

Author's response to the Editor's comments

We thank the Editor for supervising the revision round and providing very useful comments. We thank also both Reviewers for their efforts in reviewing the last version of the manuscript.

We addressed the technical comment of the second Reviewer by including the suggested reference.

We agree with the Editor's suggestions and revise the introductory and the results part making the scope of the manuscript clearer. We underscore that the presented study (1) develops a methodology for fragility analysis of dikes due to liquefaction under seismic and hydraulic load, (2) presents a framework for dike failure probability calculation for joint occurrence of earthquake and flood accounting for their respective probabilities. The latter is demonstrated for an exemplary dike section at the middle Rhine River with the seismic load computed for the study area. We point out that the full-fledged flood and seismic multi-risk assessment goes beyond the scope of the presented study. The developed fragility curves form a basis for the subsequent multi-risk analysis, which would involve hydraulic modelling of the channel flow, dike breaching, flood inundation simulation and damage assessment.

We hope the provided modifications highlighted in the 'change-mode' make these points transparent. We believe that the presented methodology for liquefaction fragility calculation and failure probability qualifies as a self-consistent manuscript.

With kind regards,

Sergiy Vorogushyn on behalf of the co-authors

1 **Multi-hazard fragility analysis for fluvial dikes in earthquake and** 2 **flood prone areas**

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14 flood; Rhine; Cologne

15

16 **Abstract**

17 The paper presents a methodology for multi-hazard fragility analysis for fluvial
18 earthen dikes in earthquake and flood prone areas due to liquefaction. The
19 methodology has been applied for the area along the Rhine River reach and
20 adjacent floodplains between the gauges Andernach and Düsseldorf. Along this
21 domain, the urban areas are partly protected by dikes, which may be prone to failure
22 during exceptional floods and/or earthquakes. The fragility of the earthen dikes is
23 analyzed in terms of liquefaction potential characterized by the factor of safety
24 estimated with the use of the procedure of Seed and Idriss (1971). Uncertainties in
25 the geometrical and geotechnical dike parameters are considered in a Monte Carlo
26 simulation (MCS). Failure probability of the earthen structures is presented in the
27 form of a fragility surface—**s** as a function of both seismic hazard and
28 hydrological**al**/hydraulic load.

29

30 **Introduction**

31 Risk assessment in areas affected by several natural perils can be carried out in two
32 possible ways: on the one hand, one can consider different types of hazards and
33 risks independently, while on the other, possible interactions between hazards can
34 be taken into account. The former approach is based on traditional methods of
35 single-type hazard and risk assessment and represents a common practice. The
36 latter is used much more rarely, as it involves scenarios with obviously lower

37 occurrence probabilities, which might, therefore, be underrated and sometimes
38 unreasonably neglected. At the same time, the tragic lessons of past disasters show
39 that in multi-hazard prone areas the ~~risk of~~ losses from single hazardous events can
40 dramatically increase due to possible interactions between different types of hazards
41 and the occurrence of cascading effects. For instance, the devastating experience of
42 the Katrina Hurricane, 2005, and the Tohoku earthquake followed by a tsunami,
43 2011, sorely demonstrated that low occurrence probability events may result in
44 extremely high consequences. Therefore, the possible interactions between hazards
45 in multi-hazard prone areas should not be ignored in decision making.

46 The earlier multi-hazard studies were solely based on the comparison of single-type
47 hazard and risk assessments without considering interactions and potential
48 cascading effects (e.g., HAZUS-MH, 2003, KATARISK, 2003, Grünthal et al., 2006,
49 Fleming et al., 2016). In the recent years, frameworks for the assessment of the
50 interactions of multiple hazards have been developed (e.g., Marzocchi et al., 2012,
51 Selva, 2013, Mignan et al., 2014).

52 The present research work, which was undertaken ~~as part of the multi-hazard~~
53 ~~(earthquake flood) risk study implemented~~ in the frame of the EU FP7 project
54 MATRIX (New Multi-Hazard and Multi-Risk Assessment Methods for Europe)
55 focuses on the ~~problem of~~ multi-hazard fragility analysis of fluvial earthen dikes or
56 levees. In the presented paper, we develop the a methodology for the assessment
57 of fragility due to liquefaction by taking into account potential flood and earthquake
58 impacts on dikes at the Rhine reach around Cologne. The assessment of dike failure
59 probability is a prerequisite for subsequent flood-earthquake multi-risk assessment
60 studies.

61 The middle Rhine is regularly affected by flooding (e.g., Fink et al., 1996) and vast
62 floodplains are protected by dikes. The areas not protected by dikes are typically
63 behind concrete walls, ~~protected safeguarded~~ by mobile flood protection walls or are
64 located on elevated banks.

65 Besides flood hazard, the areas around Cologne are exposed to other types of
66 natural hazards, in particular windstorms (e.g., Hofherr and Kunz, 2010) and
67 earthquakes (Grünthal et al., 2009, Fleming et al., 2016). Although rarer than floods
68 or windstorms, earthquakes have a higher damage potential (Grünthal et al., 2006,
69 Fleming et al., 2016). In combination with high water levels, earthquake may lead to
70 liquefaction of saturated earthen dikes.

71 Dikes may fail due to various failure mechanisms induced either by high water levels
72 and/or earthquake impact (Armbruster-Veneti, 1999, Foster et al., 2000, Apel et al.,
73 2004, Allsop et al., 2007, Briaud et al., 2008, Wolff, 2008, Van Baars and Van
74 Kempen, 2009, Vorogushyn et al., 2009, Nagy, 2012, Huang et al., 2014). When
75 considering solely hydrologic/hydraulic load, overtopping is the most common failure
76 mechanism followed by piping and slope instability (see Vorogushyn et al., 2009 and

77 references therein). For these breach mechanisms, approaches for fragility analyses
78 have been proposed (Apel et al., 2004, Vorogushyn et al., 2009). Under earthquake
79 load, the liquefaction phenomenon is indicated as the most important cause of
80 ~~embankment dam~~dike failure (Ozkan, 1998).

