

1     **UAV-based mapping, back analysis and trajectory modelling of a**  
2     **co-seismic rockfall in Lefkada Island, Greece**

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19    **Abstract**

20    We present field evidence and a kinematic study of rock block motion mobilised in  
21    the Ponti area by a  $M_w$  6.5 earthquake near the island of Lefkada on 17<sup>th</sup> November  
22    2015. A detailed survey was conducted using an Unmanned Aerial Vehicle (UAV)  
23    with an ultra-high definition (UHD) camera, which produced a high-resolution  
24    orthophoto and a Digital Terrain Model (DTM). The sequence of impact marks from  
25    the rock trajectory on the ground surface was identified from the orthophoto and field  
26    verified. Earthquake characteristics were used to estimate the acceleration of the  
27    rock slope and the initial condition of the detached block. Using the impact points  
28    from the measured rockfall trajectory, an analytical reconstruction of the trajectory  
29    was undertaken, which led to insights on the coefficients of restitution. The measured  
30    trajectory was compared with modeled rockfall trajectories using recommended

31 parameters. However, the actual trajectory could not be accurately predicted,  
32 revealing limitations of existing rockfall analysis software used in engineering  
33 practice.

## 34 **Keywords**

35 Rockfall, earthquake, DSM, DTM, modelling, restitution, UAV

## 36 **1. Introduction**

37 Active faulting, rock fracturing and high rates of seismicity contribute to a high rockfall  
38 hazard in Greece. Rockfalls primarily damage roadways and houses (Saroglou,  
39 2013) and are most often triggered by rainfall and, secondly, seismic loading. In  
40 recent years, some rockfalls have impacted archaeological sites (Marinos &  
41 Tsiambaos, 2002, Saroglou et al., 2012). The Ionian Islands, which include Lefkada  
42 Island, experience frequent  $M_w$  5-6.5 earthquakes, as well as less frequent larger (up  
43 to 7.5) earthquakes. The historical seismological record for the island is particularly  
44 well constrained with reliable detailed information for at least 23 such earthquake  
45 events that induced ground failure since 1612. On average, Lefkada experiences a  
46 damaging earthquake every 18 years. In the recent past, a  $M_w$  6.2 earthquake  
47 occurred on August 14 2003 offshore the NW coast of Lefkada, and caused  
48 landslides, rockslides and rockfalls along the western coast of the island (Karakostas  
49 et al. 2004, Papathanasiou et al., 2012). Significant damage was reported,  
50 particularly in the town of Lefkada, where a PGA of 0.42g was recorded.

51 On November 17<sup>th</sup> 2015, an  $M_w$  6.5 earthquake struck the island of Lefkada and  
52 triggered a number of landslides, rockfalls and some structural damage. The most  
53 affected area by large rockslides was the western coast of the island, especially  
54 along its central and south portion, which are popular summer tourist destinations  
55 (Zekkos et al., 2017). The coseismic landslides completely covered the majority of  
56 the west coast beaches and damaged access roads.

57 On the southeast side of Lefkada, near the Gulf of Vassiliki, a seismically-triggered  
58 rockfall in Ponti village was responsible for one of two deaths caused by the  
59 earthquake (Figure 1). Of particular interest, is the very long travel path of the rock  
60 block, which was about 800 m in plan view from the point of detachment to the end of  
61 its path. Near the end of the rock fall path, the block impacted a family residence,  
62 penetrated two brick walls and killed a person in the house. The block exited through  
63 the back of the house and came to rest in the property's backyard.

64 The Ponti village rockfall site is a characteristic example of how seismically-induced  
65 rockfalls impact human activities. It also provides an opportunity to evaluate 2D and  
66 3D rockfall analysis to predict details of the rockfall trajectory, based on field  
67 evidence. In order to create a highly accurate model of the rockfall propagation in 2D  
68 and 3D space, the rock path and the impact points on the slope were identified by a  
69 field survey. The study was performed using an Unmanned Aerial Vehicle (UAV) with  
70 an ultra-high definition (UHD) camera, which produced a high-resolution orthophoto  
71 and a Digital Terrain Model (DTM) of the slope. The orthophoto was used to identify  
72 the rolling section and the impact points of the rock along its trajectory, which were  
73 verified by field observation. The high-resolution DTM made it possible to conduct  
74 kinematic rebound analysis and a 3D rockfall analysis.

## 75 **2. Ponti rockfall - site conditions**

76 The locations of the epicenters of the 2003 and 2015 events, as well as the location  
77 of the rockfall case study are shown in Figure 1. The southwest coast of Lefkada is  
78 part of the Triassic to Eocene age Paxos zone and consists of limestones and  
79 dolomites that are covered by Neogene clastic sedimentary rocks, mostly sandstones  
80 and marls. Figure 1 also shows faults and high rockfall hazard areas as identified by  
81 Rondoyanni et al. (2007). The rockfall at Ponti is not located in an identified high  
82 rockfall hazard area. Based on measurements conducted at one location along the  
83 rockfall path using the Multichannel Analysis of Surface Waves method, the in-situ

84 shear wave velocity of the top layer was estimated to be around 800 m/s, which is a  
85 high velocity and is consistent with the limestone rock at the site.

86 The slope overhanging Ponti village (shown in Fig. 2) has a maximum height of 600  
87 m and an average slope angle of  $35^{\circ}$  to  $40^{\circ}$ . The geological formations at the Ponti  
88 rockfall site are limestones covered by moderately cemented talus materials. The  
89 thickness of the talus materials, when present, ranges between 0.5 and 4.0 m.  
90 Several detached limestone blocks were identified on the scree slope, with volumes  
91 between 0.5 and  $2 \text{ m}^3$ . Based on the size distribution of these rocks on the slope, the  
92 average expected block volume would be in the order of 1 to  $2 \text{ m}^3$ .

93 The rockfall release area was at an elevation of 500 m, while the impacted house  
94 (shown in Figure 3) at an elevation of 130 m. The volume of the detached limestone  
95 block was approximately  $2 \text{ m}^3$  and its dimensions equal to 1.4 m x 1.4 m x 1 m.  
96 There was no previously reported rockfall incident at Ponti that impacted the road or  
97 a house.

### 98 **3. UAV mapping**

#### 99 **3.1. Introduction**

100 A quadrotor UAV (Phantom 3 professional) was deployed to reach the uphill terrain  
101 that was practically inaccessible. The UAV was equipped with an Ultra-high definition  
102 (UHD) 12 MP camera and had the capacity to collect 4K video. The sensor was a  
103  $1/2.3''$  CMOS (6.47x3.41mm) and the effective pixel resolution was 12.4 MP  
104 (4096x2160 pixels). An immediate UAV data acquisition expedition was conducted 2  
105 days after the earthquake. A second more detailed mapping UAV expedition with the  
106 objective to create a DTM was conducted 5 months after the rockfall event.

107 The first objective of the UAV deployment was to find the initiation point of the rock  
108 and then identify the rockfall path (shown in Figure 2). A particular focus on that part  
109 of the task was the identification of rolling and bouncing sections of the rockfall path.

110 In addition, to generate a high-resolution orthophoto of the rockfall trajectory, aerial  
111 video imagery was collected, and the resulting digital surface model (DSM) and  
112 digital terrain model (DTM) was used to perform rockfall analysis.

113 The aerial survey was conducted by capturing 4K video along a gridded pattern  
114 covering the area of interest, at a mean flight altitude of 115m above the terrain  
115 resulting image frames of a mean ground sampling distance (GSD) of  
116 4.97cm/pix. The overlap between image frames was minimum frontal 80%, side 65%  
117 and a total of 714 camera stations (video frames extracted) were included as shown  
118 in Figure 4.

119 The Structure-from-Motion (SfM) methodology was implemented to create a 3D  
120 point cloud of the terrain and develop a 3D model. The methodology is based on  
121 identifying matching features in multiple images, and thus imagery overlap of at least  
122 70% is required. Compared to classic photogrammetry methodologies, where the  
123 location of the observing point is well established, SfM tracks specific discernible  
124 features in multiple images, and through non-linear least-squares minimisation  
125 (Westoby et al., 2012), iteratively estimates both camera positions, as well as object  
126 coordinates in an arbitrary 3D coordinate system. In this process, sparse bundle  
127 adjustment (Snavely et al., 2008) is implemented to transform measured image  
128 coordinates to three dimensional points of the area of interest. The outcome of this  
129 process is a sparse 3D point cloud in the same local 3D coordinate system  
130 (Micheletti et al., 2015). Subsequently, through an incremental 3D scene  
131 reconstruction, the 3D point cloud is densified. Paired with GPS measurements of a  
132 number of control points (for this site, 10 fast-static GPS points were collected) at the  
133 top, middle and bottom of the surveyed area, the 3D point cloud is georeferenced to  
134 a specific coordinate system and through post-processing a digital surface model  
135 (DSM), a digital terrain model (DTM) and orthophotos are created. The SfM  
136 methodology was implemented in this study using the Agisoft Photoscan software.

137 Precalibrated camera parameters by the SfM software (Photoscan) were introduced  
138 and then optimized during the matching process and the initialization of Ground  
139 Control Points.

