Re-evaluating safety risks of multifunctional dikes with a probabilistic risk framework

Richard Marijnissen[1], Matthijs Kok[2], Carolien Kroeze[1], Jantsje van Loon-Steensma[1,2]

[1]Water Systems and Global Change group, Wageningen University & Research, Wageningen, P.O. Box 47 6700 AA Wageningen, the Netherlands
[2]Hydraulic Engineering, Delft University of Technology, P.O. Box 5048, 2600 GA Delft, the Netherlands

Correspondence to: R.J.C. Marijnissen (richard.marijnissen@wur.nl)

Abstract. It is not uncommon for a flood defence to be combined with other societal uses as a multifunctional flood defence, from housing in urban areas to nature conservation in rural areas. The assessment of the safety of multifunctional flood defences is often done using conservative estimates. This study synthesises new probabilistic approaches to evaluate the safety of multifunctional flood defences employed in the Netherlands and explores the results of these approaches. In this paper a case representing a typical Dutch river dike combining a flood safety function with a nature and housing function is assessed by its probability of failure for multiple reinforcement strategies considering multiple relevant failure mechanisms. Results show how the conservative estimates of multifunctional flood defences lead to a systematic underestimation of the reliability of these dikes. Furthermore, in a probabilistic assessment uncertainties introduced by multifunctional elements affect the level of safety of the dike proportional to the reliability of the dike itself. Hence, dikes with higher protection levels are more suitable to be combined with potentially harmful uses for safety whereas dikes with low protection levels can benefit most from uses that contribute to safety.

1 Introduction

1.1 Evolution of the flood risk approach

With sea-level rising and an expected rise in extreme rainfall events due to climate change many regions in the world are faced with increasing flood-risk (Bouwer et al., 2010; Hirabayashi et al., 2013). Risk based approaches towards flood protection have been applied all over the world to inform decision makers on effective flood risk measures in spite of the large uncertainties (Jonkman et al., 2009; Kheradmand et al., 2018; Hall et al., 2003). Nevertheless, a better understanding of the fragility of flood protection measures, including innovative ones like natural flood defences (Temmerman et al., 2013), is instrumental to properly evaluate the flood risk in the future.

The Netherlands in particular is vulnerable to rising flood risks as about 60% of its area is prone to flooding from the sea or rivers (Kok et al., 2016). After the large flood of 1953 a design water level with an acceptably small exceedance probability was set based on an economic optimisation between investment costs and obtained risk reduction (Maris et al., 1961). Many studies have argued for a comprehensive probabilistic approach towards assessing the protection level provided by flood defences (Apel et al., 2006; Vrijling, 2001; Hall et al., 2003). As of January 2017 the water-level exceedance based national risk standards were replaced by a more complex full probabilistic approach to more effectively adapt to social and economic developments, and climate change (Kok et al., 2016). The Dutch Water Act is the first to require the implementation of these principles on a nation-wide scale. While these approaches were developed for dikes that serve flood protection only, in practise many dikes have features serving other functions than flood protection. It is yet unclear how such multifunctional aspects of a flood defence must be included in probabilistic safety assessments.

1.2 Multifunctional flood defences

Multifunctional flood defences (MFFDs) are engineered structures designed for the purpose of flood protection while simultaneously enabling other uses (Voorendt, 2017). Combining dikes with other functions is fairly common. Dikes can have roads on top, cables and/or pipelines running through them, structures on them, or are part of a historic landscape. In the Netherlands alone a majority of dike reinforcement projects already face the presence of one or more functions. Usually, enabling multiple functions requires strengthening of the dike beyond the minimal requirements for a traditional dike to account for uncertainties related to those functions (van Loon-Steensma and Vellinga, 2014). Multifunctional use of the flood defence does not need to decrease safety. For example, the development of green foreshores for flood protection services is an attractive option for future climate adaption (van Loon-Steensma et al., 2014) as such flood defences with green foreshores can reduce the risk of flooding by natural processes (van Loon-Steensma and Kok, 2016; van Loon-Steensma et al., 2016).

Flood defences can strengthen other values when functions are properly integrated (Lenders et al., 1999;van Loon-Steensma et al., 2014). In urban areas where space is limited there is continuous pressure to build on or integrate structures with the flood defence (Stalenberg, 2013). In rural areas nature-based solutions have gained interest, because they combine beneficial properties of natural systems for flood protection (e.g. wave attenuation by vegetation on foreshores) with conserving or developing important natural values (Temmerman et al., 2013; Pontee et al., 2016). In the Netherlands these developments favour the implementation of a multifunctional flood defence due to the limited space and government policy to consider other uses (e.g. the natural, historical, economical, etc.) (van Loon-Steensma and Vellinga, 2014).

Despite the large number of multifunctional dikes and incentives the tools to assess the safety of MFFDs have still been limited to rules of thumb and in-depth tailor-made studies. Unless the multifunctionality is a key feature assessments are often limited to proving multifunctional use does not significantly diminish the safety of the flood defence ignoring potential positive contributions to safety. Using such a conservative approach for dike assessments does ensure safe dikes from a flood risk perspective but may result in requiring larger and more expensive dikes.

1.3 Aim

There is a need for improved flood defences due to climate change (rising sea-levels, higher river discharges) and socio-economic developments. The number of people exposed to a high risk of flooding is expected to increase from 271 million in 2010 to 345 million in 2050 due to socio-economic growth alone (Jongman, Ward, & Aerts, 2012). By 2100, 168 million people per year will experience floods due to sea-level rise. By reinforcing dikes this number can already be reduced by a factor of 461 (Hinkel et al., 2013).While reinforcing dike systems, there is plenty of opportunity to enable multifunctional use of the flood defence.

However, the means to determine the safety provided by multifunctional flood defences remain limited to conservative approaches where multifunctional elements can only be shown to have no significant negative influence. Spurred by the threat of increasing flood risks by climate change and the revised legislation on flood standards in the Netherlands a new probabilistic framework to assess multifunctional flood defences is emerging that can be used for a wider context. The aim of this paper is to synthesize the new approaches to evaluate the safety of MFFDs employed in the Netherlands into a single coherent framework and evaluate how this new probabilistic approach towards MFFDs can change the assessed safety compared to the commonly applied conservative approach towards MFFDs .

To this end, first the existing official framework for assessing multifunctional dikes in the Netherlands is analysed and alternative frameworks in both scientific and grey literature for a probabilistic risk-based approach towards assessing MFFDs

as required by the new Water Act are explored. These are synthesized in an adapted framework (section.2). Secondly the methods used to calculate the probability of failure of several dikes are explained using the synthesized probabilistic approach and the traditional conservative approach (section 3) to show the differences in assessed safety level (section 4). Finally the implications and results are discussed (sections 5 and 6). By illustrating how a probabilistic approach towards multifunctional use can affect the assessed level of safety, new types of integrated solutions can be more fairly compared to monofunctional dikes both in the Netherlands and outside.

2.   Formulating a framework for MFFD assessment

2.1 Official Dutch guidelines for MFFD dike assessments and design

The methods to assess flood defences in compliance with the official Dutch safety standard are documented in official guidelines (Ministerie van Infrastructuur en Milieu, 2016; Ministerie van Verkeer en Waterstaat, 2007). The assessment can be performed on different levels: basic, detailed, and tailored. Basic assessments are a quick-scan with simple rules to approve flood defences with an insignificantly low failure probability. Detailed assessments consist of design formulas and models taken or adapted from Dutch design manuals and are commonly applied for (initial) designs and assessments. These are suitable for predicting the failure of dikes where general descriptions of dike failures can be applied. Such generalisations are not always suitable for MFFDs. Tailored assessments allow for the use of advanced models and experiments outside the guidelines to assess the probability of failure as accurately as possible. These assessments require a large amount of information for a specific location and are generally expensive to perform. The dike needs to pass at least one of these assessments to be considered safe and a proper design ensures the dike will pass the assessments for its entire designed lifespan.

In the official Dutch framework, multifunctional use of the dike is considered either directly as objects on the dike, by the materials used, or indirectly by the geometry of the dike. When only the geometry of the dike is affected or a different material is used (e.g. to integrate with the surrounding landscape) the official framework can still be applied (Slomp et al., 2016). However, if multifunctional use of the dike is facilitated by a Non-Water retaining Object (NWO), e.g. a house or pipeline, an additional assessment must be made for the NWO. For a few multifunctional elements a basic safety assessment is described in guidelines (structures, vegetation and traffic) (van Houwelingen, 2012; STOWA, 2000; TAW, 1994, 1985; STOWA, 2010; Ministerie van Infrastructuur en Milieu, 2016). Only for pipelines a more detailed assessment is available following the Eurocode (NEN, 2012) which ensures the pipeline itself has an acceptably small probability of failure. If a dike cannot be approved by a basic assessment and no suitable detailed assessment is available, a tailored assessment for that specific dike section with NWOs must be made.

The philosophy of a basic assessment is to rule out the possibility of the NWO affecting the dike significantly. Hence, the dike is considered safe only if the dike is dimensioned such that the zone of influence of the NWO does not extend into the minimum dike profile needed to meet the safety standard (see Fig. 1). As a result, in basic assessments the NWO is always assumed to be in its most critical state during design conditions (e.g. uprooting of a tree). This is the conservative approach to assess the influence of multifunctional elements on the safety because the actual probability of multifunctional elements being in a critical state is not considered. The ambition of the Dutch Water Act is to consider the actual probability of flooding which necessitates a risk-based approach to these elements.

2.2 Synthesizing a risk-based approach to MFFD design

The scientific basis for the risk-based framework adopted in the Netherlands was presented by Vrijling (2001). The risk of a flood is decomposed into a fault tree of failure mechanisms, each of which can be described with a mathematical limit state

function and evaluated probabilistically. Limit states are common for designing structures in Civil Engineering and define when a structure collapses resulting in damages and casualties (ultimate limit state) or can no longer perform its intended use (serviceability limit state) (Gulvanessian, 2009). Vrijling's approach of structuring the ultimate limit states of flood defences into a fault tree for risk analyses has been incorporated in many frameworks of flood defences, e.g. (Apel et al., 2004; van Gelder et al., 2009; Steenbergen et al., 2004; Vorogushyn et al., 2010), and has already been applied on a large scale to evaluate the Dutch flood defences (Jongejan & Maaskant, 2013). However, the framework was developed for monofunctional flood defences.

Studies on MFFDs specifically are available. However, the developed frameworks address different aspects like: to identify the degree of spatial and structural integration (Ellen et al., 2011b; Voorendt, 2017; Van Veelen et al., 2015), to identify costs and benefits (Anvarifar et al., 2013), to identify the threats and opportunities (Anvarifar et al., 2017), and to identify and evaluate flexibility for MFFDs (Anvarifar et al., 2016). Other studies on MFFDs tend to only focus on the effects of a specific multifunctional element or failure mechanism (Chen et al., 2017; Bomers et al., 2018; Zanetti et al., 2011). Only recently an assessment framework specifically for hybrid nature-based flood defences was put forward accounting for multiple failures by putting vegetation-specific equations directly into the assessment procedure (Vuik et al., 2018).

Pending an official framework practitioners in the Netherlands have used approaches to integrate multifunctional dike elements. One such approach was put forward for trees through the use of scenarios such as uprooting (van Houwelingen, 2012). An approach for assessing NWOs as indirect failure mechanisms with scenarios is being suggested in these cases (Knoeff, 2017). This approach will be explored further in the study.