81 Marcuson et al. (2007); reviewed the development of the state of practice in seismic
82 design and analysis of embankment dams or dikes, starting from the fundamental
83 publications of Newmark (1965) and Seed and Idriss (1971). Sasaki et al. (2004)
84 described empirical and analytical methods used in Japan for estimating the
85 settlement of dikes due to liquefaction, considering both the probable subsidence of
86 the bottom boundary and deformation of the dikes. Singh and Roy (2009) proposed
87 a correlation relationship for the earthquake-induced deformation of earthen
88 embankments based on the examination of 156 published case histories and using
89 the ratio of the peak horizontal ground acceleration and the yield acceleration as an
90 estimator.

91 In recent years, more sophisticated computer-based linear or non-linear methods for
92 seismic analyses of embankments have been developed, using one-, two- (Kishida
93 et al., 2009, Athanasopoulos-Zekkos and Seed, 2013) or three-dimensional (Wang
94 et al., 2013) models. At the same time, Kishida et al. (2009) concluded that simplified
95 models based on equivalent-linear analyses can provide reasonably accurate results
96 up to moderate ground shaking levels, while nonlinear analyses should be used to
97 evaluate dike responses at stronger shaking levels. We therefore focus on a
98 simplified approach, since we are concerned with the study on a regional spatial
99 scale in the areas of low to moderate seismicity.

100 Rosidi (2007) presented a seismic risk assessment procedure for earthen
101 ~~embankment dams and dikes~~levees, where dike fragility was expressed as a
102 function of earthquake-induced slope deformations. Considering different
103 strengthening scenarios, Rosidi (2007) estimated levee failure probabilities
104 depending on earthquake ground motion return period. However, possible fragility
105 changes due to flood-water elevation and dike core soil saturation was not taken into
106 account in that study.

107 For the purpose of single-type flood risk assessment, Apel et al. (2004) developed
108 fragility curves for overtopping failure based on Monte Carlo simulations.
109 Vorogushyn et al. (2009) extended this approach for piping and micro-instability
110 breach mechanisms based on the formulations of Sellmeijer (1989) and
111 Vrouwenvelder & Wubs (1985), respectively.

112 Recently, Schweckendiek et al. (2014) presented an approach to include field
113 observations in the Bayesian updating of piping failure probabilities of dikes in the
114 Netherlands. Krzhizhanovskaya et al. (2011) reported an integration of reliability
115 analysis for various breach mechanisms into a prototype flood early warning system,
116 including dike failure and associated inundation modelling. A summary of research

117 and practical methods for reliability assessment of levee systems considering
118 different failure mechanisms can be found in Wolff (2008).

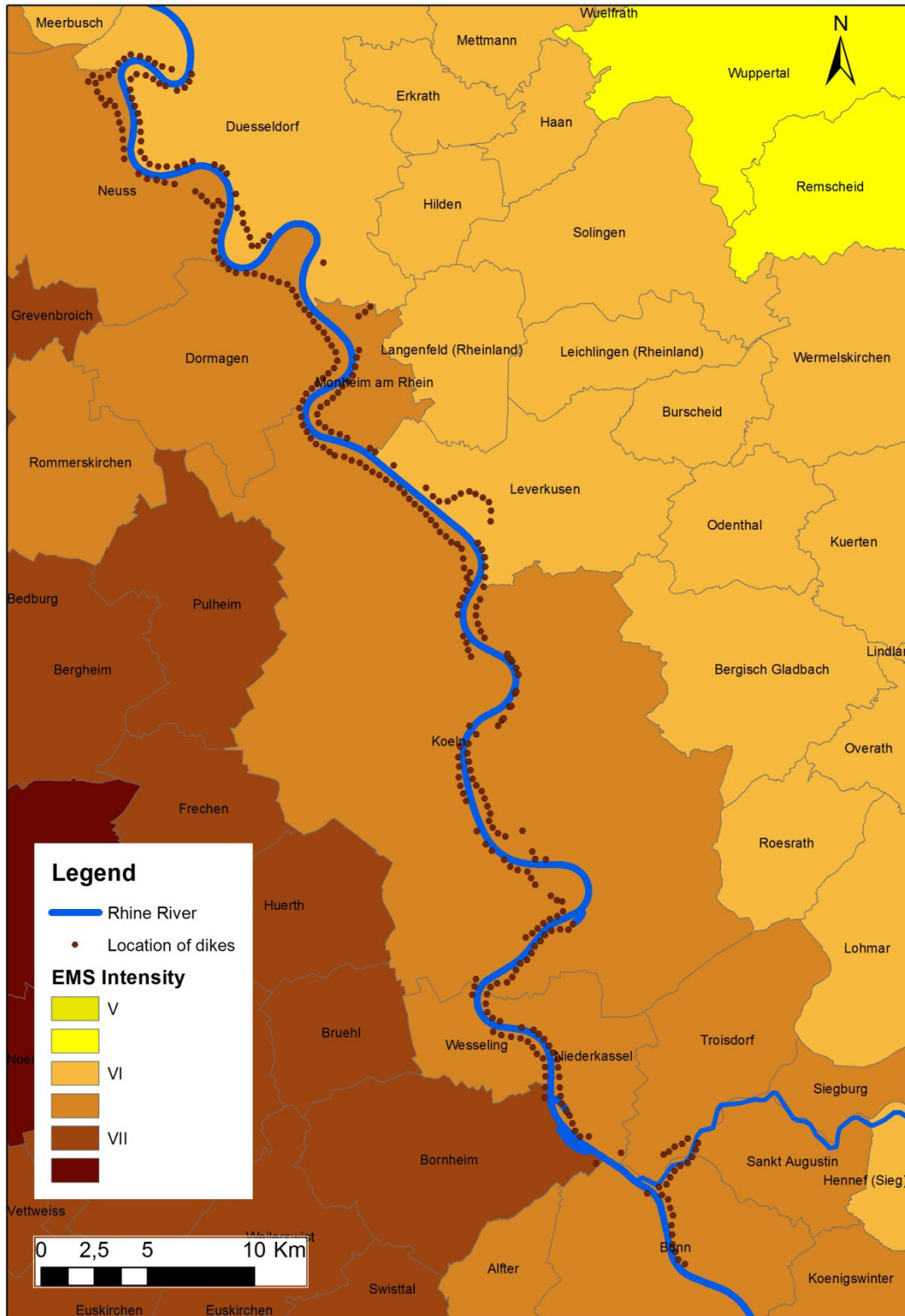
119 The reviewed studies, however, used a single-hazard approach focusing on either
120 earthquake or flood impacts on infrastructure. The present study aims at filling the
121 existing methodological gap considering both hazards together. The main goal of the
122 study is the development of a methodological approach for multi-hazard fragility
123 analyses and construction of multi-hazard fragility functions for dikes in the
124 earthquake and flood prone areas along the Rhine River. Extending the previous
125 studies, we consider here another possible failure mechanism – earthquake-
126 triggered physical damage to earthen dikes due to liquefaction. This type of
127 phenomena may occur in earthquake prone areas, where water-saturated sandy
128 soils have the potential to liquefy when subjected to seismic vibrations. –These
129 Fragility functions are meant to be incorporated into the regional flood hazard and
130 risk assessment models (e.g. Vorogushyn et al., 2010). In this way, small-scale
131 breaching process knowledge (e.g. Rifai et al., 2017) can be integrated into regional-
132 scale risk analyses. These analyses go beyond the scope of the presented paper
133 and will be elaborated in a following study.

