

1       **UAV-based mapping, back analysis and trajectory modelling of a**  
2       **co-seismic rockfall in Lefkada Island, Greece**

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19   **Abstract**

20   We present field evidence and kinematic study of rock block motion mobilised in the  
21   Ponti area by an  $M_w$  6.5 earthquake near the island of Lefkada on 17<sup>th</sup> November 2015.  
22   A detailed survey was conducted using an Unmanned Aerial Vehicle (UAV) with an  
23   ultra-high definition (UHD) camera, which produced a high-resolution orthophoto and  
24   a Digital Surface Model (DSM) of the terrain. The sequence of impact marks from the  
25   rock trajectory on the ground surface was identified from the orthophoto and field  
26   verified. Additionally, calculation of earthquake characteristics defined the acceleration  
27   of the rock slope and the initial condition of the detached block. Using the impact points  
28   from the measured rockfall trajectory, an analytical reconstruction of the trajectory was  
29   developed, which led to insights on the coefficients of restitution. The measured  
30   trajectory was compared with modeled rockfall trajectories using recommended

31 parameters. However, the actual trajectory could not be accurately predicted, revealing  
32 limitations of existing models.

### 33 **Keywords**

34 Rockfall, earthquake, DEM, modelling, restitution, UAV

## 35 **1. Introduction**

36 Active faulting, rock fracturing and high rates of seismicity contribute to common  
37 rockfall hazards in Greece. Rockfalls primarily damage roadways and houses  
38 (Saroglou, 2013) and are most often triggered by rainfall and secondly seismic loading.  
39 Additionally in recent years, some rockfalls have impacted archaeological sites  
40 (Marinos & Tsiambaos, 2002, Saroglou et al., 2012). The Ionian Islands, which include  
41 Lefkada Island, experience frequent  $M_w$  5-6.5 earthquakes, as well as less frequent  
42 larger (up to 7.5) earthquakes. The historical seismological record is particularly well  
43 constrained with reliable detailed information for at least 23 such earthquake events  
44 since 1612 that induced ground failures at the island of Lefkada. On average, Lefkada  
45 experiences a damaging earthquake every 18 years. In the recent past, a  $M_w$  6.2  
46 earthquake occurred on August 14 2003 offshore the NW coast of Lefkada, and  
47 caused landslides, rockslides and rockfalls along the western coast of the island  
48 (Karakostas et al. 2004, Papathanasiou et al., 2012). Significant damage was reported,  
49 particularly in the town of Lefkada, where a PGA of 0.42g was recorded.

50 On November 17<sup>th</sup> 2015, an  $M_w$  6.5 earthquake again struck the island of Lefkada and  
51 triggered a number of landslides, rockfalls and some structural damage. The most  
52 affected area by large rockslides was the western coast of the island, especially along  
53 its central and south portion, which are popular summer tourist destinations (Zekkos  
54 et al., 2017). The coseismic landslides completely covered the majority of the west  
55 coast beaches and damaged access roads.

56 On the southeast side of Lefkada near the Gulf of Vassiliki, a seismically-triggered  
57 rockfall in Ponti village was responsible for one of two deaths caused by the earthquake  
58 (Figure 1). Of particular interest, is the very long travel path of the rock block, which  
59 was about 800 m in plan view from the point of detachment to the end of its path. Near  
60 the end of the rock fall path, the block impacted a family residence, penetrated two  
61 brick walls and killed a person in the house. The block exited through the back of the  
62 house and came to rest in the property's backyard.

63 The Ponti village rockfall site is characteristic of earthquake induced rockfall and an  
64 example of how seismically-induced rockfall impacts human activities. It also provides  
65 an opportunity to evaluate 2D and 3D rockfall analysis to predict details of the rockfall  
66 trajectory, based on measured by field evidence. In order to create a highly accurate  
67 model of the rockfall propagation in 2D and 3D space, the rock path and the impact  
68 point on the slope was identified by a field survey. The study was performed using an  
69 Unmanned Aerial Vehicle (UAV) with an ultra-high definition (UHD) camera, which  
70 produced a high-resolution orthophoto and a Digital Surface Model (DSM) of the  
71 terrain. The orthophoto was used to identify the rolling section and the bouncing points  
72 of the rock along its trajectory, which were verified by field observation. The high-  
73 resolution DSM made it possible to conduct kinematical rebound analysis and a 3D  
74 rockfall analysis.

## 75 **2. Ponti rockfall - site conditions**

76 The locations of the epicenters of the 2003 and 2015 events, as well as the location of  
77 the rockfall study site are shown in Figure 1. The southwest coast of Lefkada is part of  
78 the Triassic to Eocene age Paxos zone and consists of limestones and dolomites that  
79 are covered by Neogene clastic sedimentary rocks, mostly sandstones and marls.  
80 Figure 1 also shows faults and high rockfall hazard areas as identified by Rondoyanni  
81 et al. (2007). The rockfall at Ponti is not located in a high rockfall hazard area. Based  
82 on measurements conducted at one location along the rockfall path using the

83 Multichannel Analysis of Surface Waves method, the in-situ shear wave velocity of the  
84 top layer was estimated to be around 800 m/sec, which is a high velocity and consistent  
85 with the rock conditions expected at the site.

86 The slope overhanging Ponti village is made of limestone and has a maximum height  
87 of 600 m and an average slope angle of  $35^{\circ}$  to  $40^{\circ}$  (Figure 2). The geological formations  
88 at the Ponti rockfall site are limestones covered by moderately cemented talus  
89 materials. The thickness of the talus materials ranges between 0.5 and 4.0 to 5.0 m. A  
90 few fallen limestone blocks were identified on the scree slope, with volumes between  
91 0.5 and  $2 \text{ m}^3$ . Based on the size distribution of these rocks on the slope, the average  
92 expected block volume would be in the order of 1 to  $2 \text{ m}^3$ .

93 The rockfall release area was at an elevation of 500 m, while the impacted house at  
94 an elevation of 130 m (Figure 3). The volume of the detached limestone block was  
95 approximately  $2 \text{ m}^3$  and its dimensions equal to 1.4 m x 1.4 m x 1 m. There was no  
96 previous rockfall incident reported for the specific slope that impacted the road or  
97 house.

### 98 **3. UAV mapping**

#### 99 **3.1. Introduction**

100 A quadrotor UAV (Phantom 3 professional) was deployed to reach the uphill terrain  
101 that was practically inaccessible. The UAV was equipped with an Ultra-high definition  
102 (UHD) 12 MP camera and had the capacity to collect 4K video. The sensor was a  
103  $1/2.3''$  CMOS (6.47x3.41mm) and the effective pixel resolution was 12.4 MP  
104 (4096x2160 pixels). An immediate UAV data acquisition expedition was conducted 2  
105 days after the earthquake. A second more detailed mapping UAV expedition with the  
106 objective to create a DEM was conducted 5 months after the rockfall event.

107 The first objective of the UAV deployment was to find the initiation point of the rock  
108 and then identify the rockfall path (shown in Figure 2). A particular focus on that part

109 of the task was the identification of rolling and bouncing sections of the rockfall path.  
110 In addition, in order to generate a high-resolution orthophoto of the rockfall trajectory,  
111 aerial video imagery was collected, and the resulting digital surface model (DSM) was  
112 used to perform rockfall analysis.

113 The Structure-from-Motion (SfM) methodology was implemented to create a 3D point  
114 cloud of the terrain and develop a 3D model. The methodology is based on identifying  
115 matching features in multiple images, and thus imagery overlap of at least 70% is  
116 required. Compared to classic photogrammetry methodologies, where the location of the  
117 observing point is well established, SfM tracks specific discernible features in multiple  
118 images, and through non-linear least-squares minimisation (Westoby et al., 2012),  
119 iteratively estimates both camera positions, as well as object coordinates in an arbitrary  
120 3D coordinate system. In this process, sparse bundle adjustment (Snavely et al., 2008)  
121 is implemented to transform measured image coordinates to three dimensional points  
122 of the area of interest. The outcome of this process is a sparse 3D point cloud in the  
123 same local 3D coordinate system (Micheletti et al., 2015). Subsequently, through an  
124 incremental 3D scene reconstruction, the 3D point cloud is densified. Paired with GPS  
125 measurements of a number of control points (for this site, 10 fast-static GPS points  
126 were collected) at the top, middle and bottom of the surveyed area, the 3D point cloud  
127 is georeferenced to a specific coordinate system and through post-processing a digital  
128 surface model (DSM) or digital terrain model (DTM) and orthophotos are created. The  
129 SfM methodology was implemented in this study using the Agisoft Photoscan software.

130 In addition, the accuracy of the model has been examined by using portions of the  
131 ground control points and developing DEM of differencing between different models,  
132 an investigation that is described in our paper by Manousakis et al. (2016). Finally, a  
133 comparison was made of the DEM developed by the UAV against the satellite-based  
134 DEM that is part of the Greek cadastre. The two surfaces were found to be very similar.

135 The overlap between pictures was minimum frontal 80%, side 65% and a total of 714  
136 camera station (video frames extracted) were included as shown in Figure 4.

### 137 **3.2. High-resolution Orthophoto**

138 A 5cm pixel size orthophoto was generated based on the methodology outlined earlier.  
139 As shown in Figure 5, the rolling section and the bouncing locations of the rock block  
140 throughout its course were identified. The rolling section was discerned as a  
141 continuous and largely linear mark left in the densely vegetated terrain that was  
142 indicative of the damage caused. Impact points that are part of the bouncing section  
143 of the rock, were identified as circular to ellipsoidal bare earth craters with no  
144 disturbance in between. The last bouncing point before impacting the house is clearly  
145 identified on the paved road. The plan view ortho-imagery, along with the original  
146 footage of the video collected was crucial to the qualitative identification of these  
147 features. The alternative, i.e., land-based, conventional field reconnaissance was  
148 physically impossible to perform in the densely vegetated and steep terrain.

