Development of bridge failure model and fragility curves for road bridges exposed to volcanic laharssinfrastructure overturning and deck sliding due to lahars

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20 **Abstract.** One of the main volcanic processes affecting road infrastructure bridges are lahars, which are flows of water and volcanic material running down the slopes of a volcano and river valleys. Several studies have evidenced the effects of other volcanic processes over road infrastructure, however, limited information is available about the effects of lahars over bridges. In this paper, a model of bridge failure models due to lahars is are proposed and, 25 based on thisthese, fragility curves for infrastructure overturning and deck sliding are developed. The fFailure models considers the limit state of the infrastructure piers and abutments overturning, moment and the tangential force over the deck sliding caused by lahars. Analytical models to estimate these loads awere calibrated to stochastically characterize simulate the effect of lahar loadss and overturning momentum onver bridges for the development of fragility curves. Monte Carlo simulations were are applied to quantify 30 the probability of bridge failure given by different lahar depths. Fragility curves of bridges were are finally parameterized by maximum likelihood estimation, using a cumulative lognormal distribution. Bridge failure models and parameterized fragility curves were successfully validated for a 95 % confidence level are empirically evaluated using data of 15 35 bridges that were reached affected by lahars in the last 50 years. Validated models Developed models evidence that confirm that decks fail mainly due to piers and/or abutments overturning, rather than sliding forces. ; these mMoreover, odels also demonstrated that it is concluded that bridges with piers are more vulnerable to lahars. Further research is being conducted to develop an application tool to simulate the effects of expected lahars in existing exposed bridges of a road network.

1 Introduction

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bridges reached by lahars.

Volcanic eruptions produce operational <u>losses restrictions</u> and <u>permanent</u> physical damage to <u>highway road</u> infrastructure, as evidenced by historical data regarding this natural hazard. The level of damage depends on the infrastructure's exposure and vulnerability as well as the type of volcanic event, namely: pyroclastic fall, pyroclastic flow, lava flow and lahar. Consequences related to pyroclastic fall, specifically tephra, are <u>temporary temporal</u> road closures <u>due to the lack ofcaused by visibility limitations</u> and <u>reduced loss of surface</u> friction between pavement and tires (Nairn, 2002; Leonard et al., 2005; Wilson et al., 2012).

Lava and pyroclastic flows may destroy the road infrastructure but, in contrast, however, the their probability of occurrence of these events is low and their influence exposed areas is smallare limited (Wilson et al., 2014). Considering that risk is a function of the hazard, exposure and vulnerability (UNISDR, 2009), This implies a lower hazard intensity and exposure and, therefore, a lower risk of lava and pyroclastic flows on the on road infrastructure is consequently expected, considering that risk is a function of the hazard, exposure and vulnerability (UNISDR, 2009). Lahars are flows of water, rock fragments and debris that descend from the slopes of volcanoes and river valleys. The highways rRoad infrastructures reached by lahars are affected damaged physically and operationally (Smith and Fritz, 1989). Volcanic debris and sediments transported by lahars make these flows especially destructive. These Lahar flows also scour the riverbed permanently affecting the foundations of the exposed infrastructure (Vallance and Iverson, 2015; Muñoz-Salinas et al., 2007; Nairn, 2000). Wilson et al. (2014) demonstrated that bridges and culverts are eritical the road infrastructures elements most exposed and vulnerable to lahars affected by lahars. Blong (1984) and Wilson et al. (2014) reported that 300 km of roads were damaged and 48 bridges were affected, as consequence because of Mount St. Helens (USA) eruption in 1980, 300 km of highways were damaged and 48 bridges were affected. Moreover, Tthe eruption of Villarrica and Calbuco volcanoes, which occurred in Chile in 2015, collapsed four of six

Several authors have calibrated fragility curves for buildings and electrical transmission systems, considering the vulnerability of both to volcanic hazard (Spence et al., 2005; Spence et al., 2007; Jenkins and Spence, 2009; Zuccaro and De Gregorio, 2013). Wilson et al. (2017) developed road infrastructure fragility curves due to tephra fall, without analyzing the effect of lahars on bridges. Fragility curves are commonly integrated in available risk modelling tools. For example, in the United States, the Federal Emergency Management Agency (FEMA) developed HAZUS-MH tool for risk management of structures and infrastructure. This GIS-based software studies covers three natural hazards: earthquakes, floods and hurricanes, excluding the volcanic hazard from the analysis (FEMA, 2011). Likewise, the

RiskScape software developed by the National Institute of Water and Atmospheric Research (NIWA) of New Zealand included the effects of earthquakes, tsunamis, floods, hurricanes and volcanic eruptions over assets such as buildings, roads and power lines. Nevertheless, the effects of volcanoes are only accounted for in terms of ash fall and the temporary effects interuption on theof infrastructure operation (Kaye, 2008). Fragility curves have been developed for some infrastructures and utilities exposed to volcanic hazard, such as buildings and electric transmission systems (Spence et al., 2005; Spence et al., 2007; Jenkins and Spence, 2009; Zuccaro and De Gregorio, 2013). In particular, Wilson et al. (2017) developed fragility curves for road infrastructure exposed to tephra fall. The effect of lahars over exposed road infrastructure, however, has not been described in detail regardless empirical evidence about their destructive effects (Wilson et al., 2014).

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From available literature and the current state-of-the-practice, it was is concluded that no bridge failure models and nor fragility curves exposed have been developed to estimate bridge failure probability due to to lahar flows have been developed. To characterize bridge fragility to lahars, failure probability of primary structural elements is required, namely: substructure (i.e. piers and abutments) and deck. Piers are columns designed to be an interior support for a bridge superstructure; abutments are the end support for a bridge superstructure; and deck is the component that supports wheel loads directly and is supported by other components (AASHTO, 2012).

The main objective of this study was is to propose a simplified bridge failure models and bridge fragility curves due to lahar hazards, considering pier and abutment overturning, as well as deck sliding caused by lahar hazard. Models development considers the calibration, and parameterization and validation of bridge fragility curves due to lahars, based on a validated limit state models. Two damage states were considered in the analysis: bridge failure and non-failure. The research starts with the characterization of the lahar process and the physical effects on bridges. An experimental design was elaborated From this analysis lahar depth was identified as a critical stochastic variable representative to the hazard intensity. to calibrate fragility curves based on analytical models that characterize the effect of lahars over bridges. A fFailure models is are then proposed, considering the limit state of the infrastructure pier and abutment overturning overturning moment due to lahar demanding forces and reduced supply moment caused by scour. and the tangential force over the deck caused by In the case of bridge deck, the limit state is analyzed considering lahar tangential force and supplied deck friction. Monte Carlo simulations were are applied to estimate the failure probability considering different lahar depths, allowing calibrating the fragility curves. The analysis is performed considering for one-span and multiple-spans bridges. An experimental design was elaborated to calibrate fragility curves based on analytical models that characterize the effect of lahars over bridges.

Best—fit probability functions are finally proposed, considering cumulative log-normal distribution and their corresponding parameters. The fragility curves were parameterized

usingfrom maximum likelihood estimationanalysis (parameterization). , considering a cumulative lognormal distribution. Limited historical data is available to empirically validate the proposed fragility curves, however, models were compared with post-event data from 15 bridges being in all cases consistent with developed models. Proposed bridge failure models and fragility curves were empirically validated with the available historical data. Finally, resulting curves are analyzed in detail Future research should be conducted to statistically validate developed fragility curves with reliable empirical data.

2 Characterization of lahars for the development of fragility curves

2.1 Physical description of lahar flows

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Lahars are high-velocity flow composed by a mix of volcanic debris and water, travelling through ravines and riverbeds (Pierson et al., 2009). Lahar flows are originated by an abrupt melting of snow and/or ice caused by the heat flow derived from lavas or pyroclastic flows issued during a volcanic event, or by avalanches of non-consolidated volcanic material during intense rains or rupture of a lake or pond (Waitt, 2013). Lahars are categorized according to their sediment/water ratio into debris flows and hyper-concentrated flows (Smith and Fritz, 1989). Debris flows are highly viscous slurries of sediment and water. Debris flows are capable of transporting gravel-sized debris in suspension, and their concentration of solid particles ranges between 75 and 80 % in weight or 55 and 60 % in volume. Hyper-concentrated flows have high-suspended fine contents, predominantly due to fluid motion and properties. The solid concentrations of hyper-concentrated flows can represent up to 55 to 60% of the total weight, and 35 to 40% of the total volume (Pierson et al., 2009).

The flow of lahars is guided by gravity, so the flow and is capable of impacting elements located tens of kilometers away from the crater of the volcano (Parfitt and Wilson, 2008). Furthermore, lahars can reach velocities up to 140 km/h, as observed in Mount St. Helens in the United States in 1980 (Pierson, 1985). The velocity and composition of lahars make them highly destructive.

According to Vallance and Iverson (2015) and Bono (2014), the most important processes of a lahar are the erosion of the steep slopes and the scouring of beds of fluvial terraces. Even more significant is the erosion observed in steeper river valleys with weaker beds. Watery sediment floods are more erosive than sediment-rich flows, where The scour of the riverbed drags massive material blocks (presenting diameters over 10 m) and vegetation. In this context, most of the bridges affected by lahars are located in valleys in volcanic areas. The erosion and the associated loads of high velocity lahars, and the impact of debris travelling with them, may cause the collapse or permanent deterioration of bridges (Nairn, 2002). This explains, in part, the high vulnerability of bridges to lahar flows.

Relevant drivers of the destructive potential of a lahar affecting a bridge are the bed material, the slope, the season in which the lahar occurs, the existence of a glacier, rainfall and the

prevailing temperatures during winter. The destructive potential of a lahar increases when the eruption occurs at the end of the winter, since in this season there is more accumulated snow compacted in layers, and more volume of ice melting. This condition is enhanced if winter temperatures are low, because greater volumes of ice and snow melting in shorter lapses of time may increase the lahars' intensity (Moreno, 2015).

2.2 Bridge fragility curves for lahar risk modelling

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In order to incorporate the uncertainty of the characteristics of lahar flows and the bridge engineering design (X), the use of fragility curves to quantify the probability of bridge failure due to lahars is proposed. Fragility curves express the probability that a-the damage state (DS) of a system exceeds different damage states levels (ds_i ; i=slight, moderate, extensive or complete), as a function of the given a certain hazard intensity (IM) (See Eq. 1). The fragility curves allow quantifying the failure probability of a system due to an event of a specific intensity (Rossetto et al., 2013), representing the systems' vulnerability to a natural hazard. In this study, bridge fragility curves for a complete damage state level are developed.

$$15 P(DS \ge ds_i|IM), (1)$$

Schulz et al. (2010) define four approaches for developing a system's fragility curves. First, there is the empirical approach, which is based on historical data and/or experiments. Fragility curves can be based on experts' opinions as well. Fragility curves can also be developed using an analytical approach through models that characterize the limit state of the element, based on probabilistic and deterministic variables defining the system. Finally, a hybrid method, which combines two or more of the recently described approaches described above, can be used.

Since there are no existing models addressing lahar risk on bridges, a challenge for the development of bridge fragility curves consists in defining a unified lahar hazard intensity (*IM*). In general, the flow depth is a measure of hazard intensity of natural events that involve liquid flows. In the flood module of the HAZUS-MH software, the Federal Emergency Management Agency developed fragility curves using the flow depth to quantify the hazard intensity (FEMA, 2011). Tsubaki et al. (2016) use the same variable (flow depth) for measuring the flood intensity when developing embankment fragility curves. Wilson et al. (2014) propose the flow depth as one of the potential intensity measures for developing fragility curves related to lahar flows as well. In this paper the lahar depth was is proposed as lahar hazard intensity, considering that this variable is correlated to other lahar flow characteristics, such as velocity and scour demand (Arneson et al., 2012).