134 ~~The existing regional Inundation Hazard Assessment Model IHAM (Vorogushyn et~~
135 ~~al., 2010) considers three breach mechanisms: overtopping, piping and micro-~~
136 ~~instability of the dike slope. More details on the parameterization of these breach~~
137 ~~mechanisms and the development of respective fragility functions are given in Apel~~
138 ~~et al. (2004) and Vorogushyn et al. (2009). Here we consider another possible failure~~
139 ~~mechanism — earthquake triggered physical damage to earthen dikes due to~~
140 ~~liquefaction. This type of phenomena may occur in earthquake prone areas, where~~
141 ~~water-saturated sandy soils have the potential to liquefy when subjected to seismic~~
142 ~~vibrations. During liquefaction, when as a consequence of increased pore water~~
143 ~~pressure the strength of bonds between soil particles is drastically reduced to~~
144 ~~essentially zero, soil deposits may lose their bearing capacity and behave as fluids~~
145 ~~(Kramer, 1996, Idriss and Boulanger, 2008). In our study, we assume that the~~
146 ~~liquefaction occurrence in the dike body may result in the subsidence of the core as~~
147 ~~well as in large slope deformations. The subsequent breach of the affected dike~~
148 ~~section is the resulting consequence.~~

149 ~~The area under study, along with the communities at risk and location of dikes along~~
150 ~~the Rhine River, is presented in Fig. 1, where the points correspond to the geometric~~
151 ~~centres of the dike sections of about 500-600m length. Fig.1 shows the~~
152 ~~administrative boundaries (communities) as well as the general zonation of the~~
153 ~~seismic hazard. The shown hazard estimates are based on the earlier map by~~
154 ~~Grünthal et al. (1998) in terms of EMS intensities for an exceedance probability of~~
155 ~~10% in 50 years, and are referred to the centres of communities (Tyagunov et al.,~~
156 ~~2006a). The accurate seismic hazard estimates for all dikes locations will be~~
157 ~~calculated below.~~

158 Data and Method

159 The area under study, along with, the communities at risk and location of dikes along
160 the Rhine River, ~~is~~are presented in Fig. 1, where the points correspond to the
161 geometric centres of the dike sections of about 500-600m length. Fig.1 shows the
162 administrative boundaries (communities) as well as the general zonation of the
163 seismic hazard. The ~~shown~~depicted hazard estimates are based on the earlier map
164 by Grünthal et al. (1998) in terms of EMS intensities for an exceedance probability of
165 10% in 50 years, and are referred to the centres of communities (Tyagunov et al.,
166 2006a). The accurate seismic hazard estimates for all dikes locations will be
167 calculated below.



168

169 Figure 1: Location of flood protection dikes along the Rhine and the spatial
 170 distribution of seismic hazard in the study area in terms of EMS intensities for an
 171 exceedance probability of 10% in 50 years (Grünthal et al., 1998).

172 During liquefaction, when as a consequence because of increased pore water
 173 pressure the strength of bonds between soil particles is drastically reduced to

174 essentially zero, soil deposits may lose their bearing capacity and behave as fluids
 175 (Kramer, 1996, Idriss and Boulanger, 2008). In our study, we assume that the
 176 liquefaction occurrence in the dike body may result in the subsidence of the core as
 177 well as in large slope deformations. The subsequent breach of the affected dike
 178 section is the resulting consequence.

179 The probability of a dike failure is considered in terms of liquefaction potential,
 180 estimated using the method of Seed and Idriss (1971). The liquefaction potential can
 181 be assessed with a factor of safety (FS) against liquefaction, which is determined as
 182 the ratio of the capacity of the soil to resist liquefaction (CRR: Cyclic Resistance
 183 Ratio) and the seismic demand placed on the soil layer (CSR: Cyclic Stress Ratio).

184 The CSR value can be estimated using the following expression:

185

$$186 \quad CSR = 0.65 \cdot \frac{a_{max}}{g} \cdot \frac{\sigma_{vo}}{\sigma'_{vo}} \cdot r_d , \quad (1)$$

187

188 where a_{max} is the horizontal peak ground acceleration (PGA), g is the gravitational
 189 acceleration, σ_{vo} and σ'_{vo} are the total and effective overburden stresses (pressure
 190 imposed by above layers) of the soil, respectively, and r_d is a stress reduction factor
 191 that depends on the depth. For the calculation of the vertical stresses as a function
 192 of depth, we also consider the variations in the water level in the river, which
 193 influences the phreatic surface and degree of saturation in the dike core.

194 As for the CRR value, there are different methods for estimating the soil resistance
 195 to liquefaction (Youd et al., 2001, Kramer and Mayfield, 2007). Probably the most
 196 common is the method based on standard penetration testing (SPT). In our study,
 197 due to the lack of SPT data, we use an approach based on the correlation between
 198 penetration resistance and the angle of internal friction for sandy soils (Table 1,
 199 Peck, 1974).