140 In addition, the accuracy of the model has been examined by using portions of the  
141 ground control points and developing DTM of differencing between different models,  
142 an investigation that is described by Manousakis et al. (2016). Finally, a comparison  
143 was made of the DTM developed by the UAV against the satellite-based DTM used  
144 for the Greek cadastre. The two surfaces were found to be very similar, as discussed  
145 subsequently.

### 146 **3.2. High-resolution Orthophoto**

147 A 5cm pixel size orthophoto was generated based on the methodology outlined  
148 earlier. As shown in Figure 5, the rolling section and the bouncing locations of the  
149 rock block throughout its course were identified. The rolling section was easily  
150 discerned as a continuous and largely linear mark left in the vegetated terrain. Impact  
151 points that are part of the bouncing section of the rock, were identified as circular to  
152 ellipsoidal bare earth craters with no disturbance in between. The last bouncing point  
153 before impacting the house is clearly identified on the paved road. The plan view  
154 ortho-imagery, along with the original footage of the video collected was crucial to the  
155 qualitative identification of these features. The alternative, i.e., land-based,  
156 conventional field reconnaissance was physically impossible to perform throughout  
157 the vegetated and steep terrain.

### 158 **3.3. Digital Surface Model and Digital Terrain Model**

159 A profile section and a 10 cm Digital Surface Model (DSM) were then developed  
160 (Manousakis et al., 2016) allowing the identification of features such as structures,  
161 slope benches or high trees, which could affect the rock's path downhill.  
162 Subsequently, this resolution of the DSM proved to be not only unnecessarily high

163 and thus difficult to manipulate in subsequent rockfall analyses, but also caused  
164 numerical instabilities in the rockfall analyses. Therefore, a downscaled 2 m DTM  
165 was produced for the rockfall analysis as described next. First, an aggregate  
166 generalization scheme where each output cell is assigned the minimum elevation of  
167 the input cells that are encompassed by that cell. In addition, noise filtering and  
168 smoothing processing were implemented to reduce the effect of vegetation in the  
169 final rasterized model. Note that this resolution is still higher than the resolution of  
170 DTM that are often used in rockfall analyses.

171 To create the DTM, algorithms for vegetation removal were executed using  
172 Whitebox GAT Geospatial Analysis Tools platform (Lindsay, 2016) .. The process  
173 involves Point Cloud neighborhood examination and DEM smoothing algorithms.  
174 Firstly, a bare-Earth digital elevation model (DEM) was interpolated from the input  
175 point cloud LAS file, by specifying the grid resolution (2m) and the inter-point slope  
176 threshold. The algorithm distinguished ground points from non-ground points based  
177 on the inter-point slope threshold. Thus, the interpolation area was divided into lattice  
178 cells, corresponding to the grid of the output DEM. All of the point cloud points within  
179 the circle containing each grid cell were then examined as a neighborhood. Those  
180 points within a neighborhood that have an inter-point slope with any other point and  
181 are also situated above the corresponding point, are attributed as non-ground points.  
182 An appropriate value for the inter-point slope threshold parameter depends on the  
183 steepness of the terrain, but generally values of 15-35 degrees produce satisfactory  
184 results. The elevation assigned to the grid cell was then the nearest ground point  
185 elevation (Lindsay, 2016.).

186 Further processing of the interpolated bare-earth DEM was executed to improve  
187 vegetation and structures removal results by applying a second algorithm to point  
188 cloud DEMs, which frequently contain numerous off-terrain objects such as buildings,  
189 trees and other vegetation, cars, fences and other anthropogenic objects. The

190 algorithm works by locating and removing steep-sided peaks within the DEM. All  
191 peaks within a sub-grid, with a dimension of the user-specified Maximum Off-Terrain  
192 Object (OTO) Size, in pixels, were identified and removed. Each of the edge cells of  
193 the peaks were then queried to check if they had a slope that is less than the user-  
194 specified Minimum OTO Edge Slope and a back-filling procedure was used. This  
195 ensured that natural topographic features such as hills are not recognized and  
196 confused as Off-Terrain features (Whitebox GAT help topics).

197 The final DTM model had a total RMS error after filtering for 6 GCPs was 0.07m,  
198 while total RMS error for 4 Check Points was 0.20m. When compared to a 5m DEM  
199 from Greek National Cadastre with a geometric accuracy of  $RMSE_z \leq 2,00m$  and  
200 absolute accuracy  $\leq 3,92m$  for a confidence level of 95%, a mean difference of 0.77  
201 m and a standard deviation of 1.25 m is observed, which is well into the range of  
202 uncertainty of the cadastre model itself.

203

## 204 **4. Earthquake characteristics – Initial conditions**

### 205 **4.1. Seismic acceleration**

206 The epicenter of the earthquake according to the National Observatory of Athens,  
207 Institute of Geodynamics (NOA) is located onshore near the west coast of Lefkada.  
208 The causative fault is estimated to be a near-vertical strike-slip fault with dextral  
209 sense of motion (Ganas et al., 2015, 2016). Based on the focal mechanism study of  
210 the earthquake, it was determined that the earthquake was related to the right lateral  
211 Kefalonia-Lefkada Transform Fault (KLTF), which runs nearly parallel to the west  
212 coasts of both Lefkada and Kefalonia island, in two segments (Papazachos et al.  
213 1998, Rondoyanni et al. 2012).

214 A strong motion station recorded the ground motions in the village of Vasiliki located  
215 at a distance of 2.5 km from the Ponti rockfall site. The ground motion characteristics



216 of the recording are summarized in Table 1 and are presented in Figure 6 (ITSAK,  
217 2016).

#### 218 **4.2. Topography effect**

219 Peak ground acceleration (PGA) along the rock slope is estimated from the PGA of  
220 the base ( $PGA_b$ ) modified by site and topographic effects (Mavrouli et al., 2009). In  
221 the present case, local shaking intensity in terms of horizontal PGA was considered.  
222 The E-W component of acceleration was considered for the determination of the  
223 initial velocity. The peak ground acceleration on the slope face ( $PGA_{sf}$ ) was  
224 considered equal to the acceleration at the slope crest ( $PGA_{cr}$ ). The acceleration at  
225 the base was equal to 0.32g and thus at the crest  $PGA_{cr} = 1.5 PGA_b$  was equal to  
226 0.48g.

#### 227 **4.3. Initial velocity of rock block**

228 The initial horizontal velocity of the block, at the time of detachment, was calculated  
229 considering equilibrium of the produced work and the kinetic energy according to  
230 equation 1.

$$231 \quad v_x = \sqrt{2 \times PGA_{sf} \times s} \quad (1),$$

232 where  $PGA_{sf}$  is the acceleration on the slope at the location of detachment and  $s$  the  
233 initial displacement of the block in order to initiate its downslope movement.

234 The initial horizontal velocity was calculated equal to 0.67 m/s, considering a  
235 displacement in the order of  $s = 0.05$  m. The vertical component of the initial velocity  
236 is assumed to be zero.

### 237 **5. Trajectory analysis**

238 In order to estimate the possible rock paths and design remedial measures,  
239 simulation programs based on lumped-mass analysis models are commonly used in  
240 engineering practice. The trajectory of a block is modelled as a combination of four

241 motion types; free falling, bouncing, rolling and sliding (Descoedres and  
242 Zimmermann, 1987). Usage of the lump-mass model has some key limitations; the  
243 block is described as rigid and dimensionless with an idealized shape (sphere);  
244 therefore the model neglects the block's actual shape and configuration at impact,  
245 even though both affect the resulting motion.

### 246 **5.1. Modelling the response to an impact**

247 The most critical input parameters are the coefficients of restitution (COR), which  
248 control the bouncing of the block. In general, the coefficient of restitution (COR) is  
249 defined as the decimal fractional value representing the ratio of velocities (or  
250 impulses or energies; depending on the definition used) before and after an impact of  
251 two colliding entities (or a body and a rigid surface). When in contact with the slope,  
252 the block's magnitude of velocity changes according to the COR value. Hence, COR  
253 is assumed to be an overall value that takes into account all the characteristics of the  
254 impact; including deformation, sliding upon contact point, transformation of rotational  
255 moments into translational and vice versa (Giani, 1992).

256 The most widely used definitions originate from the theory of inelastic collision as  
257 described by Newtonian mechanics. For an object impacting a rocky slope (Figure 7),  
258 which is considered as a steadfast object, the kinematic COR ( $v_{COR}$ ) is defined  
259 according to Eq. 2.

$$260 \quad v_{COR} = \frac{v_r}{v_i} \quad (2)$$

261 where  $v$  is the velocity magnitude and the subscripts  $i$  and  $r$  denote the trajectory  
262 stage; incident (before impact) and rebound (after impact) respectively.

263 Two different mechanisms participate in the energy dissipation process; energy loss  
264 normal to the slope is attributed to the deformation of the colliding entities, and in the  
265 tangential direction is due to friction between them. Therefore kinematic COR has  
266 been analyzed to the normal and tangential component with respect to the slope

267 surface, defining the normal ( $n_{COR}$ ) and the tangential ( $t_{COR}$ ) coefficient of restitution  
268 (Eq. 3 and 4 respectively).

$$269 \quad n_{COR} = \frac{v_{n,r}}{v_{n,i}} \quad (3)$$

270 and

$$271 \quad t_{COR} = \frac{v_{t,r}}{v_{t,i}} \quad (4)$$

272 where the first subscript, n or t denotes the normal or the tangential components of  
273 the velocity respectively.

