



- 1 A Study of Earthquake Recurrence based on a One-body
- 2 Spring-slider Model in the Presence of Thermal-pressurized
- 3 Slip-weakening Friction and Viscosity
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11 Abstract Earthquake recurrence is studied from the temporal variation in slip 12 through numerical simulations based on the normalized form of equation of motion of 13 a one-body spring-slider model with thermal-pressurized slip-weakening friction and 14 viscosity. The main parameters are the normalized characteristic displacement,  $U_c$ , of 15 the friction law and the normalized damping coefficient (to represent viscosity),  $\eta$ . 16 Define  $T_R$ , D, and  $\tau_D$  to be the recurrence time of events, the final slip of an event, 17 and the duration time of an event, respectively. Simulation results show that  $T_R$ 18 increases when  $U_c$  decreases or  $\eta$  increases; D and  $\tau_D$  decrease with increasing  $\eta$ ; and 19  $\tau_D$  increases with  $U_c$ . The time- and slip-predictable model can describe the temporal variation in cumulative slip. When the wear process is taken into account, the 20 21 thickness of slip zone, h which depends on the cumulated slip,  $S(t) = \sum D(t)$ , i.e., 22 h(t) = CS(t) (C=a dimensionless constant) is an important parameter on  $T_R$  and D.  $U_c$  is 23 a function of h and thus depends on C. In the computational time period, the wear 24 process influences the recurrence of events and such an effect increases with C when





- C>0.0001. Both  $T_R$  and D decrease when the fault becomes more mature, thus suggesting that it is more difficult to produce large earthquakes along a fault when it becomes more mature. Neither the time-predictable model nor the slip-predictable one can describe the temporal variation in S(t) under the wear process with large C.
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Key Words: Recurrence of events, final slip, rise time, one-body spring-slider
 model, thermal-pressurized slip-weakening friction, characteristic displacement,
 viscosity, wear process

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#### 35 **1 Introduction**

36 Earthquake recurrence that is relevant to the physics of faulting is an important 37 factor in seismic hazard assessment. It is related to the seismic cycle, which represents the occurrence of several earthquakes in the same segment of a fault during a time 38 39 period. Fig. 1 exhibits the general pattern of time variation in slip during a seismic 40 cycle. In the figure,  $T_R$  is the recurrence (also denoted by repeat or inter-event) time 41 of two events in a seismic cycle,  $\tau_D$  is the duration time of slip of an event, and D is 42 the final slip of an event. Sykes and Quittmeyer (1981) pointed out that the major 43 factors in controlling  $T_R$  are the plate moving speed and the geometry of the rupture 44 zone. Based on Reid's elastic rebound theory (Reid, 1910), Schwartz and 45 Coppersmith (1984) assumed that an earthquake occurs when the tectonic shear stress 46 on a fault is higher than a critical level, which is dependent on the physical conditions 47 of the fault and the loading by regional tectonics. Since in their work a fault has a homogeneous distribution of physical properties under constant tectonic loading, 48 49 earthquakes could happen regularly.





50	Some observations exhibit periodicity for different size earthquakes. Bakun and
51	McEvilly (1979) obtained $T_R \approx 23\pm 9$ years for M $\approx 6$ earthquakes at the Parkfield
52	segment of the San Andreas fault, USA since 1857. Sykes and Menke (2006)
53	estimated $T_R \approx 100$ years for $M \ge 8$ earthquakes in the Nankaido trough, Japan. Okada et
54	al. (2003) gained $T_R=5.5\pm0.7$ years for earthquakes with $M=4.8\pm0.1$ off Kamaishi,
55	Japan, since 1957. Nadeau and Johnson (1998) inferred an empirical relation between
56	$T_R$ and seismic moment, $M_o$ : $T_R \propto M_o^{1/6}$ . To make this relation valid, the stress drop,
57	$\Delta \sigma$ , or the long-term slip velocity of a fault, $v_l$ , must be in terms of $M_o$ . Based on
58	three data set from eastern Taiwan, Parkfield, USA, and northeastern Japan, Chen et
59	al. (2007) inferred $T_R \sim M_o^{0.61}$ . Beeler et al. (2001) proposed a theoretical relation:
60	$T_R = \Delta \sigma^{2/3} M_o^{1/3} / 1.81 \mu v_l$ , where $\mu$ is the rigidity of the fault-zone materials, under
61	constant $\Delta \sigma$ and $v_l$ .

However, the main factors in influencing earthquake occurrences commonly are 62 spatially heterogeneous and also vary with time. Thus, the recurrence times of 63 earthquakes, especially large events, are not constant inferred either from observations 64 65 (Ando, 1975; Sieh, 1981; Kanamori and Allen, 1986; Wang and Kuo, 1998; Wang, 2005; Sieh et al., 2008) or from modeling (Wang, 1995, 1996; Ward, 1996, 2000; 66 67 Wang and Hwang, 2001). Kanamori and Allen (1986) observed that faults with longer 68  $T_R$  are stronger than those with shorter  $T_R$ . Davies et al. (1989) proposed that the 69 longer it has been since the last earthquake, the longer the expected time till the next. 70 Wang and Kuo (1998) observed that for  $M \ge 7$  earthquakes in Taiwan  $T_R$  strongly 71 follows the Poissonian processes. Enescu et al. (2008) found that the distribution of 72  $T_R$  can be described by an exponential function. From the estimated values of  $T_R$  of 73 earthquakes happened on the Chelungpu fault in central Taiwan from trenching data, 74 Wang (2005) found that the earthquakes occurred non-periodically.