200 Table 1: Relationship between the angle of internal friction and SPT-values (Peck,
 201 1974)

SPT, N-Value	Density of sand	ϕ (degrees)
<4	Very loose	<29
4 – 10	Loose	29 - 30
10 – 30	Medium	30 - 36
30 – 50	Dense	36 - 41

>50	Very dense	>41
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202

203 In addition to the friction angle, for modelling the bearing capacity of earthen dikes,
 204 we also consider other geotechnical parameters such as specific weight, porosity
 205 and fines content. Statistical information about the characteristics of dikes used for
 206 liquefaction analysis is presented in Table 2. The typical values for the specific
 207 weight and friction angle found in dikes were taken from Vorogushyn et al. (2009)
 208 and the references therein. The fines content values are adapted from a dike at the
 209 Rhine River in the Netherlands (Van Duinen, 2013).

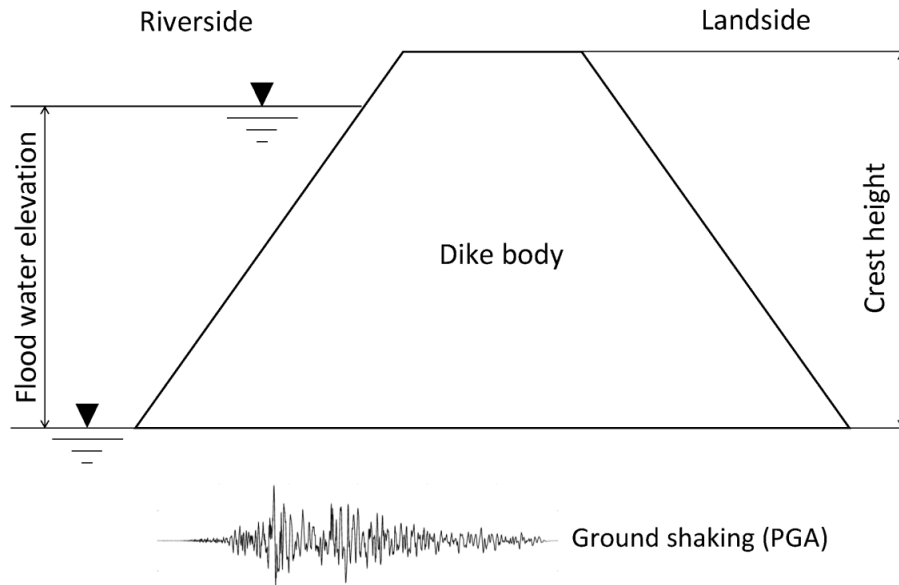
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211 Table 2: Geotechnical parameters of dikes adopted in this study

Soil properties	Mean	Standard deviation	Minimum	Maximum
Specific weight γ (kN/m ³)	18	1	13	21
Friction angle ϕ	29.2	0.3	20.8	37.6
Fines content FC (%)	5	1	3	11

212

213 The performance of dikes under seismic ground-motion loading is analyzed using a
 214 simplified one-dimensional model assuming that below the water level the soil is in a
 215 saturated state. Hence, the phreatic line within the dike body is assumed to be
 216 horizontal (obviously, this is a conservative assumption that presumes the sufficiently
 217 long duration of the flood water rise or impoundment). A cross-section of the generic
 218 dike model is shown in Fig. 2.



219

220 Figure 2: Generic dike model to illustrate the earthquake-flood-dike interaction

221

222 For the development of dike fragility curves, we assume a generic dike height of 5
 223 meters. When integrated into the dynamic flood-earthquake hazard model, the actual
 224 dike height and corresponding water level need to be taken into account.

225 In the computational algorithm, the material properties of dikes are assumed to be
 226 homogeneously distributed throughout the cross-section of the dike core. However,
 227 they can vary spatially along the river, from one cross-section to another, keeping in
 228 mind the range of existing uncertainties of the geotechnical parameters as specified
 229 in Table 2.

230 For quantifying the liquefaction potential, the values of CSR (reflecting the level of
 231 seismic ground shaking) and CRR (depending on the dike material properties and
 232 the water level) are calculated for all points of the dike cross-section from the crest to
 233 the bottom (with a discretization interval of 5 cm). Once both the CSR and CRR
 234 values have been determined at a certain point under certain load conditions, we can
 235 calculate the factor of safety against liquefaction (FS) employing the relationship
 236 (Seed and Idriss, 1971):

$$237 \quad FS = \frac{CRR}{CSR} \quad (2)$$

238

239 At the points where the loading (CSR) exceeds the resistance (CRR), i.e., the factor
 240 of safety is below 1, one can expect the initiation of liquefaction that can lead to the
 241 functional failure. In this study, we neither analyze the degree of soil deformations
 242 caused by liquefaction nor consider the variety of possible failure states of the

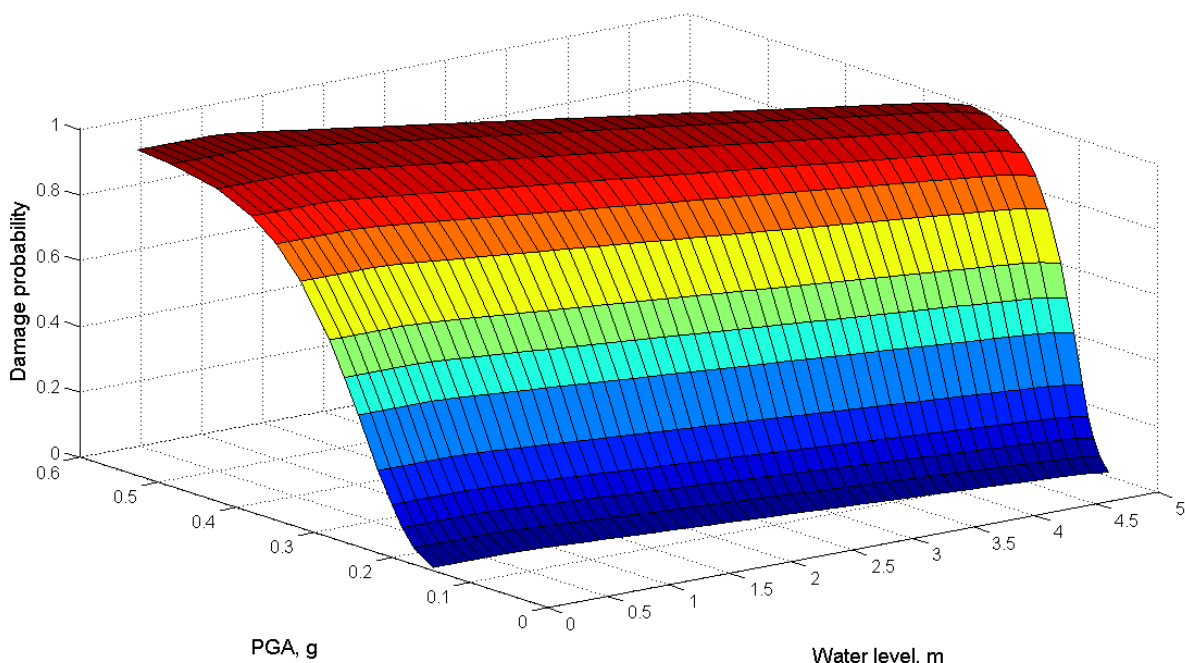
243 affected structure. Instead, we conservatively assume that the initiation of
 244 liquefaction ($FS \leq 1$) in any point throughout the dike body corresponds to the failure
 245 (loss of function) of the dike.