274 Normal and tangential COR have prevailed in natural hazard mitigation design via  
275 computer simulation due to their simplicity. Values for the coefficients of restitution  
276 are acquired from values recommended in the literature (e.g., Azzoni et al. 1995;  
277 Heidenreich 2004; Richards et al. 2001, RocScience, 2004). These values are mainly  
278 related to the surface material type and originate from experience, experimental  
279 studies or back analysis of previous rockfall events. This erroneously implies that  
280 coefficients of restitution are material properties. However, COR values depend on  
281 several parameters that cannot be easily assessed. Moreover, values suggested in  
282 the literature vary considerably and are sometimes contradictory.

## 283 **5.2. Rockfall path characteristics**

284 23 impact points were identified on the slope surface (Figure 8). Their coordinates  
285 are presented in Table 2, along block's path starting from the detachment point  
286 (where  $x=0$ ). No trees were observed along the block's path.

287 The apparent dip of the slope at impact positions was measured from the DTM; on  
288 each impact point a line was set with a length twice the block's mean dimension,  
289 oriented according to preceding trajectory direction. Moreover, the impact point was  
290 expanded on the DTM to a rectangular plane with a side twice the mean dimension

291 of the block (Figure 9). This plane was then oriented so that one side coincides with  
292 the strike direction and its vertical side towards the dip direction. Thus, direction  
293 difference,  $\Delta\phi$ , was measured by strike direction and the preceding path and  
294 deviation,  $e$ , was measured as the angle between pre- and post- impact planes  
295 (Asteriou & Tsiambaos, 2016).

296 Having a detailed field survey of the trajectory path, a back analysis according to the  
297 fundamental kinematic principles was performed with the intent to back-calculate the  
298 actual COR values.

### 299 **5.3. Kinematic analysis and assumptions**

300 The 23 impact points identified on the slope comprise a rockfall path of 22 parabolic  
301 segments. The vertical and horizontal length of each segment is acquired by  
302 subtracting consecutive points. Since no external forces act while the block is mid-air,  
303 each segment lays on a vertical plane and is described by the general equation of  
304 motion as:

$$305 \quad y = x \tan \vartheta - \frac{gx^2}{2v_i^2 \cos^2 \vartheta} \quad (5)$$

306 where:  $\theta$  the launch angle from the horizon and  $v$  the launch (initial) velocity (Figure  
307 10).

308 Since no evidence can be collected regarding launch angle and velocity, innumerable  
309 parabolas satisfy Eq. 5. However,  $\theta$  is bound between  $-\beta$  and  $90^\circ$ , so in order to  
310 acquire realistic values for the initial velocity, its sensitivity for that given range was  
311 investigated.

312 For the case presented in Fig. 11 (the first parabolic segment) it is shown that for the  
313 majority of the release angles, initial velocity variation is low and ranges between 7.2  
314 and  $12 \text{ ms}^{-1}$ . Additionally, the relationship between release angle and initial velocity is

315 expressed by a curvilinear function, with a minimum initial velocity value along with  
316 an associated release angle (denoted hereafter as  $\theta_{cr}$ ).

317 Given the minimum initial velocity and the critical release angle for each parabolic  
318 segment, the impact velocity and impact angle can be calculated. Subsequently,  
319 normal and tangential velocity components according to the apparent dip of the  
320 impact area, are calculated in order to evaluate COR values. Results are  
321 summarized in Table 3.

#### 322 **5.4. Coefficients of restitution**

323 It is observed that  $v_{cor}$  (Table 3) is greater than one in 5 out of 22 impacts. According  
324 to Eq. 3, this can only be achieved when impact velocity is less than rebound  
325 velocity. However, this indicates that energy was added to the block upon impact,  
326 which is not possible according to the law of conservation of energy. Thus, impact  
327 velocity should be greater, which is possible if the launch velocity of the previous  
328 impact was higher than the assumed minimum.

329 For the cases where  $V_{cor} < 1$ , it is observed that kinematic COR ranges between 0.55  
330 and 1.0 and presents smaller variation compared to normal or tangential coefficient  
331 of restitution, similar to what was previously reported in relevant literature (i.e.  
332 Asteriou et al, 2012; Asteriou & Tsiambaos, 2016).

333 The wide scatter of normal COR implies that the restitution coefficient cannot be a  
334 material constant. Yet, in most relevant software, normal COR is defined solely by  
335 the slope material. Moreover, normal COR values higher than one were calculated in  
336 11 out of the 15 remaining impacts. Normal COR higher than one have been  
337 observed in both experimental (e.g. Spadari et al., 2011; Buzzi et al., 2012; Asteriou  
338 et al., 2012) and back-analysis studies (e.g. Paronuzzi, 2009) and are related to  
339 irregular block shape and slope roughness, as well as to shallow impact angle and  
340 angular motion. A more detailed presentation of the reasons why normal COR

341 exceeds unity can be found in Ferrari et al. (2013). However, in rockfall software  
342 used in engineering practice, normal COR values are bounded between 0 and 1.

343 As shown in Figure 12, normal COR increases as the impact angle reduces, similarly  
344 to previous observations by Giacomini et al. (2012), Asteriou et al. (2012) and Wyllie  
345 (2014). The correlation proposed by Wyllie (2014) is also plotted in Figure 13 and  
346 seems to describe consistently, but on the unconservative side, the trend and the  
347 values acquired by the aforementioned analysis and assumptions.

## 348 **6. Rockfall modelling**

### 349 **6.1. 2-D analyses**

350 A deterministic 2D rockfall analysis was first performed using Rocfall software  
351 (RocScience, 2004). According to Asteriou & Tsiambaos (2016) the most important  
352 influence is posed by the impact configuration, which is influenced by slope  
353 roughness and block shape. In this study, roughness has been fully taken into  
354 account (considering the block's dimension scale) by the high resolution of the  
355 cross-section used in the analyses (more than 1500 x-y points were used –  
356 approximately 2 points per meter). Based on our experience, this resolution is  
357 significantly higher compared to other rockfall studies. Moreover, it was not possible  
358 to simulate block shape effect, nor the configuration of the block at impact, using  
359 lumped-mass model analysis.

360 Considering an initial velocity of 0.67 m/sec, according to the numerical analyses, the  
361 falling rock primarily rolls on the slope and stops much earlier than its actual (field-  
362 verified) run out distance, approximately 400 m downslope from its initiation point  
363 (Fig. 8; case 1). The restitution coefficients were  $n_{COR}=0.35$ ,  $t_{COR}=0.85$ , and were  
364 selected based on the suggested values for bedrock outcrops provided in the  
365 software documentation.

366 Note that for this analysis, the friction angle was set to zero. A standard deviation for  
367 the coefficients of restitution, the friction angle and roughness of the material on the

368 slope was not used for this deterministic analysis. For friction equal to  $32^{\circ}$  (as  
369 suggested by the software documentation), the rock travels downslope only 50 m.

370 Additional analysis was also performed, with lower coefficients of restitution that are  
371 representative of the talus material on the slope ( $n_{COR}=0.32$ ,  $t_{COR}=0.82$ ,  $\phi=30^{\circ}$ ) per  
372 the software documentation. In this case, the rock block rolled only a few meters  
373 downslope. Therefore, it is evident that the actual rock trajectory cannot be  
374 simulated.

375 In order to more closely simulate the actual trajectory, various combinations of  
376 restitution coefficients and friction angle were considered. The closest match  
377 occurred for  $n_{COR}=0.60$  and  $t_{COR}=0.85$ , while the friction angle was set to zero and no  
378 velocity scaling was applied. For these input parameters, the rock block reaches the  
379 house with a velocity of 18 m/s approximately (Fig. 8; case 2). These values for the  
380 restitution coefficients correspond to a bedrock material (limestone).

381 In this case, the modelled trajectory is significantly different from the actual one. The  
382 main difference is that the block rolls up to 200 m downslope while the actual rolling  
383 section is 400 m (as shown in Figure 8). Furthermore the impacts on the ground in  
384 the bouncing section of the trajectory are considerably fewer in number (14 versus  
385 23) and in different locations compared to the actual ones. Finally, the bounce height  
386 of some impacts seems unrealistically high. For example, the 2<sup>nd</sup> bounce has a jump  
387 height (f) of ~17.5m over a length (s) of ~50m, resulting to a f/s ratio of ~1/3, when  
388 the characteristic f/s ratios for high, normal and shallow jumps is 1/6, 1/8 and 1/12  
389 respectively, as suggested by Volkwein et al. (2011).

## 390 **6.2. 3-D rockfall analysis**

391 The rockfall trajectory model Rockyfor3D (Dorren, 2012) has also been used in order  
392 to validate the encountered trajectory and assess the probability that the falling rock  
393 (from the specific source area) reaches the impacted house.

394 The 3D analysis was based on the down-scaled 2 m resolution Digital Terrain Model  
395 (DTM) that was generated from the 10 cm DSM. The following raster maps were  
396 developed for the 3D analysis: a) rock density of rockfall source, b) height, width,  
397 length and shape of block, c) slope surface roughness and d) soil type on the slope,  
398 which is directly linked with the normal coefficient of restitution,  $n_{COR}$ .