3 <u>Proposed Development of failure models</u> for <u>infrastructure bridge pier/abutment</u> overturning and deck sliding due to lahars

3.1 Conceptual model

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In order to model bridge fragility due to lahars, the analytical approach is used based on reliability principles. The assessment of the bridge reliability can be considered a supply and demand problem associated with a bridge-lahar system defined by its basic variables <u>vector</u> (X). The supply function (S(X)) of the bridge corresponds to its capacity to resist the loads of the lahar. It is directly related to the design of the structural element. The demand function (D(X)) represents the load applied by the lahar on the bridge. The limit state function (g(X)) of the bridge-lahar system is given by the difference between the supply and demand functions (D(X) - S(X)). If g(X) is lower than zero, the lahar loads on the structure are greater than the bridge capacity and hence, the bridge will fail.

With the purpose of conceptualizing the loads applied by the lahar flow on the bridge components, a bridge-lahar model was developed, which is shown in the free-body diagram in Fig. 1. It shows the generic cross section of a bridge, and the main physical loads applied by the lahar on the bridge. The cross section of the bridge in Fig. 1 is composed by the subinfrastructure (foundation and pier/abutment) and the superstructure (deck and beams). The proposed failure models can be adapted to different bridge design criteria. In this paper, the Chilean design standards are considered for the fragility curves calibration. Thus, the proposed models assumes that the foundation has no piles. This assumption is based on the fact that 88 % of the bridges exposed to the volcanic hazard from the Villarrica and Calbuco volcanoes do not have piles (Moreno, 1999; Moreno, 2000). Additionally, it assumes a simple support of the superstructure on the piers and abutments.

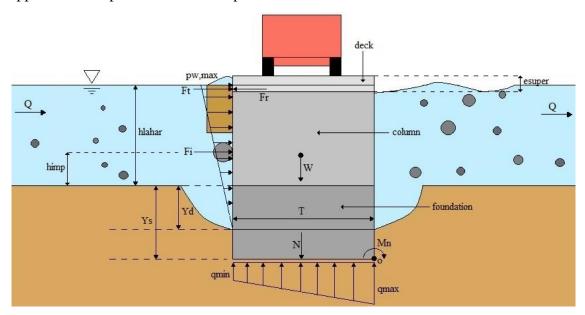


Figure 1: Free-body diagram of bridge resisting and demanding forces and moments in the presence of a lahar.

Fig. 1 shows a lahar with depth h_{Lahar} acting on a bridge of width TL. Each pier or abutment of the bridge has a weight W. The foundation of the bridge's subinfrastructure (pier/abutment) was designed with a depth Y_{so} that represents the supply or capacity of the bridge to resist scour. The lahar flow demands a scour Y_d on the bed, around the foundation. The foundation transfers loads to the ground, considering a trapezoidal distributed load model. The modelled lahar generates a hydrodynamic pressure p_w , which acts perpendicular to the bridge. This pressure produces a resulting hydrodynamic tangential force F_{wi} on the piers $\underline{\underline{}}$ and a force F_{ws} on the bridge superstructure. $\underline{\underline{}}$ Furthermore, the debris, transported by the lahar colliding with the bridge, impacts the structure with a force F_i . The tangential force F_t corresponds to the sum of the hydrodynamic force and the debris impact force applied to the superstructure. The deck of the bridge resists the sliding caused by the <u>lahar tangential force</u> F_t with a friction force F_r . The lahar also generates a scour demand Y_{set} on the bed, around the foundation. Furthermore, the debris, transported by the lahar colliding with the bridge, impacts the structure with a force F_i . All these the forces applied to the <u>substructure</u> produce a net resulting moment M_n on the lower right vortex of the foundation. The net moment M_n is equal to the difference between the overturning moment (M_v) . generated by hydrodynamic forces $(F_{wi})_{\overline{1}}$ and the debris impact $(F_i)_{\underline{1}}$ and the resistant moment (M_r) produced by the weight W of the bridge.

3.2 Bridge failure mechanisms due to lahars

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The hydrodynamic pressure of the lahar flow (p_w) and the impact force of the debris (F_i) can cause the overturning of bridge piers and abutments. This is further enhanced by the scour that these flows generate around the foundations. The hydrodynamic pressure of the lahars, together with the potential impact of debris, can cause deck sliding.

With the aim of analyzing the effects of lahars on bridges, failure mechanisms associated with three bridge components are defined: pier overturning, abutment overturning and sliding of the bridge superstructure. In addition to these failure mechanisms, the access embankment of the bridge may collapse. However, this component is not included in the modelling due to its lower replacement cost in relation to other bridge components. All these failure mechanisms are consistent with the postulates of Wilson et al. (2014) and the records of the lahar effects as a result of the eruptions of the Villarrica volcano and the Calbuco volcano in 2015 (MOP, 2015a; MOP, 2015b). Images in Fig. 2 (a) and (b) show the Río Blanco Bridge (Chile) before and after a lahar flow following the eruption of Calbuco volcano in 2015. Fig. 2 shows the structural collapse of the bridge due to the overturning of the pier and subsequent sliding of the deck.



Figure 2: (a) Original Río Blanco Bridge (Chile) (MOP, 2015). (b) Río Blanco Bridge (Chile) after lahar flow of the Calbuco volcano eruption in 2015 (MOP, 2015).

3.2.1 **SubInfra**structure overturning (piers and abutments)

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Both piers and abutments are components susceptible to overturning due to lahars. These dense and fast-travelling flows generate a resulting hydrodynamic force (F_{wi}) on the bridge subinfrastructure, which entails an overturning moment (M_{wi}) . In addition, the impact force (F_i) of the debris on piers and abutments produces the overturning moment (M_i) . The bridge weight W generates a moment (M_r) resisting the infrastructure overturning.

Through equilibrium of moments, considering the turning point O located in the vertex of the foundation, it is possible to evaluate the stability of the bridge piers and abutments in the presence of a lahar flow of a specific intensity. The overturning of piers and abutments is produced if the overturning moment $(M_v = M_{wi} + M_i)$ caused by the lahar on the component is greater than the resistant moment (M_r) . In other words, the overturning is produced when the net moment (M_n) is less than zero.

A lahar can also cause the overturning of piers and abutments when the depth of the scour generated by the flow on the bed $Y_{sd}(X)$ is greater than the design scour of the <u>subinfrastructure</u> $Y_{se}(X)$.

The above allows establishing the limit state function $g_{SOVI}(X)$ related to the overturning of piers and abutments due to lahars. This function allows quantifying the overturning probability of the <u>subinfra</u>structure considering the parameters (X) of the system and the lahar intensity h_{Lahar4} :

$$P_{SOVI} = P(g_{SOVI}(X) \le 0) , \qquad (2)$$

$$g_{SOVI}(X) = \min\{M_r(X) - M_v(X); Y_{So}(X) - Y_{sd}(X)\},$$
 (3)

This function indicates that, given a lahar with height h_{Lahar1} , the <u>subinfra</u>structure will overturn if the overturning moment M_v is greater than the resistant moment M_r and/or the lahar scour demand Y_{sd} is higher than the design scour of the bridge Y_{so} .

The scour produced caused by lahar flows near the foundations contributes to a greater

vulnerability of these bridge components, since the lahars produce destabilization and weakening around the foundation of piers and abutments. If there is scour in the bed, the foundation of the pier or abutment will be exposed to a higher hydrodynamic pressure. This load is higher in the case of lahars, given their greater density and velocity in relation to normal floods. A greater scour demand will imply a larger surface affected by the hydrodynamic pressure. In turn, this means a greater resulting hydrodynamic force (F_{wi}) and, therefore, a greater moment associated with this force (M_{wi}) .

3.2.2 Deck sliding

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In the case where the lahar height exceeds the bridge clearance, the lahar flow will exert a hydrodynamic pressure on the bridge superstructure. There is also the possibility that the debris transported by the lahar flow impacts the bridge deck. This debris impact force (F_{is}), together with the hydrodynamic force (F_{ws}) can cause failure due to deck sliding. The presence of microscopic imperfections between the contact surfaces of the superstructure (beams) and the <u>subinfrastructure</u> (piers and abutments) produces a static friction force (F_r) that opposes the start of the deck sliding.

Through the equilibrium of forces it can be inferred that the deck of a bridge subjected to a lahar will slide if the resulting tangential force ($F_t = F_{ws} + F_{is}$) is higher than the static friction force (F_r) between the <u>subinfras</u>tructure and the superstructure. It should be highlighted that this force is zero if the lahar height is lower than the bridge clearance.

This allows establishing the limit state function $g_{DS}(X)$ associated with the superstructure failure due to its potential sliding:

$$P_{DS} = P(g_{DS}(X) \le 0) , \qquad (4)$$

$$g_{DS}(X) = F_r(X) - F_t(X) , \qquad (5)$$

The limit state function defined in Eq. (5) implies that, under attributes *X*, if the friction force is lower than the tangential force produced by the lahar, the failure mechanism associated with sliding will be activated.

4 Experimental designProposal for modelling subinfrastructure overturning and deck sliding due to lahars

4.1 Physical models to estimate limit state functions

Once the limit state functions have been analytically defined, the loads presented in the free-body diagram have to be quantified. Therefore, physical existing models are used and integrated.

4.1.1 Lahar hydraulic attributes

First, the lahar mean velocity (v_{Lahar}) is quantified with the Eq. (6), suggested by Chen (1983; 1985) for a fully dynamic debris flow in a channel with an arbitrary geometric shape. For this caseIn this study, a rectangular flow shape is assumed. This formula incorporates the rheology of the lahar through the consistency index (μ_{Lahar}), which was quantified by Laenen and Hansen (1988) for the case of lahars.

$$v_{Lahar} = \frac{2}{5} \left(\frac{\gamma_{Lahar}}{\mu_{Lahar}} \right)^{\frac{1}{2}} i^{1/2} \left(\frac{A_{Lahar}}{P_{Lahar}} \right)^{3/2}, \tag{6}$$

The lahar hydrodynamic pressure (p_w) is estimated with the AASHTO model (2012). This model considers a triangular distribution of this pressure, taking a value of zero in the deepest point and a maximum value in the flow surface. The hydrodynamic pressure is a function of the specific weight of the flow, its velocity and the accumulation of debris (C_D) .

$$p_{w,max} = C_D \frac{\gamma_{Lahar}}{a} v_{Lahar}^2 , \qquad (7)$$

4.1.2 Scour models

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The lahar scour demand is based on the empirical equation proposed by Arneson et al. (2012). Müller (1996) compared 22 equations proposed in the literature to estimate scour; he used empirical data of 384 field measurements of 56 bridges. The conclusion of this studyMüller (1996) was that the equation proposed by Arneson et al. (2012) in the Hydraulic Engineering Circular No. 18 (HEC-18) was suitable for quantifying the magnitude-of-the-scour_depth.