In order to interpret earthquake recurrences, Shimazaki and Nakata (1980) 75 76 proposed three simple phenomenological models. Each model has a constantly 77 increasing tectonic stress that is controlled by a critical stress level,  $\sigma_c$ , for failure and 78 a base stress level,  $\sigma_b$ . The three models are: (1) the perfectly periodic model (with 79 constant  $\sigma_c$ ,  $\sigma_b$ , and  $\Delta\sigma$ ; (2) the time-predictable model (with constant  $\sigma_c$ , variable 80  $\sigma_b$ , and variable  $\Delta \sigma$ ); and (3) the slip-predictable model (with variable  $\sigma_c$ , constant  $\sigma_b$ , 81 and variable  $\Delta \sigma$ ). For the first model, both  $T_R$  and D of next earthquake can be 82 predicted from the values of  $T_R$  or D of previous ones. For the second model,  $T_R$  of 83 next earthquake can be predicted from the values of D of previous ones. For the third 84 model, D of next earthquake can be predicted from the values of  $T_R$  of previous ones. 85 However, debates about the three models have been made for a long time. Some 86 examples are given below. Ando (1975) suggested that the second model worked for 87 post-1707 events, yet not for pre-1707 ones in the Nankaido trough, Japan. Wang 88 (2005) assumed that the second model could describe the earthquakes occurred on the 89 Chelungpu fault, Taiwan in the past 1900 years. For the Parkfield earthquake 90 sequence, Bakun and McEvilly (1984) took different models; while Murray and 91 Segall (2002) considered the failure of the second model. From laboratory results, 92 Rubinstein et al. (2012) assumed the failure of the time- and slip-predictable models 93 for earthquakes.

94 Some models, for instance the crack model and dynamical spring-slider model, 95 have been developed for fault dynamics, even though the seismologists have not a 96 comprehensive model. There are several factors in controlling fault dynamics and 97 earthquake ruptures (see Bizzarri, 2009; Wang, 2017b). Among the factors, friction 98 (Nur, 1978; Belardinelli and Belardinelli, 1996) and viscosity (Jeffreys, 1942; Spray, 99 1993; Wang, 2007) are two significant ones.





100 Modeling earthquake recurrence based on different models has been long made and 101 is reviewed by Bizzarri (2012a,b) and Franović et al. (2016). Among the models, the 102 spring-slider model has been used to study fault dynamics and earthquake physics 103 (see Wang 2008). Burridge and Knopoff (1967) proposed the one-dimensional 104 N-body model (abbreviated as the 1-D BK model henceforth). Wang (2000, 2012) 105 extended the 1-D model to 2-D one. The one-, two-, three-, and few-body models with 106 various friction laws have also been applied to approach fault dynamics (see Turcotte, 1992). The studies for various friction laws based on spring-slider models are briefly 107 108 described below: (1) for rate- and state-dependent friction (e.g., Rice and Tse, 1986; 109 Ryabov and Ito, 2001; Erickson et al., 2008, 2011; He et al., 2003; Mitsui and 110 Hirahara, 2009; Bizzarri, 2012a; Abe and Kato, 2013;Kostić et al., 2013a; Bizzarri 111 and Crupi, 2014; Franović et al., 2016); (2) for velocity-weakening friction (e.g., 112 Carlson and Langer, 1989; Huang and Turcotte, 1992; Brun and Gomez, 1994; Wang 113 and Hwang, 2001; Wang, 2003; Kostić et al., 2013b); (3) for simple static/dynamic 114 friction (e.g., Abaimov et al., 2007; Hasumi, 2007).

115 Some results concerning earthquake recurrence are simply explained below. 116 Erickson et al. (2008) suggested that aperiodicity in earthquake dynamics is due to 117 either the nonlinear friction law (Huang and Turcotte, 1990) or the heterogeneous 118 stress distribution (Lapusta and Rice, 2003). Wang and Hwang (2001) emphasized the importance of heterogeneous frictional strengths. Mitsui and Hirahara (2009) pointed 119 120 out the effect of thermal pressurization. Dragoni and Piombo (2011) found that 121 variable strain rate causes aperiodicity of earthquakes. Bizzarri and Crupi (2014) 122 found that  $T_R$  is dependent on the loading rate, effective normal stress, and 123 characteristic distance of the rate- and state-dependent friction law.





- As mentioned previously, numerous studies have been made for exploring the frictional effect on earthquake recurrence. But, the study concerning the viscous effect on earthquake recurrence is rare. In the followings, we will investigate the effects of slip-weakening friction due to thermal-pressurization and viscosity on earthquake recurrence based on the one-body spring-slider model.
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### 130 2 One-body Model

131 Fig. 2 displays the one-body spring-slider model. In the model, m, K, N, F,  $\eta$ , u, v 132 (=du/dt),  $v_p$ , and  $u_o = v_p t$  denote, respectively, the mass of the slider, the stiffness (or 133 spring constant) of the leaf spring, the normal force, the frictional force between the 134 slider and the moving plate, the damping coefficient (to represent viscosity as 135 explained below), the displacement of the slider, the velocity of the slider, the plate 136 moving speed, and the equilibrium location of the slider. The frictional force F (with 137 the static value of  $F_o$ ) is usually a function of u or v. Viscosity results in the viscous 138 force,  $\Phi$ , between the slider and the moving plate, and  $\Phi$  is in terms of v. A driving 139 force,  $Kv_pt$ , caused by the moving plate through the leaf spring pulls the slider to 140 move. The equation of motion of the model is:

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142 
$$md^2u/dt^2 = -K(u - u_o) - F(u, v) - \Phi(v).$$
 (1)

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144 When  $Kv_p t \ge F_o$ , *F* changes from static frictional force to dynamic one and thus makes 145 the slider move.