### 149 **3.3. Digital Surface Model**

150 A profile section and a 10 cm Digital Surface Model (DSM) paired with the plan view  
151 orthophoto were first developed (Manousakis et al., 2016) allowing the identification of  
152 terrain features such as structures, slope benches or high trees, which could affect the  
153 rock's path downhill. However, this resolution of the DSM proved to be not only  
154 unnecessarily high and thus difficult to manipulate in subsequent rockfall analyses, but  
155 also resulted in numerical instabilities during the rockfall analyses. Therefore, a  
156 downscaled 2 m DSM was produced for the rockfall analysis. This was implemented  
157 through an aggregate generalization scheme where each output cell is assigned the  
158 minimum of the input cells that are encompassed by that cell. In addition, noise filtering  
159 and smoothing processing were implemented to reduce the effect of construction  
160 elements and vegetation in the final rasterized model. Note that this resolution is still  
161 higher than the resolution of DSM that are often used in rockfall analyses.

162 Algorithms for vegetation removal were executed within Whitebox GAT Geospatial  
163 Analysis Tools platform. GCPs were used for both georeferencing and solving  
164 camera's internal and external parameters. The process involves Point Cloud  
165 neighborhood examination and DEM smoothing algorithms. Firstly, a bare-Earth digital  
166 elevation model (DEM) was interpolated from the input point cloud LAS file, by  
167 specifying the grid resolution (2m) and the inter-point slope threshold. The algorithm  
168 distinguished ground points from non-ground points based on the inter-point slope  
169 threshold. The interpolation area was divided into grid cells, corresponding to the cells  
170 of the output DEM. All of the point cloud points within the circle encompassing each  
171 grid cell were then examined as a neighborhood. All points within a neighborhood that  
172 have an inter-point slope with any other point and are also situated above the  
173 corresponding point, are considered to be a non-ground point. An appropriate value  
174 for the inter-point slope threshold parameter depends on the steepness of the terrain,  
175 but generally values of 15-35 degrees produce satisfactory results. The elevation  
176 assigned to the grid cell was then the nearest ground point elevation (Whitebox GAT  
177 help topics).

178 Further processing of the interpolated bare-earth DEM was introduced to improve  
179 vegetation and structures removal results by applying a second algorithm to point cloud  
180 DEMs, which frequently contain numerous off-terrain objects such as buildings, trees  
181 and other vegetation, cars, fences and other anthropogenic objects. The algorithm  
182 works by finding and removing steep-sided peaks within the DEM. All peaks within a  
183 sub-grid, with a dimension of the user-specified Maximum Off-Terrain Object (OTO)  
184 Size, in pixels, were identified and removed. Each of the edge cells of the peaks were  
185 then examined to see if they had a slope that is less than the user-specified Minimum  
186 OTO Edge Slope and a back-filling procedure was used. This ensured that OTOs are  
187 distinguished from natural topographic features such as hills (Whitebox GAT help  
188 topics). Total RMS error after filtering for 6 GCPs was 0.07m, while total RMS error

189 for 4 Check Points was 0.20m. When compared to a 5m DEM from Greek National  
190 Cadastre with a geometric accuracy of  $RMSE_z \leq 2,00m$  and absolute accuracy  $\leq$   
191 3,92m for a confidence level of 95%, a mean difference of 0.77 m and a standard  
192 deviation of 1.25 m is observed, which is well into the range of uncertainty of the  
193 cadastre model itself.

## 194 **4. Earthquake characteristics – Initial conditions**

### 195 **4.1. Seismic acceleration**

196 The epicenter of the earthquake according to the National Observatory of Athens,  
197 Institute of Geodynamics (NOA) is located onshore near the west coast of Lefkada.  
198 The causative fault is estimated to be a near-vertical strike-slip fault with dextral sense  
199 of motion (Ganas et al., 2015, 2016). Based on the focal mechanism study of the  
200 earthquake, it was determined that the earthquake was related to the right lateral  
201 Kefalonia-Lefkada Transform Fault (KLTF), which runs nearly parallel to the west  
202 coasts of both Lefkada and Kefalonia island, in two segments (Papazachos et al. 1998,  
203 Rondoyanni et al. 2012).

204 A strong motion station recorded the ground motions in the village of Vasiliki located  
205 at a distance of 2.5 km from the Ponti rockfall site. The ground motion characteristics  
206 of the recording are summarized in Table 1 and are presented in Figure 6, according  
207 to an ITSAK preliminary report (ITSAK, 2016).

### 208 **4.2. Topography effect**

209 Peak ground acceleration along the rock slope is the intensity of base shaking modified  
210 by site and topographic effects (Mavrouli et al., 2009). In the present case, local  
211 shaking intensity in terms of horizontal PGA was considered. The E-W component of  
212 acceleration was considered for the determination of the initial velocity. The peak  
213 ground acceleration (PGA) on the slope face ( $PGA_{sf}$ ) was obtained by linear  
214 interpolation between the acceleration at the base ( $PGA_b$ ) and at the slope crest



215 (PGA<sub>cr</sub>). The acceleration at the base was equal to 0.32g and thus at the crest PGA<sub>cr</sub>=  
216 1.5 PGA<sub>b</sub> equal to 0.48g, was estimated at the site of detachment.

#### 217 **4.3. Initial velocity of rock block**

218 The initial horizontal velocity of the block, at the time of detachment, was calculated  
219 considering equilibrium of the produced work and the kinetic energy according to  
220 equation 1.

$$221 \quad v_x = \sqrt{2 \times PGA_{sf} \times s} \quad (1),$$

222 where PGA<sub>sf</sub> is the acceleration on the slope at the location of detachment and s the  
223 initial displacement of the block in order to initiate its downslope movement.

224 The initial horizontal velocity was calculated equal to 0.67 m/sec, considering a  
225 displacement in the order of s = 0.05 m. The vertical component of the initial velocity  
226 is assumed to be zero.

### 227 **5. Trajectory analysis**

228 In order to estimate the possible rock paths and design remedial measures, simulation  
229 programs based on lumped-mass analysis models are commonly used in design  
230 practice. The trajectory of a block is modelled as a combination of four motion types;  
231 free falling, bouncing, rolling and sliding (Descoedres and Zimmermann, 1987).  
232 Usage of the lump-mass model has some key limitations; the block is described as  
233 rigid and dimensionless with an idealized shape (sphere); therefore the model neglects  
234 the block's actual shape and configuration at impact, even though it is evident that they  
235 both affect the resulting motion.

236

#### 237 **5.1. Modelling the response to an impact**

238 The most critical input parameters are the coefficients of restitution (COR), which  
239 control the bouncing of the block. In general, the coefficient of restitution (COR) is

240 defined as the decimal fractional value representing the ratio of velocities (or impulses  
241 or energies; depending on the definition used) before and after an impact of two  
242 colliding entities (or a body and a rigid surface). When in contact with the slope, the  
243 block's magnitude of velocity changes according to the COR value. Hence, COR is  
244 assumed to be an overall value that takes into account all the characteristics of the  
245 impact; including deformation, sliding upon contact point, transformation of rotational  
246 moments into translational and vice versa (Giani, 1992).

247 The most widely used definitions originate from the theory of inelastic collision as  
248 described by Newtonian mechanics. For an object impacting a rocky slope (Figure 7),  
249 which is considered as a steadfast object, the kinematic COR ( $v_{COR}$ ) is defined  
250 according to Eq. 2.

$$251 \quad v_{COR} = \frac{v_r}{v_i} \quad (2)$$

252 where  $v$  is the velocity magnitude and the subscripts  $i$  and  $r$  denote the trajectory stage;  
253 incident (before impact) and rebound (after impact) respectively.

254 Two different mechanisms participate in the energy dissipation process; energy loss  
255 normal to the slope is attributed to the deformation of the colliding entities, and in the  
256 tangential direction is due to friction between them. Therefore kinematic COR has been  
257 analyzed to the normal and tangential component with respect to the slope surface,  
258 defining the normal ( $n_{COR}$ ) and the tangential ( $t_{COR}$ ) coefficient of restitution (Eq. 3 and  
259 4 respectively).

$$260 \quad n_{COR} = \frac{v_{n,r}}{v_{n,i}} \quad (3)$$

261 and

$$262 \quad t_{COR} = \frac{v_{t,r}}{v_{t,i}} \quad (4)$$

263 where the first subscript, n or t denotes the normal or the tangential components of the  
264 velocity respectively.

265 Normal and tangential COR have prevailed in natural hazard mitigation design via  
266 computer simulation due to their simplicity. Values for the coefficients of restitution are  
267 acquired from values recommended in the literature (Azzoni et al. 1995; Heidenreich  
268 2004; Richards et al. 2001, RocScience, 2004). Those are mainly related to the surface  
269 material type and originate from experience, experimental studies or back analysis of  
270 previous rockfall events. This erroneously implies that coefficients of restitution are  
271 material constants. However, COR values depend on several parameters that cannot  
272 be easily assessed. Moreover, the values suggested by different authors vary  
273 considerably and are sometimes contradictory.

## 274 **5.2. Rockfall path characteristics**

275 23 impact points were identified on the slope surface (Figure 8). Their coordinates are  
276 presented in Table 2, along block's path starting from the detachment point (where  
277  $x=0$ ). No trees were observed along the block's path.

278 The apparent dip of the slope at impact positions was measured from the topographic  
279 map; on each impact point a line was set with a length twice the block's mean  
280 dimension, oriented according to preceding trajectory direction. Moreover, the impact  
281 point was expanded on the topographic map to a rectangular plane with a side twice  
282 as much the mean dimension of the block (Figure 9). This plane was then oriented so  
283 that one side coincides with the strike direction and its' vertical side toward to the dip  
284 direction. Thus, direction difference,  $\Delta\phi$ , was measured by the strike direction and the  
285 preceding path and deviation,  $e$ , was measured as the angle between pre and post  
286 impact planes (Asteriou & Tsiambaos, 2016).

287 Having a detailed field survey of the trajectory path, a back analysis according to the  
288 fundamental kinematic principles was performed in order to back-calculate the actual  
289 COR values.