399 The slope roughness was modeled using the mean obstacle height (MOH), which is  
400 the typical height of an obstacle that the falling block encounters on the slope at a  
401 probability of 70%, 20% and 10% of the trajectories (according to the suggested  
402 procedure in Rockyfor3D). No vegetation was considered in the analysis, which  
403 favours a longer trajectory. The parameters considered in the 3D analysis for the  
404 different formations are summarised in Table 4. The spatial occurrence of each soil  
405 type is shown in Figure 13 and the assigned values of  $n_{COR}$  are according to the  
406 Rockyfor3D manual. The values for soil type 4.1 in Figure 13 are slightly different  
407 from those of soil type 4 (proposed in the manual), denoting talus with a larger  
408 percentage of fallen boulders. The block dimensions were considered equal to 2 m<sup>3</sup>  
409 and the shape of the boulder was rectangle. In order to simulate the initial velocity of  
410 the falling rock due to the earthquake, an additional initial fall height is considered in  
411 the analysis, which for this case was set equal to 0.5 m.

412 The energy line angles were recalculated from the simulated trajectories and it was  
413 determined that the energy line angle with highest frequency (39%) was 30-31°.  
414 Based on the 3D analysis no rock blocks would impact the house, although the rock  
415 paths are closer to the actual trajectories compared to RocFall software. The reach  
416 probability of the falling rocks, initiating from the source point, is shown in Figure 14.  
417 Reach probability is the percentage of the falling rocks in relation to the total number  
418 of falling rocks that reach a specific point along the line of the trajectory.

### 419 **6.3. Lateral dispersion & Deviation**



420 Lateral dispersion is defined as the ratio between the distance separating the two  
421 extreme fall paths (as seen looking at the face of the slope) and the length of the  
422 slope (Azzoni and de Freitas 1995). According to Crosta and Agliardi (2004) the  
423 factors that control lateral dispersion are (a) macro-topography factors, factors  
424 related to the overall slope geometry; (b) micro-topography factors controlled by the  
425 slope local roughness; and (c) dynamic factors, associated with the interaction  
426 between slope features and block dynamics during bouncing and rolling. Based on  
427 an experimental investigation, Azzoni and de Freitas (1995) noted that the dispersion  
428 is generally in the range of 10% to 20%, regardless of the length of the slope and that  
429 steeper slopes exhibit smaller dispersion. Agliardi and Crosta (2003) calculated  
430 lateral dispersion to be up to 34%, using high-resolution numerical models on natural  
431 rough and geometrically complex slopes.

432 Lateral dispersion cannot be defined from the actual rockfall event in Ponti since only  
433 one path is available. Using the simulated trajectories from RockyFor3D, which are in  
434 the 3d space (Figure 15), a lateral dispersion of approximately 60% is shown in the  
435 middle of the distance between detachment point and the house. This is significantly  
436 higher dispersion than the findings of Azzoni and de Freitas (1995) and Agliardi and  
437 Crosta (2003). The lateral dispersion computed by RockyFor3D is extremely  
438 pronounced and most likely due to the topography effect of the area of detachment.  
439 Specifically, the origin of the rock block is located practically on the ridgeline,  
440 facilitating the deviation of the rock fall trajectory from the slope line.

441 Asteriou & Tsiambaos (2016) defined deviation ( $e$ ) as the dihedral angle between the  
442 pre- and post-impact planes that contain the trajectory. They found that deviation is  
443 controlled by the direction difference  $\Delta\phi$ , the slope inclination and the shape of the  
444 block. For a parallel impact (i.e.  $\Delta\phi=0^\circ$ ) a spherical block presents significantly less  
445 deviation compared to a cubical. Additionally, deviation is equally distributed along  
446 the post-impact direction and reduces as the slope's inclination increases. On oblique

447 impacts, the block's direction after impact changes towards the slope aspect and as  
448  $\Delta\phi$  increases, this trend becomes more pronounced.

449 Figure 16 illustrates the relationship of deviation with direction difference. It is noted  
450 that for parallel impacts ( $\Delta\phi=0^0$ ), deviation is uniformly distributed along the post-  
451 impact direction. As direction difference increases, deviation becomes positive, which  
452 means that the change of direction is following the direction of slope's aspect. These  
453 findings are consistent with trends described by Asteriou & Tsiambaos (2016), but  
454 the deviation of the actual trajectory is significantly lower. This can be attributed to  
455 the different conditions (i.e. block shape, slope material, slope roughness, incident  
456 velocity and angle, and scale) between the experimental program conducted by  
457 Asteriou & Tsiambaos (2016) and the Ponti rockfall event.

## 458 **7. Conclusions**

459 UAV-enabled reconnaissance was successfully used for the identification of the  
460 origin of the detached rock, the rockfall trajectory and the impact points on the slope,  
461 and especially discerning the rolling and bouncing sections of the trajectory. A UAV  
462 with an ultra-high definition (UHD) camera was deployed to reach the inaccessible,  
463 steep and partly vegetated uphill terrain. A high-resolution orthophoto of the rockfall  
464 trajectory, a 10 cm DSM and a 2 m DTM were generated and formed the basis for an  
465 analytical 2D kinematic analysis and a comparison with the outcomes of 2D and 3D  
466 rockfall analysis software.

467 The initial velocity of the detached rock was estimated based on site conditions and  
468 amplification of the ground acceleration due to topography. It was found that the  
469 initial velocity of the blocks plays a significant role in the accurate re-production of the  
470 rockfall trajectory.

471 Based on the computational analysis performed, it was found that the coefficients of  
472 restitution cannot be directly connected to the material type, nor can be considered

473 material constants. The impact angle seems to influence the normal COR, which has  
474 been also observed in other recent studies, but has not been incorporated yet on  
475 analysis models.

476 It was proven impossible to replicate the actual trajectory of the rock fall by  
477 performing a 2D rockfall analysis with the recommended set of parameters indicating  
478 limitations in the present formulations. In an attempt to match the actual rock path to  
479 the analysis output, the friction angle of the limestone slope was considered equal to  
480 zero. However, the falling rock still rolled on the slope and stopped much earlier than  
481 its actual runout distance while the impacts on the ground in the bouncing section of  
482 the trajectory were considerably different in number and in location compared to the  
483 actual ones.

484 Using the 3D analysis software and recommended input parameters, rock trajectories  
485 better approximated the actual trajectory indicating that the 3D analysis can be more  
486 accurate than the 2D analysis.

487 Based on the aforementioned analyses it becomes evident that engineering  
488 judgement and experience must accompany the usage of commercial rockfall  
489 software in order to acquire realistic paths. One should never blindly use the  
490 recommended set of parameters since field performance can differ significantly, as  
491 demonstrated by this case study.

492

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601 September 2017.
- 602

602

**TABLES**

603

Table 1. Accelerometer recordings

Component	Acceleration (cm/sec <sup>2</sup> )	Velocity (cm/sec)	Displacement (cm)
NS-comp	363	59.3	21.27
EW-comp	327	34.1	14.01
Z-comp	256	17.7	6.56

604

605 Table 2. Impact points characteristics

Impact point	X (m)	Y (m)	app_dip (°)	$\Delta\phi$ (°)	e (°)
1	287.63	338	39.0	0	0
2	298.38	329.68	16.3	33	0
3	305.48	324.5	27.9	27	-1
4	321.54	314.83	41.0	11.6	0.5
5	365.34	287.6	30.4	11.9	0.3
6	373.32	284.85	39.7	10.6	1.8
7	425.1	261.64	14.7	6.6	-1.3
8	464.43	251.13	18.4	33.3	0.8
9	472.06	248.81	14.0	19.1	2.3
10	495.29	243.81	7.5	52.3	0.9
11	515.31	240.8	7.9	51	0.6
12	535.56	238.31	9.1	46.7	3
13	562.11	232.22	8.7	47.3	2.1
14	605.51	211.12	16.9	25.6	-1.7
15	619.1	204.48	27.1	4.6	-3
16	639.13	196.96	21.2	8	4.7
17	662.41	184	23.3	28.5	5.2
18	688.4	169.3	27.4	0.3	-2.5
19	712.23	157.67	25.4	0.5	0.1
20	745.28	143.16	21.9	0.5	-0.1
21	762.9	137.01	22.0	0.7	2
22	789.23	125.98	21.6	1.4	-0.8
23	801.53	132.75	8.4	0.2	0.1