Debris transported by the flows accumulates in the bridge piers, creating an additional obstruction to the flow. To incorporate the debris accumulation, the scour demand on the piers (Y_{de-pd}) is modelled with Eqs. (8) and (9) of the NCHRP (2010). The equations proposed by the NCHRP adjust the scour model proposed by the HEC-18 to estimate the scour generated by debris flows and lahars. The adjusted model considers a triangular or rectangular debris accumulation (K_E) with height H_d and width W_d to estimate an effective widening (b_d^*) of the pier with width b. It should be noted that factors K_1 , K_2 and K_3 are correction factors of the pier shape, the flow angle and the bed condition, respectively.

$$Y_{de-pd} = 2h_{Lahar} K_1 K_2 K_3 \left(\frac{b}{h_{Lahar}}\right)^{0.65} Fr_{Lahar}^{0.65}, \tag{8}$$

$$b_d^* = \frac{K_E(H_dW_d) + (h_{Lahar} - K_EH_d)b}{h_{Lahar}},\tag{9}$$

According to the HEC-18, the scour demand on the abutments (Y_{de-ad}) is based on the flow depth, the flow width, the bridge length and a bed condition amplification factor (α) .

$$Y_{\underline{de-ad}} = \alpha h_{Lahar} \left(\frac{b_{Flow}}{L_{Bridge}} \right)^{6/7} - h_{Lahar} , \qquad (10)$$

The scour supply is estimated with models adapted from bridge design manuals. For example, Breusers, Nicollet and Shen (1977) stipulate Eq. (11) and (12) assess the design scour of piers (Y_{se-pe}) and abutments (Y_{se-ae}) . These equations include variables such as design height (h_{design}) , pier width (b) and correction factors by flow angle, pier shape, among others:

$$5 Y_{se-pe} = 2b \left(K_S K_w K_g K_{gr} K_R K_d \right) \tanh \left(\frac{h_{Design}}{b} \right) + 2.0 , (11)$$

$$Y_{se-ae} = \left(K_{\phi}K_FK_hK_{\sigma}K_I\right)h_{Design} + 2.0 , \qquad (12)$$

4.1.3 **SubInfra**structure overturning moment and deck tangential force

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The overturning moment (M_v) produced by lahars on the bridge <u>subinfra</u>structure is given by the sum of the hydrodynamic moment (M_{wi}) and the debris impact moment (M_i) . The tangential force (F_t) on the deck corresponds to the sum of the resulting force from the hydrodynamic pressure on the deck (F_{ws}) and the debris impact force (F_{is}) . Considering the pressure model showed in Eq. (7), the hydrodynamic moment generated by the lahar on the <u>subinfra</u>structure (M_{wi}) can be estimated. In the case of <u>subinfra</u>structure, the hydrodynamic moment is separated into two parts: the foundation and the column. This separation is supported by the fact that these elements have different geometry and that the pressure has a triangular distribution over the foundation and trapezoidal distribution over the column (Fig. 1).

$$M_{wi} = M_{w,found} + M_{w,column} = F_{w,found} y_{w,found} + F_{w,column} y_{w,column}, \qquad (132)$$

The resulting hydrodynamic force exerted by the lahar on the foundation $(F_{w,found})$ and the height at which this force acts with respect to the turning axis $(y_{w,found})$ are given by Eq. (143) and Eq. (154), where the variable T corresponds to the width of the bridge:

$$F_{w,found} = LTC_D \left(\frac{\gamma_{Lahar}}{2g}\right) v_{Lahar}^2 \left(\frac{Y_{sd}^2}{h_{Lahar} + Y_{sd}^2}\right), \tag{143}$$

$$y_{w,fouttend} = Y_{so} - \frac{Y_{sd}}{3}, \qquad (1\underline{5}4)$$

The hydrodynamic force on the column ($F_{w,column}$) and its application point ($y_{w,column}$) depend on if the height of the lahar exceeds the height of the column or not. To incorporate this, the variable h^* was defined, which is given by the minimum between the lahar height (h_{Lahar}) and the column height (h_{Design}).

$$F_{w,column} = bC_D \left(\frac{\gamma_{Lahar}}{2g}\right) v_{Lahar}^2 \left(\frac{h^{*2} + 2h^* Y_{sd}}{h_{Lahar} + Y_{sd}}\right), \tag{1.65}$$

$$y_{w,column} = Y_{S\Theta} + \frac{\left(\frac{h^*}{2}Y_{Sd} + \frac{h^{*2}}{3}\right)}{\left(Y_{Sd} + \frac{h^*}{2}\right)},\tag{176}$$

In order to quantify the hydrodynamic force of the lahar on the deck (F_{ws}) , three cases should

be considered: (1) the lahar height is lower than the bridge clearance, (2) the lahar height is greater than the clearance but lower than the roadway level, (3) the lahar height is greater than the roadway level. In the model, the roadway level is given by the sum of the <u>subinfrastructure</u> height (h_{Design}), and the superstructure thickness (e_{Super}).

$$F_{ws} = \begin{cases} 0 & h_{Lahar} < h_{Design} \\ L_{Bridge} C_D \left(\frac{\gamma_{Lahar}}{2g} \right) v_{Lahar}^2 \left(\frac{h_{Lahar}^2 - h_{Design}^2}{h_{Lahar} + Y_{sd}} \right) & h_{Design} \le h_{Lahar} < h_{Design} + e_{Super} \\ L_{Bridge} C_D \left(\frac{\gamma_{Lahar}}{2g} \right) v_{Lahar}^2 \left(\frac{2h_{Design} e_{Super} + e_{Super}^2}{h_{Lahar} + Y_{sd}} \right) & h_{Lahar} \ge h_{Design} + e_{Super} \end{cases}$$

$$(187)$$

To quantify the impact of debris on the bridge, the model of Haehnel and Daly (2004) is used. This model assesses the impact force through a one-degree-of-freedom system assuming a rigid structure. Thus, the impact force of gravel transported by a lahar on the bridge is based on the flow velocity (v_{Lahar}), the specific weight of the gravel (γ_{Gravel}), the gravel diameter (D_{Gravel}) and the contact stiffness of collision (\hat{k}). Debris impact force on the deck (F_{is}) is given by Eq. (198).

$$F_{is} = \begin{cases} 0 & h_{imp} < h_{Design} \\ v_{Lahar} \sqrt{\hat{k} \gamma_{Gravel} \frac{4}{3} \pi \left(\frac{D_{Gravel}}{2}\right)^3} & h_{Design} \leq h_{imp} < h_{Design} + e_{Super} \end{cases}, \qquad (198)$$

$$h_{imp} \geq h_{Design} + e_{Super}$$

The moment of debris impact (M_i) on the <u>subinfrastructure</u> with respect to the rotation axis is shown in Eq. (2019). This indicates that if the impact height (h_{imp}) is greater than the <u>subinfrastructure</u> (h_{Design}) , the associated moment is zero. For the impact height, a triangular distribution with the mode equal to the lahar height is assumed, considering that the debris tends to collect in the flow surface (Zevenbergen et al., 2007).

$$M_{i} = \begin{cases} v_{Lahar} \sqrt{\gamma_{Gravela}} \frac{4}{3} \pi \left(\frac{D_{Gravela}}{2} \right)^{3} \left(h_{imp} + Y_{so} \right) & h_{imp} \leq h_{Design} \\ 0 & h_{imp} > h_{Design} \end{cases}, \quad (\underline{2019})$$

4.1.4 SubInfrastructure resistant moment and deck friction force

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The <u>subinfra</u>structure capacity to oppose overturning depends on the bridge elements' design and condition, including the bridge geometry, materials and the scours' design (Y_{se-pe} and Y_{se-ae}). Thus, the lahar loads on the bridge and the scour are considered only in the demand function (overturning moment M_v). The resistant moment (M_r) of the infrastructure to lahars is given by the weight (W) of the pier or abutment and the elements that are supported on it.
Among the elements supported by the <u>subinfra</u>structure, the superstructure and the soil on the abutments' foundations must be considered. The weight of the piers and abutments without considering the soil and the superstructure are:

$$W_{SubInfra} = \gamma_{SubInfra} Y_{So} L T^2 + \gamma_{SubInfra} h_{Design} b L T, \qquad (2\underline{1}\theta)$$

The weight of the soil on the abutment foundation in the access to the bridge is given by Eq.

(221).

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$$W_{Soil-Abutment} = 0.5\gamma_{Soil}h_{Design}(TL^2 - bLT), \qquad (221)$$

The model considers that the weight of the superstructure is distributed uniformly in all its supports (NA). Thus, the force exerted by the superstructure on each foundation is:

$$5 W_{Super} = \frac{(\gamma_{Super})(TL)(L_{Bridge})(e_{Super})}{NA}, (2\underline{32})$$

Since the elements of the modeled bridge are symmetrical with respect to the vertical axis, the weight acts at a distance LT/2 from the overturning point. Thus, the resistant moment of the infrastructure is given by the following expression:

$$M_r = (W_{SubInfra} + W_{Soil-Abutment} + W_{Super})^{\frac{LT}{2}}, \qquad (2\underline{43})$$

Finally, the force that opposes the deck sliding corresponds to the friction between the superstructure and the <u>subinfrastructure</u>. This force is given by the Eq. $(2\underline{5}4)$:

$$F_r = \mu_s N_{Super} = \mu_{Super} (\gamma_{Super}) (LT) (L_{Bridge}) (e_{Super}), \qquad (2\underline{5}4)$$

4.2 Values of the variables involved in the limit state functions

In order to quantify the independent variables of the limit state function, the first step is to define the nature of the variables, based on their degree of uncertainty. The system bridge-lahar presents random variables associated with lahar hazard, such as lahar density and debris accumulation. To quantify these variables, probability distribution functions are used, based on studies prepared by the Chilean National Geology and Mining Service (Sernageomin) (Castruccio et al., 2010; Bono, 2014) and the United States Geological Survey (Pierson et al., 2009; Vallance and Iverson, 2015).

Furthermore, regarding variables associated with the bridges' capacity to resist lahars, random variables are also considered due to the uncertainty in the bridge design. Goodness of fit tests were undertaken to determine the probability functions and the parameters of these variables, using the information from the Chilean bridge inventory and the Highway Manual of the Ministry of Public Works (MOP, 2016). Table 1 summarizes the values of the variables involved in the limit state functions.

Table 1: <u>Basic <u>V</u>variables involved in the limit state functions.</u>

Variable	Name	Unit	Deterministic Value/ Probabilistic Distribution	Value Reference
h_{Lahar}	Lahar Height	m	Lahar Intensity	Hazard Intensity
$K_w;K_2;K_\phi$	Flow Skew Factor	-	1.0	Bridge Inventory (MOP)
$K_{\sigma};K_{g};K_{d}$	Granulometric Dispersion Factor	-	1.0	MOP (2016)
K_{gr}	Pier Group Factor	-	Uniform (1.0; 1.9)	MOP (2016)
K_R	Foundation Emergence Factor	-	Triangular (1.0; 1.06; 1.06)	MOP (2016)
$h_{Design} \\$	Flow Design Depth	m	Lognormal (1.16; 0.53) - 1.0	Bridge Inventory (MOP)
NP	Number of Lanes	-	1 lane; 57.8 %	Bridge Inventory (MOP)