### 290 **5.3. Kinematic analysis and assumptions**

291 The 23 impact points identified on the slope comprise a rockfall path of 22 parabolic  
292 segments. The vertical and horizontal length of each segment is acquired by  
293 subtracting consecutive points. Since no external forces act while the block is in the  
294 air, each segment lays on a vertical plane and is described by the general equation of  
295 motion as:

$$296 \quad y = x \tan \vartheta - \frac{gx^2}{2v_i^2 \cos^2 \vartheta} \quad (5)$$

297 where:  $\theta$  the launch angle from the horizon and  $v$  the launch (initial) velocity (Figure  
298 10).

299 Since no evidence can be collected regarding launch angle and velocity, innumerable  
300 parabolas satisfy Eq. 5. However,  $\theta$  is bound between  $-\beta$  and  $90^\circ$ , so in order to  
301 acquire realistic values for the initial velocity, its sensitivity for that given range was  
302 addressed (Figure 11).

303 For the case presented in Fig. 11 (the first parabolic segment) it is seen that for the  
304 majority of the release angles, initial velocity variation is low and ranges between 7.2  
305 and  $12 \text{ ms}^{-1}$ . Additionally, the relationship between release angle and initial velocity is  
306 expressed by a curvilinear function, thus a minimum initial velocity value along with its  
307 release angle (denoted hereafter as  $\theta_{cr}$ ) can be easily acquired.

308 Given the minimum initial velocity and the critical release angle for each parabolic  
309 segment, the impact velocity and angle can be calculated. Afterwards, normal and  
310 tangential velocity components according to the apparent dip of the impact area, are  
311 calculated in order to evaluate COR values. Results are summarized in Table 3.

#### 312 **5.4. Coefficients of restitution**

313 It is observed that  $v_{cor}$  (Table 3) is slightly greater than one in 5 out of 22 impacts.  
314 According to Eq. 3, this can only be achieved when impact velocity is less than rebound  
315 velocity. However, this indicates that energy was added to the block during contact,  
316 which is not possible according to the law of conservation of energy. Thus, impact  
317 velocity should be greater, which is possible if the launch velocity of the previous  
318 impact was more than the assumed minimum.

319 Omitting the impacts with  $V_{cor}>1$ , it is observed that kinematic COR ranges between  
320 0.55 and 1.0 and presents smaller variation compared to normal or tangential  
321 coefficient of restitution, similar to what was previously reported in relevant literature  
322 (i.e. Asteriou et al, 2012; Asteriou & Tsiambaos, 2016).

323 The considerably wide scatter of normal COR implies that the restitution coefficient  
324 cannot be a material constant. Yet, in most relevant software, normal COR is defined  
325 solely by the slope material. Moreover, normal COR values higher than one were  
326 calculated in 11 out of the 15 remaining impacts. Normal COR higher than one have  
327 been observed in both experimental (e.g. Spadari et al., 2011; Buzzi et al., 2012;  
328 Asteriou et al., 2012) and back-analysis studies (e.g. Paronuzzi, 2009) and are related  
329 to irregular block shape and slope roughness, as well as to shallow impact angle and  
330 angular motion. A more detailed presentation of the reasons why normal COR exceeds  
331 unity can be found in Ferrari et al. (2013). However, in relevant software normal COR  
332 values are bounded between 0 and 1.

333 Moreover, it is observed in Figure 12 that normal COR increases as the impact angle  
334 reduces, similarly to previous observations by Giacomini et al. (2012), Asteriou et al.  
335 (2012) and Wyllie (2014). The correlation proposed by Wyllie (2014) is also plotted in  
336 Figure 13 and seems to describe consistently, but on the unconservative side, the  
337 trend and the values acquired by the aforementioned analysis and assumptions.

## 338 **6. Rockfall modelling**

### 339 **6.1. 2-D analyses**

340 Initially, a deterministic 2D rockfall analysis was performed using Rocfall software  
341 (RocScience, 2004). According to Asteriou & Tsiambaos (2016) the most important  
342 influence is posed by the impact configuration, which is influenced by slope roughness  
343 and block shape. In this study, roughness has been fully taken into account  
344 (considering the block's dimension scale) by the accurate cross-section used in the  
345 analyses (more than 1500 x-y points were used – approximately 2 points per meter).  
346 Based on our experience, this accuracy is significantly higher compared to other similar  
347 research projects. Moreover, with the available data and the performed lump-mass  
348 model analysis, it was not possible to simulate block shape effect nor the configuration  
349 of the block at impact.

350 Considering an initial velocity of 0.67 m/sec, according to the numerical analyses, the  
351 falling rock primarily rolls on the slope and stops much earlier than its actual run out  
352 distance, approximately 400 m downslope from its starting point (Fig. 8; case 1). The  
353 restitution coefficients were  $n_{COR}=0.35$ ,  $t_{COR}=0.85$ , which represent properties of  
354 bedrock outcrops according to the suggested values provided in the documentation of  
355 the software.

356 The friction angle was set to zero. A standard deviation for the coefficients of restitution,  
357 the friction angle and roughness of the material on the slope was not used, as the  
358 analysis was deterministic. If the friction angle is set to  $\varphi=32^{\circ}$  (as suggested by the  
359 software documentation), the rock travels downslope only 50 m.

360 A separate analysis was performed, with lower coefficients of restitution, resembling  
361 that of talus material on the slope ( $n_{COR}=0.32$ ,  $t_{COR}=0.82$ ,  $\varphi=30^{\circ}$ ) as proposed by the  
362 suggested values provided in the documentation of the software. In this case, the rock  
363 block rolled only a few meters downslope. Therefore, it is evident that the actual rock  
364 trajectory cannot be simulated.

365 In order to simulate the actual trajectory as much as possible, various combinations of  
366 restitution coefficients and friction angle were considered. The closest match occurred  
367 for  $n_{COR}=0.60$  and  $t_{COR}=0.85$ , while the friction angle was set to zero and no velocity  
368 scaling was applied. Only in such an analysis, the rock block reaches the house; with  
369 a velocity equal to  $v=18$  m/s approximately (Fig. 8; case 2). According to the suggested  
370 values, these values for the coefficients correspond to a bedrock material (limestone).

371 In this case, the modelled trajectory is significantly different from the actual one. The  
372 main difference is that the block is rolling up to 200 m downslope while the actual rolling  
373 section is 400 m (as shown in Figure 8). Furthermore the impacts on the ground in the  
374 bouncing section of the trajectory are considerably different in number (14 versus 23)  
375 and in location from the actual ones. Finally, the bounce height of some impacts seems  
376 unrealistically high. For example, the 2<sup>nd</sup> bounce presents a jump height ( $f$ ) of  $\sim 17.5$ m  
377 over a length ( $s$ ) of  $\sim 50$ m, resulting to a  $f/s$  ratio of  $\sim 1/3$ , when the characteristic  $f/s$   
378 ratios for high, normal and shallow jumps is  $1/6$ ,  $1/8$  and  $1/12$  respectively, as  
379 suggested by Volkwein et al. (2011).

## 380 **6.2. 3-D rockfall analysis**

381 The rockfall trajectory model Rockyfor3D (Dorren, 2012) has also been used in order  
382 to validate the encountered trajectory and determine the reach probability of the falling  
383 rock (from the specific source area) on the impacted house.

384 The 3D analysis was based on the down-scaled 2 m resolution Digital Elevation Model  
385 (DEM) that was generated from the 10 cm DSM. The terrain features such as low  
386 vegetation (e.g. bushes) and the trees were removed from the DEM as they affected  
387 the rock's path downhill. The following raster maps were developed for the 3D analysis:  
388 a) rock density of rockfall source, b) height, width, length and shape of block, c) slope  
389 surface roughness and d) soil type on the slope, which is directly linked with the normal  
390 coefficient of restitution,  $n_{COR}$ .

391 The slope roughness was modeled using the mean obstacle height (MOH), which is  
392 the typical height of an obstacle that the falling block encounters on the slope at a  
393 possibility percentage of 70%, 20% and 10% of the trajectories (according to the  
394 suggested procedure in Rockyfor3D). No vegetation was considered in the analysis,  
395 which favours a longer trajectory. The parameters considered in the 3D analysis for  
396 the different formations are summarised in Table 4. The spatial occurrence of each soil  
397 type is shown in Figure 13 and the assigned values of  $n_{COR}$  are according to the  
398 Rockyfor3D manual. The values for soil type 4.1 in Figure 13 are slightly different from  
399 soil type 4 (proposed in the manual), denoting talus with a larger percentage of fallen  
400 boulders. The block dimensions were considered equal to  $2 \text{ m}^3$  and the shape of the  
401 boulder was rectangle. In order to simulate the initial velocity of the falling rock due to  
402 the earthquake, an additional initial fall height is considered in the analysis, which for  
403 this case was set equal to 0.5 m.

404 The energy line angles were recalculated from the simulated trajectories and it was  
405 determined that the energy line angle with highest frequency (39%) was  $30\text{-}31^\circ$ . Based  
406 on the 3D analysis no rock blocks would impact the house, although the rock paths are  
407 closer to the actual trajectories compared to RocFall software. The reach probability of  
408 the falling rocks, initiating from the source point, is shown in Figure 14.

### 409 **6.3. Lateral dispersion & Deviation**

410 Lateral dispersion is defined as the ratio between the distance separating the two  
411 extreme fall paths (as seen looking at the face of the slope) and the length of the slope  
412 (Azzoni and de Freitas 1995). According to Crosta and Agliardi (2004) the factors that  
413 control lateral dispersion are classified in three groups: macro-topography factors,  
414 factors related to the overall slope geometry; micro-topography factors controlled by  
415 the slope local roughness; and dynamic factors, associated with the interaction  
416 between slope features and block dynamics during bouncing and rolling. Assessing  
417 the results of an experimental investigation, Azzoni and de Freitas (1995) commented



418 that the dispersion is generally in the range of 10% to 20%, regardless of the length of  
419 the slope and that steeper slopes present smaller dispersion. Agliardi and Crosta  
420 (2003) calculated lateral dispersion to be up to 34%, via high-resolution numerical  
421 models on natural rough and geometrically complex slopes.