606 Table 3. Parabolic paths characteristics for the minimum release velocity

Segment	$\Delta x(m)$	$\Delta y(m)$	$\theta_{cr} (^{\circ})$	$v_{r,min}$	$v_{impact}$	$a_i$	$v_{COR}$	$n_{COR}$	$t_{COR}$
1-2	10.75	-8.33	26.8	7.19	13.19	44.5	0.55	0.71	0.31
2-3	7.1	-5.18	25.7	5.95	9.51	27.8	0.63	0.90	0.53
3-4	16.07	-9.66	31.5	9.45	12.68	9.6	0.75	3.86	0.38
4-5	43.79	-27.23	27.7	15.46	23.13	23.3	0.67	1.57	0.26
5-6	7.98	-2.75	35.7	7.47	10.49	14.9	0.71	2.52	0.30
6-7	51.78	-23.21	34.8	18.15	21.61	31.7	0.84	1.54	0.26
7-8	39.33	-10.5	35.9	17.23	24.01	36.1	0.72	0.94	0.56
8-9	7.63	-2.32	35.9	7.45	10.54	41.1	0.71	0.87	0.55
9-10	23.23	-5	40.5	13.58	13.12	30.7	1.03	1.65	0.70
10-11	20.02	-3.01	41.1	13.00	11.57	24.2	1.12	2.06	0.82
11-12	20.25	-2.49	40.9	13.26	11.22	17.6	1.18	2.94	0.82
12-13	26.55	-6.1	38.0	14.40	14.25	28.5	1.01	1.55	0.78
13-14	43.41	-21.1	32.9	16.33	25.70	40.9	0.64	0.64	0.63
14-15	13.59	-6.64	30.7	9.13	12.81	25.1	0.71	1.24	0.53
15-16	20.03	-7.52	33.8	11.67	15.42	29.8	0.76	1.33	0.42
16-17	23.27	-12.96	31.9	11.59	15.89	28.5	0.73	1.22	0.50
17-18	25.99	-14.7	29.9	12.20	20.11	30.9	0.61	0.95	0.42
18-19	23.83	-11.63	32.2	12.08	17.10	27.9	0.71	1.30	0.40
19-20	33.05	-14.51	33.6	14.55	20.62	32.1	0.71	1.14	0.43
20-21	17.62	-6.15	34.5	11.08	11.99	18.4	0.92	2.44	0.54
21-22	26.33	-11.03	35.1	13.11	16.33	27.3	0.80	1.47	0.49
22-23	12.3	6.77	58.1	14.30	13.97	48.9	1.02	1.34	0.28

607

608

608 Table 4. Restitution parameters for Rockyfor3D

Geological formation/ other	Mean $n_{COR}$	MOH			Soil type (Rockyfor3D)
		rg70	rg20	rg10	
Scree ( $\emptyset < \sim 10$ cm), or medium compact soil with small rock fragments	0.33	0.03	0.05	0.05	3
Talus slope ( $\emptyset > \sim 10$ cm), or compact soil with large rock fragments	0.38	0.05	0.1	0.2	4
Talus with fallen boulders	0.42	0.15	0.15	0.2	4.1
Bedrock with thin weathered material	0.43	0	0.05	0.1	5
Asphalt road	0.35	0	0	0	7

609

## FIGURES

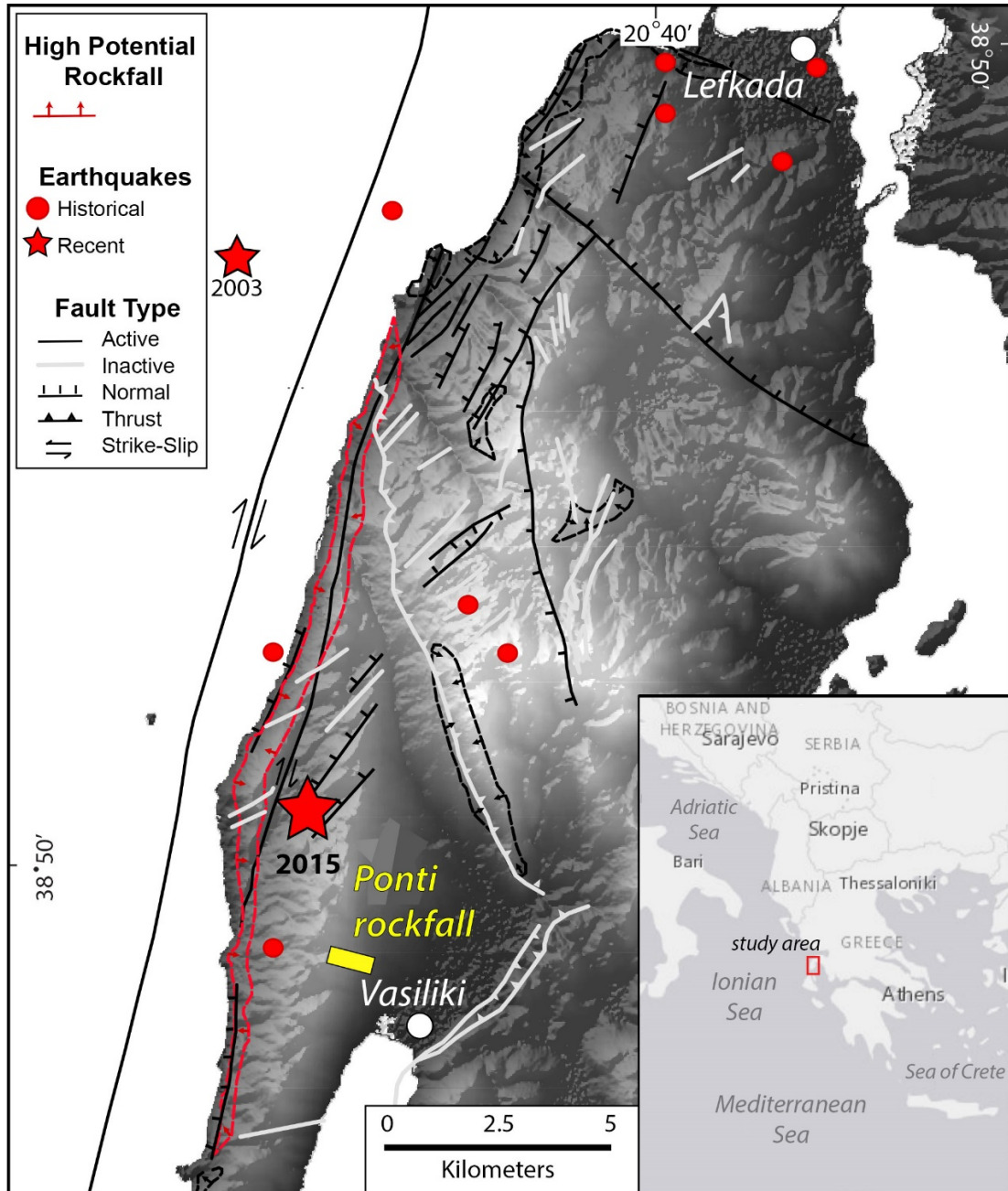


Figure 1. Map of Lefkada Island, Greece with location of study site (Ponti) and epicenters of recent earthquakes (stars) in 2003 ( $M_w$ 6.2) and 2015 ( $M_w$ 6.5), as well as historical ones (circles) Map also shows faults and high potential rockfall areas as identified by Rondoyanni et al. (2007).

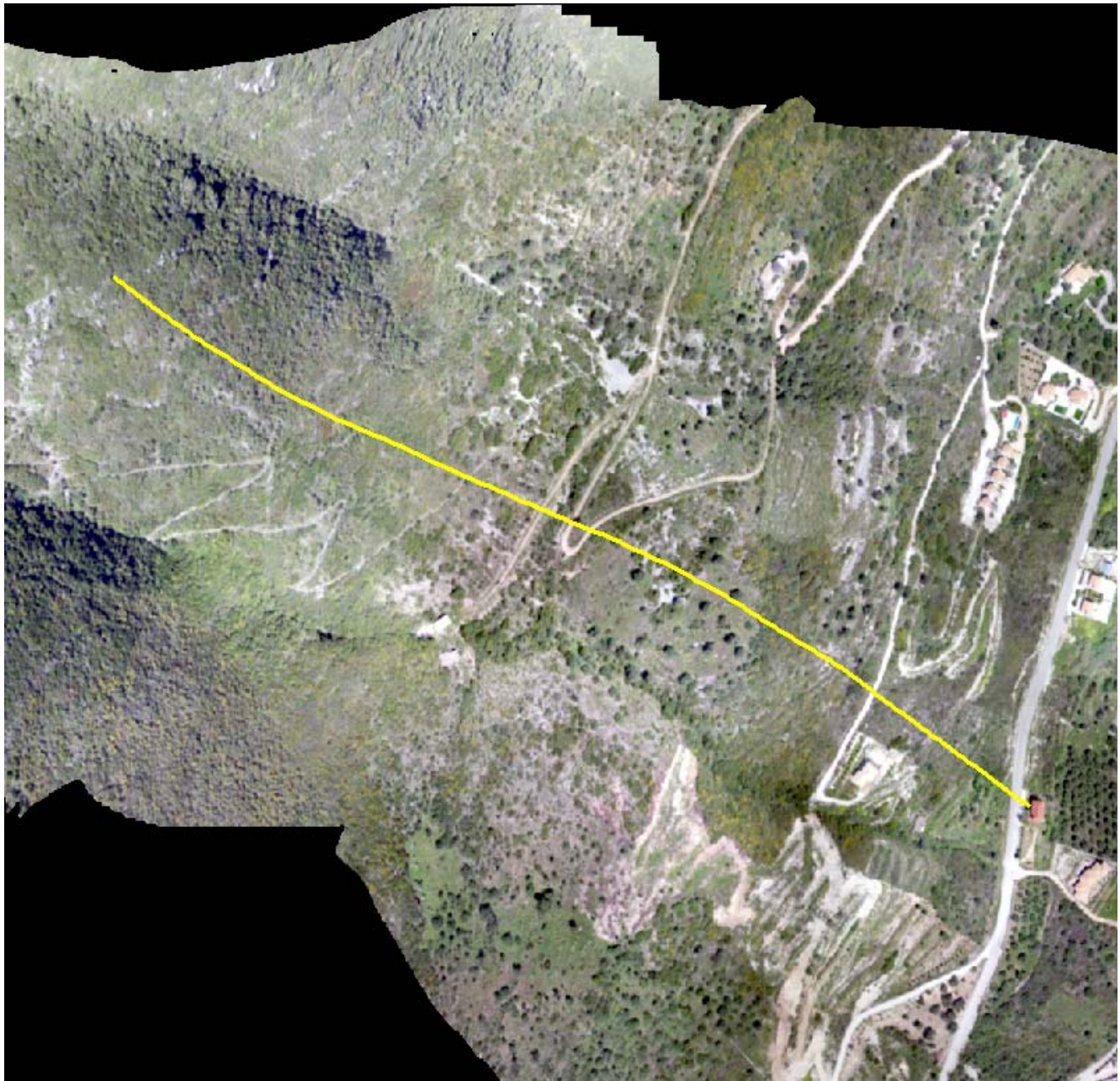


Figure 2. Orthophoto of case study. The total length of the trajectory shown with a yellow line, is 800 m.