The frictional force F(u,v) is controlled by several factors (see Wang, 2016; and cited references therein). An effect combined from temperature and fluids in a fault zone can result in thermal pressurization (abbreviated as TP below) which would yield





149	a shear stress (resistance) on the fault plane (Sibson, 1973; Lachenbruch, 1980; Rice,
150	2006; Wang, 2009, 2011, 2016, 2017a,b,c; Bizzarri, 2009). Rice (2006) proposed two
151	end-member models of TP, i.e., the adiabatic-undrained-deformation (AUD) model
152	and slip-on-a-plane (SOP) model. The latter is not appropriate in this study because of
153	the request of constant velocity. The former is related to a homogeneous simple strain
154	$\varepsilon$ at a constant normal stress $\sigma_n$ on a spatial scale of the sheared layer. Its shear
155	stress-slip function, $\tau(u)$ , is: $\tau(u)=f(\sigma_n-p_o)exp(-u/u_c)$ (Rice, 2006), which decreases
156	exponentially with increasing u. The characteristic displacement is $u_c = \rho_f C_v h/\mu_f \Lambda$ ,
157	where $\rho_f$ , $C_v$ , $h$ , $\mu_f$ , and $\Lambda$ are, respectively, the fluid density, heat capacity (in
158	J/°C/kg), the thickness, frictional strength, and the undrained pressurization factor of
159	the fault zone.

Based on the AUD model, Wang (2009, 2016, 2017a,b,c) took a simplified slip-weakening friction law (denoted by the TP law hereafter):

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163 
$$F(u) = F_o exp(-u/u_c).$$
(2)

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165 An example of the plot of F(u) versus u for five values of  $u_c$ , i.e., 0.1, 0.3, 0.5, 0.7, 166 and 0.9 m, which are taken from Wang (2016), is displayed in Fig. 3. F(u) decreases 167 with increasing u and its decreasing rate,  $\gamma$ , decreases with increasing  $u_c$ . The force 168 drop is lower for larger  $u_c$  than for smaller  $u_c$ . When  $u << u_c$ ,  $exp(-u/u_c) \approx 1 - u/u_c$ , thus 169 indicating that  $u_c^{-1}$  is almost  $\gamma$  at small u. This TP law is used in this study.

170 A detailed description about viscosity and the viscous force  $\Phi(v)$  can be found in 171 Wang (2016), and only a brief explanation is given below. Jeffreys (1942) first and 172 then numerous authors (Byerlee, 1968; Turcotte and Schubert, 1982; Scholz, 1990; 173 Rice et al., 2001; Wang, 2016) emphasized the viscous effect on faulting due to





174 frictional melts. The viscosity coefficient, v, of rocks is influenced by T (see Turcotte 175 and Schubert, 1982; Wang, 2011). Spray (2005; and cited references therein) observed 176 a decrease in v with increasing T. He also stressed that frictional melts with low v177 could produce a large volume of melting, thus reducing the effective normal stress. 178 This behaves like fault lubricants during seismic slip.

179 The physical models of viscosity can be found in several articles (e.g., Cohen, 1979; 180 Hudson, 1980). The stress-strain relationship is  $\sigma = E\varepsilon$  where  $\sigma$  and E are, respectively, 181 the stress and the elastic modulus for an elastic body and  $\sigma = v(d\varepsilon/dt)$ , where v is the 182 viscosity coefficient, for a viscous body. Two simple models with a viscous damper 183 and an elastic spring are often used to describe the viscous materials. A viscous 184 damper and an elastic spring are connected in series leading to the Maxwell model 185 and in parallel resulting in the Kelvin-Voigt model (or the Voigt model). According to 186 Hudson (1980), Wang (2016) proposed that the latter is more suitable than the former 187 for seismological problems and thus the Kelvin-Voigt model, whose constitution law is  $\sigma(t) = E\varepsilon(t) + \upsilon d\varepsilon(t)/dt$ , is taken here and displayed in Fig. 2. The viscous stress is  $\upsilon v$ . 188 189 In order to investigate the viscous effect in a dynamical system, Wang (2016) 190 defined the damping coefficient,  $\eta$ , based on the phenomenon that an oscillating body 191 damps in viscous fluids. According to Stokes' law,  $\eta = 6\pi R \upsilon$  for a sphere of radius R in 192 a viscous fluid of v (see Kittel et al., 1968). Hence, the viscous force in Equation 1 is 193 represented by  $\Phi = \eta v$ . Note that the unit of  $\eta$  is N(m/s)<sup>-1</sup>.

Some authors (Knopoff et al., 1973; Cohen, 1979; Rice, 1993; Xu and Knopoff,
195 1994; Knopoff and Ni, 2001; Bizzarri, 2012a; Dragoni and Santini, 2015) considered
that viscosity plays a role on causing seismic radiation to release strain energy during
faulting.