Formulating a practical framework for the assessments of MFFDs is challenging due to the large variety of possible configurations and range of multifunctional elements. Multifunctional elements can be evaluated in different scenarios with simple or complex models in literature while preserving the established structure of the existing Dutch framework. Scenarios in this context are different possible states of a multifunctional element with a probability of occurrence in which the element affects the flood defence. By assessing each scenario and weighing the probability of failure in each scenario by the probability of the scenario, the probability of failure of the flood defence is calculated accounting for the uncertainty in the state of the multifunctional element. Therefore the steps for MFFD assessments in the Netherlands are synthesized as follows (also see Fig. 2):

- Step 1: Establish the required safety level of the dike segment
- Step 2: Assign a portion of the required safety level to unknown/unquantifiable risks
- Step 3: Distribute the remaining failure budget across the known failure mechanisms
- Step 4: Divide the dike in (close to) homogeneous sections
- Step 5: Determine a representative cross section and safety level taking variations along the dike section into account (length effect)
- Step 6 (Addition): Determine the scenarios, i.e. states in which the NWO affects the flood defence differently, assess the probability of these scenarios, and combine them based on their probability of occurrence.

The difference between a basic assessment and a probabilistic one is the addition of step 6. In a basic assessment, i.e. a detailed assessment without NWOs followed by a basic NWO assessment to exclude significant potential negative influences, first a dike cross-section would be designed with the criteria found in steps 1 to 5 and then adapted such that the influence of the intended NWO is outside the designed profile. In the risk-based probabilistic assessment the effects of NWOs are calculated directly with the scenarios in step 6 and combined with their probability of occurrence to arrive at a safe cross-section.

3 Application of the risk frameworks

3.1 Comparing the basic assessment with the expanded probabilistic assessment

To answer how a probabilistic approach towards multifunctional dikes can affect the evaluated safety compared to a monofunctional dike, a set of MFFDs is assessed with the new probabilistic approach and the traditional conservative approach (see Table 1 for the approaches). The calculations are performed on a cross-sectional level. The reliability of a cross-section is calculated for the most common dike failure mechanisms by probabilistically evaluating the models describing failure for the different scenarios. The failure probabilities per scenario and failure mechanism are combined to arrive at the probability of failure.

3.2 Failure mechanisms

To assess the risk of a flood it is important to know the mechanisms by which the flood defence could fail. Though many failure mechanisms are possible (Kok et al., 2016) the vast majority of documented dike failures worldwide are the result of three dominant mechanisms: overtopping (resulting in erosion of the inner slope), internal erosion (also referred to as piping), and inner slope stability (Danka and Zhang, 2015; Vorogushyn et al., 2009) .Within the Netherlands predominantly overtopping and slope instability have been the cause of dike breaches in the past (van Baars and van Kempen, 2009). For this study the probability of a flood is calculated by considering the failure mechanisms overtopping, piping, and macro stability (see Table 2). Whether the flood defence fails by a failure mechanism is expressed in an equation called a limit state function:

$$Z = R - S \tag{3.1}$$

where Z<0 denotes failure, R is the resistance to failure, and S is the soliciting load.

For overtopping and overflow the load (S) is the amount water flowing over the dike while the resistance (R) is the capacity of the crest and inner slope to resist the flow of water without eroding. For piping the method of Sellmeijer et al. (2011) is used to calculate the stability of the sand particles in the subsoil under a pore water pressure gradient. It is expressed as a critical head difference (R) that cannot be exceeded by the head difference across the dike (S). Macro stability is calculated within the program D-Geo Stability (Brinkman and Nuttall, 2018) with the stability method by Van (2001) and ground water model by TAW (2004). The method by Van (2001), like the Bishop (1955) method, calculates the sum of the driving moments (S) and the total resisting moment (R) along the slip plane. However, it also accounts for uplift forces on the interface of aquifers present beneath most dikes. The resulting limit states are:

$$Z_{\text{overflow \& overtopping}} = q_{\text{c}} - q \tag{3.2}$$

$$Z_{\text{piping}} = H_{\text{c}} - H \tag{3.3}$$

$$Z_{\text{macro stability}} = \Sigma M_{\text{R}} - \Sigma M_{\text{S}} \tag{3.4}$$

Here q_c is the empirically determined critical overtopping discharge, q is the overtopping discharge calculated according the methods of van der Meer et al. (2016) and TAW (2002), H_c is the critical hydraulic head according to Sellmeijer et al. (2011), H is the difference in water level in front and behind the dike, ΣM_{S} is the sum of the active moments in the critical slip plane, and ΣM_{R} is the sum of resisting moment in the critical slip plane.

3.3 Probabilistic procedure

Multiple procedures are available for calculating the reliability of a flood defence. A fully probabilistic procedure like Monte Carlo relies on evaluating the limit state function for many variations of the random variables and determines the failure probability as the number of failures over the total number of samples. Meanwhile, a semi-probabilistic approach evaluates the limit state function once and captures uncertainties with (partial) safety factors to determine (non)failure. A probabilistic procedure like the first order reliability method (FORM) iteratively converges to an approximation of the probability of failure

(Hasofer and Lind, 1974). This option was chosen as it does not require millions of evaluations of the limit state function to assess the small failure probabilities required for dikes while still retaining the probabilistic distribution of the variables otherwise lost in a semi-probabilistic approach.

5   While the FORM procedure can approximate the failure probability of a single limit state function of a single failure mechanism, a combination of failure mechanisms is more complex to evaluate. When the only dependence between failure mechanisms is assumed to be the water level, each failure mechanism becomes an independent event for each discrete water level such that the probability of failure of the system is:

$$P_{f,sys|h} = P_{sys}(f|h) = 1 - \prod_{i=1}^{n}\left(1 - P_{f,i|h}\right) \qquad (3.5)$$

Where $P_{f,i|h}$ is the probability of failure given water level h for the ith failure mechanism and $P_{f,sys|h}$ is the probability of failure
10 given water level h. Repeating this calculation across all relevant water levels results in the fragility curve of the system to the water level (Bachmann et al., 2013). The failure probability of the system is computed by integrating the fragility curve of the system ($F_R(h)$) over the probability density function (PDF) of the water level ($f_h(h)$):

$$P_{f,sys} = \int_{h=-\infty}^{h=\infty} f_h(h) * F_R(h) \, dh \qquad (3.6)$$

Eq. 3.6 is discretised to:

$$P_{f,sys} = \sum_{j=1}^{m} P(h_j) * P_{sys}(f|h_j) \qquad (3.7)$$

Low failure probabilities can more easily be expressed in terms of the reliability index which is defined as:

$$\beta = -\Phi^{-1}(P_f) \qquad (3.8)$$

15 Where Φ^{-1} is the inverse standard normal cumulative distribution function.

The probabilistic procedure described above has been utilised before successfully by Lendering et al. (2018) and Bischiniotis et al. (2018) to compute the reliability of canal levees and a cost-optimal river dike respectively. An overview of the entire process as applied in this study is schematised in Fig. 3.

20 **3.4 Case-study**

3.4.1 Setting and cross sections

The multifunctional dike for the case-study is situated in a riverine area, with nature on the floodplain side and a building on the landward side. To test how a risk approach can affect the calculated level of safety 8 cross-sections of multifunctional dike profiles (Fig. 4) are evaluated with three methods: a conservative, a probabilistic and a monofunctional approach (see Sect.
25 3.1).

If a dike does not meet the set safety standards a reinforcement by adapting the profile, among other options, is explored. Each profile in this study represents a common reinforcement strategy. Broadening the dike by widening the crest or expanding the slope reduces the risk of a piping failure by increasing the piping length by a few meters. Furthermore broadening inwards and
30 making the inner slope shallower makes the inner slope more stable. A berm also improves the stability of the inner slope. Finally heightening the dike decreases the risk of overtopping waves and overflow during high water. The final reinforcement strategy is a combination of heightening and decreasing the steepness of the inner slope.

Each multifunctional element can compromise a section of the dike resulting in failure. For the purpose of this study the multifunctional elements have been simplified so these can be incorporated directly in variables of the limit state functions or dike geometry (see Sect. 3.4.2). When broadening the dike on the flood plain or making a shallow outer slope (see profiles 1 and 5 in Fig. 4) the hinterland remains unaffected by the dike itself, while in the other alternatives the building becomes part of the flood defence. By reviewing the options the effect of the multifunctional elements on the safety after the reinforcements is evaluated in each framework.

3.4.2 Schematisation of multifunctional elements

Effects of multifunctional elements on dike failure are incorporated through scenarios based on the fact-sheet by Knoeff (2017). For each mechanism scenarios are defined in which the element (e.g. tree, structure, pipeline, etc.) affects the failure mechanisms. The probability of failure can then be calculated for each scenario. The total probability of failure for the specific mechanism is computed by weighing the probability of failure of each scenario with the probability of the scenario.

A natural flood plain can add ecological, landscape and recreational values to the flood protection system. However, elements like trees can penetrate the clay top soil resulting in cavities within the clay when the tree dies (Zanetti et al., 2011). Following a conservative estimation for the uprooting of trees by TAW (1994) a 2% annual probability of a cavity within the flood plain is assumed. If a cavity is present the effective length for piping is reduced to the distance between the dike's inner toe and the location of the disturbance. The trees on the flood plain do not affect the inner slope stability nor is the tree density in the case-study high enough to expect an influence on overtopping by wave dampening properties of trees.

A building on or close to the dike affects multiple failure mechanisms. The weight of the structure is transferred to the underlying soil where the load increases both friction with the subsoil, increasing slope stability, and lateral stress on the soil, decreasing slope stability. On the slope itself the structure affects the overtopping mechanism through the inner slope cover that prevents erosion. When a structure is present it acts as a discontinuity in the outer grass cover such that water can more easily erode soil during overtopping and is reflected in a lower critical overtopping rate. When the structure is absent the space occupied by it in the profile is assumed to be empty. Furthermore there is no grass cover but instead loose bare soil with practically no overtopping resistance (see Table 3). In the case-study the effect of the structure on piping is insignificant as it: does not penetrate the aquifer, and pipes can still develop along the outside of the structure rather than directly beneath it.

The structure in the case-study is located 3 m behind the inner dike toe. The structure is taken to be 15 m wide, exerts a weight of 17 kN/m and is embedded 1 m into the soil on a shallow foundation without additional geotechnical measures like piles or sheet pile walls. The horizontal position of the structure remains fixed for each reinforcement strategy while vertically the landward end of the structure is always embedded only 1 m in the soil when the dike is expanded inwards. The probability the structure is absent during a high water event is estimated to be 1%. This probability is based on the percentage of houses demolished in the Netherlands annually which has varied between 0.13 and 0.23% per year (van der Flier and Thomsen, 2006) rather than the probability of structural failure of the house. The structure in its demolished state leaves a discontinuity in the dike profile, exerts no weight on the dike and exposes bare clay on the dike slope while leaving the remaining dike intact.

4. Results

The results are presented in Fig. 5. As expected the conservative approach consistently yields the highest probabilities of failure for the assessed dikes. Both the probabilistic assessment of the additional multifunctional uses and the monofunctional assessment yield a lower probability of failure for each dike profile (Fig. 5).

4.1 Slope stability

The weight of the structure can improve the slope stability of the dike in the probabilistic assessment as shown in the assessment of profile 1 with the structure only. The changes in annual failure probabilities are solely due to the presence/absence of weight increasing friction in the passive zone of the slip circle. In the conservative approach the weight of structure is always ignored leading to a noticeably higher failure probability. This effect is most noticeable in profile 2 with only a structure. The reliability increases by a factor 10 in the probabilistic assessment compared to a monofunctional dike due to a favourable position of the structure in the critical slip circle (see Fig. 6). In contrast to profile 2, in profile 4 the position of the structure is detrimental to stability where a monofunctional dike has a three times larger reliability ($1.6*10^{-8}$ versus $5.02*10^{-8}$) for the probabilistically assessed dike with a structure. Both the structure and berm add weight, but the structure has a risk of being absent while the risk of a monofunctional berm being absent is negligible. This makes the berm a safer option. Nevertheless this effect on the reliability of profile 4 was insignificant compared to the overall failure probability which was dominated by piping and overtopping.