422 Lateral dispersion cannot be defined from the actual rockfall event in Ponti since only  
423 one path is available. Using the simulated trajectories from RockyFor3D, which are in  
424 the 3d space (Figure 15), a lateral dispersion of approximately 60% is shown in the  
425 middle of the distance between detachment point and the house. This is significantly  
426 higher compared to the findings of Azzoni and de Freitas (1995) and Agliardi and  
427 Crosta (2003). Moreover, based on the actual event and intuition, the lateral dispersion  
428 computed by RockyFor3D is extremely pronounced and most likely due to the  
429 topography effect of the area of detachment. Specifically the origin of the rock block  
430 is located practically on the ridgeline, facilitating the deviation of the rock fall trajectory  
431 from the slope line. Examining Figure 15, it is notable that the rock paths are severely  
432 affected by topography. Therefore, assessing lateral dispersion seems to be a case  
433 specific task.

434 Asteriou & Tsiambaos (2016) defined deviation ( $e$ ) as the dihedral angle between the  
435 pre- and post-impact planes that contain the trajectory. They found that deviation is  
436 controlled by the direction difference  $\Delta\phi$ , the slope inclination and the shape of the  
437 block. For a parallel impact (i.e.  $\Delta\phi=0^\circ$ ) a spherical block presents significantly less  
438 deviation compared to a cubical. Additionally, deviation is equally distributed along the  
439 post-impact direction and reduces as the slope's inclination increases. On oblique  
440 impacts the block's direction after impact changes towards the aspect of slope and as  
441  $\Delta\phi$  increases this trend becomes more pronounced.

442 Figure 16 presents deviation as a function of direction difference. It is noted that for  
443 parallel impacts deviation is also equally distributed along the post-impact direction.  
444 As direction difference increases, deviation becomes positive, which means that the

445 change of direction is following the direction of slope's aspect. These findings are in  
446 line with trends described by Asteriou & Tsiambaos (2016), but the deviation of the  
447 actual trajectory is significantly lower. This can be attributed to the different conditions  
448 (i.e. block shape, slope material, slope roughness, incident velocity and angle, and  
449 scale) between the experimental program conducted by Asteriou & Tsiambaos (2016)  
450 and the Ponti rockfall event.

## 451 **7. Discussion - conclusions**

452 UAV-enabled reconnaissance was successfully used for the identification of the origin  
453 of the detached rock, the rockfall trajectory and the impact points on the slope,  
454 emphasizing on the motion types of the trajectory (rolling and bouncing sections). A  
455 UAV with an ultra-high definition (UHD) camera was deployed to reach the  
456 inaccessible, steep and partly vegetated uphill terrain. A high-resolution orthophoto of  
457 the rockfall trajectory and a 10 cm DSM was prepared, which formed the basis for an  
458 analytical 2D kinematic analysis and a comparison with the outcomes of 2D and 3D  
459 rockfall analysis software.

460 The initial velocity of the detached rock was estimated based on site conditions and  
461 amplification of the ground acceleration due to topography. It was found that the  
462 estimation of the initial velocity of the blocks plays a significant role in the accurate re-  
463 production of the rockfall trajectory.

464 Based on the analytical analysis performed, it was found that the coefficients of  
465 restitution cannot be directly connected to the material type, nor can be considered  
466 constants. The impact angle seems to pose a consistent effect on normal COR, which  
467 has been observed also in other recent relevant studies, but has not been incorporated  
468 yet on analysis models.

469 It was proven impossible to replicate the actual trajectory of the rock fall by performing  
470 a 2D rockfall analysis with the set of parameters recommended by the developers

471 revealing some limitations in the present formulations. In an attempt to match the  
472 actual rock path to the analysis output, the friction angle of the limestone slope was  
473 considered equal to zero. However, the falling rock still rolled on the slope and stopped  
474 much earlier than its actual runout distance while the impacts on the ground in the  
475 bouncing section of the trajectory were considerably different in number and in location  
476 compared to the actual ones.

477 Using the 3D analysis software, some rock trajectories better approximated the actual  
478 trajectory using the suggested values by the software developers, indicating that the  
479 3D analysis can be more accurate than the 2D analysis.

480 Based on the aforementioned analyses it becomes evident that engineering judgement  
481 and experience must accompany the usage of commercial rockfall software in order to  
482 acquire realistic paths. One should never blindly use the suggested set of parameters  
483 since field performance can differ significantly, as demonstrated by this case study.

484

## 485 **References**

- 486 1. Agliardi F, Crosta GB (2003) High resolution three-dimensional numerical  
487 modelling of rockfalls. *International Journal of Rock Mechanics and Mining*  
488 *Sciences* 40:455-471. doi: 10.1016/S1365-1609(03)00021-2
- 489 2. Asteriou P, Saroglou H, Tsiambaos G (2012). Geotechnical and kinematic  
490 parameters affecting the coefficients of restitution for rock fall analysis.  
491 *International Journal of Rock Mechanics and Mining Sciences* 54:103-113.  
492 doi:10.1016/j.ijrmms.2012.05.029.
- 493 3. Asteriou P and Tsiambaos G. (2016). Empirical Model for Predicting Rockfall  
494 Trajectory Direction. *Rock Mechanics and Rock Engineering* 49.3, pp. 927–  
495 941.

- 496 4. Azzoni A, de Freitas MH (1995). Experimentally gained parameters, decisive  
497 for rock fall analysis. *Rock Mechanics and Rock Engineering* 28:111-124. doi:  
498 10.1007/BF01020064
- 499 5. Buzzi O, Giacomini A, Spadari M (2012) Laboratory investigation on high  
500 values of restitution coefficients. *Rock Mechanics and Rock Engineering* 45:35-  
501 43
- 502 6. Crosta GB, Agliardi F (2004) Parametric evaluation of 3D dispersion of rockfall  
503 trajectories. *Natural Hazards and Earth System Science* 4:583-598.  
504 doi:10.5194/nhess-4-583-2004
- 505 7. Descoedres F, Zimmermann TH. Three-dimensional dynamic calculation of  
506 rockfalls. In: *Proceedings of the 6th International Congress on Rock*  
507 *Mechanics*. Montreal; 30 August -3 September 1987. p. 337–42.
- 508 8. Dorren, L.K.A., 2012. Rockyfor3D (v5.1) revealed - Transparent description of  
509 the complete 3D rockfall model. ecorisQ paper, 31 p.
- 510 9. Ganas, A., Briole, P., Papathanassiou, G., Bozionelos, G., Avallone, A.,  
511 Melgar, D., Argyrakis, P., Valkaniotis, S., Mendonidis, E., Moshou, A. and Elias,  
512 P. (2015). A preliminary report on the Nov 17, 2015 M=6.4 South Lefkada  
513 earthquake, Ionian Sea, Greece, Report to EPPO, December 4 2015.
- 514 10. Ganas A., Elias P., Bozionelos G., Papathanassiou G., Avallone A.,  
515 Papastergios P. Valkaniotis S., Parcharidis I., Briole P. (2016). Coseismic  
516 deformation, field observations and seismic fault of the 17 November 2015 M  
517 = 6.5, Lefkada Island, Greece earthquake. *Tectonophysics* 687, pp. 210–222.
- 518 11. Giani GP. *Rock Slope Stability Analysis*. Rotterdam: Balkema A.A; 1992.
- 519 12. Giacomini A, Thoeni K, Lambert C, Booth S, Sloan SW (2012) Experimental  
520 study on rockfall drapery systems for open pit highwalls. *International Journal*

- 521 of Rock Mechanics and Mining Sciences 56:171-181.  
522 doi:10.1016/j.ijrmms.2012.07.030
- 523 13. Ferrari F, Giani GP, Apuani T (2013) Why can rockfall normal restitution  
524 coefficient be higher than one? Rendiconti Online Societa Geologica Italiana  
525 24
- 526 14. Heidenreich B (2004) Small- and half-scale experimental studies of rockfall  
527 impacts on sandy slopes. Dissertation, EPFL.
- 528 15. ITSAK (2016). Preliminary presentation of the main recording of ITSAK – OASP  
529 accelerometer network in Central Ionian. Earthquake M6.4 17/11/2015.  
530 Thessaloniki, 11 pp.
- 531 16. Karakostas, V. G., Papadimitriou, E. E., and Papazachos, C. B. 2004.  
532 Properties of the 2003 Lefkada, Ionian Islands, Greece, Earthquake Seismic  
533 Sequence and Seismicity Triggering. Bulletin of the Seismological Society of  
534 America, 94 (5), 1976–1981, October 2004
- 535 17. Manousakis J., Zekkos D., Saroglou H., Clark M. (2016). Comparison of UAV-  
536 enabled photogrammetry-based 3D point clouds and interpolated DSMs of  
537 sloping terrain for rockfall hazard analysis. Proc. Int. Archives of the  
538 Photogrammetry, Remote Sensing and Spatial Information Sciences, Vol. XLII-  
539 2/W2, p. 71-78.
- 540 18. Marinou P, Tsiambaos G., 2002. Earthquake triggering rock falls affecting  
541 historic monuments and a traditional settlement in Skyros Island, Greece. Proc.  
542 of the Int. Symposium: Landslide risk mitigation and protection of cultural and  
543 natural heritage, Kyoto, Japan, pp. 343-346.
- 544 19. Mavrouli O., Corominas J., Wartman J. (2009). Methodology to evaluate rock  
545 slope stability under seismic conditions at Sol`a de Santa Coloma, Andorra.  
546 Nat. Hazards Earth Syst. Sci., 9, 1763–1773. Micheletti N., Chandler J., Lane