Figure 3. Impact of rock on house in Ponti, Lefkada, Greece.

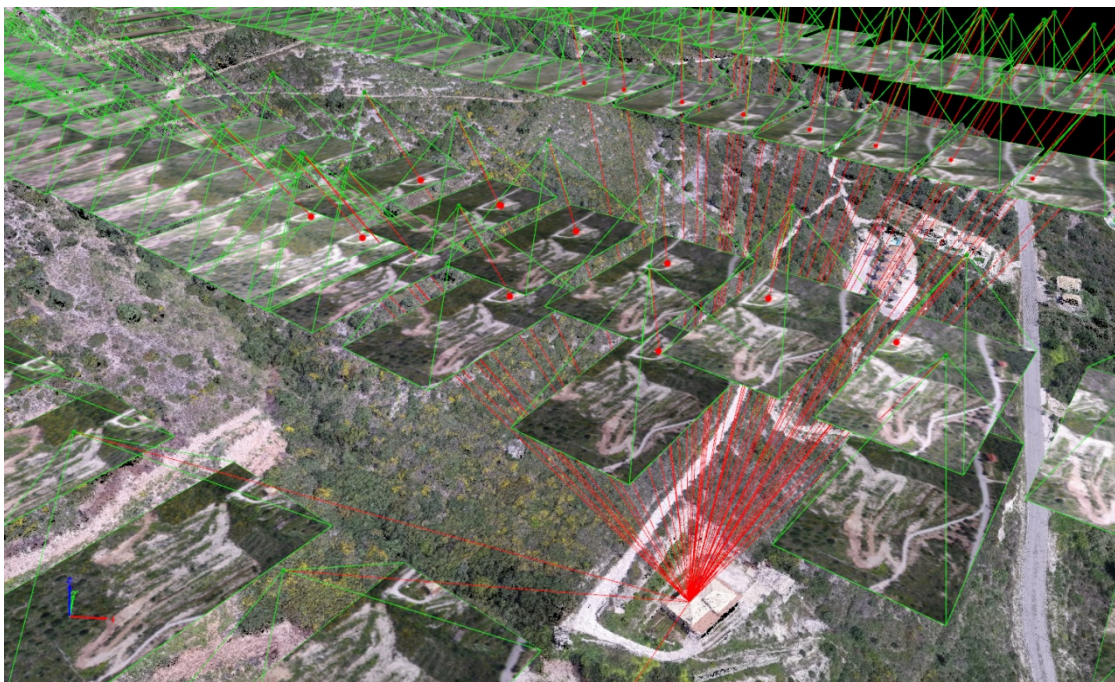


Figure 4. Schematic illustrating the overlap between pictures in the study site using SfM methodology.

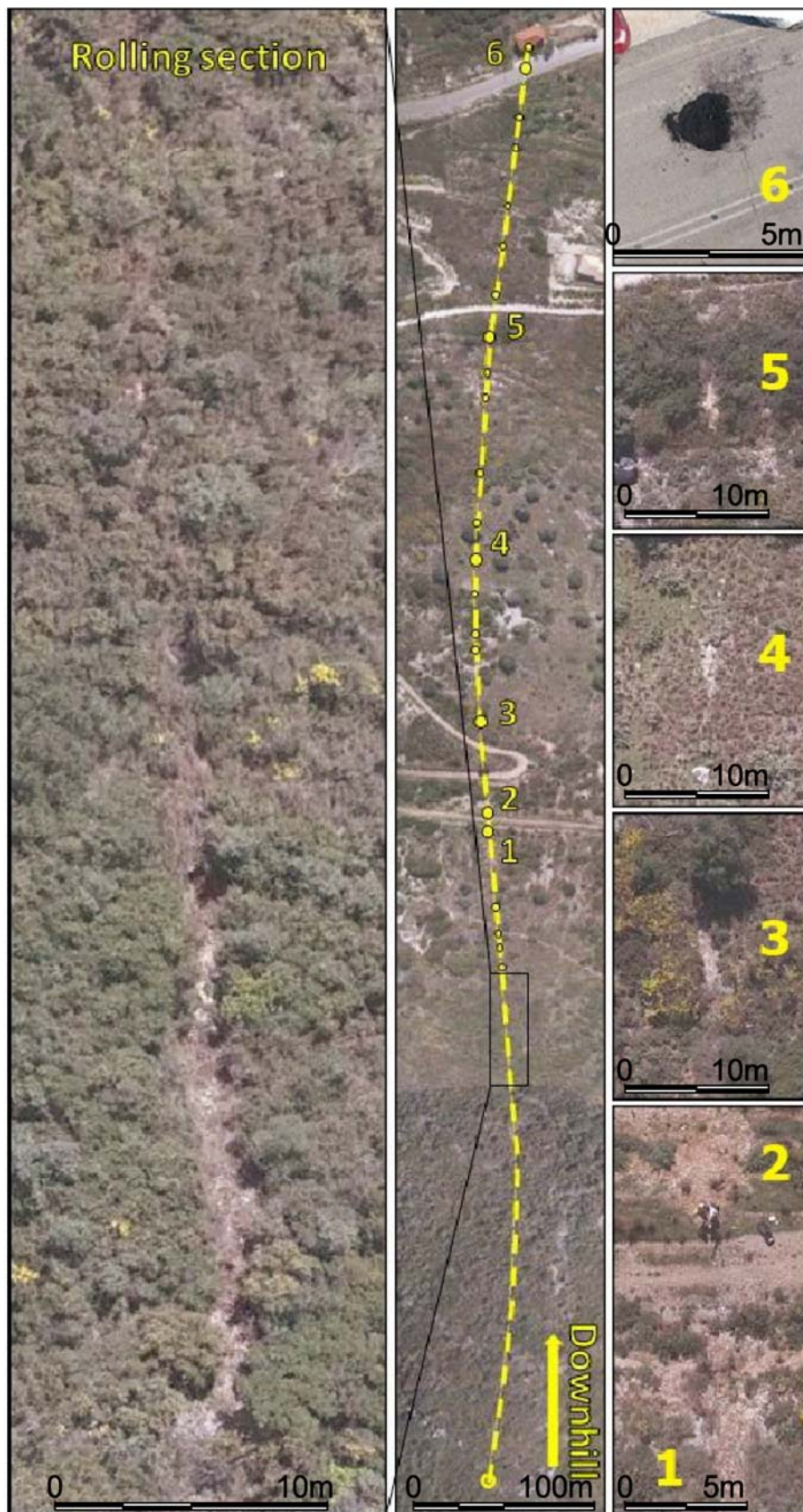


Figure 5. Top view orthophoto denoting rolling section, bouncing positions and indicative close-ups of impact points.

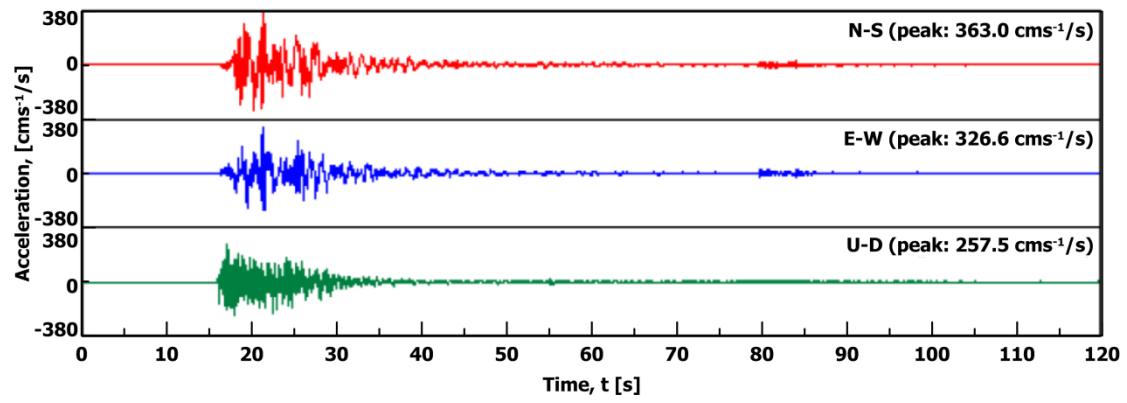


Figure 6. Acceleration time history recording at Vassiliki site (ITSAK, 2016)