				2 lanes; 42.2 %	
	<u>T</u>	Bridge Width	m	Burr (4.5; 14.1; 4.9)	Bridge Inventory (MOP)
	b	Column Width	m	Triangular (0.063L; 1.0L; 0.08L)	Bridge Inventory (MOP)
	i	Bed Slope in Bridge	<u>°</u> _	Uniform (1.0; 1.3)	Bono (2014)
	$L_{\rm Bridge}$	Bridge Length	m	Lognormal (0.78; 2.79)	Bridge Inventory (MOP)
	K_1	Pier Shape Factor	-	Triangular (0.65; 1.2; 1.1)	Bridge Inventory (MOP)
	K_3	Bed Condition Factor	-	1 <u>.</u> ,1	MOP (2016)
	K_{E}	Debris Accumulation Factor	-	Uniform Discrete (0.21; 0.79)	Zavenbergen et al. (2007)
	W_d / b	Debris Width/Pier Width Ratio	-	Normal (15.1; 8.2)	Zavenbergen et al. (2007)
	b_F/L_B	Lahar Width/Bridge Length Ratio	-	Uniform (1.22; 1.83)	Self-prepared with historical data
	μ_{Lahar}	Lahar Consistency Index	kg/m	Uniform (5; 2,260)	Laenen and Hansen (1988)
	K_F	Abutment Shape Factor	-	Triangular (0.3; 1.0; 0.75)	Bridge Inventory (MOP)
	K_{I}	Flow Intensity Factor	-	1.0	MOP (2016)
	C_D	Drag Coefficient	-	1.4	AASHTO (2012)
	γ_{Lahar}	Lahar Specific Weight	N/m^3	Triangular (15,598; 19,031; 19,031)	Pierson et al. (2009)
	γ_{Gravel}	Gravel Specific Weight	N/m^3	24,525	Vallance and Iverson (2015)
	D_{Gravel}	Gravel Diameter	mm	Triangular (0.031; 32.0; 2.0)	Castruccio et al. (2010)
	k	Effective Contact Stiffness	MN/m	14.0	Haehnel and Daly (2004); AASHTO (2012)
	γ _{Sub} Infra	<u>SubInfra</u> structure Specific Weight	N/m^3	Concrete (24,500; 61.6 %) Wood (7,450; 35.8 %) Steel (7,450; 2.6 %)	Bridge Inventory (MOP); Cobb (2008)
	γ_{Super}	Superstructure Specific Weight	N/m^3	Concrete (24,500; 45.7 %) Wood (7,450; 53.8 %) Steel (7,450; 0.5 %)	Bridge Inventory (MOP); Cobb (2008)
	γ_{Soil}	Soil on Abutment Specific Weight	N/m^3	Uniform (12,250; 19,600)	MOP (2016)
	NA	Number of Deck Supports	-	2 supports; $L_{Bridge} \le 19.05 \text{ m}$ 3 supports; $19.05 \text{ m} < L_{Bridge} \le 32.10 \text{ m}$ 4 supports; $L_{Bridge} > 32.10 \text{ m}$	Bridge Inventory (MOP)
1	$\mu_{ ext{super}}$	Static Friction InfraSub-Super	-	Concrete-Concrete (0.50; 44.9 %) Concrete-Wood (0.48; 17.1 %) Concrete-Steel (0.70; 0.4 %) Wood-Wood (0.35; 35.0 %) Wood-Steel (0.40; 2.6 %) Steel-Steel (0.80; 0.0 %)	Bridge Inventory (MOP); Cobb (2008)
	$\mathbf{h}_{\mathrm{imp}}$	Gravel Impact Height	m	Triangular (0; h_{Lahar} ; h_{Lahar})	Assumption
	e_{Super}	Superstructure Thickness	cm	Gen. Ext. Value (<u>18.6</u> 0.3; 4.7; <u>0.3</u> 18.6)	Bridge Inventory (MOP)

2 lanes: 42.2 %

5 Calibration and parameterization of bridge fragility curves due to lahars

5.1 Monte Carlo simulations for fragility curves calibration

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Reliability analysis comprises analytical solution methods and numerical solution methods. Analytical solution methods feature the first-order second-moment (FOSM) method, the first-order reliability method (FORM) and the second-order reliability method (SORM). Numerical solution methods include the Monte Carlo simulation (MCS) and the response surface method (RSM). The MCS method is used to develop bridge fragility curves due to lahars. The choice of the MCS as the solution method is based on the limitations of the analytical solution methods with regard to the probability distributions of the random variables (Schultz et al., 2010). MCS allows incorporating the uncertainty of the

characteristics of lahars and the structure in the quantification of the bridge failure probability, without the mentioned limitation.

With the limit state functions and variables already defined, the Monte Carlo simulations can be performed. Therefore, a fixed intensity lahar h_1 is considered. The probability distributions of the system's random variables imply the obtainment of different values of limit state functions g(X). If this function is less than zero in a specific simulation, it means that in this simulation the bridge fails due to a lahar with intensity h_1 . The bridge failure probability due to a lahar of intensity h_1 is equal to the sum of the number of simulations where function g(X) is negative, divided by the number of total simulations with this intensity (NS) (Vorogushyn et al., 2009).

$$P_{Failure} = P(g(X) < 0 | H = h_1) = \frac{\sum_{i=1}^{NS} k_i}{NS},$$
 (265)

$$k_i = \begin{cases} 1 & \text{si } g_i(X) < 0 \\ \text{si } g_i(X) \ge 0 \end{cases}$$
 (276)

Simulations with fixed intensity h_1 allow quantifying the failure probability of the fragility curve at the abscissa h_1 . This experiment is carried out repeatedly for several intensity levels, to obtain the complete fragility curve for each failure mechanism identified. Specifically, 10,000 simulations were performed for each intensity level. The failure probability is quantified for lahar heights discretized every 0.25 m.

5.2 Calibrated bridge fragility curves due to lahars

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5.2.1 Fragility curves by bridge failure mechanism

Once the supply and demand functions of the failure mechanisms are defined, together with their variables, simulations are run for a fixed lahar height level h_1 . The percentage of simulations where function $g_{SOVI}(X)$ is less than zero is equivalent to the overturning probability of the <u>subinfrastructure</u> in the presence of a lahar of h_1 . After doing this for different lahar height levels, the overturning fragility curves of the piers and abutments are obtained. The same experiment was performed for the function $g_{DS}(X)$ to calibrate the deck sliding fragility curve. Figure 3 shows the fragility curves by bridge failure mechanism.

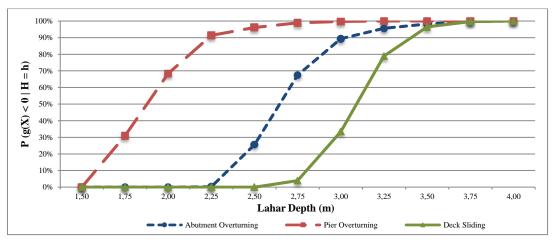


Figure 3: Fragility curves for bridge infrastructure overturning and deck sliding due to lahars.

The analysis of <u>subinfra</u>structure overturning fragility curves allows us to conclude that, when impacted by lahar flows, piers are more susceptible to overturn than the abutments. Given any intensity level of the hazard, piers have a greater probability of overturning than abutments. The functional shape of the overturning fragility curves shows that, regarding the abutments; the maximum failure probability increase is achieved when the intensity grows from 2.5 to 2.75 m, where the failure probability increases 41.8 percentage points. In the case of piers, the maximum growth of the probability of failure is reached between 1.75 and 2.0 m; increasing the overturning probability by 37.4 percentage points.

When analyzing the deck sliding fragility curve, the deck failure probability is zero if the lahar intensity is less or equal to 2.50 m. This is mainly due to the fact that a low-height lahar does not reach the bridge clearance and, consequently, the flow does not affect the superstructure. Nevertheless, if the intensity of the lahar exceeds this level, the failure probability increases rapidly. The growth rate of this fragility curve also has a maximum, which is reached when the lahar arrives at 3.25 m, particularly if the lahar increases from 3.0 to 3.25 m the sliding probability of the deck increases 45.5 percentage points. This is mainly due to the fact that if the lahar reaches 3.50 m, it already touches the road elevation of most bridges of the inventory.

5.2.2 Fragility curves by bridge categories

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The previous analysis allows us to conclude that a relevant factor in a bridge failure due to a lahar is the presence of piers. Therefore, two bridge categories were defined: bridges with one span (C1) and bridges with multiple spans (C2). Category C1 corresponds to bridges with <u>subinfrastructure</u> composed only of abutments and category C2 represents bridges with one or more piers.

To obtain the fragility curves for these two bridge categories, each simulation considered that the failure of the bridge occurs when at least one of its components fails. For example, a bridge of category C1 fails when the abutment overturns and/or when the deck slides. A category C2 bridge fails when the pier or abutment overturns and/or the deck slides. Figure 4 shows the fragility curves for both bridge categories, in addition to the failure probability of each component in a histogram.

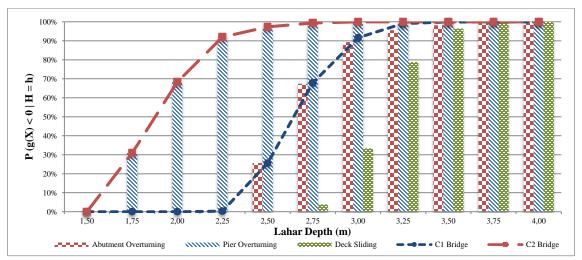


Figure 4: Fragility curves for one-span bridges (C1) and multiple-spans bridges (C2). due to labors

Fig. 4 allows us to conclude that bridges with one span (C1) are stronger than bridges with two or more spans (C2) in the presence of lahar flows. The reason is that piers are more susceptible to overturn than abutments. The failure of bridges with one span is guided by the abutments overturning, while in the bridges with multiple spans, the failure is guided by the piers overturning. The deck sliding is not a triggering factor of bridge failures due to lahars generated by Villarrica and Calbuco volcanoes.

5.3 Parameterization of bridge fragility curves due to lahars

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- When considering risk management from a strategic point of view, the parameterization of bridge fragility curves due to lahars entails a series of advantages. It allows directly estimating the failure or collapse probability of each bridge category based on the lahar depth. Moreover, it allows quantifying the failure probability continuously, that is, not every 25 cm of lahar.
- For the parameterization of fragility curves, a cumulative lognormal distribution is considered. When assessing parameters μ and β of the cumulative lognormal distribution reflecting the fragility curve, the bridge failure probability associated with a lahar of intensity h_i can be estimated through the following equation:

$$P(g(X) < 0 | H = h_i) = \Phi\left(\frac{\ln(h_i) - \mu}{\beta}\right), \tag{287}$$

The method of maximum likelihood estimation (MLE) was used for fragility curves parameterization. This tool allows determining the distribution parameters that maximize the

occurrence probability of data obtained in the Monte Carlo simulations. In this case, the objective of the MLE is to determine the value of the bridge failure probability (p_i) due to a lahar of intensity h_i that maximizes the probability of obtaining the pairs (n_i, N_i) associated to the simulations of all lahar intensity levels h_i . This is obtained by maximizing the likelihood function, which is equal to the product of the binomial probabilities for each height level h_i .

$$Likelihood = \prod_{i=0}^{4.0} P(n_i \ in \ N_i \ collapse | H = h_i) = \prod_{i=0}^{4.0} \binom{N_i}{n_i} p_i^{n_i} (1 - p_i)^{N_i - n_i}, \quad (2\underline{98})$$

Considering a fragility curve with cumulative lognormal distribution, p_i is replaced by the cumulative lognormal function, and parameters μ and β are estimated. In this case, it is best to maximize the likelihood logarithm instead of the likelihood function. Thus, parameters of the cumulative lognormal distribution are obtained through the following expression proposed by Lallemant et al. (2015):

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$$\hat{\mu}, \hat{\beta} = argmax_{\mu,\beta} \sum_{i=0}^{4.0} \left[n_i ln \left(\Phi\left(\frac{\ln(h_i) - \mu}{\beta}\right) \right) + (N_i - n_i) ln \left(1 - \Phi\left(\frac{\ln(h_i) - \mu}{\beta}\right) \right) \right], \quad (3029)$$

Parameters μ and β were obtained by iterating their values and finding the combination that maximizes Eq. (3029). The process was carried out for bridges with one span (C1) and bridges with multiple spans (C2). For bridges without piers (C1), the result was that the likelihood function is maximized with μ equal to 0.98 and β equal to 0.08. In this manner, we conclude that the failure height of bridges with one span (C1) due to lahars can be modeled with a cumulative lognormal distribution (μ = 0.98; β = 0.08). Regarding the bridges with two or more spans (C2), it was concluded that its collapse height due to lahars could be represented by a cumulative lognormal distribution with μ equal to 0.63 and β equal to 0.13. Fig. 5 shows both analytical fragility curve and parameterized fragility curve of bridges with one span (C1) and with two or more spans (C2).

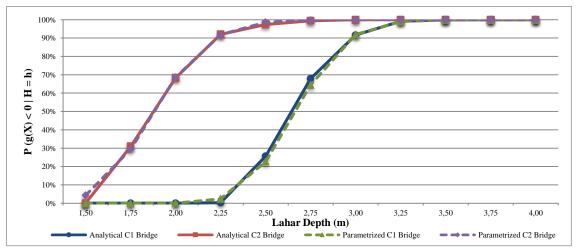


Figure 5: Analytical and parameterized fragility curves for one-span bridges (C1) and multiple-spans bridges (C2). due to lahars.

