + e^{-(61.6386 + 0.004W_c - 0.1262W_p - 12.4077U_r - 0.012P - 29.0963DS_r)}}$$
(20)

Substituting the sequences of  $W_c$ ,  $W_p$ ,  $U_r$ , P and  $DS_r$  from 1979 to 2012 into Eq. (20), the predicted probability values of water shortage risk by the maximum entropy estimation is shown in Fig. 3.









	The prediction is	The prediction is that	
	that risk occurs	no risk occurs	Accuracy rate
Risk actually occurs	19	3	86.36%
Risk actually does	0	12	100%
not occur			
The average			91.18%
accuracy rate			91.1070





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- 333 The K-S test and Pearson  $\chi^2$  test are performed and the results of the tests are
- 334 obtained. The value of K-S is 0.955 and according to Table 1, the logistic probability
- 335 prediction model was applicable. Moreover, the probability value was 0.000(i.e., less
- than 0.05), so the null hypothesis was rejected. Therefore, the ability of the logistic
- 337 regression model to predict water shortage is very strong.
- 338 Substituting the observed frequency and the predicted frequency into Eq. (19),
- the value of the  $\chi^2$  statistics was 2.333 (the number of covariant type was 8). Because
- 340 the number of parameters was 6, there were 2 degrees of freedom. The  $\chi^2_{0.1}(2)$  was
- 341 equal to 4.605 and was much greater than 2.333. Therefore, the null hypothesis was
- 342 accepted, i.e., the fitting of the model was very good. Based on the results of the K-S
- test and Pearson  $\chi^2$  test, it was concluded that the model was applicable.
- 344 3.2 Risk probability prediction in 2020 in Beijing

## 345 3.2.1 Risk probability prediction (without considering the use of 346 transferred and reclaimed water)

Because the inflow of 2020 is unknown, the inflow condition in 2020 was assumed to 347 348 be any annual inflow conditions from 1956 to 2012. In this section we predict the risk probability of 2020 under different inflow conditions from 1956 to 2012. The 349 sequences for risk factors  $(W_c, W_p, U_r, P \text{ and } DS_r)$  were obtained and computed as 350 follows. The precipitation in 2020 is assumed to be any annual precipitation from 351 352 1956 to 2012. First, an analysis of the balance between water supply and demand was performed and the sequences of water supply and demand under the inflow scenarios 353 of 1956-2012 were obtained (Qian et al., 2016). The GDP of 2020 was the sum of the 354





355	gross agricultural product, gross industrial product, and gross product of the third
356	industry (details of the third industry are shown in Appendix A), using information
357	taken from the literature, and was estimated to be 4711.852 billion CNY (Qian et al.,
358	2016). $N$ (the population size of 2020) was 24.43 million (Qian et al. 2016). The
359	total amount of water resources from 1956 to 2020 were considered to consist of
360	fifty-seven types of water resources in 2020. Substituting the total water resources
361	sequences and N of 2020 into Eq. (1), the sequence of $W_p$ could be computed.
362	Substituting the water demand sequences and GDP of 2020 into Eq. (2), the sequence
363	of $W_c$ could be computed. Substituting the sequence of the total water resources and
364	water supply for 2020 into Eq. (3), the sequence of $U_r$ could be obtained. The $DS_r$ of
365	2020 was about 90% (Beijing Municipal Development and Reform Commission and
366	Beijing Municipal Bureau of Water Affairs, 2009).

Substituting the sequences of  $W_c$ ,  $W_p$ ,  $U_r$ , P and  $DS_r$  into Eq. (20), the probability that a water shortage risk will occur in 2020 under the inflow scenarios of 1956–2012 was predicted, and is shown in Figure 4.

In Figure 4, the horizontal axis represents the inflow conditions of 1956–2012. Figure 4 shows that in 2020, the water shortage risk probability exceeded 0.95 under 33 different inflow conditions (accounting for 63.5% of all the inflow conditions) and exceeded 0.5 under 38 different inflow conditions (accounting for 73.1% of all the inflow conditions). In summary, there was a high probability of a water shortage risk in 2020, although the probability was very low in some high precipitation periods.





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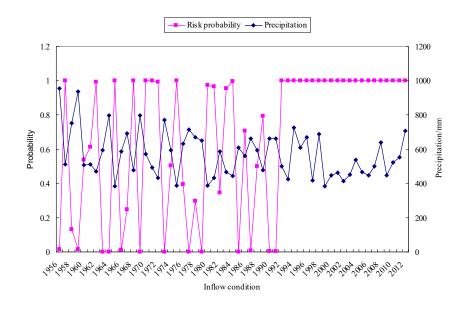


Figure 4. Risk probability under the inflow conditions of 1956–2012

## 378 3.2.2 Risk probability prediction after using transferred and reclaimed

#### 379 *water*

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377

According to Qian et al. (2016), 1.05 billion m<sup>3</sup> of water will have been transferred 380 to Beijing in 2020 and the amount of reclaimed water used may reach 1 billion m<sup>3</sup>. 381 382 After using transferred and reclaimed water, the total amount of water resources would increase,  $W_p$  and  $U_r$  would change and other indicators would remain 383 unchanged. Therefore, the sequences of  $W_p$  and  $U_r$  under the inflow scenarios of 384 385 1956-2012 had to be computed again. Substituting the sequences of  $W_c$ ,  $W_p$ ,  $U_r$ , P and DS<sub>r</sub> into Eq. (20), the water shortage risk probability in 2020 386 under the inflow scenarios of 1956-2012 (after using transferred and reclaimed 387 water) was predicted, and the results are shown in Figure 5. 388