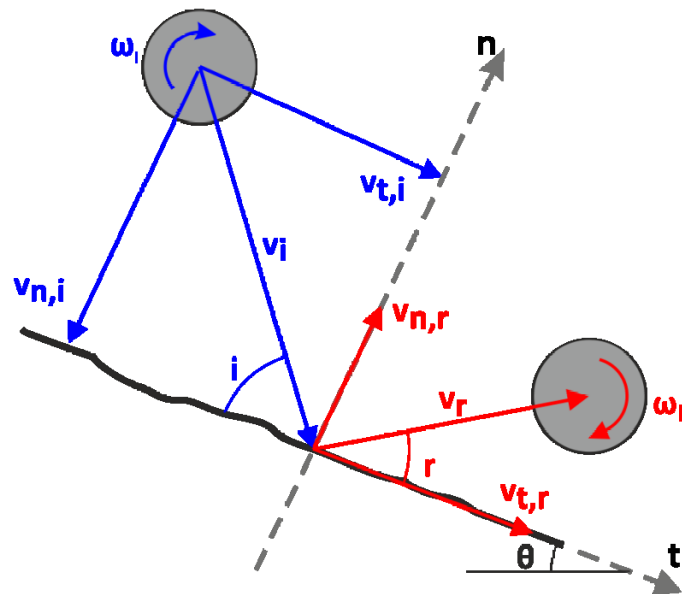


Figure 7. Coefficients of restitution

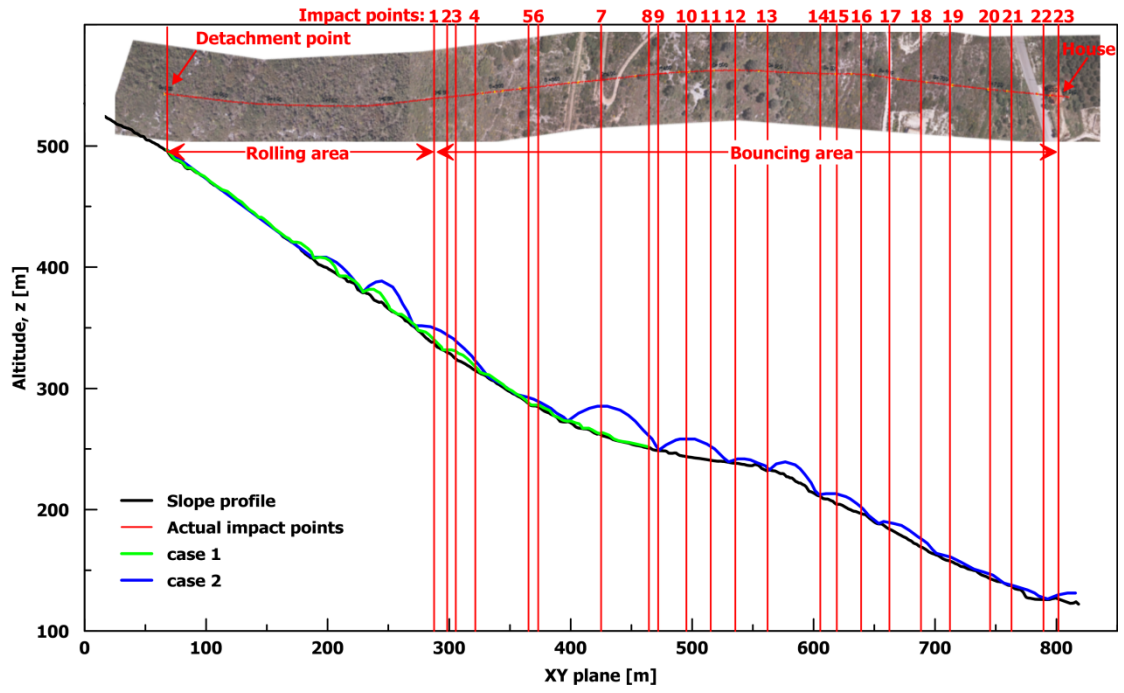


Figure 8. Plan view and cross section along block's path (units in m); 2D rockfall trajectory analysis results are plotted with green and blue line

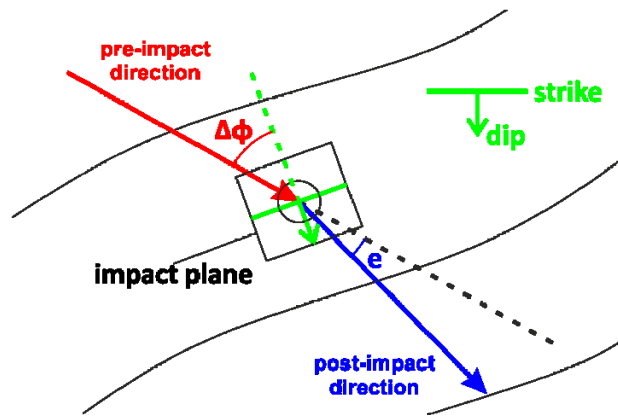


Figure 9 : Out of plane geometry

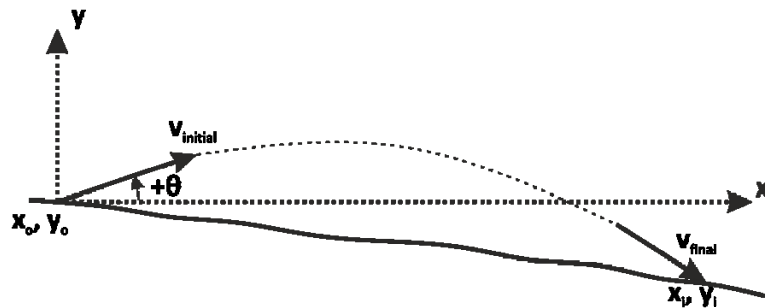


Figure 10. Parabolic segment



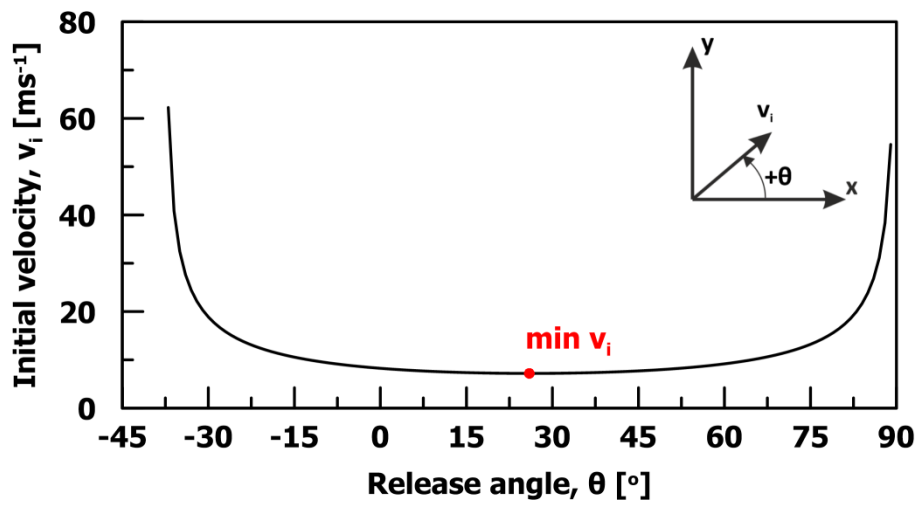


Figure 11. Release angle versus initial velocity for the first parabolic section ( $\delta x=10.75\text{m}$ ,  $\delta y=8.33\text{m}$ )