- 547 S., 2015. Structure from Motion (SfM) Photogrammetry. British Society for  
548 Geomorphology. *Geomorphological Techniques*, Chap. 2, Sec. 2.2 (2015)
- 549 21. Papathanassiou, G., Valkaniotis, S., Ganas, A. and Pavlides, S. 2012. GIS-  
550 based statistical analysis of the spatial distribution of earthquake-induced  
551 landslides in the island of Lefkada, Ionian Islands, Greece, *Landslides*, Journal  
552 of the International Consortium on Landslides, DOI 10.1007/s10346-012-0357-  
553 1
- 554 22. Papazachos B.C., Papadimitriou E.E., Kiratzi A.A., Papazachou C.B., Louvari  
555 E.K. 1998. Fault plane solutions in the Aegean sea and the surrounding area  
556 and their tectonic implication. *Bull Geof Teor Appl* 39(3), 199–218.
- 557 23. Paronuzzi P. (2009) Field Evidence and Kinematical Back-Analysis of Block  
558 Rebounds: The Lavone Rockfall, Northern Italy. *Rock Mech Rock Eng*, 42:783–  
559 813
- 560 24. Richards LR, Peng B, Bell DH (2001) Laboratory and field evaluation of the  
561 normal Coefficient of Restitution for rocks. Proceedings of ISRM Regional  
562 Symposium EUROCK2001:149-155
- 563 25. RocScience, 2004. Rocfall Manual.
- 564 26. Rondoyanni Th., Mettos A., Paschos P., Georgiou Ch. 2007. Neotectonic map  
565 of Greece, scale 1:100.000, Lefkada sheet. I.G.M.E., Athens.
- 566 27. Saroglou, H. 2013. Rockfall hazard in Greece. *Bulletin of the Geological*  
567 *Society of Greece*, vol. XLVII, no3, 1429-1438.
- 568 28. Saroglou, H., Marinos, V., Marinos, P., Tsiambaos, G. 2012. Rockfall hazard  
569 and risk assessment: an example from a high promontory at the historical site  
570 of Monemvasia, Greece. *Natural Hazards and Earth System Sciences*, 12,  
571 1823–1836. doi:10.5194/nhess-12-1823-2012.

- 572 29. Snavely N., Seitz S.N., Szeliski R., 2008. Modeling the world from internet  
573 photo collections. *International Journal of Computer Vision* 80: 189-210.
- 574 30. Spadari M, Giacomini A., Buzzi O., Fityus S., Giani G.P.(2011). In situ rockfall  
575 testing in New South Wales, Australia. *Int J Rock Mech Mining Sci*, 49, pp. 84–  
576 93.
- 577 31. Volkwein, A., Schellenberg, K., Labiouse, V., Agliardi, F., Berger, F., Bourrier,  
578 F., Dorren, L. K. A., Gerber, W., and Jaboyedoff, M., 2011. Rockfall  
579 characterisation and structural protection – a review, *Nat. Hazards Earth Syst.*  
580 *Sci.*, 11, 2617–2651, doi:10.5194/nhess-11-2617-2011.
- 581 34. Westoby M.J., Brasington J., Glasser N.F., Hambrey M.J., Reynolds J.M.,  
582 2012. ‘Structure-from-Motion’ photogrammetry: A low-cost, effective tool for  
583 geoscience applications. *Geomorphology* 179 (2012) 300-314.
- 584 35. Wyllie, D. C. (2014). Calibration of rock fall modeling parameters.  
585 *International Journal of Rock Mechanics and Mining Sciences* 67: 170-180
- 586 36. Zekkos D., Clark M., Cowell K., Medwedeff W., Manousakis J., Saroglou H.  
587 Tsiambaos G. (2017). Satellite and UAV-enabled mapping of landslides caused  
588 by the November 17<sup>th</sup> 2015  $M_w$  6.5 Lefkada earthquake. *Proc. 19<sup>th</sup> Int.*  
589 *Conference on Soil Mechanics and Geotechnical Engineering, Seoul 2017*  
590 (accepted for publication).
- 591

592

**TABLES**

593

Table 1. Accelerometer recordings

<b>Component</b>	<b>Acceleration (cm/sec<sup>2</sup>)</b>	<b>Velocity (cm/sec)</b>	<b>Displacement (cm)</b>
NS-comp	363	59.3	21.27
EW-comp	327	34.1	14.01
Z-comp	256	17.7	6.56

594

595 Table 2. Impact points characteristics

<b>Impact point</b>	<b>X (m)</b>	<b>Y (m)</b>	<b>app_dip (°)</b>	<b>Δφ (°)</b>	<b>e (°)</b>
1	287.63	338	39.0	0	0
2	298.38	329.68	16.3	33	0
3	305.48	324.5	27.9	27	-1
4	321.54	314.83	41.0	11.6	0.5
5	365.34	287.6	30.4	11.9	0.3
6	373.32	284.85	39.7	10.6	1.8
7	425.1	261.64	14.7	6.6	-1.3
8	464.43	251.13	18.4	33.3	0.8
9	472.06	248.81	14.0	19.1	2.3
10	495.29	243.81	7.5	52.3	0.9
11	515.31	240.8	7.9	51	0.6
12	535.56	238.31	9.1	46.7	3
13	562.11	232.22	8.7	47.3	2.1
14	605.51	211.12	16.9	25.6	-1.7
15	619.1	204.48	27.1	4.6	-3
16	639.13	196.96	21.2	8	4.7
17	662.41	184	23.3	28.5	5.2
18	688.4	169.3	27.4	0.3	-2.5
19	712.23	157.67	25.4	0.5	0.1
20	745.28	143.16	21.9	0.5	-0.1
21	762.9	137.01	22.0	0.7	2
22	789.23	125.98	21.6	1.4	-0.8
23	801.53	132.75	8.4	0.2	0.1



596 Table 3. Parabolic paths characteristics for the minimum release velocity

Segment	$\Delta x(m)$	$\Delta y (m)$	$\theta_{cr} (^\circ)$	$V_{r,min}$	$V_{impact}$	$a_i$	$V_{COR}$	$n_{COR}$	$t_{COR}$
1-2	10.75	-8.33	26.8	7.19	13.19	44.5	0.55	0.71	0.31
2-3	7.1	-5.18	25.7	5.95	9.51	27.8	0.63	0.90	0.53
3-4	16.07	-9.66	31.5	9.45	12.68	9.6	0.75	3.86	0.38
4-5	43.79	-27.23	27.7	15.46	23.13	23.3	0.67	1.57	0.26
5-6	7.98	-2.75	35.7	7.47	10.49	14.9	0.71	2.52	0.30
6-7	51.78	-23.21	34.8	18.15	21.61	31.7	0.84	1.54	0.26
7-8	39.33	-10.5	35.9	17.23	24.01	36.1	0.72	0.94	0.56
8-9	7.63	-2.32	35.9	7.45	10.54	41.1	0.71	0.87	0.55
9-10	23.23	-5	40.5	13.58	13.12	30.7	1.03	1.65	0.70
10-11	20.02	-3.01	41.1	13.00	11.57	24.2	1.12	2.06	0.82
11-12	20.25	-2.49	40.9	13.26	11.22	17.6	1.18	2.94	0.82
12-13	26.55	-6.1	38.0	14.40	14.25	28.5	1.01	1.55	0.78
13-14	43.41	-21.1	32.9	16.33	25.70	40.9	0.64	0.64	0.63
14-15	13.59	-6.64	30.7	9.13	12.81	25.1	0.71	1.24	0.53
15-16	20.03	-7.52	33.8	11.67	15.42	29.8	0.76	1.33	0.42
16-17	23.27	-12.96	31.9	11.59	15.89	28.5	0.73	1.22	0.50
17-18	25.99	-14.7	29.9	12.20	20.11	30.9	0.61	0.95	0.42
18-19	23.83	-11.63	32.2	12.08	17.10	27.9	0.71	1.30	0.40
19-20	33.05	-14.51	33.6	14.55	20.62	32.1	0.71	1.14	0.43
20-21	17.62	-6.15	34.5	11.08	11.99	18.4	0.92	2.44	0.54
21-22	26.33	-11.03	35.1	13.11	16.33	27.3	0.80	1.47	0.49
22-23	12.3	6.77	58.1	14.30	13.97	48.9	1.02	1.34	0.28

597

598

599 Table 4. Restitution parameters for Rockyfor3D

Geological formation/ other	Mean $n_{COR}$	MOH			Soil type (Rockyfor3D)
		rg70	rg20	rg10	
Scree ( $\emptyset < \sim 10$ cm), or medium compact soil with small rock fragments	0.33	0.03	0.05	0.05	3
Talus slope ( $\emptyset > \sim 10$ cm), or compact soil with large rock fragments	0.38	0.05	0.1	0.2	4
Talus with fallen boulders	0.42	0.15	0.15	0.2	4.1
Bedrock with thin weathered material	0.43	0	0.05	0.1	5
Asphalt road	0.35	0	0	0	7