6 Validation of the bridge failure model and fragility curves due to lahars Evaluation of the bridge failure models against empirical data and analysis of results

6.1 Validation of the model of bridge failure due to lahars

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The models of bridge failure due to lahars is are based on physical models and expressions recommended in the literature; for example, this includes the equations given by the Highway Manual of the Chilean Ministry of Public Works (MOP, 2016) for estimating the scour supply in order to design bridges as well as the expressions of HEC-18 (Arneson et al., 2012) for quantifying the scour demand of the flows. All this requires the validationan empirical evaluation of the developed analytical failure models.

The bridge failure models is are validated evaluated empirically using data from historical lahars of Chile. Considering the attributes of the historical lahars and bridges that were affected, the models quantifyies the net moment (M_n) and net force (F_n) exerted by the flow on the bridge. If the demand moment or force exceeds that of supply, the models indicates that the analyzed bridge failed due to that historical lahar. The model's result for each bridge (failure/not failure) is compared with that indicated in the damage reports. For the validationevaluation, the damage attributes and records of lahars produced during the eruptions of the Villarrica volcano in 1964, 1971 and 2015, and the Calbuco volcano in 1961 and 2015 were used. The historical information was compiled from Klohn (1963), Naranjo and Moreno (2004), Moreno, Naranjo and Clavero (2006), MOP (2015a), MOP (2015b) and Flores (2016). The results of the bridge failure models validation empirical evaluation are shown in Table 2:

Table 2: Results of the bridge failure models empirical evaluation validation.

Nº	Bridge	Lahar Height (m)	Mn Abutment (MN-m)	Mn Pier (MN-m)	Fn Super (MN)	Analytical Damage	Empirical Damage
1	Turbio	3.5	-1.98	-	0.62	Failure	Failure
2	Correntoso (Villarrica)	3.0	-8.56	-22.23	-3.02	Failure	Failure
3	Madera S/N	5.0	-3.71	-	-1.09	Failure	Failure
4	Challupén	5.0	-2.42	-	-0.02	Failure	Failure
5	El Cerdúo	3.5	-3.12	-	-0.82	Failure	Failure
6	Madera S/N 2	1.5	0.73	0.88	1.01	No Failure	No Failure
7	Carmelito	1.5	21.29	-	2.12	No Failure	No Failure
8	Zanjón Seco	1.5	1.99	-	1.81	No Failure	No Failure
9	Seco	1.5	2.43	0.21	1.36	No Failure	No Failure
10	Tepú	3.0	-1.13	-10.42	-1.08	Failure	Failure
11	Tronador	3.5	-2.04	-	-0.18	Failure	Failure
12	Río Blanco	3.5	-3.51	-	0.93	Failure	Failure
13	Zapatero	2.5	-0.13	-	0.48	Failure	Failure
14	Pescado 2	2.5	1.39	-	1.92	No Failure	No Failure
15	Correntoso (Calbuco)	2.5	22,16	-	1.49	No Failure	No Failure

The 15 historical cases evaluated analytically with the failure models, considering the specific inputs of the system, have the same state of damage (failure/no failure) as that reported experimentally by the agencies. The historical data of Table 2 consider lahars from 1.5 m to 5.0 m of depth, covering the entire range of hazard intensity of developed fragility curves (1.5 m to 4.0 m). The density of the evaluated lahars ranges from 16,000 to 19,000 N/m³; the slope from 1.0° to 1.2°; the bridge length from 11.3 m to 72.5 m; the bridge width from 3.9 m to 8.3 m; the bridge height from 2.5 m to 5.5 m; the number of deck support from 0 to 5; the bridge materials are concrete and wood; the number of bridge lanes are 1 and 2. Thus, the empirical data evaluated demonstrate representativeness of the range of the basic variables of the analytical model (Table 1). It can be concluded that the bridge failure model reflects the empirical impacts of the lahars on bridges.

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Through the satisfactory validation we conclude that the existing models integrated in the limit state functions and the values of the used variables reflect the stability of the bridge due to a lahar flow. This allows inferring that the developed failure models represent the fragility of its components in the presence of these flows.

The analysis of the models and equations used in the limit state functions demonstrates that the lahar depth is the main variable in the quantification of lahar loads and bridge capacity to response to these flows. The lahar velocity, the scour demand, the hydrodynamic pressure and the height of the debris impact depend on the flow height. Thus, it is concluded that this variable can be used to represent the hazard intensity in the fragility curves associated to lahars.

In order to validate parameterized fragility curves, the analytical bridge failure probability (p_a) for a lahar intensity h_{Lahar} should be statistically compared with the empirical failure probability (p_e) for the same lahar intensity. The empirical failure probability p_e can be estimated as the proportion of bridges reached by historical lahars with intensity h_{Lahar} that were destroyed. However, there is insufficient empirical data to provide a statistical validation of the bridge fragility curves. There are only 15 empirical points (h_{Lahar}, p_e) to validate two fragility curves (C1 bridges and C2 bridges). Thus, a deficiency of empirical data on impacts of lahars on bridges is identified.

Regarding the simulations of calibrated fragility curves for the overturning of piers and abutments, it is worthy to note the greater contribution of the moment associated with the hydrodynamic pressure than the debris impact. The average impact moment does not exceed 0.21 % of the hydrodynamic moment in the case of piers and 0.39 % for abutments. Moreover, it should be noted that the contribution percentage of the impact moment decreases as the lahar height increases.

Concerning the deck sliding, it is important to indicate that the net force is kept relatively constant when the lahar intensity is lower or equal to 2.5 m. This is because the tangential force of the lahar on the superstructure is null. Afterwards, when the lahar reaches the beams

and decks, the average, minimum and maximum net forces obtained in the simulations start to decrease. For example, the average net force is negative when the lahar height is higher or equal than 3.25 m, where the failure probability is 78.9 %. Moreover, if the lahar intensity is higher or equal than 4.0 m, the deck has a 100 % probability of sliding, because the maximum net force obtained in the simulations is negative.

Furthermore, the results showed that the contribution of the force of the debris impact on the superstructure is lower in relation to the hydrodynamic force. In this particular case, the maximum average impact force represents 0.68 % of the hydrodynamic force. The reason is that the impact of debris on the superstructure is infrequent, since it requires the height of the impact to be higher than the height of the substructure, but lower than the road elevation. Nevertheless, if such impact should occur, the impact force would be high.

Regarding the fragility curves by bridge categories, the failure of bridges from category C2 is mainly due to the overturning of piers. In fact, when the lahar height is less or equal to 2.0 m, the pier is the only triggering component, because the other ones have no failure probability. The failure probability of the abutments is greater than zero when the lahar intensity is greater or equal to 2.25 m. At that intensity level, the pier already has a failure probability of 91.4 %, which means that the influence of the abutment on the bridge failure is lower. That is why the fragility curve of C2 bridges is similar to that of the piers overturning.

Something similar occurs in one-span bridges (C1). In this case, the triggering component is the abutment, because it is more vulnerable to lahars than the deck. When the flow depth is higher than 2.25 m and lower than 2.5 m, the C1 bridges can fail only if the abutments overturn, since the sliding probability of the deck is zero. The deck sliding probability is no longer null at 2.75 m, reaching a sliding probability of just 3.9 %, compared with an abutment overturning probability of 67.4 %. Therefore, the abutment is always the main failure factor in this type of bridges.

6.2 Validation of bridge fragility curves due to lahars

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Once the failure model has been validated, the fragility curves must also be validated. The fragility curve validation is necessary to conclude that the probabilistic functions used in the model represent the uncertainty of the system variables. In order to validate parameterized fragility curves, the analytical bridge failure probability (p_a) for a lahar intensity h_{Lahar} was statistically compared with the empirical failure probability (p_e) for the same lahar intensity. A Z-test was performed for every empirical set of points (h_{Lahar}, p_e) to determine whether the difference between two proportions was significant or not. Then, the following null hypothesis was proposed:

$$H_0: p_a = p_e \ vs \ H_a: p_a \neq p_e$$
, (30)

The empirical failure probability is estimated as the proportion of bridges reached by historical lahars with intensity h_{Lahar} that were destroyed. The empirical set of points was obtained from the same information used for the bridge failure model validation (See Table 2).

5 Considering the null hypothesis, the test statistic Z_{test} is given by the following expression:

$$Z_{\overline{test}} = \frac{(\hat{p}_{\alpha} - \hat{p}_{e})}{\sqrt{\hat{p}(1-\hat{p})(\frac{1}{n_{\alpha}} + \frac{1}{n_{e}})}} \sim Normal(0,1) , \qquad (31)$$

$$\hat{p} = \frac{x_a - x_e}{n_a + n_a},\tag{32}$$

Where n_a is the number of bridges evaluated analytically with a lahar with intensity h_{Lahar} (10,000 simulations), x_a the number of simulations in which the bridge fails considering an intensity h_{Lahar} in the analytical model; where n_e is the number of bridges that were reached empirically by lahars with intensity h_{Lahar} and, x_e the number of bridges that were destroyed empirically by lahars with intensity h_{Lahar} . The data and results of the test statistic Z_{test} obtained for each hypothesis test associated with each point are shown in Table 3 and Table 4.

Table 3: Validation data for fragility curves of one-span bridges (C1).

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h (m) -	One-span bridges (C1)						
	n _a	X a	p a	n e	₩e	₽e	Z test
1.50	10,000	0	0.0 %	2	0	0	0.00
2.50	10,000	2,265	22.7 %	3	+	33.3 %	-0.44
3.50	10,000	9,993	99.9 %	4	4	100.0 %	-0.03
5.00	10,000	10,000	100.0 %	2	2	100.0 %	0.00

Table 4: Validation data for fragility curves of multiple-spans bridges (C2).

h (m)	Multiple-spans bridges (C2)							
h (m) -	n _a	X a	p a	n e	₩e	P e	$\mathbf{Z}_{ ext{test}}$	
1.50	10,000	421	4. 21 %	2	0	0	0.30	
3.00	10,000	9,938	99.9 %	2	2	100.0 %	-0.01	

Once the test statistic Z_{test} of every hypothesis test associated with each point is calculated, it is compared with a significance level α for validation. For the fragility curve validation, a significance level of 5% was considered. The critical value ($Z_{crittc=t}$) of ±1.96 delimits the region of acceptance and rejection of the null hypothesis. If the test statistic Z_{test} is located in the acceptance region [-1.96; +1.96], the null hypothesis H_{θ} , stating that the bridge empirical failure probability due to lahars is equal to that obtained by the parameterization (H_{θ} : $p_{\alpha} = p_{e}$); this should be accepted with that significance level. In this case, the Z_{test} values of all the empirical points evaluated are within the acceptance region. The maximum absolute value obtained from Z_{test} was 0.44, for one-span bridges reached by lahars of 2.50 m. Therefore, we conclude that it is possible to accept the null hypothesis H_{θ} , which

establishes that empirical bridge failure probability due to lahars is equal to that indicated by the analytical model, with a 5 % significance level.

6.3 Analysis of validated fragility curves and failure model

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Once the bridge fragility curves due to lahars are calibrated, parameterized and validated, the main results obtained in the research are analyzed. First, it should be highlighted that the model of bridge failure due to lahars proposed was successfully validated for the 15 historical bridges and lahars evaluated. This allows inferring that the developed failure model represents the fragility of its components in the presence of these flows. The null hypothesis H_0 was statistically accepted with a 5 % significance level, completing an empirical validation of the fragility curves. Thus, we can deduce that the modelling method based on the reliability theory and the Monte Carlo simulations can be used for calibrating bridge fragility curves due to lahars. Through the satisfactory validation we conclude that the existing models integrated in the limit state functions and the values of the used variables reflect the stability of the bridge due to a lahar flow. Finally, the validation of the parameterized fragility curves allows us to infer that the cumulative lognormal distribution with the parameters obtained through the MLE represent the bridges' fragility in case of lahars.