246 Computations of the liquefaction potential are done in a Monte-Carlo simulation
 247 (MCS) considering the variability (uncertainty) of the geotechnical parameters of the
 248 dikes (Table 2). Based on a frequency analysis of the MCS results, dike failure
 249 probabilities are computed for different points of the discretized two-dimensional load
 250 space, considering possible combinations of peak ground acceleration and flood
 251 water level.

252

253 **Fragility surface**

254 In the single hazard fragility analysis, the failure probability is expressed as a
 255 function of single hazard load parameter(s). In a multi-hazard fragility analysis the
 256 response of the structure is described as a function of multiple-hazard load
 257 parameters. Thus, in our case the calculated fragility results are presented in the
 258 three-dimensional form with seismic and hydraulic load described by peak ground
 259 acceleration and water level, respectively (Fig. 3). The fragility surface represents
 260 the conditional failure probability given the combination of load.



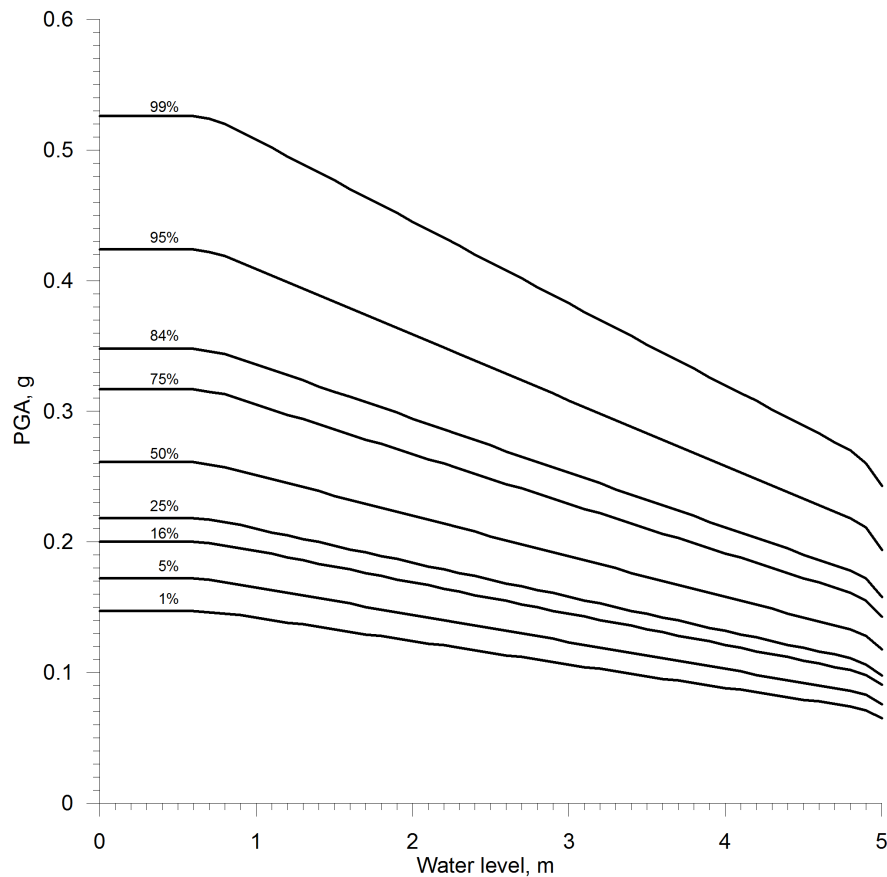
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262 Figure 3: Multi-hazard fragility surface for liquefaction failure of a dike.

263

264 The fragility surface can be interpreted as a set of iso-lines corresponding to different
 265 percentiles of the calculated distribution of the FS values, as shown in Fig. 4. The

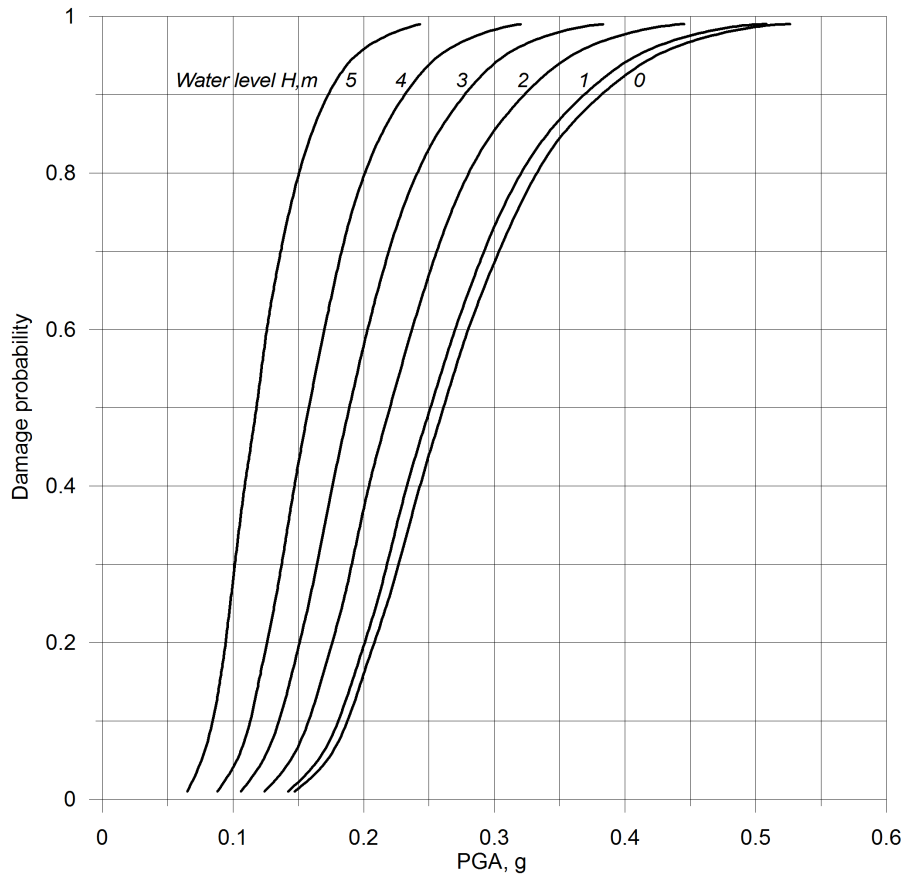
266 presented iso-lines correspond to the occurrence of the limit state ($FS = 1$) and
 267 specify the failure probabilities in the two-dimensional space of hazards (in units of
 268 PGA and flood water level).-