600

## FIGURES

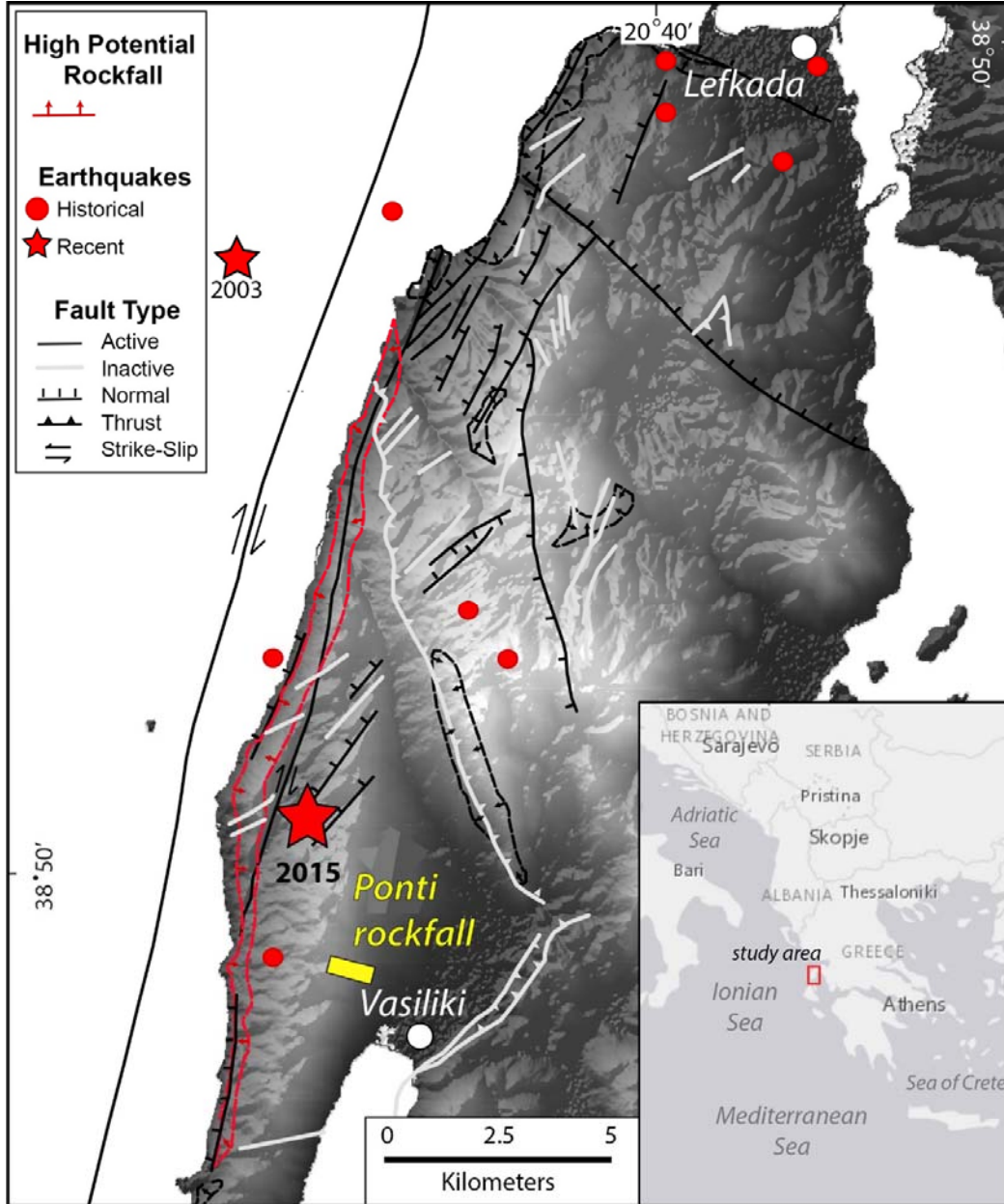


Figure 1. Map of Lefkada Island, Greece with location of study site (Ponti) and epicenters of recent earthquakes (stars) in 2003 ( $M_w$ 6.2) and 2015 ( $M_w$ 6.5), as well as historical ones (circles) Map also shows faults and high potential rockfall areas as identified by Rondoyanni et al. (2007).

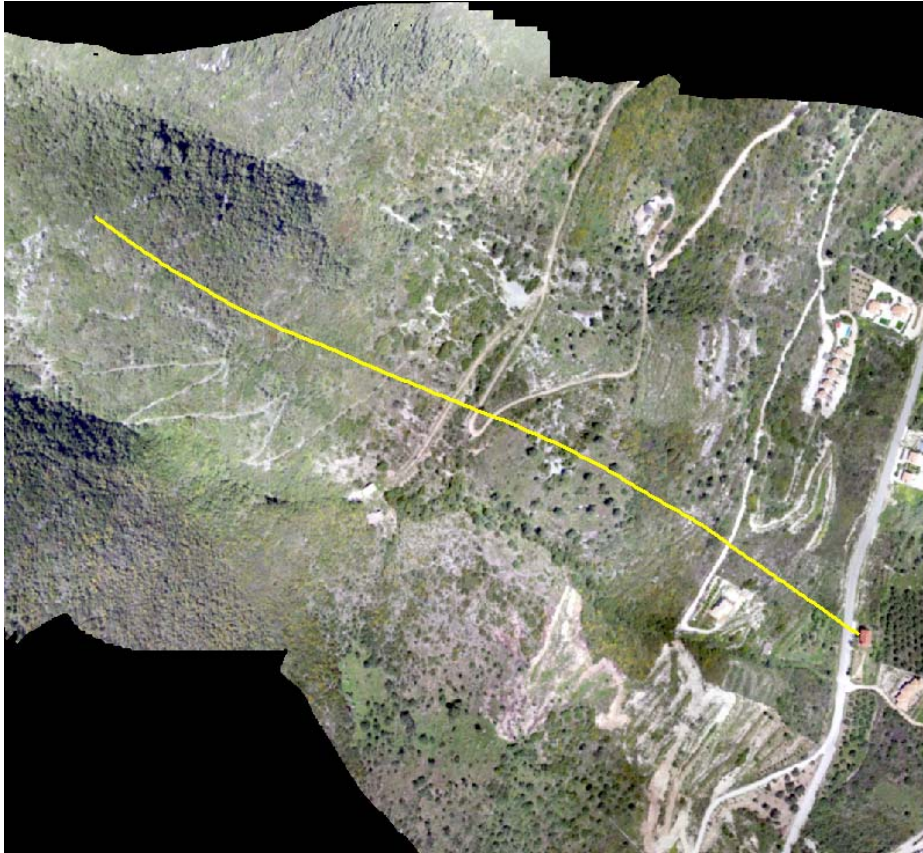


Figure 2. Orthophoto of study site. The total length of the trajectory shown with a yellow line, is 800 m.



Figure 3. Impact of rock on house in Ponti, Lefkada, Greece.

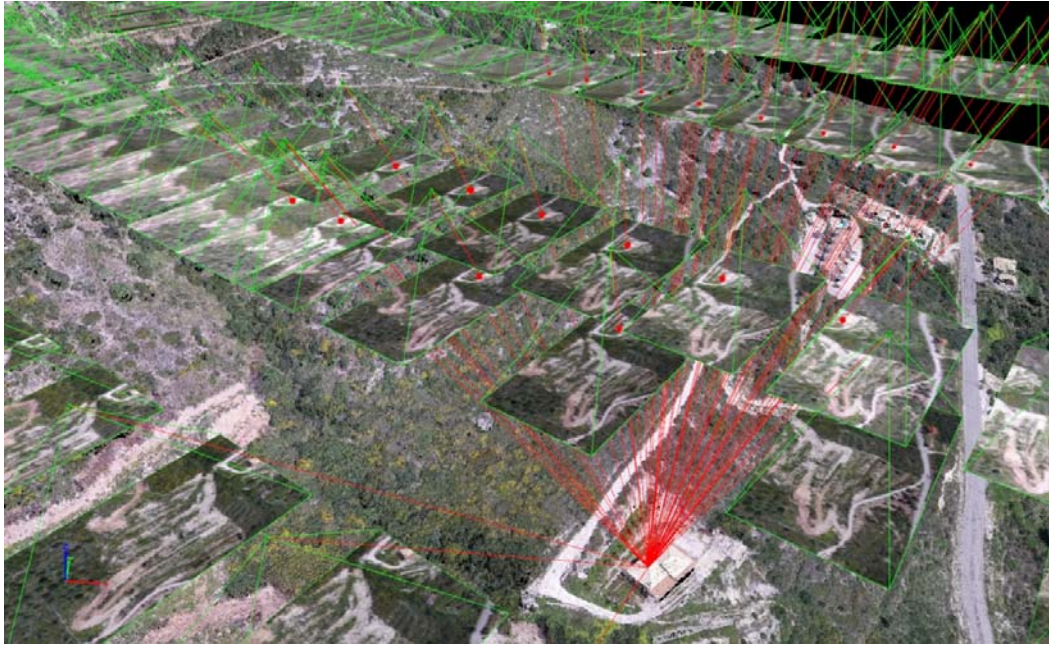


Figure 4. Schematic illustrating the overlap between pictures in the study site using SfM methodology.