The analysis of the models and equations used in the limit state functions demonstrates that the lahar depth is the main variable in the quantification of lahar loads and bridge capacity to response to these flows. The lahar velocity, the scour demand, the hydrodynamic pressure and the height of the debris impact depend on the flow height. Thus, it is concluded that this variable can be used to represent the hazard intensity in the fragility curves associated to lahars.

Regarding the simulations of calibrated fragility curves for the overturning of piers and abutments, it is worthy to note the greater contribution of the moment associated with the hydrodynamic pressure than the debris impact. The average impact moment does not exceed 0.21 % of the hydrodynamic moment in the case of piers and 0.39 % for abutments. Moreover, it should be noted that the contribution percentage of the impact moment decreases as the lahar height increases.

Concerning the deck sliding, it is important to indicate that the net force is kept relatively constant when the lahar intensity is lower or equal to 2.5 m. This is because the tangential force of the lahar on the superstructure is null. Afterwards, when the lahar reaches the beams and decks, the average, minimum and maximum net forces obtained in the simulations start to decrease. For example, the average net force is negative when the lahar height is higher or equal than 3.25 m, where the failure probability is 78.9 %. Moreover, if the lahar intensity is higher or equal than 4.0 m, the deck has a 100 % probability of sliding, because the maximum net force obtained in the simulations is negative.

Furthermore, the results showed that the contribution of the force of the debris impact on the superstructure is lower in relation to the hydrodynamic force. In this particular case, the maximum average impact force represents 0.68 % of the hydrodynamic force. The reason is that the impact of debris on the superstructure is infrequent, since it requires the height of the impact to be higher than the height of the infrastructure, but lower than the road elevation. Nevertheless, if such impact should occur, the impact force would be high.

Regarding the fragility curves by bridge categories, the failure of bridges from category C2 is mainly due to the overturning of piers. In fact, when the lahar height is less or equal to 2.0 m, the pier is the only triggering component, because the other ones have no failure probability. The failure probability of the abutments is greater than zero when the lahar intensity is greater or equal to 2.25 m. At that intensity level, the pier already has a failure probability of 91.4 %, which means that the influence of the abutment on the bridge failure is lower. That is why the fragility curve of C2 bridges is similar to that of the piers overturning.

Something similar occurs in one-span bridges (C1). In this case, the triggering component is the abutment, because it is more vulnerable to lahars than the deck. When the flow depth is higher than 2.25 m and lower than 2.5 m, the C1 bridges can fail only if the abutments overturn, since the sliding probability of the deck is zero. The deck sliding probability is no longer null at 2.75 m, reaching a sliding probability of just 3.9 %, compared with an abutment overturning probability of 67.4 %. Therefore, the abutment is always the main failure factor in this type of bridges.

7 Conclusions and recommendations

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In this paper, a-bridge failure models and bridge fragility curves due to lahars are proposed, considering pier and abutment overturning, as well as, deck sliding. The models development considers the calibration, and parameterization and validation of bridge fragility curves due to lahars based on a-limit state models. Two types of bridges were considered in the analysis: one-span and multiple-span bridges. Monte Carlo simulations were applied to estimate the failure probability given by different lahar depths. Fragility curves of bridges were parameterized by maximum likelihood estimation, using a cumulative lognormal distribution. Through the satisfactory empirical validation evaluation of the failure models and the parameterized fragility curves, we concluded that the models included in the limit state functions and the proposed values to characterize lahar flows are representative of prevailing loads and bridge capacity. In addition, the empirical data deficiency demonstrates the need to develop more effective protocols to report damage from volcanic events on bridges. With this, the empirical validation of developed fragility curves is a source of future research.

The analysis of the validated fragility curves demonstrated that decks fail due to <u>subinfrastructure</u> overturning prior to sliding. The deck sliding probability ceases to null (3.9)

%) when the lahar height is equal to 2.75 m. In the presence of a lahar of this intensity, the pier and abutment overturning probabilities are 98.9 % and 67.4 %, respectively. This implies that the probability that the deck fails and the <u>subinfra</u>structure does not fail is 0.01 %, considering that these are independent events. In addition, the research concluded that bridges with multiple spans are more vulnerable to lahar flows compared to bridges with one span. The most evident difference between these bridges was obtained in the lahars of height 2.25 m. Given this intensity, bridges with one span (C1) have a 0.3 % probability of failure, while those with multiple spans (C2) have a 92.0 % probability of failure. This result was expected because when impacted by lahars, piers are more susceptible to overturn than abutments.

With the developed fragility curves, agencies can determine the failure probability of bridges due to a lahar presenting a specific depth. The proposed failure models can be adapted and calibrated to bridge designs that are different than the structures accounted for in the article. When required, the supply function considered in the models can be conditioned to local bridge design standards and adjusted accordingly.

For the application of these models, it is recommended that expected hazard scenarios, in terms of recurrence and intensity, should be first simulated. The resulting hazard intensity can then be estimated for the affected road network, in particular exposed bridges, and their failure probability can be consequently calculated. Further research is being conducted in this regard, where a computational platform is being developed for the consistent application of the developed fragility curves for the exposed networks. With this, local authorities can review their road and bridge designs and existing infrastructure in order to assess and apply mitigation strategies prior to the occurrence of a volcanic event.

Acknowledgements

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The authors thank the National Commission for Scientific and Technological Research (CONICYT), which has financed the FONDEF Project ID14I10309 Research and Development of Models to Quantify and Mitigate the Risk of Natural Hazards in the National Road Network. Likewise, we express our gratitude to the institutions that participated and contributed to this research project, especially to: the Research Center for Integrated Disaster Risk Management CONICYT/FONDAP/15110017 (CIGIDEN), the Highways Department of the Chilean Ministry of Public Works and the National Geology and Mining Service of the Chilean Ministry of Mining, the National Emergency Office of the Ministry of Interior and Public Security (ONEMI) and the Chilean Association of Concessionaires (COPSA).

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REPLY TO REFEREES AND GUIDE TO THE REVISION OF THE PAPER

Natural Hazards and Earth System Sciences

Title: Development of Bridge Failure Model and Fragility Curves for Infrastructure Overturning and Deck Sliding due to Lahars

5 **Authors:** Joaquín Dagá, Alondra Chamorro, Hernán de Solminihac, Tomás Echaveguren

MS Nº: nhess-2017-330

Anonymous Referee #1

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The authors appreciate the comments made by Referee # 1. In this version of the paper, the text, figures, tables and equations were adjusted taking into account all the suggestions of the referees. In addition, the writing, punctuation and English level were improved.

<u>Point 1.1:</u> Title: the concept of 'bridge failure model', the difference between 'bridge failure' and 'infrastructure overturning and deck sliding', the definition of 'infrastructure' are not clear, this leads the reader to imagine what will come from the manuscript from the title difficult. My suggestion is, something like, 'Development of failure model and fragility curves for road bridges under lahar impact' or simpler 'Development of fragility curves for road bridges under lahar impact'.

We appreciate the suggestion of Referee #1 and we realize that the title is not completely clear to a potential reader. The 'infrastructure' concept can be confusing in the title. The adjusted title reads as follows:

20 "Development of fragility curves for road bridges exposed to volcanic lahars"

<u>Point 1.2:</u> The ambiguity of terminologies makes difficult to follow the meaning of not only title but remaining part of the manuscript. E.g. 'infrastructure' covers a broad sense. Road network itself can be included in the concept of 'infrastructure' (as used in the first line of the abstract). 'Infrastructure' is mainly used to mean a foundation of something in this manuscript, especially for a bridge. If so, it is better to describe 'bridge infrastructure' or 'bridge foundation'.

We completely agree with Referee #1 that the term 'infrastructure' was used ambiguously to refer to the infrastructure in general (roads, bridges, buildings, etc.) and to the part of the bridge that supports the superstructure (piers and abutments).

We reviewed in detail the definitions of the bridge elements given by the LRFD Bridge Design Specifications of American Association of State Highway and Transportation Officials (AASHTO, 2012) and to refer to the piers and abutments the term 'substructure' should be used instead of 'infrastructure'. According to AASHTO (2012), substructure is the structural part of the bridge that support the horizontal span (i.e. piers and abutments). Thus, the term 'infrastructure' now is used only to refer to the infrastructure in general (roads,

bridges, buildings, etc.) and 'substructure' to piers and abutments. The term 'substructure' is defined in section 1:

"To characterize bridge fragility to lahars, failure probability of primary structural elements is required, namely: substructure (i.e. piers and abutments) and deck."

<u>Point 1.3:</u> The word 'abutment' has potentially two meaning, one is the foundation of bridge pier and other is the marginal area between a river bank and the bridge. So the reader wonders what you want to say using the word 'abutment', so it is needed to clarify which do you want to mean or use another word.

We agree with Referee #1, the term 'abutment' generates confusion since it has potentially two meanings. In order to clarify this, in the introduction we formally define the most vulnerable elements of bridges due to lahars (piers, abutments and deck). The LRFD Bridge Design Specifications of American Association of State Highway and Transportation Officials (AASHTO, 2012) are used for the elements definitions. The definitions of the elements read as follows:

"Piers are columns designed to be an interior support for a bridge superstructure; abutments are the end support for a bridge superstructure; and deck is the component that supports wheel loads directly and is supported by other components (AASHTO, 2012)."

Point 1.4: You used 'failure model' (singular) so maybe you want to define 'failure model' as the toolbox to identify damage or non-damage for all possible types of failure mode. On the other hand, 'fragility curves' (plural) were made for each failure type. This means, the failure model was actually composed of several sub-models corresponding to each failure mode, and the sub-models were used to develop each fragility curve, if my understanding is correct. What I want to say is that it is better to use 'failure models' instead of 'failure model'.

Again we agree with Referee #1. Indeed, the failure model was composed of several sub-models and each sub-model was used to develop a fragility curve. Thus, it is better to use 'failure models' instead of 'failure model'. We adopted the suggestion of the referee and the terms 'failure model' are now in plural. For example, the second sentence of the abstract reads as follows:

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"In this paper, bridge failure models due to lahars are proposed and, based on these, fragility curves are developed."

<u>Point 1.5:</u> Page 1, line 35, I'd like to replace 'losses' --> 'restrictions' and remove 'permanent'.

We completely agree that the terms used in that sentence are not precise. The effects of volcanic eruptions on roads are operational restrictions and physical damage. The sentence was adjusted as follows:

"Volcanic eruptions produce operational restrictions and physical damage to road infrastructure."

Point 1.6: Page 1, line 35, It is not clear how 'highway' and 'road' distinguished in the manuscript.

We agree that the terms 'highway' and 'road' could generate confusion in the reader. To avoid this, now only the general term 'road' is used. Thus, the terms 'highway' were replaced by 'road' in the paper. The adjusted sentence reads as follows:

40 "Volcanic eruptions produce operational restrictions and physical damage to road infrastructure."

Point 1.7: Page 2, line 2, 'temporary' --> 'temporal'?

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We appreciate the comment of Referee #1. The text was adjusted as follows:

"Consequences related to pyroclastic fall, specifically tephra, are temporal road closures caused by visibility limitations and reduced friction between pavement and tires (Nairn, 2002; Leonard et al., 2005; Wilson et al., 2012)."

<u>Point 1.8:</u> Page 2, line 3, 'loss of surface friction' --> 'loss of friction between (road) pavement and tires'?

We agree with Referee #1 that in this sentence we should specify the surfaces that lose friction due to pyroclastic fall. In order to detail this, the sentence was adjusted as follows:

"Consequences related to pyroclastic fall, specifically tephra, are temporal road closures caused by visibility limitations and reduced friction between pavement and tires (Nairn, 2002; Leonard et al., 2005; Wilson et al., 2012)."

<u>Point 1.9:</u> Page 2, line 10, 'affect(ed)' is quite neutral but here you want to say some negative meaning so ''damaged' or something like this may be better to use here (not only here but other sentences using 'affect(ed)').