# 199 **3 Normalization of Equation of Motion**

- 200 Putting Eq. 2 and  $\Phi = \eta v$  into Eq. 1 leads to
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$$md^2u/dt^2 = -K(u - v_p t) - F_o exp(-u/u_c) - \eta v.$$
 (3)

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Eq. 3 is normalized for easy numerical computations based on the normalization parameters, which is dimensionless:  $D_o = F_o/K$ ,  $\omega_o = (K/m)^{1/2}$ ,  $\tau = \omega_o t$ ,  $U = u/D_o$ , and  $U_c = u_c/D_o$ . The normalized velocity, acceleration, and driving velocity are  $V = dU/d\tau =$  $[F_o/(mK)^{1/2}]^{-1}du/dt$ ,  $A = d^2U/d\tau^2 = (F_o/m)^{-1}d^2u/dt^2$ , and  $V_p = v_p/(D_o\omega_o)$ , respectively. Define  $\Omega = \omega/\omega_o$  to be the dimensionless angular frequency, and thus the phase  $\omega t$ becomes  $\Omega \tau$ . For the purpose of simplification,  $\eta/(mK)^{1/2}$  is denoted by  $\eta$  below. Substituting all normalization parameters into Eq. 3 leads to

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212 
$$d^2 U/d\tau^2 = -U - \eta dU/d\tau - exp(-U/U_c) + V_p \tau.$$
(4)

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214 In order to numerically solve Eq. (4), we define two new parameters, i.e.,  $y_1 = U$  and 215  $y_2 = dU/d\tau$ . Eq. 4 can be re-written as two first-order differential equations:

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$$217 dy_1/d\tau = y_2 (5a)$$

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219 
$$dy_2/d\tau = -y_1 - \eta y_2 - exp(-y_1/U_c) + V_p \tau.$$
 (5b)

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We can numerically solve Eq. 5 by using the fourth-order Runge-Kutta method (Press et al., 1986). Because of  $v_p \approx 10^{-10}$  m/s,  $V_p$  must be much smaller than 1. To shorten the





223 computational times,  $V_p$  is taken to be 10<sup>-2</sup>. The backward slip is not allowed in the

simulations, because of common behavior of forward earthquake ruptures.

225 A phase portrait, which is a plot of a physical quantity, y, versus another, x, i.e., 226 y=f(x), is commonly used to represent nonlinear behavior of a dynamical system 227 (Thompson and Stewart, 1986). The intersection point between f(x) and the bisection line of y=x, is defined as the fixed point, that is, f(x)=x. If f(x) is continuously 228 229 differentiable in an open domain near a fixed point  $x_f$  and  $|f'(x_f)| < 1$ , attraction can 230 appear at the fixed point. Chaos can also be generated at some attractors. The details 231 can be seen in Thompson and Stewart (1986). In this study, the phase portrait is the 232 plot of  $V/V_{max}$  versus  $U/U_{max}$ .

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#### 234 **4 Simulation Results**

235 The results of numerical simulations are shown in Figs. 4-12. The temporal 236 variations in  $V/V_{max}$  (displayed by thin solid lines) and cumulative slip  $\Sigma U/U_{max}$ 237 (displayed by solid lines) are displayed in the left-handed-side panels; while the phase 238 portraits of  $V/V_{max}$  versus  $U/U_{max}$  (displayed by solid lines) are shown in the right-239 handed-side panels. Because the maximum values of both V and U decrease from case 240 (a) to case (d), denote the maximum velocity and maximum displacement for case (a) 241 of each figure are denoted by, respectively,  $V_{max}$  and  $U_{max}$  which are taken as a factor 242 in scaling the waveforms from case (a) to case (d). In the right-handed-side panels of 243 Figs. 4–12, the dashed line represents the bisection line.

The cases not including the viscous effect, i.e.,  $\eta=0$ , are first simulated and results are shown in Fig. 4 for four values of  $U_c$ : (a) for  $U_c=0.2$ ; (b) for  $U_c=0.4$ ; (c) for  $U_c=0.8$ ; and (d) for  $U_c=1.0$ . The results of the cases including viscosity, i.e.,  $\eta\neq 0$ , are displayed in Figs. 5–7 for four values of  $\eta$ : (a) for  $\eta=0.20$ ; (b) for  $\eta=0.40$ ; (c) for





- 248  $\eta$ =0.6; and (d) for  $\eta$ =0.8. The values of  $U_c$  are 0.20 in Fig. 5, 0.50 in Fig. 6, and 0.80
- 249 in Fig. 7.