269

270 Figure 4: Dike failure probability in the PGA and water level space

271 It becomes apparent that liquefaction failure can be initiated already at small water
 272 levels given sufficient earthquake load. On the other turn, a certain degree of
 273 shaking is required for liquefaction failure even at the maximum water levels (Fig. 4).
 274 The estimated PGA threshold ranges from 0.15 g to 0.54 g for the interval from 1 to
 275 99 percentiles. When the flood water rises up to about 0.7 - 0.8 m, it has no visible
 276 effect on the PGA threshold, while further increases in water levels lead to a
 277 considerable shift towards lower PGA values and this change is linear. When the
 278 water level reaches the top of the structure, the threshold PGA values and the
 279 liquefaction occurrence probabilities change significantly. In comparison with the
 280 initial state (water level at the toe of the dike), the PGA threshold values decrease to
 281 between 0.07 - 0.24 g (for the interval from 1 to 99 percentiles). Comparing the two
 282 extreme cases, the liquefaction triggering PGA threshold values decrease more than
 283 half and the spread of the values becomes narrower. Water level is thus a
 284 considerable factor determining the dike core moisture content and liquefaction
 285 failure.



286

287 Figure 5: Fragility functions for earthen dikes for different water levels ranging from
 288 dike toe to assumed crest height.

289

290 The developed dike fragility model may find practical application in regions of low to
 291 moderate seismicity. For the lower PGA values (0.15 - 0.30 g) the contribution of the
 292 effect of impoundment can be more critical than for the higher PGA, when
 293 earthquake ground shaking is sufficiently strong to trigger liquefaction under
 294 conditions without extra-flooding (Fig.5). It should be stressed here that presented
 295 fragility curves represent the conservative estimates due to the assumption of full
 296 saturation of a dike core below the water level. In practice, some time is however
 297 required for the development of the phreatic line. More sophisticated dynamic
 298 models considering the degree of soil saturation can be adapted in future to adjust
 299 failure probability estimates.

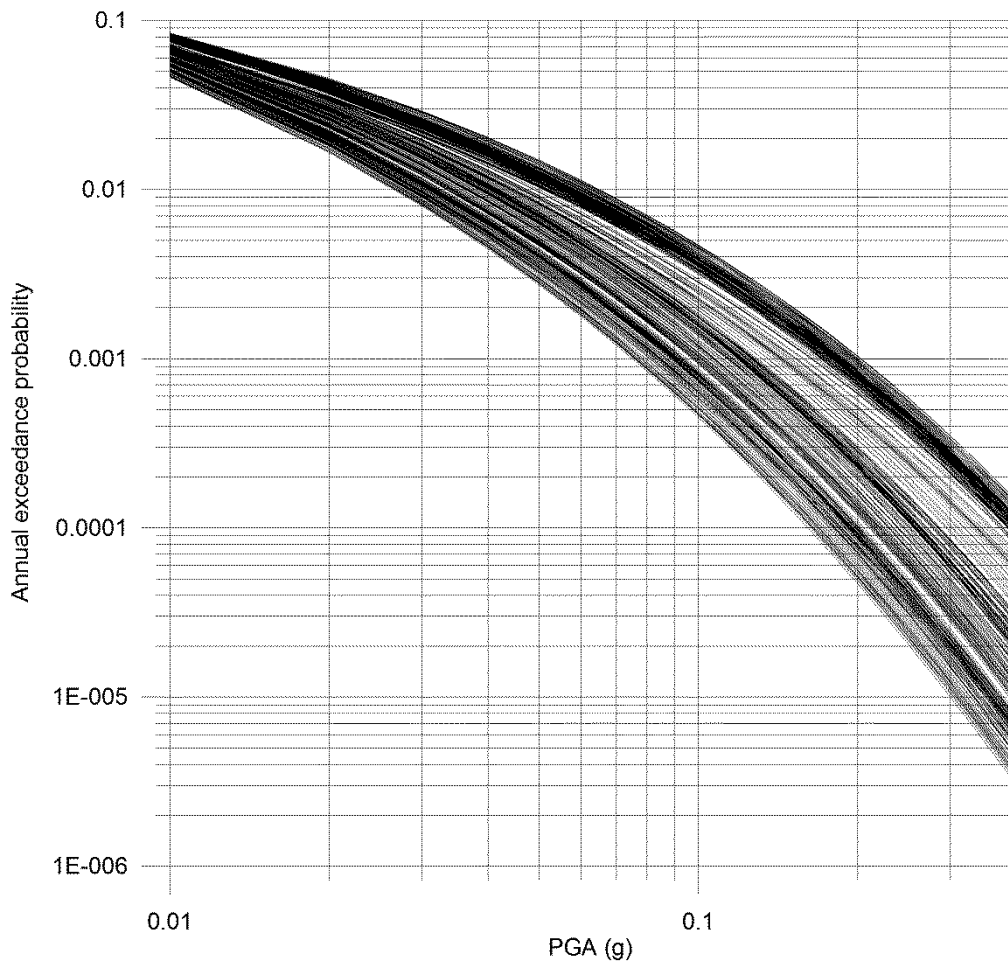
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301 **Dike failure probability assessment**

302 To estimate the actual failure probability of a dike in the area of interest, the
 303 developed multi-hazard fragility functions should be combined with the probabilistic
 304 hazard estimates of earthquake and flood considering their respective return period
 305 values.