4.2 Overtopping

The presence/absence of the structure had a minor impact on overtopping as can be seen in Fig. 6. This is mainly the result of the relatively high predictability of the mechanism itself (reflected by the steepness of the fragility curve) rather than the direct influence of the structure on the mechanism (reflected by the shift of the fragility curve) or additional uncertainty introduced by the structure (reflected by a decreasing steepness of the fragility curve). Because overtopping has a steep fragility curve, the influence of the structure only affects a limited range of water levels and thus the net effect of the structure on the safety of the dike is limited.

4.3 Piping

Including uncertainty because of unmanaged vegetation on the flood plain has a large effect on piping failure which was ignored in the assessments with the structure. Because the flood plain in the case-study is wide, a scenario with a cavity close to the dike results in a major reduction of the piping length in the probabilistic assessment. Fig. 6 shows where large difference between the fragility curves of critical state and the ordinary state. The presence of trees on the floodplain on piping is even more pronounced in the conservative approach because the entire width of the flood plain is automatically excluded in the assessment. This leads to a different assessment in the need for piping specific reinforcement measures in, particular for the conservative assessment. Due to the dominance of the piping failure mechanism in a conservative schematisation there is an increasing discrepancy between the conservative assessment and the other assessments.

4.4 Assessments

Finally the difference in probability of failure between a monofunctional dike and a multifunctional dike depends on the reliability of the monofunctional dike itself. Unless there are large differences in the schematisation of a failure mechanism (as was discussed for piping), differences in failure probabilities between assessments scale roughly by the same order of magnitude as the decrease in failure probability after a reinforcement (Fig. 5 note the log-scale for the probability of failure). However, the relative differences become more pronounced leading to proportionally higher failure probabilities in a conservative assessment compared to a probabilistic assessment.

5. Discussion

The results show a large difference between the reliability assessed between the conservative approach and the probabilistic approach. A prevailing view against multifunctional use of flood defences is that these require larger dimensions to meet the same safety standard as a traditional dike (Ellen et al., 2011a; van Loon-Steensma and Vellinga, 2014). However, as the case-study above illustrated this perception only holds true for a conservative approach that omits multifunctional elements from the assessment. With a more probabilistic approach towards multifunctional elements their perceived negative influence was significantly smaller or could even result in a net positive influence. Positive contributions of multifunctional elements under likely conditions can be included as well as the likelihood of the multifunctional elements affecting the flood defence negatively.

A drawback of the probabilistic approach is that it needs specific information about the failures and states of multifunctional elements before an assessment can be conducted. For example, erosion around or over discontinuities during overtopping (possibly due the presence of multifunctional elements like a road) is highly variable and hard to capture in a generic limit-state function even with well-calibrated models (Hoffmans et al., 2009; Bomers et al., 2018). Depending on the sensitivity of the failure probability to these processes assumptions on effects and statistical distributions would need to be increasingly conservative to guarantee the safety level is met. However, new information on the interaction between multifunctional uses and failure mechanisms is becoming increasingly available through ongoing research (Aguilar-López et al., 2018; Vuik et al., 2018). Furthermore, new techniques are being employed to continuously monitor the dikes in detail (Hanssen and van Leijen, 2008; Herle et al., 2016) while advances in remote sensing allow for closer monitoring of the state of foreshores (Niedermeier et al., 2005; Friess et al., 2012). As a result, a probabilistic approach towards multifunctional elements can capitalise on these advances by updating the previously assumed risks in assessments with observations of the actual performance of MFFDs over time.

Aside from the effects of multifunctional elements themselves, other uncertainties influence how much multifunctional use of the flood defence can affect the level of safety. For piping Aguilar-López et al. (2015) demonstrated that reducing the uncertainty in the seepage properties of the soil of a multifunctional dike the probability of a piping failure is already significantly reduced. Lanzafame (2017) concluded variability introduced by vegetation has only a small effect on the probability of a slope failure due to larger uncertainties in strength and seepage of the soil. In contrast a relatively small disturbance by burrowing animals in a fragile dike has resulted in a breach under conditions it had previously survived (Orlandini et al., 2015). The observation that the dike's own reliability influences the degree to which multifunctional use can affect the probability of failure of the dike was also found in this study. As the reliability of the dike itself increases, the influence of a multifunctional element on the level of safety decreases as the added variability of the multifunctional element becomes smaller compared to the uncertainties in other parameters the dike was already designed for. This effect of dike reliability on the influence of multifunctional element has implications. An increase in failure probability due to multifunctional element is likely to be over-estimated in a traditional assessment for dikes with a high protection level while similarly for these dikes also only a limited decrease in failure probability can be expected from beneficial multifunctional elements. Conversely, dikes with a low protection level are influenced more by both beneficial and detrimental effects of multifunctional use of the flood defence.

This study only looked at the effects of multifunctional use on flood protection. However, multifunctional use comes with its own set of requirements that must be taken into account. For example structures need to comply with building codes, flood protection measures in nature reserves can be subject to environmental protection regulations while to preserve landscape

values substantial dike heightening may be unacceptable. How much such additional non-flood protection requirements influence the design of dikes need to be researched for a successful implementation of MFFDs.

This study investigated the assessments of multifunctional flood defences for the current situation. In the design of these defences, however, future conditions, like for example climate change or societal trends, need to be taken into account. Scenarios for future sea-level rise in the coming century vary between 0.23 and 0.98 m (IPCC, 2013). Incorporating beneficial multifunctional uses of flood defences, either natural like marshes or man-made like structures, can become an asset to achieve the levels of flood protection needed in the future.

6. Conclusion

This study analysed how a full probabilistic approach towards multifunctional flood defences can change the assessed safety compared to the commonly applied conservative approach where multifunctional use of the flood defence can only be shown to have no significant negative influence. Although probabilistic assessments have been used before, the new regulations of the Water Act in the Netherlands necessitate a full probabilistic assessment of flood defences. Therefore a probabilistic framework incorporating multifunctional elements probabilistically was developed. The overall conclusion is that application of a probabilistic approach towards multifunctional use of the flood defence will lead to a lower assessed risk of flooding compared to conservative assessments because: 1) positive contributions of multifunctional elements to safety can be included, even when in a critical state there is a negative contribution to safety and 2) the risk of multifunctional elements being in such a critical state is made explicit. Another important aspect is that effects of multifunctional use on safety become smaller as the reliability of the dike increases. Therefore monofunctional dikes with already a high reliability are more suitable to be combined with multifunctional uses detrimental to safety whereas dikes with a low reliability can benefit more from multifunctional uses that contribute to safety.

Based on the results we recommend that a probabilistic framework is further developed and implemented for including multifunctional elements into dike assessments. While many knowledge gaps are still present in quantifying the effects of multifunctional use of flood defences, incorporating scenarios in which a multifunctional element can harm or help flood protection can already provide insights in synergies that can be exploited or dangers that can be mitigated. These scenarios and associated probabilities will need to rely on expert judgment. However, it is expected that with the growing number of methods to monitor dike performance and ongoing studies in dike failures these gaps can be filled in the future. To this end further research is required on the proper scenarios and their associated probabilities that can be used to improve future assessments of multifunctional dikes. Additionally, more research is needed to assess how multifunctional elements influence the safety of dikes over longer periods especially in relation to the large uncertainties involved in climate change. A real-world case-study for design should be used to explore how these aspects can be incorporated in practise.

7. Author contributions

The study and methodology were conceived by RM, JvL and MK. RM carried out the analyses, produced the results and wrote the manuscript under the supervision of JvL, MK and CK. The results were discussed and reviewed among all authors.

8. Competing interests

The authors declare that they have no conflict of interest.

9. Acknowledgements

This work is part of the Perspectief research programme All-Risk with project number P15-21, which is financed by NWO Domain Applied and Engineering Sciences. We thank Wim Kanning for his advice on the probabilistic stability calculations. Furthermore we would like to thank Harry Schelfhout and Reindert Stellingwerf for the discussions on the current practices for multifunctional dikes. Finally we thank the two anonymous reviewers for their helpful comments.

Appendix

A: Case-study parameters

The dike geometry of the base case is captured by the variables in Table A1.

The soil was divided into 3 layers: the dike core, the blanket layer and the aquifer. Representative values for the soil layers were taken from known soil types in the Dutch riverine area (Table A2, Table A3 and Table A4).

Hydraulic load parameters are given in Table A5. Representative water and wind characteristics were estimated from the
10   hydraulic loads database of the upper Rhine area in the Netherlands which is available as part of the WBI software. For simplification the wind direction is only considered in the direction perpendicular to the dike.

B: Overflow and overtopping limit state function

Overflow is calculated directly from the water level (h) and crest height (z_{crest}) by the formula for a broad crested weir:

$$q_{\text{overflow}} = \sqrt{2g} * \frac{2\sqrt{3}}{9}(h - z_{\text{crest}})^{\frac{3}{2}} \tag{B1}$$

To calculate the overtopping discharge first the significant wave height (H_s) and period (T_s) perpendicular to the dike are
15   estimated from the water depth (h), fetch length (F), and wind speed (u_{wind}) with the equations of Bretschneider as presented by Holthuijsen (1980):

$$F_x = \frac{gF}{u_{\text{wind}}^2} \tag{B2}$$

$$h_x = \frac{gh}{u_{\text{wind}}^2} \tag{B3}$$

$$p_1 = \tanh(0.53 * h_x^{0.75}) \tag{B4}$$

$$p_2 = \tanh(0.833 * h_x^{0.375}) \tag{B5}$$

$$H_s = 0.283 * \frac{u_{wind}^2}{g} * p_1 * \tanh\left(0.0125 * \frac{F_x^{0.42}}{p_1}\right) * m_{\text{Bret,H}} \tag{B6}$$

$$T_s = 7.54 * \frac{u_{\text{wind}}}{g} * p_2 * \tanh\left(0.077 * \frac{F_x^{0.25}}{p_2}\right) * m_{\text{Bret,T}} \tag{B7}$$

With the wave characteristics the average overtopping discharge is calculated following the formulas by TAW (2002) and van der Meer et al. (2016). Since no berm is present on the dike of the case-study and waves are assumed perpendicular factors
20   related to these aspects are omitted.

$$\xi_0 = \frac{\tan(\alpha_{\text{out}})}{\sqrt{\frac{2\pi H_s}{g T_s^2}}} \tag{B8}$$

$$q_1 = \min\left(\begin{array}{c} \frac{0.067}{\sqrt{\tan \alpha_{\text{out}}}} * \xi_0 * \exp\left(c_1 * \frac{z_{\text{crest}} - h}{H_s} * \frac{1}{\xi_0 * \gamma_f}\right) \\ 0.2 * \exp\left(-2.6 * \frac{z_{\text{crest}} - h}{H_s} * \frac{1}{\gamma_f}\right) \end{array}\right) * \sqrt{g * H_s^3} \tag{B9}$$

$$q_2 = 10^{c_2} * \exp\left(-\frac{z_{\text{crest}} - h}{\gamma_f * H_s * (0.33 + 0.022 * \xi_0)}\right) * \sqrt{g * H_s^3} \tag{B10}$$

$$q_{\text{overtopping}} = \begin{cases} q_1 & \xi_0 < 5 \\ 10^{\frac{\log(q_1) + \log(q_2)}{2}} & 5 \geq \xi_0 \geq 7 \\ q_2 & \xi_0 > 7 \end{cases} \tag{B11}$$

A description and values for the variables are presented in Table B1.