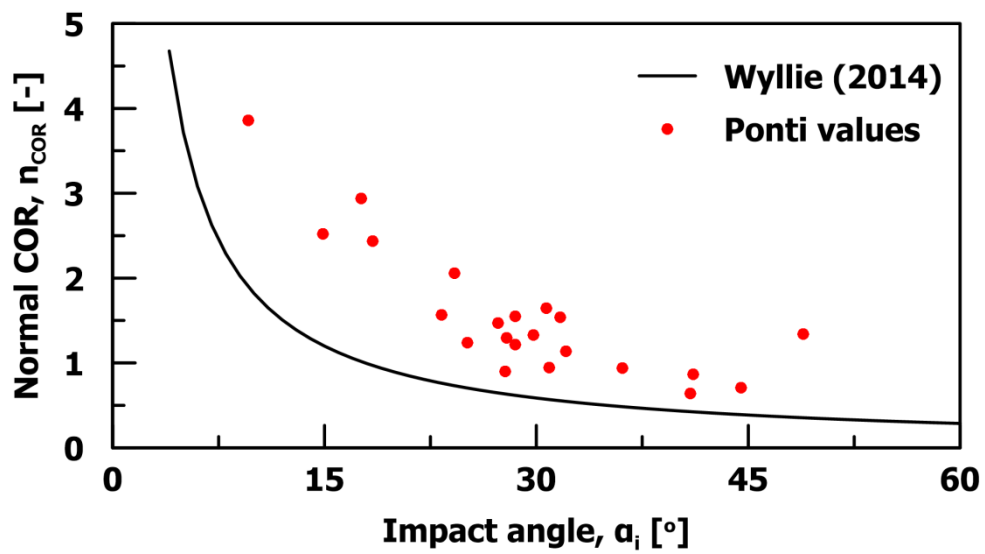


Figure 12. Normal COR versus impact angle

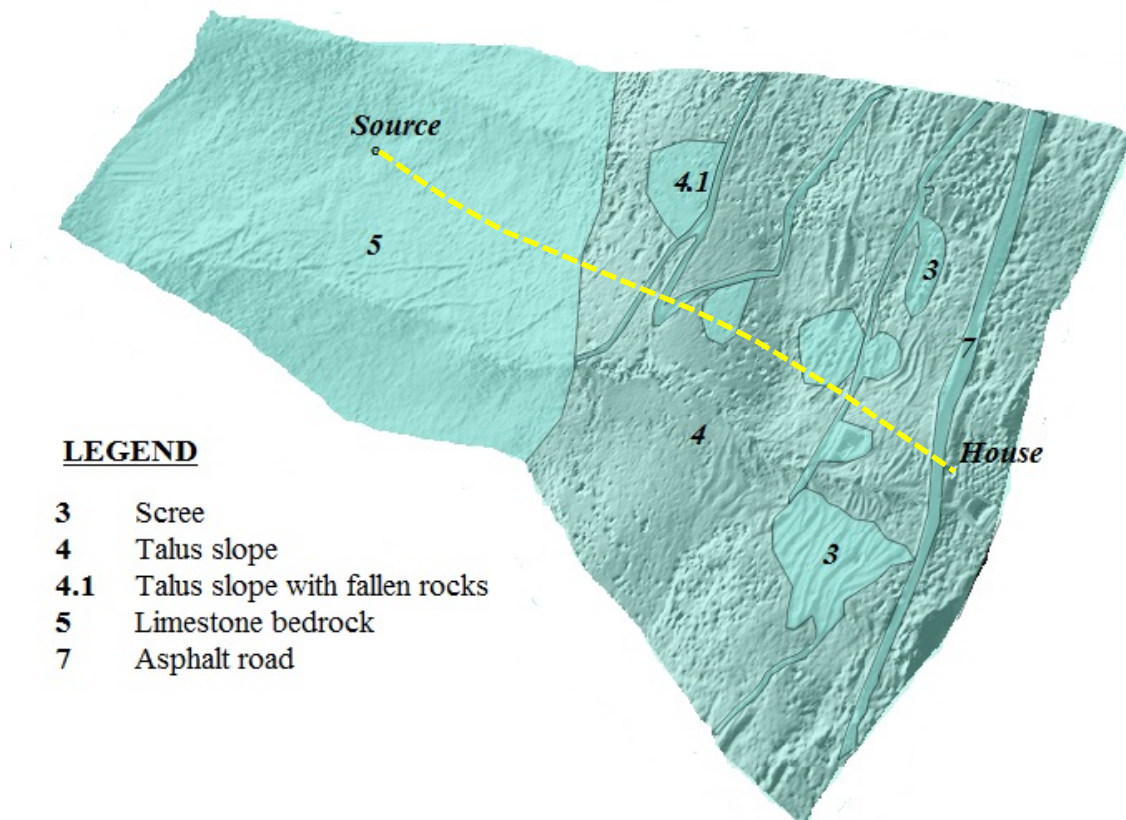


Figure 13. Soil types for 3D rockfall analysis (according to Rockyfor3D). Yellow path of trajectory is 800 m.

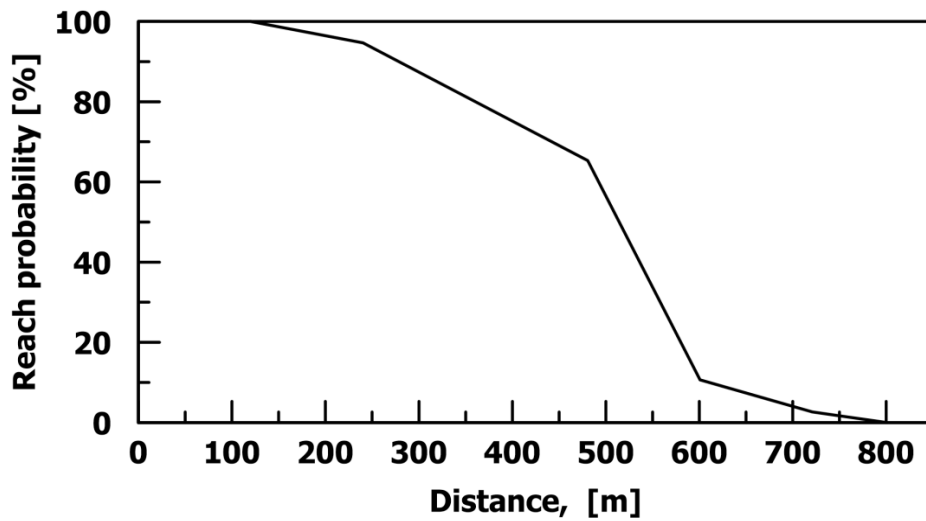


Figure 14. Reach probability graph calculated from 3D rockfall analysis

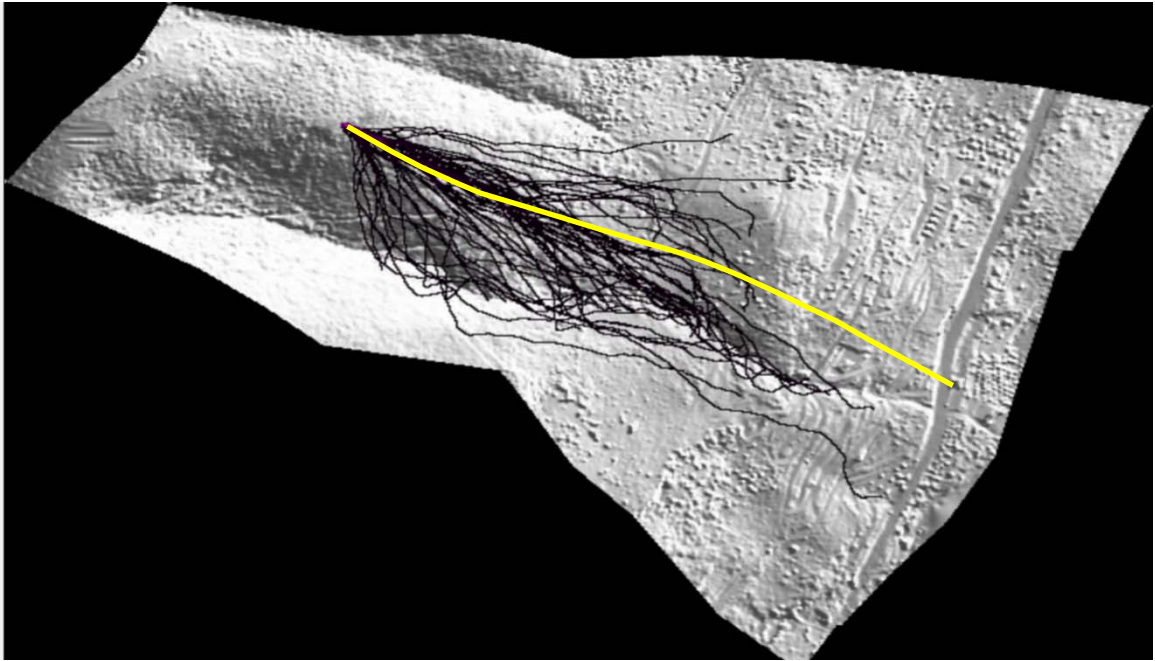


Figure 15. 3D trajectory analysis (from RockyFor3D analysis). Yellow line shows the actual trajectory. Black lines show the simulated trajectory.

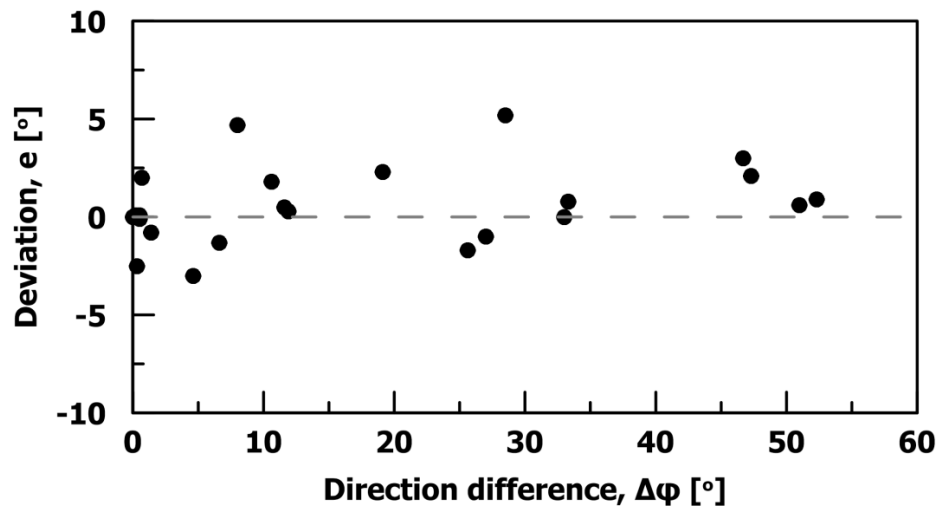


Figure 16. Deviation as a function of direction difference.