306 The developed fragility curves are intended to be used in a subsequent multi-risk
307 analysis study along the Rhine River reach between Andernach (Rhine-km 613.8)
308 and Düsseldorf (Rhine-km 744.2) considering flood scenarios with return periods
309 between 20 and 1000 years. In particular, the effect of multi-hazard is expected to
310 manifest for flood return periods below the dike design level (200-year return period
311 on the middle Rhine). In the single-type flood hazard analysis, only piping failure
312 could possibly impact dikes below design level, whereas multi-hazard consideration
313 would slightly increase the probability of failure if the occurrence of earthquakes and
314 subsequent liquefaction is taken into account. The effect of multi-hazard
315 consideration on total risk is expected to decrease with increasing flood return period
316 beyond design level since dikes would fail (in most cases) due to overtopping
317 anyway. A full multi-risk assessment considering dike failures among others due to
318 liquefaction is beyond the scope of the presented study. Hereafter, we illustrate a
319 framework, how to integrate seismic and hydraulic load for the calculation of the
320 multi-hazard failure probability and demonstrate this with one example of a selected
321 dike section.

322 The seismic hazard calculations were ~~implemented~~ accomplished for all locations at
323 the center points of dike segments on both sides of the Rhine River reach (Fig. 1).
324 The input data for the seismic hazard analyses were taken in accordance with the
325 regional model of Grünthal et al. (2010). The hazard calculations were ~~implemented~~
326 carried out using the GEM (Global Earthquake Model) OpenQuake software
327 (Crowley et al., 2011a, b) for soil sites characterized by 300 m/s shear wave (S-
328 wave) velocity in the uppermost 30 m, which was assigned considering the results of
329 previous seismological studies in the area (Tyagunov et al., 2006b, Parolai et al.,
330 2007). Note that amongst the waves generated by an earthquake, the S-wave, that
331 are those for which the motion is perpendicular to the direction of wave propagation
332 are expected to determine the largest impact on the building structures. Their
333 variations in the velocity of propagation, accounted in the calculation, are used as a
334 proxy to estimate the spatial differences in the amplitude of shaking. The set of
335 calculated seismic hazard curves in terms of PGA characterize the range of probable
336 level of ground shaking for the different dike locations is shown in Fig. 6. In total,
337 339 dike sections are analysed: 157 of them are on the left side and 182 on the right side
338 of the river.



339

340 Figure 6: Seismic hazard (mean) curves for the locations of the dikes along the
 341 Rhine River. Each curve corresponds to one dike segment.

342 The calculated PGA values vary in space for different points along the river stretch
 343 and the level of ground shaking depends on the return period of interest. Thus, for
 344 the level of exceedance probability of 10% in 50 years, which is the common
 345 standard in the practice of earthquake engineering and corresponds to an average
 346 return period of 475 years, the PGA estimates vary over a range of about 0.06 – 0.15
 347 g. For a shorter return period of 100 years, PGA varies in the range of about 0.03 –
 348 0.06 g, whereas for a longer return period of 1000 years the range is about 0.08 –
 349 0.20 g. Note, however, that for the return periods longer than 1000 years, even
 350 higher levels of ground shaking are probable in the area and such low probability
 351 phenomena cannot be ruled out.

352 The spread in the calculated PGA values is not very large, because the course of the
 353 Rhine River and corresponding dikes closely follows the shape of the seismic hazard
 354 zones around Cologne (Grünthal et al., 1998, DIN 4149, 2005). Therefore, the
 355 seismic hazard distribution in the area under study (Fig. 1) appears rather uniform.

356 ~~On the basis of~~Based on the obtained results and referring to the liquefaction
 357 susceptibility categorization for different soil types (Youd and Perkins, 1978, HAZUS-

358 MH, 2003), one can make a qualitative conclusion that in this area, there is a risk of
 359 dike ~~damage–failure~~ due to liquefaction induced by seismic ground shaking.
 360 According to observations from past earthquakes (Sasaki et al., 2004) seismic
 361 ~~impact~~ damage to river dikes can be triggered by PGA of 0.16 g or higher. There is
 362 even evidence that the PGA threshold for liquefaction occurrence can be even less
 363 than 0.10 g (Santucci de Magistries et al., 2013, Quigley et al., 2013).

364 The actual dike failure probabilities can be quantified by considering the probabilities
 365 of occurrence of the earthquake ground shaking level and flood return periods at
 366 different dike locations combined with the presented fragility curves. The
 367 simultaneous occurrence of a flood and an earthquake should be assumed. The
 368 typical duration of a flood wave of 30 days is considered for the Rhine. It is assumed
 369 that no dike repair actions are undertaken in this period, which may affect the
 370 probability of failure. Thus, the earthquake probability is computed for this period to
 371 be combined in the following expression to determine the actual failure probability

372

$$373 \quad P(F) = \iint P(F|S_i^{30}, W_j) * P(S_i^{30}) * P(W_j) dSdW, \quad (3)$$

374

375 where $P(F|S_i^{30}, W_j)$ is the conditional failure probability given the combination of
 376 the seismic ground shaking S_i^{30} within a time window of 30 days and the water level
 377 W_j ;

378 $P(S_i^{30})$ is the probability of occurrence of the seismic input S (peak ground
 379 acceleration) of the level i within a time window of 30 days;

380 $P(W_j)$ is the probability that the water level W corresponds to the level j .

381 The first factor in the integral represents the conditional failure probabilities, which
 382 can be obtained from the multi-hazard fragility surface (Fig. 3), while the second and
 383 third ones represent probabilistic estimates of the seismic (PGA level) and flood
 384 hazard (water level) at the dike locations and can be obtained from the
 385 corresponding hazard curves.