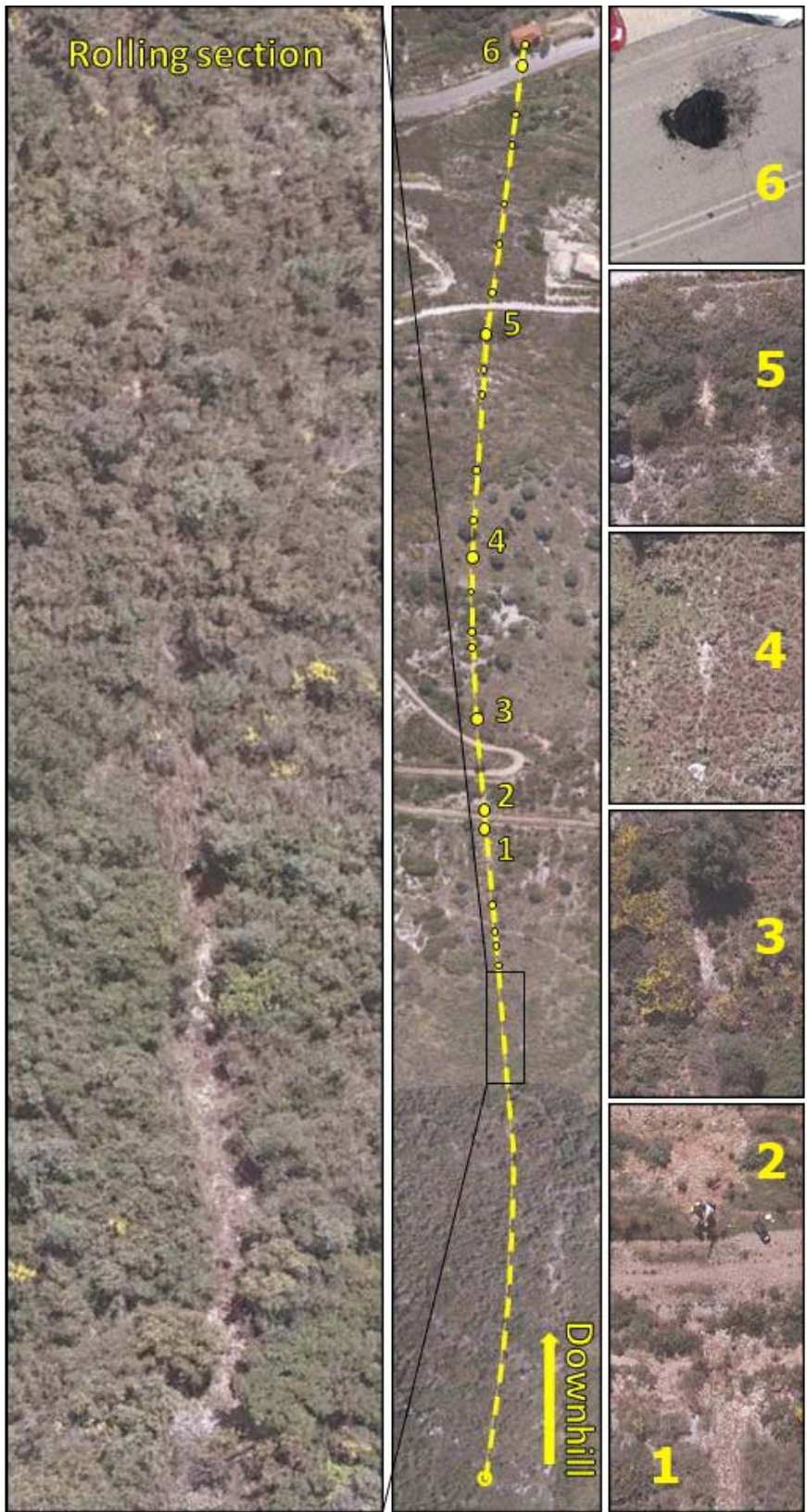


Figure 5. Top view orthophoto denoting rolling section, bouncing positions and indicative close-ups of impact points.

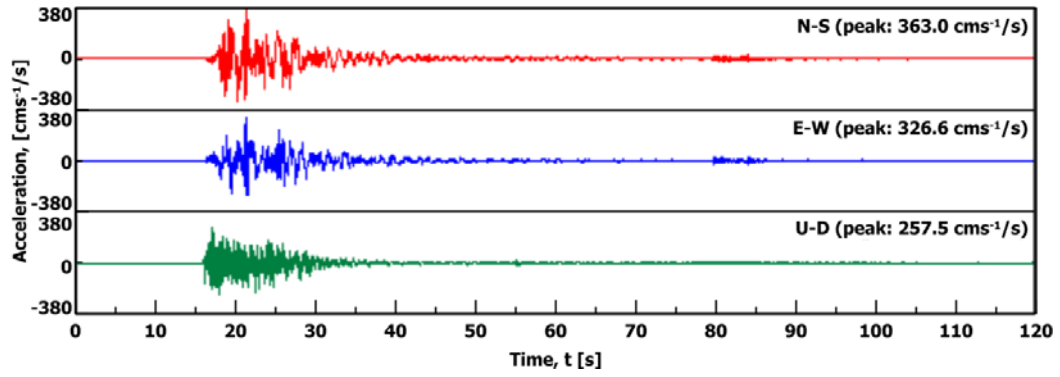


Figure 6. Acceleration recording at Vassiliki site (ITSAK, 2016)

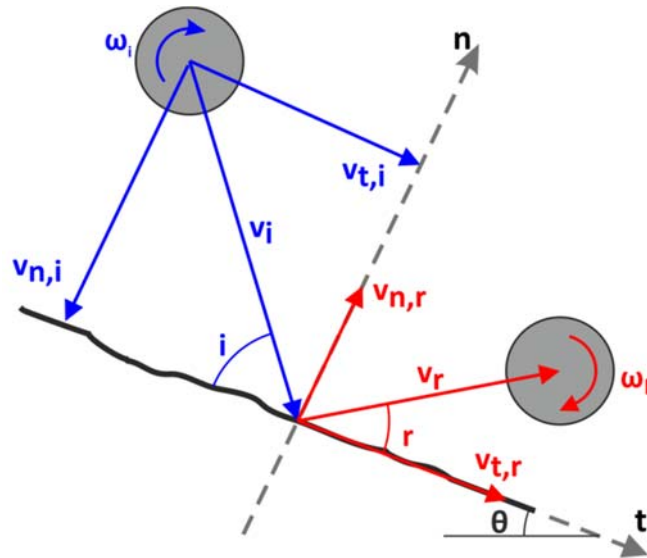


Figure 7. Coefficients of restitution

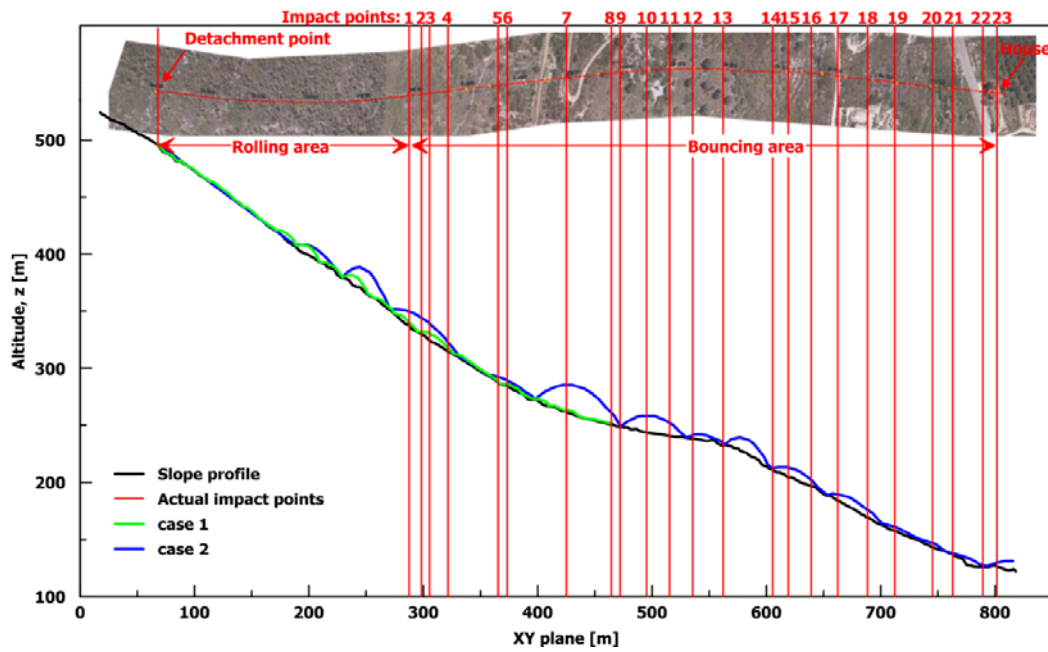


Figure 8. Plan view and cross section along block's path (units in m); 2D rockfall trajectory analysis results are plotted with green and blue line

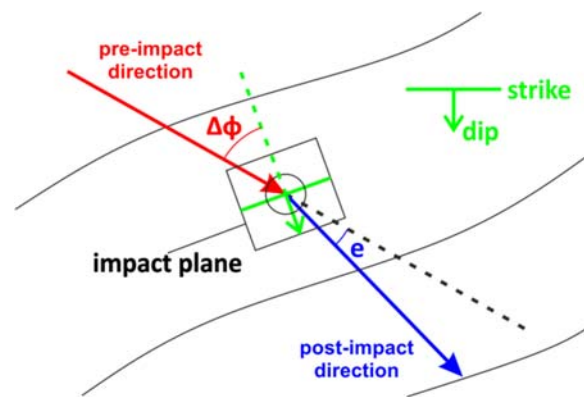


Figure 9 : Out of plane geometry

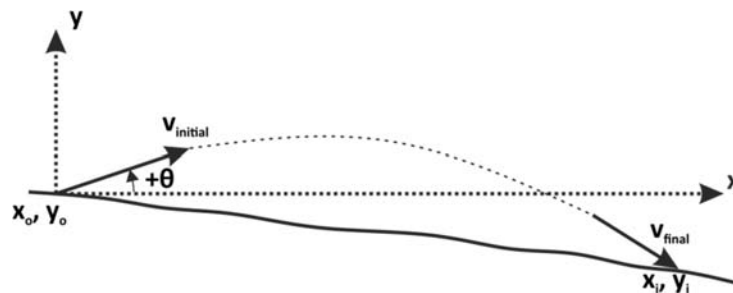


Figure 10. Parabolic segment



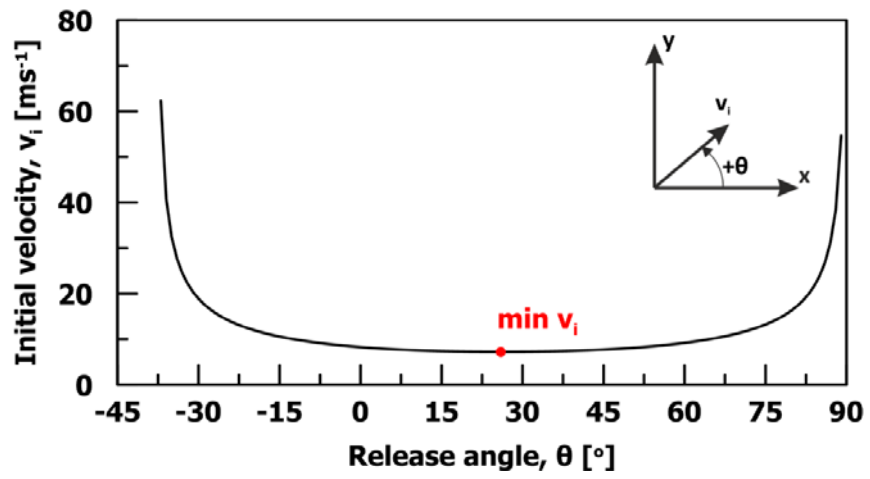


Figure 11. Release angle versus initial velocity for the first parabolic section ( $\delta x=10.75\text{m}$ ,  $\delta y=8.33\text{m}$ )