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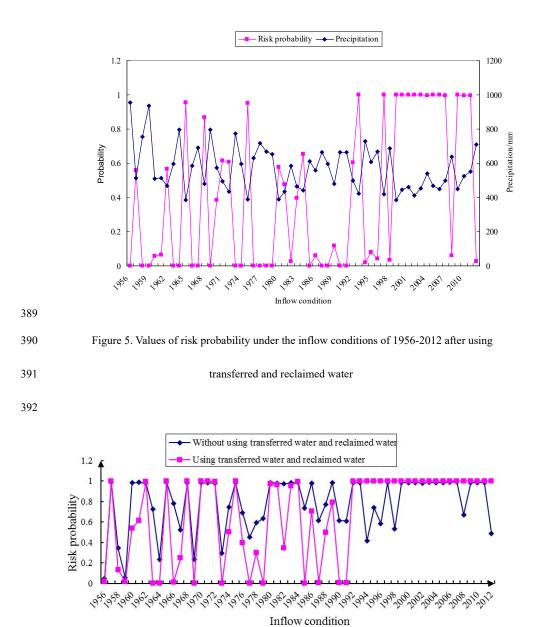




Figure 6. Comparison of risk probability before and after using transferred and reclaimed

water

395

396 From Figures 5 and 6, it was concluded that the water shortage risk probability

397 would decline under all inflow conditions (59.1% on average). However, the water





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- 398 shortage risk probability would still be high in some low inflow conditions. The risk
- 399 probability exceeded 0.5 under 24 different inflow conditions (accounting for 46.2%
- 400 of all inflow conditions). For example, the water shortage risk probability reached 1
- 401 under the inflow conditions of 1999–2008.

402 According to Qian et al. (2016), since 1999, Beijing has experienced drought in ten consecutive years. This has had a strong effect on the water resources of Beijing, 403 404 including a significant reduction in surface water and severe over-exploitation of 405 groundwater. This means that a water shortage may occur in 2020 under the inflow 406 conditions of 1999–2008 although some measures have been taken. Moreover, water resources vulnerability was still high in 2020 after using transferred and reclaimed 407 water (Qian et al., 2016). Therefore, we concluded that the water shortage risk 408 409 probability would still be high in 2020 after using transferred and reclaimed water, especially in the case of precipitation deficits. 410

## 411 4 Conclusions

This study developed an improved logistic probability prediction model for water
shortage risk in situations when there is insufficient data. The model consists of the
following steps:

(1) Information flow was used to select some important factors that were likely
to have a significant impact on water shortage risk. This could determine the
cause-effect relation between the water shortage risk and its factors.

418 (2) The logistic regression model was applied to describe the nonlinear relation
419 between water shortage risk and its factors. A new parameter estimation method based





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420 on the entropy principle, i.e. maximum entropy estimation, was proposed for

421 parameter estimation when insufficient data is available.

The results of the study were as follows. In 2020, the probability that a water 422 shortage risk will occur exceeded 0.95 under 33 different inflow conditions 423 424 (accounting for 63.5% of all inflow conditions) and exceeded 0.5 under 38 different inflow conditions (accounting for 73.1% of all inflow conditions). After using the 425 426 transferred and reclaimed water, the water shortage risk probability declined under all 427 inflow conditions (by 59.1% on average), but the water shortage risk probability was 428 still high for some low inflow conditions. Risk probability exceeded 0.5 under 24 429 different inflow conditions (accounting for 46.2% of all inflow conditions).

However, some problems still exist with regard to the maximum entropy estimation. Initial values of the parameters should be given for the optimization function, but the optimization function belongs to local optimization, which was very sensitive to the initial values. Therefore, we may obtain an unsatisfactory result if the initial values are not correct. How best to search for a global optimum is an important and difficult issue, and will be the focus of our further study.

436

## 437 Appendix A. Glossary used in this paper

438 1. Logistic regression model. It is nonlinear regression method of studying binary439 categorical or multi-categorical variable and its impact factors.

440 2. Maximum likelihood estimation. It is a method of parameter estimation in441 statistics.





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- 442 3. Maximum entropy estimation. We propose a new parameter estimation method
- 443 for a logistic regression model when insufficient data is available. We called this new
- 444 method maximum entropy estimation.
- 445 4. Backward. It is a method of selecting the variables for a logistic regression model.
- 446 The methods of selecting the variables for a logistic regression model include enter,
- 447 forward and backward.
- 448 5. Information flow. Information flow, proposed and named by Liang (2014), is a
- 449 method for unraveling the cause-effect relation between time series.
- 450 6. The extreme theory of multivariate function. This is a theory used for
- 451 calculating extreme values in advanced mathematics.
- 452 7. Two independent samples test. This is one type of Kolmogorov-Smirnov (K-S)
- 453 test. The K-S test includes a one-sample K-S test, two independent sample test, and a
- 454 test for several independent samples.
- 455 8. The third industry. In China, the third industry is also known as the service
- 456 industry, and includes the traffic and transportation industry, communication industry,
- 457 and commercial industry.

## 458 Appendix B. Abbreviations used in this paper

- 459 1. PLA People's Liberation Army of China.
- 460 2. GDP Gross domestic product
- 461 3. P. Precipitation.
- 462 4.  $W_p$ . Water resources per capita
- 463 5.  $W_c$  Water consumption per 10 thousand CNY GDP





- 464 6.  $S_r$  Satisfactory rate of water demand
- 465 7.  $U_r$  Utilization rate of water resources
- 466 8.  $IW_p$  Proportion of industrial water use
- 467 9.  $AW_n$  Proportion of agriculture water use
- 468 10.  $DW_p$  Proportion of domestic water use
- 469 11.  $DS_r$  Treatment rate of domestic sewage
- 470 12. CNY. The Chinese Yuan
- 471 13. K-S test. Kolmogorov-Smirnov Test
- 472
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