The limit state function is then evaluated as:

$$Z_{\text{overflow and overtopping}} = q_c - q_{\text{overflow}} - q_{\text{overtop}} \tag{B12}$$

C: Piping limit state function

Piping is evaluated with the piping erosion formulae of Sellmeijer et al. (2011). The critical head difference (H_c) is calculated as:

$$F_R = \frac{\gamma_p - \gamma_w}{\gamma_w} * \eta * \tan\theta * \left(\frac{RD}{RD_m}\right)^{0.35} \tag{C1}$$

$$F_S = \frac{d_{70}}{\sqrt[3]{\kappa L}} * \left(\frac{d_{70m}}{d_{70}}\right)^{0.6} \tag{C2}$$

$$F_G = 0.91 * \left(\frac{d_{\text{aquifer}}}{L}\right)^{\frac{0.28}{\left(\frac{d_{\text{aquifer}}}{L}\right)^{2.8} - 1} + 0.04} \tag{C3}$$

$$H_c = F_R * F_S * F_G * L \tag{C4}$$

Failure occurs when the critical head level (H_c) is exceeded by the head difference (H) and the resistance of the blanket layer:

$$Z_{\text{piping}} = m_p * H_c - (H - 0.3 * d_{\text{blanket}}) \tag{C5}$$

The variables introduced by Eq. (C1) to Eq. (C5) are given in Table C1. and are based on estimates used in Dutch dike assessments. The intrinsic permeability (κ) which is directly converted from the permeability of the aquifer (k_{aquifer}).

D: Macro stability limit state function

The macro stability of the dike is evaluated using the schematisation of the phreatic surface of a clay dike from the TAW (2004) following the official Dutch guidelines (see Fig. D1). The TAW (2004) schematisation assumes a drop in the phreatic surface on the interface of the dike with the outside water (1 m as by default) and a linear drop towards the inner toe. The water head in the aquifer was calculated using the equations by TAW (2004) as implemented in the D-stability software (Brinkman and Nuttall, 2018).

The stability of the slope is calculated with the method by Van (2001) for the slip plane and works on the same principle as the method by Bishop (1955). The main difference between the methods is the separation of the slip plane in an active circle connected by a straight section followed by a passive circle. The centres of these circles of the critical slip plane (R_A and R_P) are found iteratively using the D-stability software (Brinkman and Nuttall, 2018).

The slip plane is divided into slices and the net force induced by each slice is calculated. If the moment induced by the active slices (ΣM_S) is greater than the combination of friction forces and moments induced by the passive slices (ΣM_R) the slope is unstable. This is both expressed in a factor of safety (F_S) and Z-function.

$$F_S = \frac{\Sigma M_R}{\Sigma M_S} \tag{D1}$$

$$Z_{\text{macrostability}} = F_{\text{S}} - 1 \tag{D2}$$

To calculate the probability of failure with FORM the factor of safety needs to be evaluated during each iteration with D-stability. An experimental version of D-stability with an additional piece of software from the same developers called the probabilistic toolkit (PTK) was utilised to automatically execute D-stability with updated parameters calculated by the FORM
5   algorithm in the PTK.

The iterative procedure of finding the critical slip plane is both computationally demanding and complicates conversion in the probabilistic FORM algorithm. To speed up the procedure in the computation first a test run is performed using average soil strength parameters at a fixed critical slip plane with a water level halfway at the crest . With the results of the first indicative
10   run, stochastic variables with little to no influence ($|\alpha|$<0.001) are set as constants. Then the entire model was run for each discretised water level.

After the run the fragility curve was checked for points where no convergence was achieved with FORM or a non-critical slip circle must have been evaluated. To this end points where the maximum number of iterations was reached or the probability
15   of failure decreased with ascending water level were removed to obtain a monotonically increasing fragility curve.

E: FORM algorithm

The first order reliability method (FORM) is a method to iteratively calculate the probability of a limit state function ($Z(\mathbf{X}) \leq 0$) being exceeded given a set of independent random variables ($\mathbf{X}$) (Hasofer and Lind, 1974). The starting point for the iteration is arbitrary, but usually the mean of the variables is taken as the first point to evaluate ($\mathbf{x}^*$). The problem is first
20   simplified by converting the random variables before each iteration into realisations of equivalent normally distributed variables ($\mathbf{x}'$) with an equivalent normal transformation (Rackwitz and Flessler, 1978).

$$\mu'_{X_i} = x_i^* - \sigma'_{X_i} * \Phi^{-1}[F(x_i^*)] \tag{E1}$$

$$\sigma'_{X_i} = \frac{\varphi\{\Phi^{-1}[F(x_i^*)]\}}{f(x_i^*)} \tag{E2}$$

Where μ'_{X_i} and σ'_{X_i} are the mean and standard deviation of the equivalent normal distribution of variable x_i in the point $\mathbf{x}^*$. Also f and F are the probability density function (PDF) and cumulative distribution function (CDF) of variable x_i while φ and Φ are the standard normal PDF and CDF.

The mean and standard deviation of the limit state function are evaluated by:

$$\mu_Z = Z(\boldsymbol{x}^*) + \sum_{i=1}^{n} \frac{\partial Z}{\partial X_i} (\mu'_{X_i} - x_i^*) \tag{E3}$$

$$\sigma_Z = \sqrt{\sum_{i=1}^{n} \left(\frac{\partial Z}{\partial X_i}\right)^2 \sigma'_{X_i}{}^2} \tag{E4}$$

With the mean and standard deviation calculated from the design point ($\mathbf{x}^*$) the reliability index (β) and influence factor of each variable (α_{X_i}) are calculated.

$$\beta = \frac{\mu_Z}{\sigma_Z} \tag{E5}$$

$$\alpha_{X_i} = \frac{\partial Z}{\partial X_i} * \frac{\sigma'_{X_i}}{\sigma_Z} \tag{E6}$$

The point is updated by adjusting each variable based on the overall safety level (β) and the sensitivity of the limit state to the variable (α_{X_i}):

$$x_i^* = \mu'_{X_i} - \alpha_{X_i} \beta \sigma'_{X_i} \tag{E7}$$

The process is repeated until the reliability index has converged and no longer changes significantly after an iteration.

While the method is effective there are limitations. It is not guaranteed FORM finds the design point with the highest probability but rather converges to a local design point. Furthermore for FORM to converge the limit state function should be smooth without jumps or discontinuities. This complicated the implementation of for example macro stability as when a different slip circle becomes critical there can be a sudden jump in the evaluation of the limit state function.

References

Aguilar-López, J. P., Warmink, J. J., Schielen, R. M. J., and Hulscher, S. J. M. H.: Correlation Effect in Probabilistic Design against Piping in Multi-Functional Flood Defences, in: Geotechnical Safety and Risk V, edited by: Schweckendiek, T., Van Tol, A. F., Pereboom, D., Van Staveren, A., and Cools, P. M. C. B. M., IOS Press, Amsterdam, the Netherlands, https://doi.org/10.3233/978-1-61499-580-7-237, 2015.

Aguilar-López, J. P., Warmink, J. J., Schielen, R. M. J., and Hulscher, S. J. M. H.: Piping erosion safety assessment of flood defences founded over sewer pipes, Eur. J. Environ. Civ. En., 22, 707-735, https://dx.doi.org/10.1080/19648189.2016.1217793, 2018.

Anvarifar, F., Oderkerk, M., van der Horst, B. R., and Zevenbergen, C.: Cost-effectiveness study on preventive interventions: A survey of multifunctional flood defences, in: Comprehensive Flood Risk Management: research for policy and practice, edited by: Klijn, F., and Schweckendiek, T., CRC Press, London, the United Kingdom, 891-899, 2013.

Anvarifar, F., Zevenbergen, C., Thissen, W., and Islam, T.: Understanding flexibility for multifunctional flood defences: a conceptual framework, J. Water Clim. Change, 7, 467-484, https://doi.org/10.2166/wcc.2016.064, 2016.

Anvarifar, F., Voorendt, M., Zevenbergen, C., and Thissen, W.: An application of the Functional Resonance Analysis Method (FRAM) to risk analysis of multifunctional flood defences in the Netherlands, Reliab. Eng. Syst. Safe., 158, 130-141, https://doi.org/10.1016/j.ress.2016.10.004, 2017.

Apel, H., Thieken, A. H., Merz, B., and Blöschl, G.: Flood risk assessment and associated uncertainty, Nat. Hazards Earth Syst. Sci., 4, 295-308, https://doi.org/10.5194/nhess-4-295-2004, 2004.

Apel, H., Thieken, A. H., Merz, B., and Blöschl, G.: A Probabilistic Modelling System for Assessing Flood Risks, Nat. Hazards, 38, 79-100, https://doi.org/10.1007/s11069-005-8603-7, 2006.

van Baars, S., and van Kempen, I.: The causes and mechanisms of historical dike failures in the Netherlands, E-Water, 2009/06, 1-14, available at: http://www.dwa.de/portale/ewa/ewa.nsf/home?readform&objectid=8428F628AB57BECFC125766C003024B6 (last access: 21 february 2019), 2009.

Bachmann, D., Huber, N. P., Johann, G., and Schüttrumpf, H.: Fragility curves in operational dike reliability assessment, Georisk: Assessment and Management of Risk for Engineered Systems and Geohazards, 7, 49-60, https://doi.org/10.1080/17499518.2013.767664 , 2013.

Bischiniotis, K., Kanning, W., Jonkman, S. N., and Kok, M.: Cost-optimal design of river dikes using probabilistic methods, J. Flood Risk Manag., 11, S1002-S1014, https://doi.org/10.1111/jfr3.12277, 2018.

Bishop, A. W.: The use of the slip circle in the stability analysis of slopes, Géotechnique, 5, 7-17, https://doi.org/10.1680/geot.1955.5.1.7, 1955.

Bomers, A., Aguilar Lopez, J. P., Warmink, J. J., and Hulscher, S. J. M. H.: Modelling effects of an asphalt road at a dike crest on dike cover erosion onset during wave overtopping, Nat.Hazards, 93, 1-30, https://dx.doi.org/10.1007/s11069-018-3287-y, 2018.

Bouwer, L. M., Bubeck, P., and Aerts, J. C. J. H.: Changes in future flood risk due to climate and development in a Dutch polder area, Global Environ. Chang., 20, 463-471, https://doi.org/10.1016/j.gloenvcha.2010.04.002, 2010.

Brinkman, R., and Nuttall, J. D.: Failure mechanisms – Macro Stability kernel; Scientific Background, Deltares, Delft, The Netherlands, 11201523-001-HYE-001, 2018.

Chen, X., Jonkman, S. N., Pasterkamp, S., Suzuki, T., and Altomare, C.: Vulnerability of Buildings on Coastal Dikes due to Wave Overtopping, Water, 9, 394, https://doi.org/10.3390/w9060394, 2017.

Danka, J., and Zhang, L. M.: Dike Failure Mechanisms and Breaching Parameters, Journal of Geotechnical and Geoenvironmental Engineering, 141, 04015039, https://doi.org/10.1061/(ASCE)GT.1943-5606.0001335, 2015.

van der Flier, C., and Thomsen, A.: Life cycle of dwellings: Analysis and assessment of demolition by Dutch housing associations, International Conference ENHR, Ljubljana, Slovenia, 2-5 July 2006, Workshop 7: Physical Aspects of Design and Regeneration, 2006.

van der Meer, J. W., Allsop, N. W. H., Bruce, T., De Rouck, J., Kortenhaus, A., Pullen, T., and Zanuttigh, B.: EurOtop 2016: Manual on wave overtopping of sea defences and related structures. An overtopping manual largely based on European research, but for worldwide application, Retrieved from: www. overtopping-manual.com (last access: 21 february 2019), 2016.