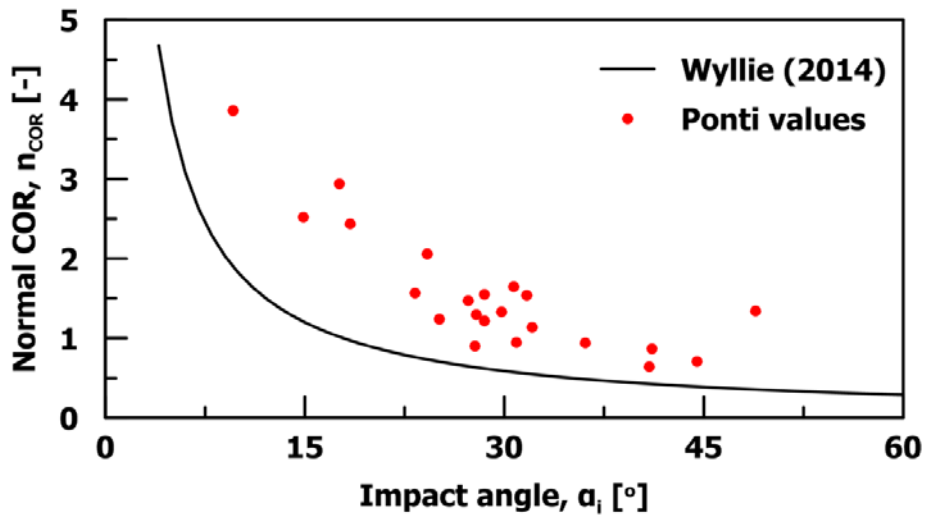
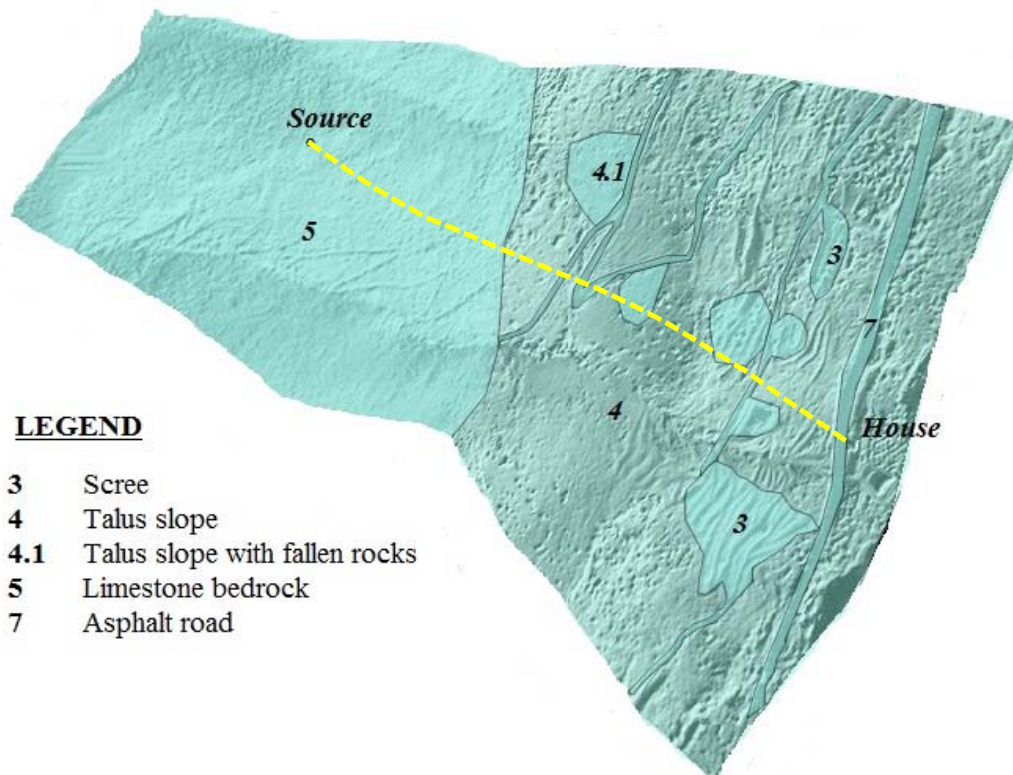


Figure 12. Normal COR versus impact angle



**LEGEND**

- 3 Scree
- 4 Talus slope
- 4.1 Talus slope with fallen rocks
- 5 Limestone bedrock
- 7 Asphalt road

Figure 13. Soil types for 3D rockfall analysis (according to Rockyfor3D). Yellow path of trajectory is 800 m.

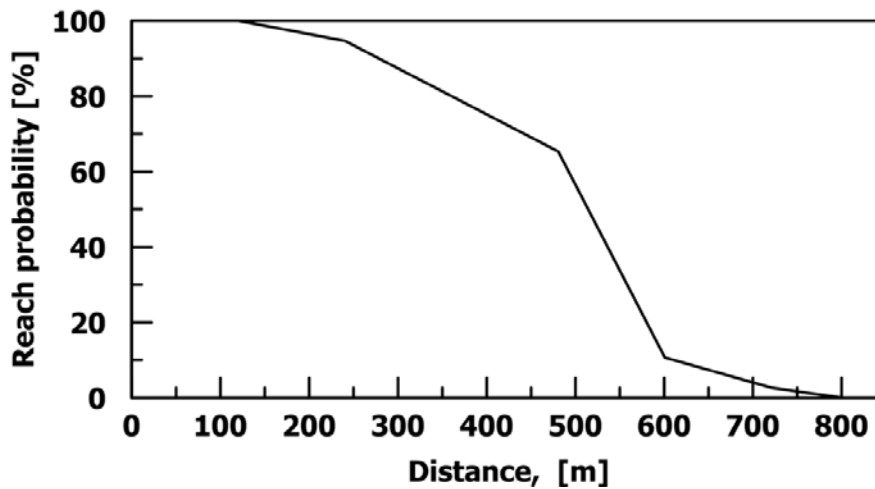


Figure 14. Reach probability graph calculated from 3D rockfall analysis

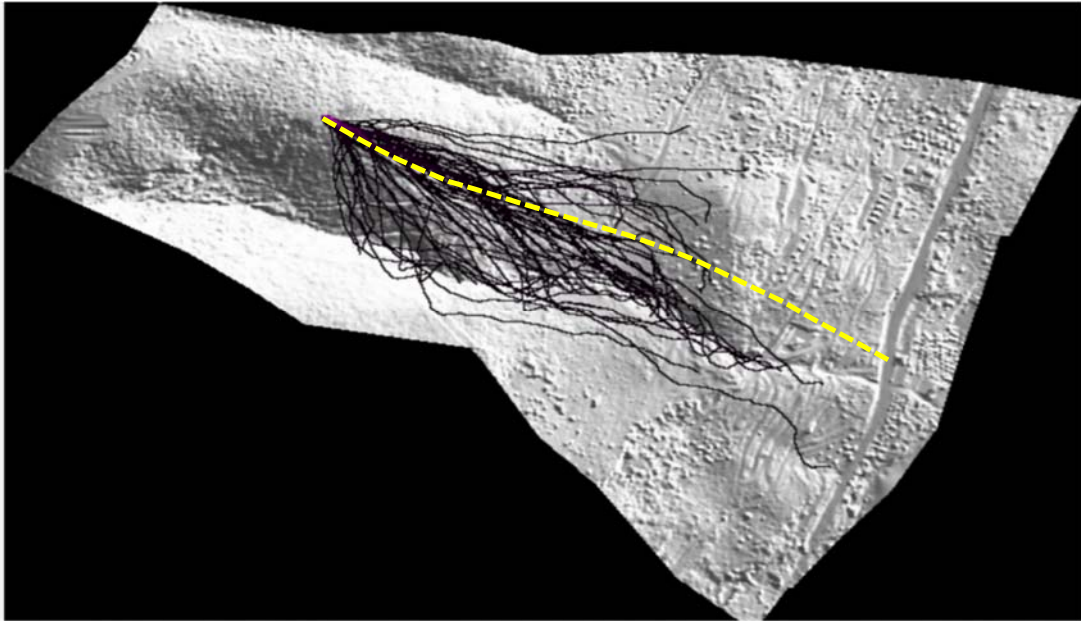


Figure 15. 3D trajectory analysis (from RockyFor3D analysis). Yellow line shows the actual trajectory. Black lines show the simulated trajectory.

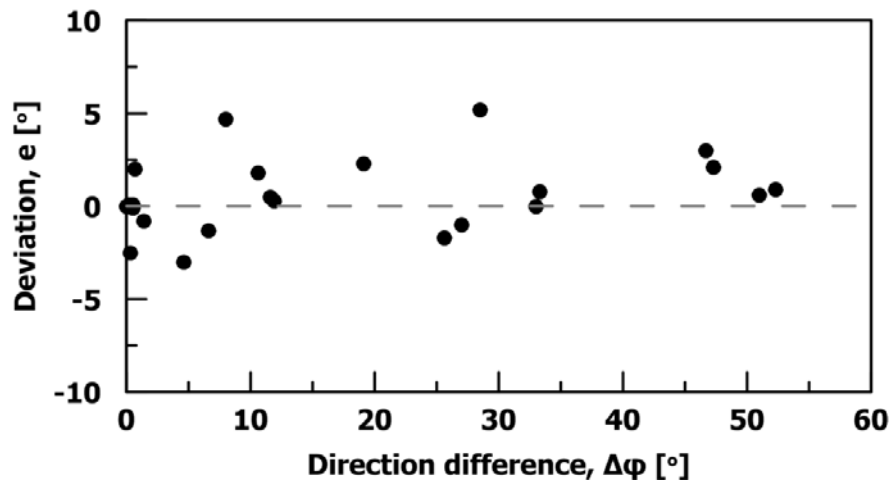


Figure 16. Deviation as a function of direction difference.