250 Figs. 4–7 show that when  $U_c$  and  $\eta$  are constants during the computational time 251 periods, the general patterns of temporal variations in cumulated slip do not change. 252 Some of the previous studies suggest that the patterns of temporal variations in 253 cumulated slip can change with time. The changes of  $U_c$  and  $\eta$  with time should play 254 the main roles. From  $u_c = \rho_f C_V h/\mu_f \Lambda$  of the TP model (see Rice 2006), the width of the 255 slipping zone, h, where the maximum deformation is concentrated (Bizzarri, 2009), is 256 a significant parameter in this study. The reasons to select h to be the main factor are 257 explained below in the section of "Discussion.". From geological surveys, Rathbun 258 and Marone (2010) observed that h is not spatially uniform even within a single fault. 259 Hull (1988) and Marrett and Allmendinger (1990) found that the wear processes 260 occurring during faulting could widen h, and thus h could vary with time. According 261 to the results gained by several authors (e.g., Power et al., 1988; Robertson, 1983; and 262 Bizzarri, 2010), Bizzarri (2012b) assumed that h is linearly dependent on the 263 cumulated slip,  $S(t) = \sum D(t)$ , and can be represented by h(t) = CS(t) where C is a 264 dimensionless constant. Since  $u_c$  is proportional to h and  $U_c = u_c/D_o$ ,  $U_c$  is proportional to C. This means that the more mature the fault is, the thicker its slip 265 266 zone is. Simulation results for four values of C are shown in Figs. 8-12: (a) for 267 C=0.0001; (b) for C=0.001; (c) for C=0.01; and (d) for C=0.05 when  $U_c=0.1$  and  $\eta=0$ 268 in Fig. 8, when  $U_c=0.5$  and  $\eta=0$  in Fig. 9, when  $U_c=0.9$  and  $\eta=0$  in Fig. 10, when 269  $U_c=0.1$  and  $\eta=1$  in Fig. 11, and when  $U_c=0.5$  and  $\eta=1$  in Fig. 12.

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### 271 5 Discussion

272 The left-handed-side panels in Fig. 4 with  $\eta=0$  show that the peak velocity,  $V_m$ , and





273	final slip, $D$ , with the respective maximum values in case (a) as mentioned above, for
274	all simulated events decrease with increasing $U_c$ . From Fig. 3, the force drop, $\Delta F$ ,
275	decreases with increasing $U_c$ , thus indicating that larger $\Delta F$ yields higher $V_m$ and
276	larger <i>D</i> . This interprets the negative dependence of $V_m$ and <i>D</i> on $U_c$ . The value of $\tau_D$
277	increases with $U_c$ ; while $T_R$ decreases with increasing $U_c$ . When $U_c=1$ , $V_m$ and $D$ are
278	both very small and the system behaves like creeping of a fault. In the right-handed-
279	side panels, there are two fixed points: one at $V=0$ and $U=0$ and the other at larger V
280	and larger $U$ . The slope values at the two fixed points decrease with increasing $U_c$ ,
281	thus suggesting that the fixed point is not an attractor for small $U_c$ and can be an
282	attractor for larger $U_c$ . The phase portrait for $U_c=1$ is very tiny, because the final slip
283	for $U_c=1.0$ is much smaller than those for $U_c=0.2$ , 0.4, and 0.8. Hence, $U_c=1$ will not
284	be taken into account in the following simulations.

285 The left-handed-side panels in Figs. 5–7 show that  $V_m$  and D decrease when either  $U_c$  or  $\eta$  increases; while  $\tau_D$  increases with  $\eta$  and  $U_c$ . Meanwhile,  $T_R$  increases when 286 287 either  $\eta$  increases or  $U_c$  decreases. The right-handed-side panel exhibits that the 288 phase portraits are coincided for all simulated events for a certain  $\eta$ . There are two fixed points for each case: one at V=0 and U=0 and the other at larger V and larger U. 289 290 The slope values at the two fixed points decrease when either  $U_c$  or  $\eta$  increases. This 291 suggests that the fixed point is not an attractor for small  $U_c$  and low  $\eta$ , and can be an 292 attractor for large  $U_c$  and high  $\eta$ . Clearly, the final slip is shorter for  $U_c=0.9$  than for 293  $U_c = 0.1$  and 0.5.

From Figs. 5–7, we can see that the temporal variation in cumulative slip can be described by the perfectly periodic model as mentioned above. Hence, when  $U_c$  and  $\eta$ do not change with time, the rate of cumulative slip retains a constant in the computational time period. This is similar to the simulation results with the periodical





298 earthquake occurrences obtained by some authors (e.g., Rice and Tse, 1986; Ryabov 299 and Ito, 2001; Erickson et al., 2008; Mitsui and Hirahara, 2009) based on the 300 one-body model with rate- and state-dependent friction or velocity- weakening 301 friction. But, the present result is inconsistent with the simulation results, from which 302 either the time-predictable model or the slip-predictable model cannot interpret the 303 temporal variation in cumulative slip, based on the same model obtained by others 304 (e.g., He et al., 2003; Bazzarri 2012b; Bizzarri and Crupi, 2014; Kostić et al., 2013a,b; 305 Franović et al., 2016). The differences between the two groups of researchers might 306 be due to distinct additional constrains in respective studies. Although the detailed 307 discussion of such differences is important and significant, it is out of the scope of this 308 study and ignored here.

309 The phase portraits shown in the right-handed-side panels of Figs. 5–7 exhibit that 310 the period related to  $T_R$  and the size associated with D decrease with increasing h. 311 This is similar to that obtained from the left-handed-side panels. There are two fixed 312 points for each case: one at larger V and larger U and the other at V=0 and U=0. The 313 slope values of the fixed point at larger V and larger U are higher than 1 and decreases 314 with increasing  $\eta$ . This means that larger  $\eta$  is easier to generate chaos than small  $\eta$ . 315 However, the reducing rate of slop value decreases with increasing  $U_c$ . The slope 316 values of the fixed point at V=0 and U=0 are higher than 1 and only decrease with 317 increasing  $\eta$ . This suggests that the fixed points at V=0 and U=0 can be an attractor. 318 This behavior becomes weaker when  $U_c$  increases.