Diermanse, F.: WBI - Onzekerheden; Overzicht van belasting- en sterkteonzekerheden in het wettelijk beoordelingsinstrumentarium, Deltares, Delft, the Netherlands, 1220080-001-ZWS-0004, 2016.

Ellen, G. J., Boers, M., Knoeff, H., Schelfhout, H. A., Tromp, E., van den Berg, F., Borgers, H., and Rengers, J.: Multifunctioneel medegebruik van de waterkering: beantwoording signaleringsvraag #5 van de Deltacommissaris, Deltares, Delft, the Netherlands, 1204871-000, 41, 2011a.

Ellen, G. J., Hommes, S., Kalweit, A. M., van Lamoen, F., Melisie, E., Maring, L., Paalman, M., Peerdeman, K., van Rooij, S. A. M., and Steingrover, E. G.: Multifunctioneel landgebruik als adaptatiestrategie - Puzzelen met ondernemers en beleidsmakers, Kennis voor Klimaat, Wageningen, the Netherlands, KvK/036/2011, 2011b.

Friess, D. A., Spencer, T., Smith, G. M., Möller, I., Brooks, S. M., and Thomson, A. G.: Remote sensing of geomorphological and ecological change in response to saltmarsh managed realignment, The Wash, UK, Int. J. Appl. Earth Obs., 18, 57-68, https://doi.org/10.1016/j.jag.2012.01.016, 2012.

van Gelder, P., Buijs, F., Horst, W., Kanning, W., Mai Van, C., Rajabalinejad, M., de Boer, E., Gupta, S., Shams, R., van Erp, N., Gouldby B., Kingston G., Sayers P., Wills M., Kortenhaus A. and Lambrecht H.: Reliability analysis of flood defence structures and systems in Europe, in: Flood Risk Management: Research and Practice, edited by: Samuals P., Huntington S., Allsop W. and Harrop J., CRC press, London, the United Kingdom, 603-611, 2009.

Gulvanessian, H.: EN 1990 Eurocode "Basis of structural design" – the innovative head Eurocode, Steel Construction, 2, 222-227, https://doi.org/10.1002/stco.200910030, 2009.

Hall, J. W., Dawson, R., Sayers, P., Rosu, C., Chatterton, J., and Deakin, R.: A methodology for national-scale flood risk assessment, P. I. Civil. Eng.-Water, 156, 235-248, https://doi.org/10.1680/wame.2003.156.3.235, 2003.

Hanssen, R. F., and van Leijen, F. J.: Monitoring deformation of water defense structures using satellite radar interferometry, Proceedings of the 13th FIG Symposium on Deformation Measurement and Analysis, Lisbon, Portugal, ps03_04_hanssen_mc136, 2008.

Hasofer, A. M., and Lind, N. C.: Exact and invariant second-moment code format, J. Eng. Mech. Div.-ASCE, 100, 111-121, 1974.

Herle, S., Becker, R., and Blankenbach, J.: Smart sensor-based geospatial architecture for dike monitoring, IOP Conf. Ser.: Earth Environ. Sci., 34, 012014, https://doi.org/10.1088/1755-1315/34/1/012014, 2016.

Hinkel, J., van Vuuren, D. P., Nicholls, R. J., and Klein, R. J. T.: The effects of adaptation and mitigation on coastal flood impacts during the 21st century. An application of the DIVA and IMAGE models, Climatic Change, 117, 783-794, https://doi.org/10.1007/s10584-012-0564-8, 2013.

Hirabayashi, Y., Mahendran, R., Koirala, S., Konoshima, L., Yamazaki, D., Watanabe, S., Kim, H., and Kanae, S.: Global flood risk under climate change, Nat. Clim. Change, 3, 816, https://doi.org/10.1038/nclimate1911, 2013.

Hoffmans, G., Akkerman, G. J., Verheij, H., van Hoven, A., and van der Meer, J.: The erodability of grassed inner dike slopes against wave overtopping, in: Coastal Engineering 2008: Proceedings of the 31st International Conference, Hamburg, Germany, 31 August- 5 September 2008, 3224-3236, https://doi.org/10.1142/9789814277426_0267, 2009.

Holthuijsen, L. H.: Methoden voor golfvoorspelling, Technische Adviescommissie voor de Waterkeringen, Delft, the Netherlands, TAWP80-01, 1980.

van Houwelingen, A. W.: BomenT fase 3, Gedetaileerde toets, DHV B.V., Amersfoort, the Netherlands, LW-AF20122371, 2012.

van Hoven, A.: Verderlingen kritisch overslagdebiet WTI2017, Deltares, Delft, the Netherlands, 220086-005-HYE-0003, 2015.

IPCC: Climate Change 2013: The Physical Science Basis. Contribution of Working Group I to the Fifth Assessment Report of the Intergovernmental Panel on Climate Change, Cambridge University Press, Cambridge, United Kingdom, 2013.

Jongejan, R. and Maaskant, B.: Applications of VNK2, a fully probabilistic risk analysis for all major levee systems in the Netherlands, in: Comprehensive Flood Risk Management: research for policy and practice, edited by: Klijn, F., and Schweckendiek, T., CRC Press, London, the United Kingdom, 693-700, 2013.

5   Jongman, B., Ward, P. J., and Aerts, J. C. J. H.: Global exposure to river and coastal flooding: Long term trends and changes, Global Environ. Chang., 22, 823-835, https://doi.org/10.1016/j.gloenvcha.2012.07.004, 2012.

Jonkman, S. N., Kok, M., Van Ledden, M., and Vrijling, J. K.: Risk-based design of flood defence systems: a preliminary analysis of the optimal protection level for the New Orleans metropolitan area, J. Flood Risk Manag., 2, 170-181,
10   https://doi.org/10.1111/j.1753-318X.2009.01036.x, 2009.

Kheradmand, S., Seidou, O., Konte, D., and Barmou Batoure, M. B.: Evaluation of adaptation options to flood risk in a probabilistic framework, J. Hydrol., 19, 1-16, https://doi.org/10.1016/j.ejrh.2018.07.001, 2018.

15   Knoeff, H.: Factsheet indirecte mechanismen, Deltares, Delft, the Netherlands, 11200574-007-GEO-0001, 2017.

Kok, M., Jongejan, R., Nieuwjaar, M., and Tanczos, I.: Fundamentals
of Flood Protection, Ministery of Infrastructure and the Environment and Expertise Network for Flood Protection (ENW), Breda, the Netherlands, 2016.
20
Lanzafame, R. C.: Reliability Analysis of the Influence of Vegetation on Levee Performance, Ph. D. thesis , University of California, Berkley United States, 2017.

Lendering, K., Schweckendiek, T., and Kok, M.: Quantifying the failure probability of a canal levee, Georisk, 12, 1-15,
25   https://doi.org/10.1080/17499518.2018.1426865, 2018.

Lenders, H., Huijbregts, M., Aarts, B., and Van Turnhout, C.: Assessing the degree of preservation of landscape, natural and cultural-historical values in river dike reinforcement planning in the Netherlands, Regul. River., 15, 325-337, https://doi.org/10.1002/(SICI)1099-1646(199907/08)15:4%3C325::AID-RRR545%3E3.0.CO;2-G, 1999.
30
van Loon-Steensma, J. M., Schelfhout, H. A., and Vellinga, P.: Green adaptation by innovative dike concepts along the Dutch Wadden Sea coast, Environ. Sci. Policy, 44, 108-125, http://dx.doi.org/10.1016/j.envsci.2014.06.009, 2014.

van Loon-Steensma, J. M., and Vellinga, P.: Robust, multifunctional flood protection zones in the Dutch rural riverine area,
35   Nat. Hazard. Earth Sys., 14, 1085-1098, https://doi.org/10.5194/nhess-14-1085-2014, 2014.

van Loon-Steensma, J. M., Hu, Z., and Slim, P. A.: Modelled Impact of Vegetation Heterogeneity and Salt-Marsh Zonation on Wave Damping, J. Coastal Res., 32, 241-252, https://doi.org/10.2112/JCOASTRES-D-15-00095.1, 2016.

40   van Loon-Steensma, J. M. and Kok, M.: Risk reduction by combining nature values with flood protection?, E3S Web Conf., 7, 13003, https://doi.org/10.1051/e3sconf/20160713003, 2016.

Maris, A.G., De Blocq van Kuffeler, V.J.P., Harmsen, W.J.H., Jansen, P.P., Nijhoff, G.P., Thijsse, J.T., Verloren van Themaat, R., de Vries, J.W., Van der Wal, L.T.: Rapport Deltacommissie. Deel 1. Eindverslag en interimadviezen, Delta
45   Committee, Delft, the Netherlands, http://resolver.tudelft.nl/uuid:0e28dfd8-4e67-4267-a443-54b74a062bcb (last access: 21 february 2019), 1961.

Ministerie van Infrastructuur en Milieu: Regeling van de Minister van Infrastructuur en Milieu, van 2 december 2016, nr. IENM/BSK-2016/283517, ter uitvoering van de artikelen 2.3, eerste lid, en 2.12, vierde lid, van de Waterwet, houdende
50   regels voor het bepalen van de hydraulische belasting en de sterkte en procedurele regels voor de beoordeling van de veiligheid van primaire waterkeringen, Ministerie van Infrastructuur en Milieu, the Hague, the Netherlands, 2016.

Ministerie van Verkeer en Waterstaat: Voorschrift Toetsen op Veiligheid Primaire Waterkeringen, Ministerie van Verkeer en Waterstaat, Delft, the Netherlands, ISBN 978-90-369-5762, 2007.
55
NEN: NEN 3651:2012 nl: Additional requirements for pipelines in or nearby important public works, NEN, Delft, the Netherlands, ICS 23.040.10; 93.010, 2012.

Niedermeier, A., Hoja, D., and Lehner, S.: Topography and morphodynamics in the German Bight using SAR and optical
60   remote sensing data, Ocean Dynam., 55, 100-109, https://doi.org/10.1007/s10236-005-0114-2, 2005.

Orlandini, S., Moretti, G., and Albertson, J. D.: Evidence of an emerging levee failure mechanism causing disastrous floods in Italy, Water Resour. Res., 51, 7995-8011, https://doi.org/10.1002/2015WR017426, 2015.

Pontee, N., Narayan, S., Beck, M. W., and Hosking, A. H.: Nature-based solutions: lessons from around the world, P. I. Civil Eng.-Mar. En., 169, 29-36, https://doi.org/10.1680/jmaen.15.00027, 2016.

Rackwitz, R., and Flessler, B.: Structural reliability under combined random load sequences, Comput. Struct., 9, 489-494,
5   https://doi.org/10.1016/0045-7949(78)90046-9, 1978.

Rijkswaterstaat: Handreiking ontwerpen met overstromingskansen: Veiligheidsfactoren en belastingen bij nieuwe overstromingskansnormen OI2014v4, Rijkswaterstaat Water, Verkeer en Leefomgeving, Utrecht, the Netherlands, 2017.

10   Sellmeijer, H., de la Cruz, J. L., van Beek, V. M., and Knoeff, H.: Fine-tuning of the backward erosion piping model through small-scale, medium-scale and IJkdijk experiments, Eur. J. Environ. Civ. En., 15, 1139-1154, https://doi.org/10.1080/19648189.2011.9714845, 2011.