We completely agree with Referee #1. Indeed, in this sentence we want to highlight the negative effects of lahars on roads. Thus, we replaced the term 'affect(ed)' (quite neutral) by the term 'damaged' (negative). The adjusted sentence reads as follows:

"Road infrastructures reached by lahars are damaged physically and operationally (Smith and Fritz, 1989)."

Point 1.10: Page 2, line 14, The meaning of 'critical' here is not clear.

We agree that in this sentence the term 'critical' was not clear. To avoid confusion, we decided to replace the term 'critical' by 'most exposed and vulnerable'. The adjusted text reads as follows:

"Wilson et al. (2014) demonstrated that bridges and culverts are the road infrastructures elements most exposed and vulnerable to lahars."

Point 1.11: Page 2, line 16, put 'a' before 'consequence'.

We appreciate again the comment of Referee #1. The corrected sentence reads as follows:

"Blong (1984) and Wilson et al. (2014) reported that 300 km of roads were damaged and 48 bridges were affected because of Mount St. Helens (USA) eruption in 1980."

Point 1.12: Page 2, line 27, 'studies' --> 'covers'?

We completely agree that in this case the term 'covers' is better than 'studies' to refer to the scope of the software HAZUS-MH. Thus, the sentence was adjusted as follows:

"This GIS-based software covers three natural hazards: earthquakes, floods and hurricanes, excluding the volcanic hazard from the analysis (FEMA, 2011)."

Point 1.13: Page 2, line 33, 'effects' --> 'interruption'

We agree with Referee #1 that the term 'effects' should be replaced by 'interruption'. The term 'effects' was duplicated in the sentence. The adjusted text reads as follows:

"Nevertheless, the effects of volcanoes are only accounted for in terms of ash fall and the temporary interruption of infrastructure operation (Kaye, 2008)."

Point 1.14: Page 2, line 36, 'and' --> 'nor'?

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We agree with Referee #1 that this sentence was not written correctly. The text was adjusted as follows:

"From available literature and the current state-of-the-practice, it is concluded that no bridge fragility curves exposed to lahar flows have been developed."

<u>Point 1.15:</u> Page 2, line 40, It is not clear how 'calibration' and 'parameterization' distinguished.

We sincerely appreciate the comment from Referee #1. Indeed, the terms 'calibration' and 'parameterization' could generate confusion. In order to clarify the concepts, the term 'parameterization' is described in the section 1. The adjusted text reads as follows:

"Best-fit probability functions are finally proposed, considering cumulative lognormal distribution and their corresponding parameters from maximum likelihood analysis (parameterization)."

Point 1.16: Page 3, line 7, What do you mean by 'analytical models'?

We appreciate the comment of Referee #1. The term 'analytical models' refers to models that characterize the limit state of the element (bridge), based on probabilistic and deterministic variables defining the system (lahar-bridge).

We note that this term ('analytical models') could be confusing for the reader, because this type of models is not yet defined in the text. Thus, we decided to remove it from this sentence and let the general term 'models'. Analytical models are defined later (section 2.2). The adjusted sentence reads as follows:

"Failure models are then proposed, considering the limit state of pier and abutment overturning due to lahar demanding forces and reduced supply moment caused by scour."

<u>Point 1.17:</u> Page 3, lines 21-22, 'Debris flows are highly viscous slurries of sediment and water'. I think 'debris' is explained but not about 'flows'.

We appreciate the comment of Referee #1. As noted in the text, Smith and Fritz (1989) categorized lahars according to their sediment/water ratio into: (1) debris flows and (2) hyper-concentrated flows. These are the two types of lahars. Both are defined between lines 21 and 27 on page 3.

<u>Debris flows:</u> are highly viscous slurries of sediment and water. Debris flows are capable of transporting gravel-sized debris in suspension, and their concentration of solid particles ranges between 75 and 80 % in weight or 55 and 60 % in volume.

35 <u>Hyper-concentrated flows:</u> have high-suspended fine contents, predominantly due to fluid motion and properties. The solid concentrations of hyper-concentrated flows can represent up to 55 to 60% of the total weight, and 35 to 40% of the total volume.

We hope the question of Referee #1 has been answered.

Point 1.18: Page 3, line 28, I think you can remove 'so'.

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We agree with Referee #1 that the term 'so' can be removed. The text was adjusted as follows:

"The flow of lahars is guided by gravity and is capable of impacting elements located tens of kilometers away from the crater of the volcano (Parfitt and Wilson, 2008)."

<u>Point 1.19:</u> Page 3, lines 36-37, 'scour of the riverbed drags massive material blocks' doesn't make sense.

We sincerely appreciate the comment of Referee #1. The sentence was not written correctly. The text was adjusted as follows:

10 "Watery sediment floods are more erosive than sediment-rich flows. The scour of the riverbed drags material blocks and vegetation."

Point 1.20: Equation (1): Is DS defined? What is the meaning of subscript i?

We appreciate the comment of Referee #1. The variable 'DS' was not defined in the paper and the meaning of the subscript 'i' was not explained. A definition of both elements was added. The text was adjusted as follows:

"Fragility curves express the probability that the damage state (DS) of a system exceeds different levels (ds_i ; i=slight, moderate, extensive or complete), given a certain hazard intensity (IM) (See Eq. 1)."

Point 1.21: Page 4, line 26, 'the recently described approaches' --> 'the approaches described above'?

Again we agree with Referee #1 that the sentence was not written properly. The corrected text reads as follows:

"Finally, a hybrid method, which combines two or more of the approaches described above, can be used."

25 <u>Point 1.22:</u> Title of Section 3. I'd like to suggest to replace as '(Development of) failure model(s) for bridge pier/abutment overturning and deck sliding due to lahars'

We appreciate the suggestion of Referee #1. The title of Section 3 was not clear, because of the confusion that the 'infrastructure' concept can generate for the reader. The corrected title reads as follows:

30 "3 Development of failure models for bridge pier/abutment overturning and deck sliding due to lahars"

<u>Point 1.23:</u> Page 5, The first paragraph of section 3.1, so do you define that g(X)=D(X)-S(X)? If so, it is better to describe so using equation.

We sincerely appreciate the comment from Referee #1. Indeed, the limit state function is defined as the difference between the supply and demand functions (i.e. g(X)=D(X)-S(X)). In order to better describe this relationship, an equation was added, as suggested by Referee #1. The adjusted text reads as follows:

"The limit state function (g(X)) of the bridge-lahar system is given by the difference between the supply and demand functions (D(X) - S(X)). If g(X) is lower than zero, the lahar loads

on the structure are greater than the bridge capacity and hence, the bridge will fail."

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<u>Point 1.24:</u> Figure 1: It is not clear how the abutment overturning and the pier overturning were distinguished. Maybe, it is better to specify where are the deck, pier and abutment in Figure 1. Can we discuss the pier overturning using the moment Mn defined in Figure 1? Can you define Fwi, Fws, Fr in Figure 1?

We appreciate the comment from Referee #1. Figure 1 shows a generic cross section of a pier or abutment and the deck. To clearly show where each element is in the figure, the deck, the column and the foundation are now indicated. The main forces of the system are also shown (F_t , F_r , F_i , etc.). Figure 1 was adjusted as follows:

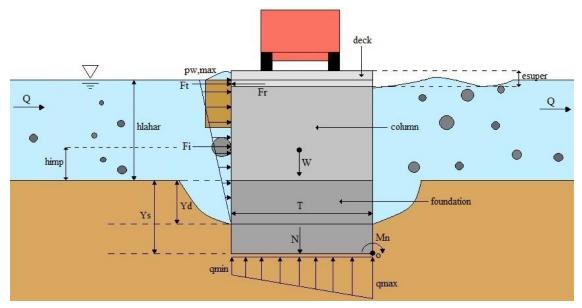


Figure 1: Free-body diagram of bridge resisting and demanding forces and moments in the presence of a lahar.

<u>Point 1.25:</u> Equations (3) and (5) Are Yso and Fr function of X? If so, how do you change Yso and Fr depending on X?

- We sincerely appreciate the comment from Referee #1. 'X' is the basic variables vector of the bridge-lahar system. The supply (overturning moment M_r , friction force F_r and scour supply Y_{so}) and demand functions (overturning moment M_v , tangential force F_t and scour demand Y_{sd}) depend on these basic variables (X).
- For example, the scour supply (Y_{so}) depends on the design height, pier width and correction factors by flow angle, pier shape, among others (Eqs. 11 and 12). The friction force (F_r) depends on the bridge specific weight, superstructure thickness, bridge length, among others (Eq. 25).

Point 1.26: Page 8, line 5, 'produced' --> 'caused'

Again we agree with Referee #1. The term 'produced' should be replaced by 'caused'. The text was adjusted as follows:

"The scour caused by lahar flows near the foundations contributes to a greater vulnerability of these bridge components, since the lahars produce destabilization and weakening around the foundation of piers and abutments."

Point 1.27: Title of Section 4. It is not clear what do you want to mean by 'experiment'.

We completely agree with Referee #1 that the term "experiment' generates confusion. The title of section '4 Experimental design for modelling infrastructure overturning and deck sliding due to lahars' was replaced by '4 Proposal for modelling substructure overturning and deck sliding due to lahars'. In this section the physical models integrated in the bridge failure model are detailed and the values of the basic variables are indicated.

10 Point 1.28: Page 9, line 10, 'For this case' --> 'In this study'?

We completely agree with Referee #1 that the term 'For this case' should be replaced by 'In this study'. The adjusted text reads as follows:

"In this study, a rectangular shape is assumed."

Point 1.29: Page 9, line 22, 'this study' --> 'Muller (1996)'?

We appreciate the comment from Referee #1. We agree that the study referred to in this sentence should be indicated by the author and the year of publication. The adjusted sentence reads as follows:

"The conclusion of Müller (1996) was that the equation proposed by Arneson et al. (2012) in the Hydraulic Engineering Circular No. 18 (HEC-18) was suitable for quantifying the scour depth."

Point 1.30: Page 9, line 24, 'the magnitude of the scour' --> 'the scour depth'?

We agree that the 'magnitude of the scour' should be replaced by 'the scour depth', because in this study the scour is directly measured through the scour depth. The sentence was adjusted as follows:

25 "The conclusion of Müller (1996) was that the equation proposed by Arneson et al. (2012) in the Hydraulic Engineering Circular No. 18 (HEC-18) was suitable for quantifying the scour depth."

<u>Point 1.31:</u> Page 9, line 27, The meaning subscript of Y is not clear. (c-d, e-d, c-o, e-o, etc.) Maybe you can specify this by a figure.

We noted that the subscripts of Y (c-d, e-d, c-o, e-o, etc.) could be confusing for the reader. Thus, we decided to change them to the initial letters of demand (d), offer (s), pier (p) and abutment (a). The new subscripts of Y and their meanings are:

Y_d: scour demand

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Y_s: scour supply

 Y_{d-p} : scour demand on piers

Y_{d-a}: scour demand on abutments

Y_{s-p}: scour supply on piers

Y_{s-a}: scour supply on abutments

Point 1.32: Page 9, line 27, Eq. (8) and (9) --> Eqs. (8) and (9).

We appreciate the comment from Referee #1. Indeed, the term 'Eq.' should be plural ('Eqs.') because it refers to both equations (8 and 9). The corrected sentence reads as follows:

"To incorporate the debris accumulation, the scour demand on the piers (Y_{d-p}) is modelled with Eqs. (8) and (9) of the NCHRP (2010)."

Point 1.33: Page 11, Can you define h_design, e_super, h_imp etc. using figure?