The previous study demonstrates that when  $U_c$  and  $\eta$  are constants during the computational time periods, the general patterns of temporal variations in cumulated slip cannot change. In order to investigate the effects on the patterns of temporal variations in cumulated slip, we must consider changes of  $U_c$  and  $\eta$  with time. The





323 viscosity coefficient can actually vary immediately before and after the occurrence of 324 an earthquake (see Spray, 1883, 2005; Wang, 2017b,c). But, a lack of long-term 325 variation in  $\eta$  does not allow us to explore its possible effect on the change of general 326 patterns of temporal variations in cumulated slip. Here, only the possible effect due to 327 time-varying  $U_c$ .

328 As mentioned above,  $U_c$  is  $u_c/D_o$  and thus  $U_c = \rho_f C_v h/\mu_f D_o A$ , where A =329  $(\lambda_f - \lambda_n)/(\beta_f + \beta_n)$  (Rice, 2006). Obviously,  $U_c$  is controlled by six factors, i.e.,  $\rho_f$ ,  $C_V$ , h, 330  $\mu_{f}$ ,  $D_{o}$ , and  $\Lambda$ . Since the tectonics of a region is generally stable during a long time, 331 the value of  $D_o = F_o/K$  could not change too much and thus would not influence  $U_c$ . 332 The Debye law (cf. Reif, 1965) gives  $C_{v} \sim (T+273.16)^3$ , where 273.16 is the value to 333 convert temperature from Celsius to Kelvin, at low T and  $C_{\nu} \approx \text{constant}$  at high T. The 334 threshold temperature, from which  $C_{\nu}$  begins to approach a constant, is 200–300 °K. 335 In this study,  $C_{\nu}$  is almost a constant because of T>250 °C=523.16 °K, which is the average ambient temperature of fault zone with depths ranging from 0 to 20 km. 336 337 Hence,  $C_{\nu}$  is almost constant during a long time and thus cannot influence  $U_c$ .

338 The frictional strength,  $\mu_f$ , is influenced by several factors including humidity, 339 temperature, sliding velocity, strain rate, normal stress, thermally activated rheology 340 etc (Marone, 1998; Rice, 2006), and thus can change with time (Sibson, 1992; Rice, 341 2006). Hirose and Bystricky (2007) observed that serpentine dehydration and 342 subsequent fluid pressurization due to co-seismic frictional heating may reduce  $\mu_f$  and 343 thus promote further weakening in a fault zone. The pore fluid pressure exists in wet 344 rocks, yet not in dry rocks. Clearly, the time variation in  $\mu_f$  can affect the earthquake 345 recurrences. However, a lack of long-term observations of  $\mu_f$  during a seismic cycle 346 makes the studies of its effect on earthquake recurrence be impossible.

347 The fluid density  $\rho_f$  and the porosity n depend on T and p. Although there are





348 numerous studies on such dependence (Lachenbruch, 1980; Bizzarri, 2012b; and cited

references therein), observed data and theoretical analyses about the values of  $\rho_f$  and n

350 during a seismic cycle are rare.

351 The porosity is associated with the permeability,  $\kappa$ . Bizzarri (2012c) pointed out 352 that the time-varying permeability,  $\kappa(t)$ , and porosity of a fault zone (cf. Mitsui and Cocco, 2010; Bizzarri, 2012b) can reduce  $T_R$ . One of the Kozeny–Carman's (KC) 353 354 relations (Costa, 2006; and references cited therein) is:  $\kappa(t) = \kappa c \phi^2(t) d^3(t) / [1 - \phi(t)]^2$ , 355 where  $\kappa_{\rm C}$  is a dimensionless constant depending on the material in consideration;  $\phi$  is 356  $V_{voids}/V_{tot}$  where  $V_{voids}$  and  $V_{tot}$  are, respectively, the pore volume and the total volume 357 of the porous materials; and d is the (average) diameter of the grains, ranging between  $4 \times 10^{-5}$  m and  $1 \times 10^{-4}$  m (Niemeijer et al., 2010). Usually,  $\kappa$ ,  $\phi$ , and d can vary in the 358 fault zone (Segall and Rice, 1995). After faulting  $\kappa$  and  $\phi$  would change and d 359 360 becomes smaller because of refining of the grains. According to this relation, Bizzarri 361 (2012b) found that  $\kappa(t)$  could significantly reduce  $T_R$  in comparison with the base 362 model with constant  $\kappa$ . The reason is explained below. The time-varying permeability 363 can result in the time-varying pore pressure,  $p_f$ . This can reduce the frictional resistance from  $\tau = \mu(\sigma_n p_f)$  and thus could trigger earthquakes earlier. Hence, the 364 365 time-varying permeability can change  $T_R$ . Nevertheless, we cannot investigate its 366 influence on earthquake recurrence here because there is a lack of a long-term 367 observation of hydraulic parameters during a seismic cycle.