Slomp, R., Knoeff, H., Bizzarri, A., Bottema, M., and de Vries, W.: Probabilistic flood defence assessment tools, E3S Web
15   of Conferences, 7, 03015, https://doi.org/10.1051/e3sconf/20160703015, 2016.

Stalenberg, B.: Innovative flood defences in highly urbanised water cities, in: Climate Adaptation and Flood Risk in Coastal Cities, edited by: Aerts, J., Botzen, W., Bowman, M.J., Ward, P.J. and Dircke, P., Earthscan, Oxon, the United Kingdom, 145-164, 2013.

Steenbergen, H., Lassing, B., Vrouwenvelder, A., and Waarts, P.: Reliability analysis of flood defence systems, Heron, 49, http://heronjournal.nl/49-1/3.html (last access: 21 february 2019), 2004.

Stichting Toegepast Onderzoek Waterbeheer: Bomen op en nabij waterkeringen, achtergrondrapport, STOWA, Utrecht, the
25   Netherlands, ISBN 90-5773-086.3, 2000.

Stichting Toegepast Onderzoek Waterbeheer: Addendum op de leidraad toetsen op veiligheid regionale waterkeringen betreffende de boezemkaden, STOWA, Amersfoort, the Netherlands, ISBN 978.90.5773.481.6, 2010.

30   Technische Adviescommissie voor de Waterkeringen: Leidraad voor het ontwerpen van rivierdijken: Deel 1, Bovenrivierengebied, TAW, 's-Gravenhage, the Netherlands, ISBN 90-12-05169-X, 1985.

Technische Adviescommissie voor de Waterkeringen: Handreiking Constructief ontwerpen: Onderzoek en berekening naar het constructief ontwerp van de dijkversterking, TAW, Delft, the Netherlands, L9, 1994.
35

Technische Adviescommissie voor de Waterkeringen: Technisch Rapport Golfoploop en Golfoverslag bij Dijken, TAW, Delft, the Netherlands, TR33, 2002.

Technische Adviescommissie voor de Waterkeringen: Technisch Rapport Waterspanningen bij dijken, TAW, Delft, the
40   Netherlands, ISBN-90-369-5565-3, 2004.

Temmerman, S., Meire, P., Bouma, T. J., Herman, P. M. J., Ysebaert, T., and De Vriend, H. J.: Ecosystem-based coastal defence in the face of global change, Nature, 504, 79-83, https://doi.org/10.1038/nature12859, 2013.

45   Van, M.: New approach for uplift induced slope failure, in: Proceedings of the 15th International Conference on Soil Mechanics and Foundation Engineering, Istanbul, 27 - 31 August 2001, Turkey, 2285-2288, 2001.

Van Veelen, P., Voorendt, M., and van der Zwet, C.: Design challenges of multifunctional flood defences. A comparative approach to assess spatial and structural integration, Research in Urbanism Series, 3, 275-292,
50   https://doi.org/10.7480/rius.3.841, 2015.

Voorendt, M. Z.: Design principles of multifunctional flood defences, Ph.D. thesis, Delft university of technology, Delft, the Netherlands, 342 pp., 2017.

55   Vorogushyn, S., Merz, B., and Apel, H.: Development of dike fragility curves for piping and micro-instability breach mechanisms, Nat. Hazards Earth Syst. Sci., 9, 1383-1401, https://doi.org/10.5194/nhess-9-1383-2009, 2009.

Vorogushyn, S., Merz, B., Lindenschmidt, K.-E., and Apel, H.: A new methodology for flood hazard assessment considering dike breaches, Water Resour. Res., 46, https://doi.org/10.1029/2009WR008475, 2010.
60

Vrijling, J. K.: Probabilistic design of water defense systems in The Netherlands, Reliab. Eng. Syst. Safe., 74, 337-344, https://doi.org/10.1016/S0951-8320(01)00082-5, 2001.

Vuik, V., van Vuren, S., Borsje, B. W., van Wesenbeeck, B. K., and Jonkman, S. N.: Assessing safety of nature-based flood defenses: Dealing with extremes and uncertainties, Coast. Eng., 139, 47-64, https://doi.org/10.1016/j.coastaleng.2018.05.002, 2018.

5 de Waal, J. P.: Deelrapport 9: Modellering dammen, voorlanden en golfoploop, in: Achtergronden hydraulische belastingen dijken IJsselmeergebied, Rijksinstituut voor Integraal Zoetwaterbeheer en Afvalwaterbehandeling (RIZA), Lelystad, the Netherlands, ISBN 9036952700, 1999.

Zanetti, C., Vennetier, M., Mériaux, P., Royet, P., and Provansal, M.: Managing woody vegetation on earth dikes: Risks
10 assessment and maintenance solutions, Procedia Environ. Sci., 9, 196-200, https://doi.org/10.1016/j.proenv.2011.11.030, 2011.
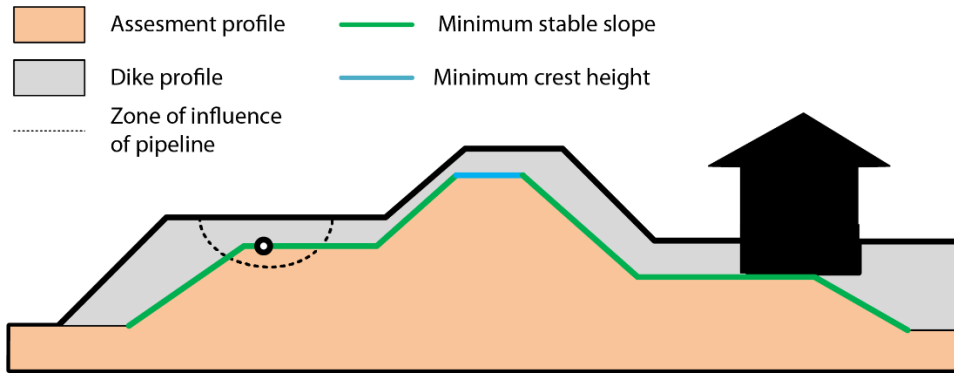
Fig. 1 Assessment profile for a dike with NWOs (pipeline and house with basement). Adapted from figure A.4 of the current Dutch guidelines (Rijkswaterstaat, 2016)

Design: Top-down

Existing framework

1: Safety standard — Dike segment failure

2: Additional safety for unknowns — Failure mechanisms — Other

3: Failures — Piping — Overtopping — Macro-stability — Erosion — Other

4: Dike section — Section reliability

5: Cross-section — Target reliability

6: Scenarios — NWO fails — NWO survives — Addition

Assessment: Bottom-up
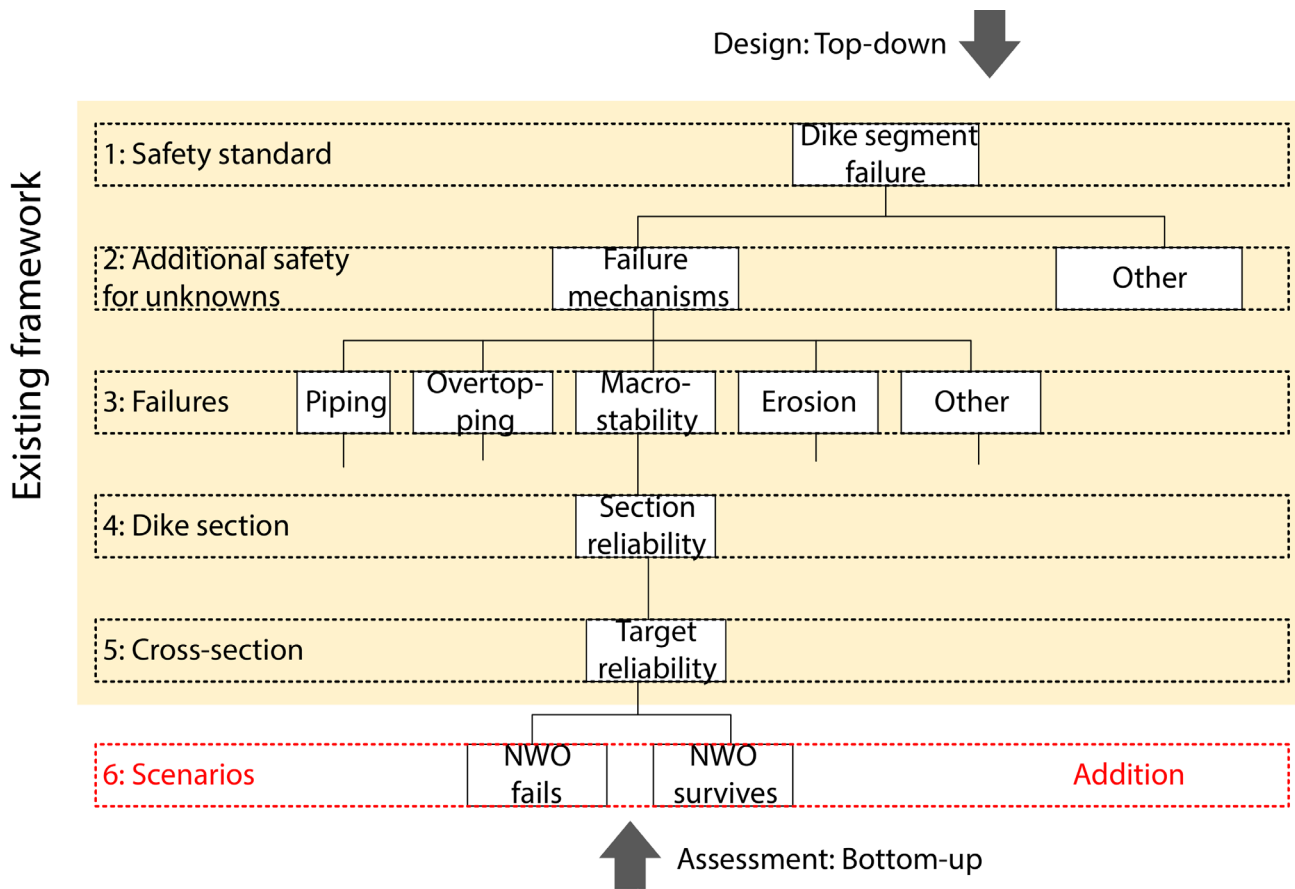
Fig. 2 A framework for a detailed assessment and design of a dike with multifunctional elements. The yellow section is the existing framework while the last step in *red* denotes the addition of scenarios (e.g. a failed NWO and functioning NWO) to conform to a risk-based approach.
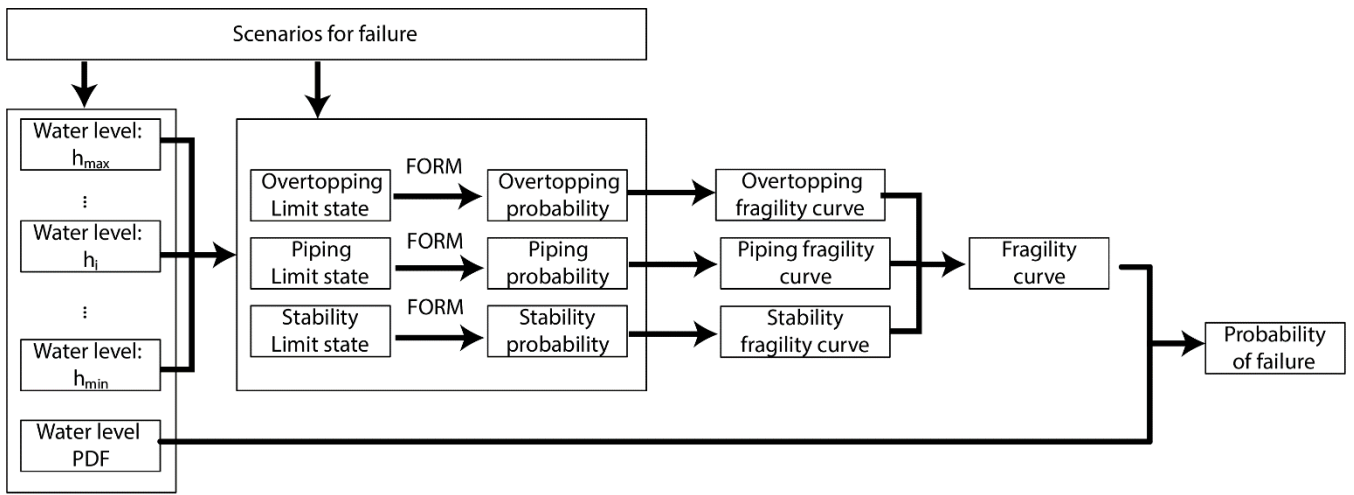
Fig. 3 The probabilistic procedure for calculating the probability of failure of a dike cross-section in this study