386 For the situation without flooding by combining the seismic hazard curves (Fig. 6)
 387 with the fragility curve corresponding to the water level of 0 m (Fig. 5), the
 388 earthquake-triggered liquefaction may occur at some of the considered dike
 389 locations though the probability is not very high. The probability varies in this case
 390 within the range of $1 - 4 \cdot 10^{-5}$ per year.

391 The current design criteria of fluvial dikes take into account only flood hazard and do
 392 not consider potential multi-hazard impact. Therefore, in case of ~~probable–potential~~
 393 temporal coincidence of flooding and strong earthquakes, dike protection structures

394 may fail due to liquefaction at flood return periods below the design level. This may
395 lead to perplexity and negatively affect population, infrastructure, and flood
396 response, requiring emergency actions.

397 A comprehensive quantitative risk analysis considering the joint probability of seismic
398 and flood events and their– interactions in time and space requires continuous
399 hydraulic model and multi-hazard integration. This goes beyond the scope of
400 presented research and will be a subject of a subsequent study. Here, for the
401 illustration purpose, we present an example for estimation of the failure probability
402 for a specific dike section considering previously computed seismic and hydraulic
403 load.

404 For a left-side dike section at Rhine-km 668 near the town Wesseling (south to the
405 city of Cologne, Fig.1), the average maximum water levels were estimated for three
406 return periods 200, 500 and 1000 years, using a dynamic probabilistic-deterministic
407 coupled 1D-2D model (Vorogushyn et al., 2010) setup for the study area at the
408 Rhine River within the EU-FP7 MATRIX project (Garcia-Aristizabal and Marzocchi,
409 2013). The hydraulic model uses the flow records at gauge Andernach (Rhine-km
410 613.8) for estimation of hydrographs and corresponding return periods. Hydrographs
411 are then routed with a coupled 1D-2D model considering dike breaches and
412 associated inundation. The estimated water levels at the selected location are: for
413 the 200-year return period ($p=0.005$ per year) 50.38 m asl (above sea level); for 500-
414 year ($p=0.002$) and 1000-year ($p=0.001$) 50.49 m and 50.52 m asl, correspondingly.

415 Assuming the height of the dike of 5 metres at the selected location, the dike would
416 be impounded by 4.50 metres during a 200-year flood event. Correspondingly, the
417 estimated impoundment level would reach 4.61 m for the 500-year and 4.64 m for
418 the 1000-year flood scenarios. The small difference between the calculated
419 estimates can be explained, in particular, by the used model, which considers dike
420 breaches upstream, i.e. the water level at one dike location depends on performance
421 of other dike sections (e.g., if one of the upstream dikes fails, the water outflow
422 would reduce the flood loads on the other dike sections).

423 Combining the flood hazard estimates with seismic hazard curves and fragility
424 function for the point of interest, the probability of liquefaction at Wesseling without
425 flooding is about $3.9 \cdot 10^{-5}$ per year. Applying Eq. 3, we obtain for the 200-year flood
426 scenario the liquefaction failure probability of $1 \cdot 10^{-6}$ per year, for the 500-year flood –
427 about $4.1 \cdot 10^{-7}$ per year and for the 1000-year flood – about $2.1 \cdot 10^{-7}$ per year. All
428 these return period scenarios contribute to the total risk value. Consequently, it is
429 expected that the multi-hazard interaction scenarios essentially increase the total risk
430 level in comparison with the estimated single hazard risk level though the combined
431 probabilities of earthquake and floods are very small.

432 Nevertheless, dike failures due to liquefaction in case of a multi-hazard impact bears
433 the potential of surprise and malign consequences, which should be considered in a

434 comprehensive risk assessment (Merz et al., 2015). In particular, under hydraulic
 435 load below the (hydraulic) design level (< 200-year return period at the German
 436 Rhine reach), dikes might be considered predominantly safe in a single-type hazard
 437 analysis, whereas the occurrence of liquefaction would dramatically change flood
 438 inundation patterns and loss distribution. Though not necessarily extreme, but still
 439 significantly strong floods and ‘unexpected’ dike failures in combination may still
 440 harmfully affect the densely populated areas with high asset concentration such as
 441 floodplains along the Rhine. Hence, a quantitative multi-risk analysis is advocated in
 442 earthquake and flood prone areas considering the effect of dike liquefaction despite
 443 a relatively small probability of the joint occurrence of both perils.

444

445 Conclusions

446 A methodology for multi-hazard fragility and failure probability analyses of fluvial
 447 dikes in earthquake and flood prone areas is presented. ~~The system of flood~~
 448 ~~protection dikes along the Rhine River in the area around Cologne is analysed,~~
 449 ~~considering their possible failures due to liquefaction induced by seismic ground~~
 450 ~~shaking in combination with flooding. We conservatively assume the initiation of~~
 451 ~~liquefaction at any point throughout the dike body leads to the dike failure.~~ The failure
 452 probability is presented as described by a three-dimensional fragility surface as a
 453 function of both earthquake ground shaking (PGA) and flood water level
 454 (impoundment of the dike). Quantitative fragility analysis shows that a rise in flood
 455 water level reduces the liquefaction triggering PGA threshold due to high moisture
 456 content in the dike core. When considering earthquake and flood hazard and the
 457 developed fragility curves, the non-zero liquefaction probability for an exemplary dike
 458 location becomes evident.

459 A framework for the multi-hazard calculation of dike failure probability due to seismic
 460 shaking and hydraulic load was presented and exemplified for ~~the system of flood~~
 461 protection dikes along the Rhine River in the area around Cologne. ~~is analysed,~~
 462 ~~considering their possible failures due to liquefaction induced by seismic ground~~
 463 ~~shaking in combination with flooding. We conservatively assume the initiation of~~
 464 ~~liquefaction at any point throughout the dike body leads to the dike failure.~~ Though
 465 the probability of joint occurrence of both perils is rather low, we argue that such
 466 incidents bear a high potential of surprise with substantial negative consequences.
 467 The latter can be, however, avoided by multi-risk considerations and awareness at
 468 civil protection authorities and within the public.

469 The developed fragility curves for liquefaction will be used for comprehensive multi-
 470 risk assessment study along the Rhine River in a subsequent work. This will take
 471 into—the interaction of earthquake and flood hazards into account, dynamic
 472 inundation effects and damage modelling.

473

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478

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