It is significant to explore the factors that can yield a non-perfectly periodic seismic cycle. The width of the slipping zone, h, can be a candidate as pointed out by some authors (e.g., Bizzarri, 2009; Rathbun and Marone, 2010). Since the displacement along a fault is controlled by the fault rheology, h should depend on the rheology on the sliding interface. The wear processes occurring during faulting could widen h





(Hull, 1988; Marrett and Allmendinger, 1990). According to the results gained by 373 374 several authors (e.g., Power et al., 1988; Robertson, 1983; and Bizzarri, 2010), 375 Bizzarri (2012b) proposed a linear dependence of h on the cumulated slip,  $S(t) = \sum D(t)$ , 376 i.e., h(t) = CS(t) where C is a dimensionless constant. When the slip zone is thicker, the 377 fault should be more mature. Since  $U_c$  is a function of h,  $U_c = u_c/D_o = \rho_f C_v h/\mu_f A D_o$  is 378 also proportional to C and thus  $U_c$  increases with C. Hence, numerical simulations for 379 various values of C and the results are shown in Figs. 8–12, which are different from 380 Figs. 4–8 especially for large C.

381 The left-handed-side panels of Figs. 8–12 show that  $V_m$ , D,  $\tau_D$ , and  $T_R$  are all 382 similar when C  $\leq$  0.001; while their values are larger for C = 0.01 than for C = 0.05 and 383 also decrease with time. A decrease in D is particularly remarkable when  $C \ge 0.01$ . 384 When C=0.05 or h is wider than a critical value, normal earthquakes cannot occur and 385 only creeping can happen. Obviously,  $T_R$  decreases with increasing C, thus leading to 386 an decrease in  $T_R$  with increasing h. This is similar to the result obtained by Bizzarri 387 (2010; 2012b). As mentioned above, the fault should be more mature when the slip 388 zone is thicker. Consequently, both  $T_R$  and D decrease when the fault becomes more 389 mature. This might suggest that it is more difficult to produce large earthquakes along 390 a fault when it becomes more mature. This implicates that seismic hazard is higher for a young fault than a mature one. This sounds physically reasonable. Meanwhile, 391 392 either the time- or slip- predictable model can only describe the temporal variations of 393 cumulative slip in the earlier time period, yet not in the later one.

The right-handed-side panels of Figs. 8–12 exhibit that the phase portraits for C=0.001 are slightly different from those for C=0.0001 even though the patterns of their variations in V and U are similar; while the phase portraits for C>0.001 are different from those for  $C\leq0.001$ . An increase in h due to an increase in C with





398	cumulative slip enlarges $U_c$ . This can be explained from Fig. 3 which shows that
399	larger $U_c$ yields a lower $\Delta F$ than smaller $U_c$ . Hence, an increase in $U_c$ produces a
400	decrease in $\Delta F$ , thus resulting in low $V_m$ and small $D$ . In addition, An increase in $U_c$
401	makes $exp(-U/U_c)$ approach unity, especially for small U, thus reducing the nonlinear
402	effect caused by TP friction.
403	Unlike Figs. 4–7, the size of phase portraits in the right-handed-side panels of Figs.
404	8–12 decreases with increasing C. This reflects a decrease in $T_R$ and D of events with
405	increasing $C$ as mentioned previously. In the phase portraits, there are two fixed
406	points for each case: one at larger V and larger U and the other at V=0 and U=0. The

slope values at the fixed point at larger *V* and larger *U* are higher than 1 and only slightly decreases with time when  $C \le 0.01$ ; while the values remarkably decrease with time when C = 0.05. The slope values at the fixed point at V = 0 and U = 0 are higher than

410 1 and only slightly decreases with time when  $\underline{C} \le 0.01$ ; while those decrease with time 411 and finally approaches unity when C=0.05. Results suggest that the fixed points at 412 larger V and larger U for all cases in study are not an attractor; and those at V=0 and 413 U=0 can evolve to an attractor with time when C=0.05. The phenomenon for C=0.05414 is more remarkable and the evolution is faster for large  $U_c$  than for small  $U_c$ .

415

## 416 6 Conclusions

To study the frictional and viscous effects on earthquake recurrence, numerical simulations of the temporal variations in cumulative slip have been conducted based on the normalized equation of a one-body model in the presence of thermalpressurized slip-weakening friction and viscosity. The major model parameters of friction and viscosity are represented, respectively, by  $U_c$  and  $\eta$ , where  $U_c=u_c/D_o$  is the normalized characteristic distance and  $\eta$  is the normalized damping coefficient.





- 423 Numerical simulation of the time variations in  $V/V_{max}$  and cumulative slip  $\Sigma U/U_{max}$ ,
- 424 the phase portrait of  $V/V_{max}$  versus  $U/U_{max}$ , and the phase portrait of  $exp(-U/U_c)$  versus
- 425  $U/U_{max}$  are made for various values of  $U_c$  and  $\eta$ .

426 Results exhibit that both friction and viscosity remarkably affect earthquake 427 recurrence. The recurrence time,  $T_R$ , increase when  $\eta$  increases or  $U_c$  decreases. The 428 final slip, D, and the duration time of slip,  $\tau_D$ , of an event slightly decrease when  $\eta$  or 429  $\tau_D$  increases and slightly increases with  $U_c$ . Considering the effect due to wear process, 430 the thickness of slip zone, h that depends on the cumulated slip,  $S(t) = \sum D(t)$ , i.e., 431 h(t)=CS(t) (C=a dimensionless constant), is an important factor in influencing 432 earthquake recurrences. Because of  $U_c = \rho_f C_v h/\mu_f \Lambda D_o$ ,  $U_c$  increases with C. When 433 C>0.0001, the wear process influences the recurrence of slip and the effect increases 434 with C. When the slip zone is thicker, the fault should be more mature and  $T_R$ 435 increases. Hence, both  $T_R$  and D decrease when the fault becomes more mature. This 436 might suggest that it is more difficult to produce large earthquakes along a fault when 437 it becomes more mature. The temporal variation in slip cannot be interpreted by the 438 time-predictable or slip-predictable model when the fault is affected by wear process 439 with large C. In addition, the size of phase portrait of V/Vmax versus U/Umax decreases 440 with increasing C. This reflects a decrease in  $T_R$  and D of events with increasing C as 441 inferred from the temporal variations in cumulative slip.