0: Base case

1: Broadening river side

2: Broadening land side

3: Heightening

4: Inner berm

5: Expand outer slope

6: Expand inner slope

7: Robust dike
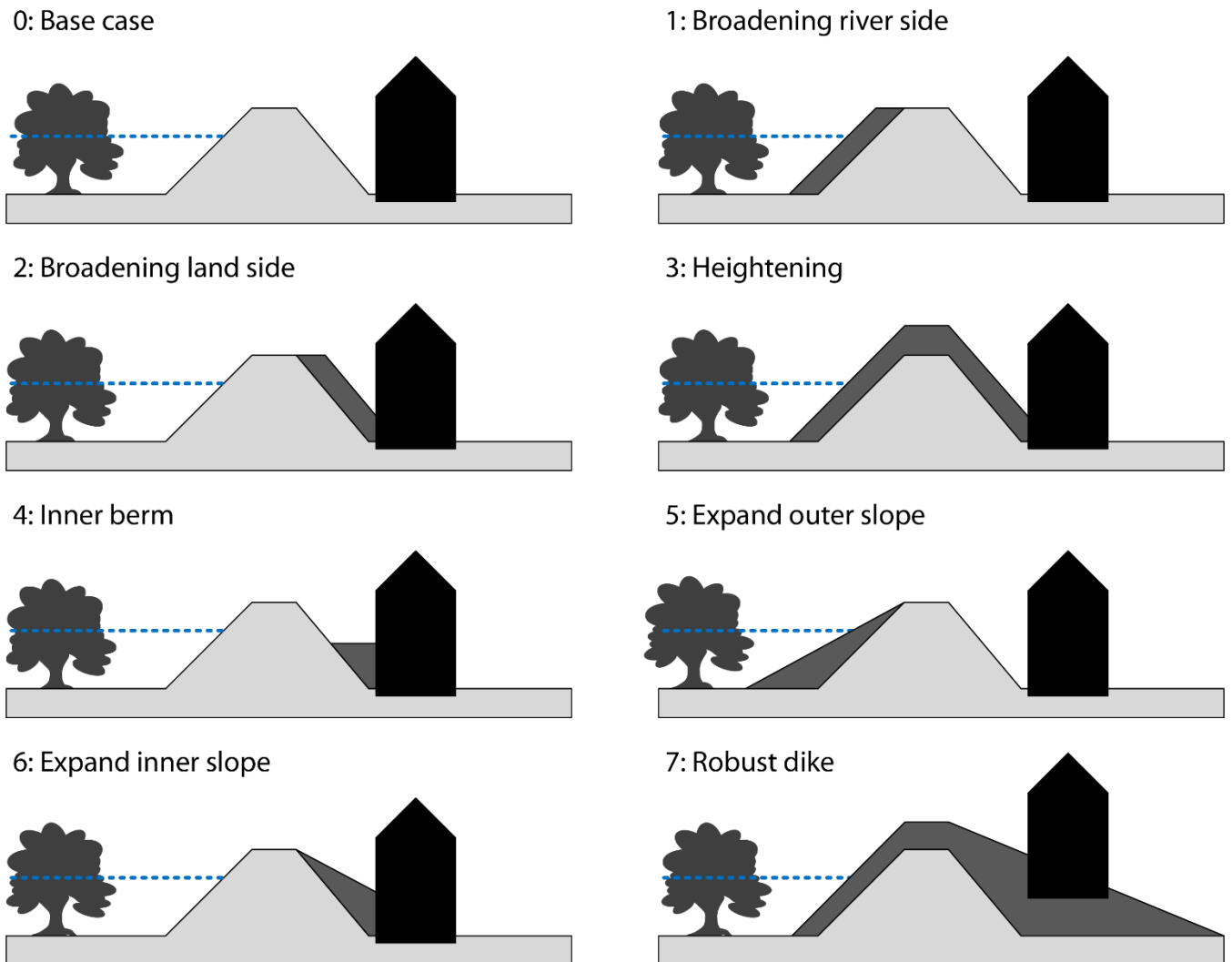
Fig. 4 Case studies for comparing the conservative and the new probabilistic approach in this study
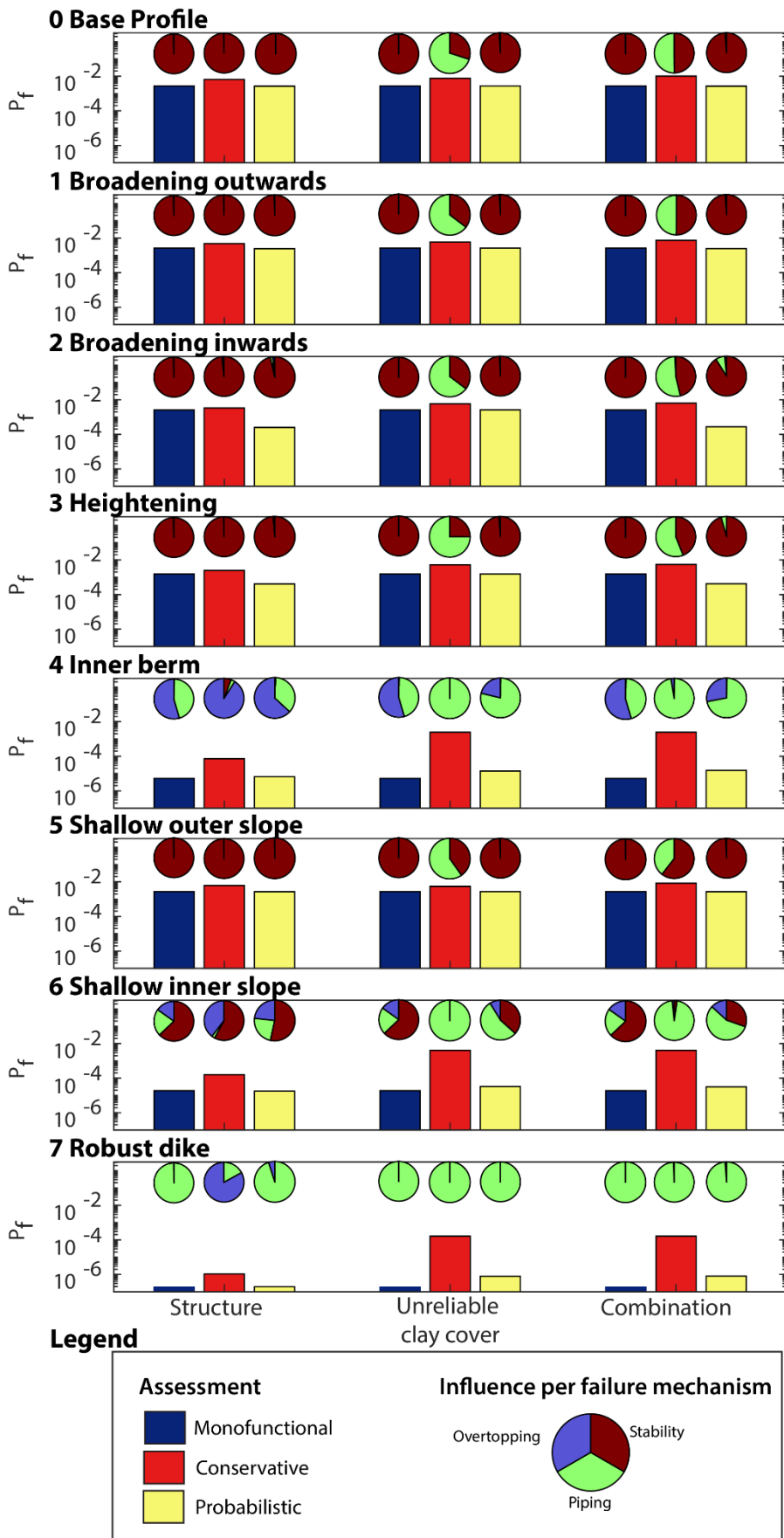
Fig. 5 The probability of failure (P_f) for every dike profile (0 to 7) assessed as a monofunctional dike (blue bar), a multifunctional dike with a conservative approach (red bar) and a multifunctional dike using a probabilistic approach (yellow bar) in the situation where a structure is present (left), an impaired clay cover on the flood plain could be present (middle) and both a structure and unreliable clay cover are present (right). The influence of the three failure mechanisms overtopping (blue), piping (green) and stability (red) is given per bar with a pie chart.
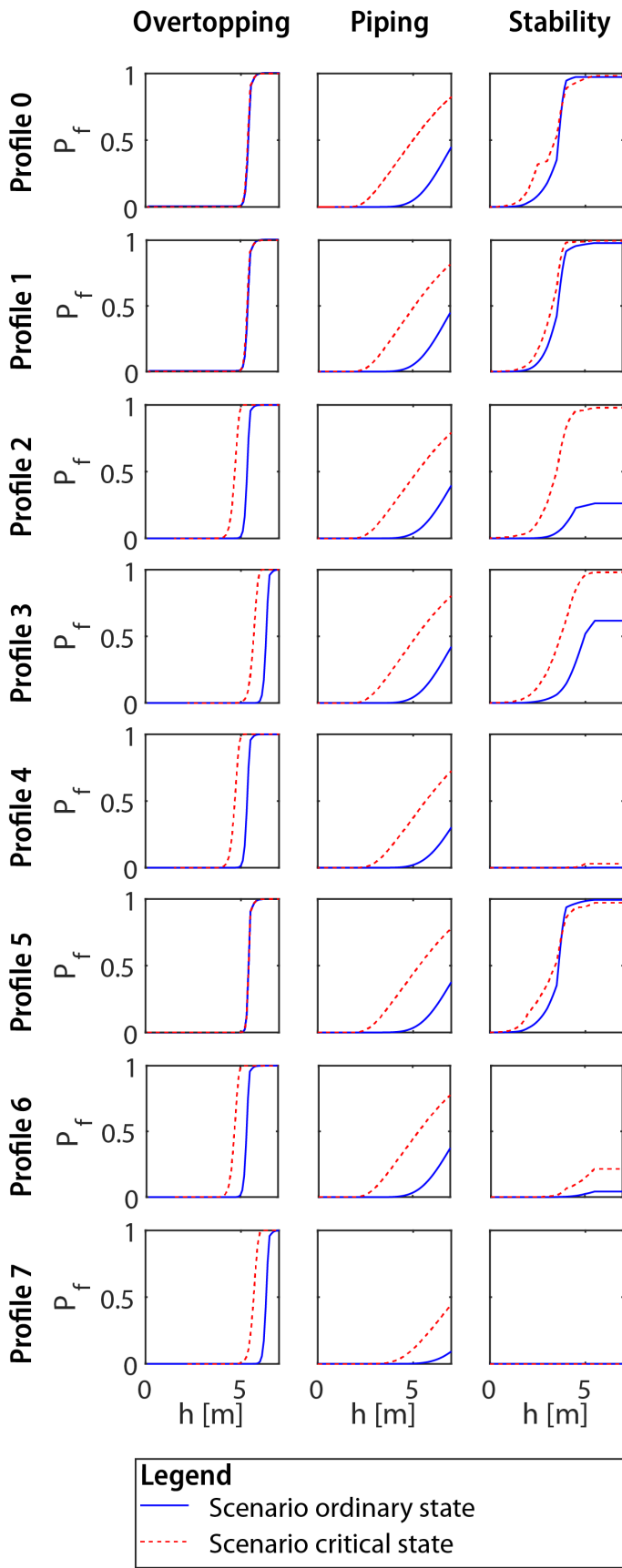
Fig. 6 The difference between the fragility curves of the 3 failure mechanisms and each profile with both multifunctional elements intact in blue and both multifunctional elements in a critical state in red.
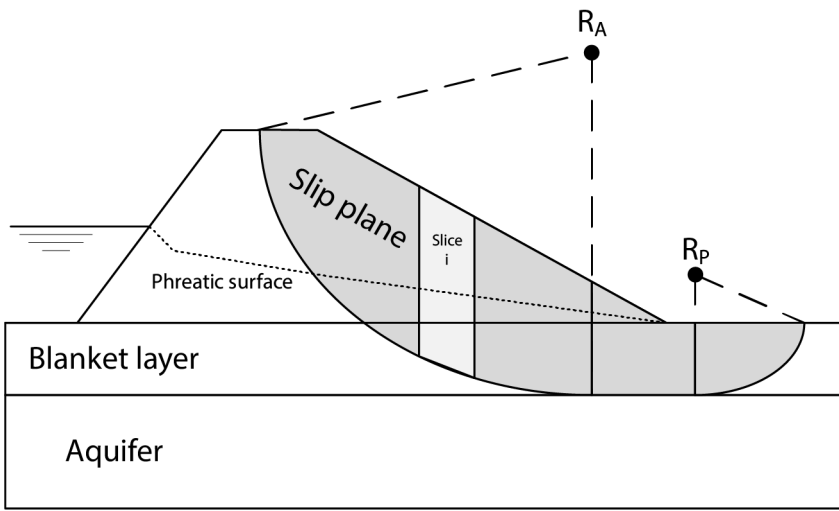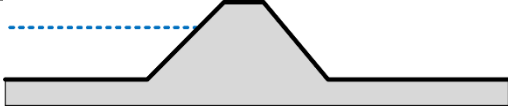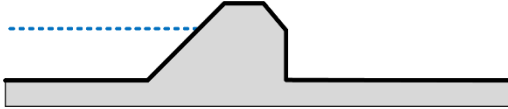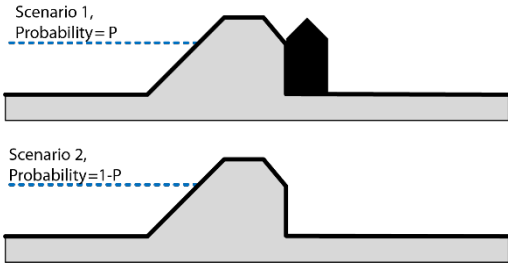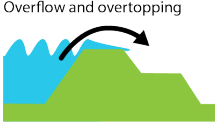
Fig. D1 Schematisation of the slip plane and phreatic surface used for the macro stability calculation