We sincerely appreciate the comment from Referee #1. In order to better describe some geometric variables of the system, the main variables (h_{lahar}, e_{super}, h_{imp}, Y_s, Y_d) were defined using Figure 1, as suggested by Referee #1. The meaning of these variables is described in the paragraph located under Figure 1 and in Table 1. Figure 1 was adjusted as follows:

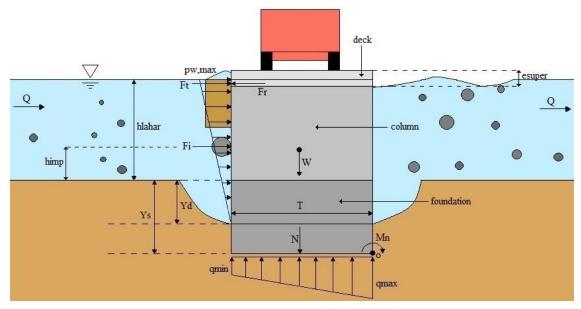


Figure 1: Free-body diagram of bridge resisting and demanding forces and moments in the presence of a lahar.

Point 1.34: Page 11, 'grava'-->'gravel'

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We appreciate the suggestion of Referee #1. The variables ' γ_{Grava} ' and ' D_{Grava} ' in Eq. (19) should be ' γ_{Gravel} ' and ' D_{Gravel} '. The corrected Eq. (19) reads as follows:

$$M_{i} = \begin{cases} v_{Lahar} \sqrt{\gamma_{Gravel}} \frac{4}{3} \pi \left(\frac{D_{Gravel}}{2}\right)^{3} \left(h_{imp} + Y_{s}\right) & h_{imp} \leq h_{Design} \\ 0 & h_{imp} > h_{Design} \end{cases}, \tag{19}$$

20 <u>Point 1.35</u>: Table 1, Definition of numbers in Deterministic value/probabilistic distribution is not clear. E.g. what is the meaning of 1.0 and 1.9 for $K_{\rm gr}$? What 1.0, 1.06 and 1.06 mean for $K_{\rm R}$? What is the meaning of '1,1' for $K_{\rm 3}$?

We sincerely appreciate the comment from Referee #1. In the fourth column of Table 1 the deterministic value or probabilistic distribution of the system basic variables are detailed. If

the variable is stochastic, the probabilistic distribution and the related parameters are indicated. If the variable is deterministic, the constant value of the variable is indicated.

For example, K_{gr} has a uniform distribution with parameters 1.0 and 1.9 (i.e. minimum 1.0 and maximum 1.9). K_R has a triangular distribution with parameters 1.0, 1.6 and 1.6 (i.e. minimum 1.0, maximum 1.6 and mode 1.6). The value of K_3 was incorrect. It should be '1.1' instead of '1,1', because it is a deterministic variable.

<u>Point 1.36:</u> Table 2, can you show the type of failure (actual and predicted) for each bridge? Also can you show the predicted failure probability for each bridge?

Regrettably, there is a lack of quality empirical information related to the impacts of volcanic events on Chilean bridges. From the agencies reports we can only know if the bridges failed or not due to the lahars. Thus, we cannot know in detail what was the type of failure (pier/abutment overturning and/or deck sliding).

Once again, the authors appreciate the comments made by Referee #1 and believe that the manuscript improved significantly after including the suggested adjustments.

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REPLY TO REFEREES AND GUIDE TO THE REVISION OF THE PAPER

Natural Hazards and Earth System Sciences

35 **Title:** Development of Bridge Failure Model and Fragility Curves for Infrastructure Overturning and Deck Sliding due to Lahars

Authors: Joaquín Dagá, Alondra Chamorro, Hernán de Solminihac, Tomás Echaveguren

MS N°: nhess-2017-330

Anonymous Referee #2

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The authors appreciate the comments made by Referee # 2. In this version of the paper, the text, figures, tables and equations were adjusted taking into account all the suggestions of the referees. In addition, the writing, punctuation and English level were improved.

<u>Point 2.1:</u> Section 6.2, and all references to the statistical validation (p. 1, lines 27-29; section 6.3 first paragraph; p. 22, line 16) should be removed completely.

We sincerely appreciate the comment from Referee #2. Indeed, the number of empirical data for the fragility curves validation (section 6.2) is too small. Thus, the probability of not rejecting the null hypothesis when it is actually false is high due to the small sample.

There is a lack of quality empirical information related to the impacts of volcanic events on infrastructure. Although we used all the records of lahars produced during the eruptions of the Villarrica volcano in 1964, 1971 and 2015, and the Calbuco volcano in 1961 and 2015, which were the most destructive volcanic events in Chile in the last 50 years, there is not enough empirical data available.

We adopted the suggestion of Referee #2 and removed the section 6.2 (and all the related references) and the section 6.3 first paragraph. The adjusted paper has a section '6 Evaluation of the bridge failure models against empirical data and analysis of results', in which the validation of the failure model is explained and analyzed considering the 15 empirical data. In addition, the lack of empirical information for the validation of fragility curves is highlighted. The results of the failure models and the developed fragility curves are also analyzed.

- Point 2.2: In section 6.3, the authors should additionally highlight the data-deficiency issue (possibly as a source of future work) and critically evaluate the success of the model in reference to Table 2. How representative is the empirical data of the range of conditions used to generate the analytical fragility curves? Are the main sources of force/vulnerability sufficiently explored with the empirical data and/or could qualitative 'bounds' on the reliability of these curves be determined?
- 30 Again we appreciate the comment from Referee #2. In the new section 6 and in 'Conclusions' the deficiency and lack of empirical data to statistically validate the developed fragility curves is highlighted:
- "However, there is insufficient empirical data to provide a statistical validation of the bridge fragility curves. There are only 15 empirical points (h_{Lahar}, p_e) to validate two fragility curves (C1 bridges and C2 bridges). Thus, a deficiency of empirical data on impacts of lahars on bridges is identified."
 - In addition, section '7 Conclusions and recommendations' indicates that the statistical validation of developed fragility curves using empirical data is a source of future research:
- "In addition, the empirical data deficiency demonstrates the need to develop more effective protocols to report damage from volcanic events on bridges. With this, the empirical validation of developed fragility curves is a source of future research."

Finally, in section 6 the ranges of the empirical values of some variables (lahar density, lahar speed, slope, bridge length, bridge width, etc.) of the system lahars-bridges of the 15 historical data are given and analyzed:

"The historical data of Table 2 consider lahars from 1.5 m to 5.0 m of depth, covering the entire range of hazard intensity of developed fragility curves (1.5 m to 4.0 m). The density of the evaluated lahars ranges from 16,000 to 19,000 N/m³; the slope from 1.0° to 1.2°; the bridge length from 11.3 m to 72.5 m; the bridge width from 3.9 m to 8.3 m; the bridge height from 2.5 m to 5.5 m; the number of deck support from 0 to 5; the bridge height from 2.5 m to 8.3 m; the number of deck support from 0 to 5; the bridge materials are concrete and wood; the number of bridge lanes are 1 and 2. Thus, the empirical data evaluated demonstrate representativeness of the range of the basic variables of the analytical model (Table 1)."

Point 2.3: p.1 Line 29: "...that were reached..." change to "affected"

We agree that the term 'reached' should be replaced by 'affected'. We adopted the suggestion and the corrected sentence reads as follows:

15 "Bridge failure models are empirically evaluated using data of 15 bridges that were affected by lahars in the last 50 years."

<u>Point 2.4:</u> p.2 Line 6: This implies a lower hazard only, not hazard intensity. Remove "intensity".

We completely agree with Referee #2. The low probability of occurrence and the small influence area of lava and pyroclastic flows imply only a lower hazard and exposure, but not necessary a lower hazard intensity. A lower risk of lava and pyroclastic flows on road infrastructure is consequently expected. We adjusted the text as follows:

"Lava and pyroclastic flows may destroy road infrastructure, however, the probability of occurrence of these events is low and exposed areas are limited (Wilson et al., 2014). Considering that risk is a function of the hazard, exposure and vulnerability (UNISDR, 2009), a lower risk of lava and pyroclastic flows on road infrastructure is consequently expected."

<u>Point 2.5:</u> p.3 Line 6: "...experimental design was elaborated..." not sure what this means here - possibly reword.

We agree that the term "experimental design' generates confusion. In order to avoid misunderstandings, this sentence was removed and the title of section '4 Experimental design for modelling infrastructure overturning and deck sliding due to lahars' was replaced by '4 Proposal for modelling substructure overturning and deck sliding due to lahars'. In this section the physical models integrated in the bridge failure model are detailed and the values of the basic variables are indicated.

Point 2.6: p.6 Figure 1: What is Ft?

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We appreciate the comment from Referee #2. The variable Ft was not defined under Figure 1. The following sentence was added to the paragraph located below Figure 1:

"The tangential force F_t corresponds to the sum of the hydrodynamic force and the debris impact force applied to the superstructure."

Point 2.7: p.9 Line 10: Change to "...a rectangular shape is assumed."

Again we agree with Referee #2. The term 'rectangular flow' should be replaced by 'rectangular shape'. The corrected sentence reads as follows:

"In this study, a rectangular shape is assumed."

Point 2.8: p.10 Equation 14: Change to Yw; found (misspelt as fuond)

We appreciate the comment from Referee #2. The variable ' $y_{w,fuond}$ ' in Eq. (14) should be ' $y_{w,found}$ '. The adjusted Eq. (14) reads as follows:

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$$y_{w,found} = Y_s - \frac{Y_d}{3}$$
, (14)

<u>Point 2.9:</u> Equations 13, 20, 21, 24 use the parameter L, which is bridge width. Introduce it at the first instance (Eq. 13) and I would suggest changing it to a less confusing variable (perhaps T for thickness).

We completely agree that the use of the parameter 'L' for the bridge width could be confusing for the reader. To avoid this confusion, the 'L' parameter was changed to 'T' (Thickness) in the Eqs. 13, 20, 21, 22, 23, 24 and in Table 1, as suggested by Referee # 2.

In addition, the variable 'T' was defined before the Eq. 13, as shown below:

"The resulting hydrodynamic force exerted by the lahar on the foundation $(F_{w,found})$ and the height at which this force acts with respect to the turning axis $(y_{w,found})$ are given by Eq. (13) and Eq. (14), where the variable T corresponds to the bridge width:"

$$F_{w,found} = TC_D \left(\frac{\gamma_{Lahar}}{2g} \right) v_{Lahar}^2 \left(\frac{Y_d^2}{h_{Lahar} + Y_d} \right), \tag{13}$$

Point 2.10: p.13 Table 1: Variable e_{super} is not listed on the table - what is its value?

We sincerely appreciate the comment from Referee #2. Indeed, the variable 'e_{super}' was not listed on Table 1. To show the name, unit, value (probabilistic distribution) and reference of 'e_{super}', the following row was added in Table 1:

Table 1: Basic variables involved in the limit state functions.

Variable	Name	Unit	Deterministic Value/Probabilistic Distribution	Value Reference
e_{Super}	Superstructure Thickness	cm	Gen. Ext. Value (18.6; 4.7; 0.3)	Bridge Inventory (MOP)

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<u>Point 2.11:</u> p.16 Line 20: This is a valid statement for your study, although I believe it may vary with type and depth of foundations (e.g. the use of piers).

We completely agree with Referee #2 that we can indicate that deck sliding is not a triggering factor of bridge failures only in this case (Villarrica and Calbuco volcanoes). In order to highlight this, the text was adjusted as follows:

"The deck sliding is not a triggering factor of bridge failures due to lahars generated by Villarrica and Calbuco volcanoes."

Point 2.12: p.17 Line 29: Remove "...it was concluded that its..."

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We appreciate the comment from Referee #2. We adopted the suggestion and removed the term 'it was concluded that its'. The adjusted sentence reads as follows:

"Regarding the bridges with two or more spans (C2), it was concluded that its collapse height due to lahars could be represented by a cumulative lognormal distribution with μ equal to 0.63 and β equal to 0.13."

Once again, the authors appreciate the comments made by Referee #2 and believe his/her suggestions and observations have greatly improved the manuscript.