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Figure 1. A general pattern of time variation in slip during a seismic cycle:  $T_R$ =the recurrence time or the inter-event time of two events in a seismic cycle;  $\tau_D$ =the duration time of slip of an event; and D=the final slip of an event.







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Figure 2. One-body spring-slider model. In the figure,  $t, m, K, \eta, V_p, N, F u$ , and  $u_o$ denote, respectively, the time, the mass of the slider, the spring constant, the damping coefficient, the driving velocity, the normal force, the frictional force, displacement of the slider, and the equilibrium location of the slider. (after Wang, 2016)

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718 Figure 3. The plots of  $F(u) = exp(-u/u_c)$  versus *u* when  $u_c = 0.1, 0.3, 0.5, 0.7, and 0.9 m$ .

- 719 (after Wang, 2016)







Figure 4. The time variations in  $V/V_{max}$  (thin solid line) and cumulative slip  $\Sigma U/U_{max}$ (solid line) and the phase portrait of  $V/V_{max}$  versus  $U/U_{max}$  (solid line) for four values of  $U_c$ : (a) for  $U_c=0.2$ ; (b) for  $U_c=0.4$ ; (c) for  $U_c=0.8$ ; and (d) for  $U_c=1.0$ when  $\eta=0.0$ .

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Figure 5. The time variations in  $V/V_{max}$  (thin solid line) and cumulative slip  $\Sigma U/U_{max}$ (solid line) and the phase portrait of  $V/V_{max}$  versus  $U/U_{max}$  (solid line) for four values of  $\eta$ : (a) for  $\eta$ =0.2; (b) for  $\eta$ =0.4; (c) for  $\eta$ =0.8; and (d) for  $\eta$ =1.0 when  $U_c$ =0.2.

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750 Figure 6. The time variations in  $V/V_{max}$  (thin solid line) and cumulative slip  $\Sigma U/U_{max}$ 

751 (solid line) and the phase portrait of  $V/V_{max}$  versus  $U/U_{max}$  (solid line) for four

752 values of  $\eta$ : (a) for  $\eta=0.2$ ; (b) for  $\eta=0.4$ ; (c) for  $\eta=0.8$ ; and (d) for  $\eta=1.0$  when 753  $U_c = 0.5.$ 





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758 759 Figure 7. The time variations in  $V/V_{max}$  (thin solid line) and cumulative slip  $\Sigma U/U_{max}$ 760 (solid line) and the phase portrait of  $V/V_{max}$  versus  $U/U_{max}$  (solid line) for four 761 values of  $\eta$ : (a) for  $\eta=0.2$ ; (b) for  $\eta=0.4$ ; (c) for  $\eta=0.8$ ; and (d) for  $\eta=1.0$  when 762  $U_c = 0.8.$ 

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770Figure 8. The time variations in  $V/V_{max}$  (thin solid line) and cumulative slip  $\Sigma U/U_{max}$ 771(solid line) and the phase portrait of  $V/V_{max}$  versus  $U/U_{max}$  (solid line) for four772values of C: (a) for C=0.0001; (b) for C=0.001; (c) for C=0.01; and (d) for773C=0.05 when  $U_c=0.1$  and  $\eta=0$ .







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779 Figure 9. The time variations in  $V/V_{max}$  (thin solid line) and cumulative slip  $\Sigma U/U_{max}$ 780 (solid line) and the phase portrait of  $V/V_{max}$  versus  $U/U_{max}$  (solid line) for four 781 values of C: (a) for C=0.0001; (b) for C=0.001; (c) for C=0.01; and (d) for 782 C=0.05 when  $U_c$ =0.5 and  $\eta$ =0.







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788 Figure 10. The time variations in  $V/V_{max}$  (thin solid line) and cumulative slip  $\Sigma U/U_{max}$ 789 (solid line) and the phase portrait of V/Vmax versus U/Umax (solid line) for four 790 values of C: (a) for C=0.0001; (b) for C=0.001; (c) for C=0.01; and (d) for 791 C=0.05 when  $U_c$ =0.9 and  $\eta$ =0.







797Figure 11. The time variations in  $V/V_{max}$  (thin solid line) and cumulative slip  $\Sigma U/U_{max}$ 798(solid line) and the phase portrait of  $V/V_{max}$  versus  $U/U_{max}$  (solid line) for four799values of C: (a) for C=0.0001; (b) for C=0.001; (c) for C=0.01; and (d) for800C=0.05 when  $U_c$ =0.1 and  $\eta$ =1.







807Figure 12. The time variations in  $V/V_{max}$  (thin solid line) and cumulative slip  $\Sigma U/U_{max}$ 808(solid line) and the phase portrait of  $V/V_{max}$  versus  $U/U_{max}$  (solid line) for four809values of C: (a) for C=0.0001; (b) for C=0.001; (c) for C=0.01; and (d) for810C=0.05 when  $U_c$ =0.5 and  $\eta$ =1.