Tables

Table 1 The different approaches for assessing the cross-section of a multifunctional dike in this study

Approach		Assumptions	Example
Mono-functional		• No multifunctional elements present	
Multi-functional	Conservative	• Functions are always in the critical state for a given failure mechanism • Dike zones affected by the multifunctional elements are omitted from the profile	
	Probabilistic	• Uncertainty of multifunctional elements split into scenarios (e.g. present or absent) • Each scenario has a probability	Scenario 1, Probability=P Scenario 2, Probability=1-P

Table 2 Overview of failure mechanisms and corresponding methods

Failure mechanism	Description	Limit state function	Method
Overflow and overtopping	Excessive flow of water over the dike with severe inundation of the hinterland as a result, possibly by erosion of the revetment and soil on the crest and inner slope leading to a dike breach	$q_c - q$	Overtopping: van der Meer et al. (2016), TAW (2002), de Waal (1999)
Piping	Erosion of soil particles under the dike as a result of seepage. This in turn leads to collapse of the dike and failure by inundation of the hinterland.	$H_c - H$	Ground water: TAW (2004) Erosion: Sellmeijer et al. (2011)
Macro stability	Loss of slope stability as the dike becomes saturated. The collapse of the dike results in inundation of the hinterland	$\Sigma M_R - \Sigma M_S$	Ground water: TAW (2004) Slope stability: Van (2001)

Table 3 Variation in parameters between reinforcement strategies

Profile nr.	Inner slope [-]	Outer slope [-]	Crest height [m+REF]	Berm width [m]	Crest width [m]	Flood plain length [m]	Max. overtopping rate (μ, σ)* [l/m/s]					
							House present		House absent		No house	
0	1:2.5	1:3	5.5	0	5	100	-	-	-	-	100	120
1	1:2.5	1:3	5.5	0	10	95	-	-	-	-	100	120
2	1:2.5	1:3	5.5	0	10	100	70	80	0.1	0	100	120
3	1:2.5	1:3	6.5	0	5	97	70	80	0.1	0	100	120
4	1:2.5	1:3	5.5	15	5	100	70	80	0.1	0	100	120
5	1:2.5	1:4.5	5.5	0	5	91.75	-	-	-	-	100	120
6	1:4	1:3	5.5	0	5	100	70	80	0.1	0	100	120
7	1:10	1:3	6.5	0	5	97	70	80	0.1	0	100	120

*parameters of the lognormal distribution based on (van Hoven, 2015)

Table A1 The standard geometry parameters for the dikes in the hypothetical case-study

Symbol	Description	Distribution	Parameters	
			μ	σ
z_{hinter}	elevation of the hinterland [m] above REF	Deterministic	0	–
z_{crest}	elevation of the crest [m] above REF	Deterministic	5.5	–
z_{fore}	elevation of the foreshore (at the dike toe) [m] above REF	Deterministic	0	–
z_{deep}	the average bed level, [m] above NAP along the fetch of the wind	Deterministic	-0.8	–
$\tan(\alpha_{in})$	inner slope angle [-]	Deterministic	1/2.5	–
$\tan(\alpha_{out})$	outer slope angle [-]	Deterministic	1/3	–
B_{crest}	crest width [m]	Deterministic	5	–
L_f	length of the foreshore	Lognormal	100	10

Table A2 Standard parameters of the blanket layer for the dikes in the hypothetical case-study

Symbol	Description	Distribution	Parameters	
			μ	σ
$d_{blanket}$	blanket layer thickness [m]	Lognormal	2	0.6
$\gamma_{sat,blanket}$	saturated volumetric weight of the blanket layer [kN/m^3]	Normal	18.8	0.1
$k_{blanket}$	specific conductivity of the blanket layer [m/s]	Lognormal	2.00E-08	2.00E-08
$ch_{blanket}$	cohesion of blanket material [kN/m^2]	Deterministic	0	0
$\phi_{blanket}$	Friction angle of blanket material [deg]	Normal	28	4.5

Table A3 Standard parameters of the aquifer layer for the dikes in the hypothetical case-study

Symbol	Description	Distribution	Parameters	
			μ	σ
$d_{aquifer}$	Aquifer layer thickness [m]	Deterministic	30	
$\gamma_{sat,aquifer}$	saturated volumetric weight of the aquifer layer [kN/m^3]	Normal	18	0.1
η	drag factor/White's coefficient [-]	Deterministic	0.25	
θ	bedding angle [rad]	Deterministic	0.61	
d_{70}	70%-percentile of the grain size distribution [m]	Lognormal	3.07E-04	4.61E-05
$k_{aquifer}$	specific conductivity aquifer [m/s]	Lognormal	4.86E-04	2.82E-04
$ch_{aquifer}$	cohesion of aquifer material [kN/m^2]	Deterministic	0	0
$\phi_{aquifer}$	Friction angle of aquifer material [deg]	Deterministic	31.3	4.5

Table A4 Standard parameters for the dike soil material for the dikes in the hypothetical case-study

Symbol	Description	Distribution	Parameters	
			μ	σ
$\gamma_{sat,core}$	saturated volumetric weight of the dike core [kN/m^3]	Normal	18.2	0.1
$\gamma_{dry,core}$	dry volumetric weight of the core [kN/m^3]	Normal	13.1	0.1
ch_{core}	cohesion of core material [kN/m^2]	Deterministic	0	0
ϕ_{core}	Friction angle of core material [deg]	Normal	33	4.5

Table A5 Standard hydraulic load and resistance parameters for the dikes in the hypothetical case-study

Symbol	Description	Distribution	Parameters		Source
			μ	σ	
ρ_w	density of water [kg/m^3]	Normal	1000	1	Known constant
h	water level [m] above REF	Generalized extreme value	-2.5	σ =1.5, ξ= -0.17	Assumed
γ_{break}	breaker index of waves [-]	Normal	0.425	0.075	Estimated (van der Meer et al., 2016;TAW, 2002)
γ_f	roughness factor for an outer slope with grass [-]	Deterministic	1	-	(van der Meer et al., 2016;TAW, 2002)
u_v	hourly wind speed at 10 m above the surface [m/s]	Gumbel	16.8	1.6	Assumed
F_{max}	fetch [m]	Deterministic	1800		Assumed
q_c	critical overtopping discharge [l/m/s]				(van Hoven, 2015)
	- No house (closed grass cover)	Lognormal	100	120	
	- Intact house (open grass cover)	Lognormal	70	80	
	- Collapsed house (no major overtopping allowed)	Lognormal	0.1	-	

Table B1 Description and values of variables in the overtopping and overflow limit state function

Variable	Description	Note
α_{out}	Outer slope angle [-]	-
γ_f	Friction factor for the outer slope [-]	1 (TAW, 2002)
H_s	Significant wave height [m]	See Eq. (B6)
ξ_0	Iribaren number [-]	See Eq. (B8)
c_1	Factor for overtopping [-]	Normally distributed with μ=4.75 and σ=0.5 (TAW, 2002)
c_2	Factor for overtopping [-]	Normally distributed with μ=-0.92 and σ=0.24 (TAW, 2002)
$m_{Bret,H}$	Model factor for Bretschneider equation	Lognormally distributed with μ=1 and σ=0.27 (Diermanse, 2016)
$m_{Bret,T}$	Model factor for Bretschneider equation	Lognormally distributed with μ=1 and σ=0.13 (Diermanse, 2016)

5   **Table C1 Description and values of variables in the piping limit state function**

Variable	Description	Destribution	Parameters	Unit
γ_p	specific weight of sand particles	Deterministic	26	$\frac{kN}{m^3}$
γ_w	specific weight of water	Deterministic	10	$\frac{kN}{m^3}$
η	drag factor	Deterministic	0.25	-
θ	bedding angle [°]	Deterministic	35	-
$\frac{RD}{RD_m}$	Relative density of the material compared to small-scale piping experiments	Determinsistic	1	-
d_{70m}	Reference d_{70} of the material used in small-scale piping experiments	Determinsistic	$2 * 10^{-4}$	m
m_p	Model factor for piping	Lognormal	$\mu = 1, \sigma = 0.12$	-