We feel very grateful to the reviewer who has given us the valuable suggestions and comments for our paper. We have revised our manuscript accordingly.

Huayong Chen

Responses to the reviewer' comments:

Co	mments of Anonymous Referee #1:	Author's Reply		
1.	0.1, line 2 not sure, if "downriver of a check Thanks very much for the reviewer's			
	dam" would better describe the exact location	ment. The phrase "behind a check dam" has		
	of the scour.	been replaced by "downriver of a check dam"		
		for better description of the exact scour loca-		
		tion.		
2.	p.1, line 11 in cases where debris flow is used	A hyphen was added between debris and flow		
	in a word composition (e.g. debris-flow pat-	in a sentence throughout the manuscript		
	tern, debris-flow nappe) I learned, that there is	where "debris flow" was used as attributive.		
	a hyphen between debris and flow Please			
	check the manuscript accordingly.			
3.	p.2, line 29 more common is "initiation zone",	The wrong phrases in the sentence have been		
	not "formation region"; delete "by debris flow"	revised according to the reviewer's com-		
	at the end of the sentence, it's an unnecessary	ments.		
	repetition.			
4.	p.3, line 56/57 not really clear, what this sen-	To avoid misunderstanding, the sentence has		
	tence means. Do you mean that the proposed	been modified in the manuscript.		
	geometry of such spillways is something that			
	should be used especcially for torrents with			
	high sediment disposability?			
5.	p.3, line 58 "is" instead of "was".	The word "was" has been replaced by "is" in		
		this sentence.		
6.	p.8, line 165 are the values for the density of	The flow densities were measured after de-		
	the debris-flow densities measured values or	bris-flow samples were taken. Frankly, as for		
	assumptions? Both values seems to me more	debris flows the flow density in our experi-		
	valid for hyperconcentrated flows. I would	ments seems lower. The experimental analy-		

	espect values in the order of 1700 - 1900	sis here is considered to be the preliminary
	kg/m^3.	achievements. The authors appreciate the re-
		viewer's valuable suggestions to carry out
		more experiments involving debris-flow den-
		sities in the order of 1700 - 1900 kg/m ³ in
		the future.
7.	#1: indicate flow direction and exchange the	The word "behind" has been replaced by
	word "behind" with "downriver of".	"downriver of".
8.	#2a: Sabo dam is never use in the text. Use	The word "Sabo dam" has been replaced by
0.		"check dam".
	check dam or replace check dam with sabo	
	dam in the text.	
9.	#5: desribe it as "debris-flow hydrograph". If	The caption of Figure 5 was changed to "de-
	your LRF gave you min, max and mean values,	bris-flow hydrograph". The information on
	you could perhaps explain the outliers. And:	the sampling rate of the device was added in
	this hydrograph does not really show a typicall	line 90, page 5.
	steep front of a debris flow. It looks more like a	
	hyperconcentraded flood. Again: add infor-	
	mation on the sampling rate of the device.	
10.	#6: add an arrow to show flow directions. Very	An arrow in each figure was added to show
	small images. Perhaps increase contrast.	debris-flow directions in Fig.6.
11.	Scaling effects are not discussed. Please add a	The scaling effects are discussed in the re-
	section to explain how the results of the ex-	vised vision in lines 207-215, page 11. The
	periments can be use in real dimensions. What	Froude number in our experiment ranged
	is the Froude number of your experiments?	from 1.14 to 1.16. It meant that the debris
		flows in the experiments were supercritical
		flow (in lines91-92, page 5).
12.	I miss a sensitivity study on different de-	The variation of debris-flow density (different
	bris-flow mixtures (e.g. higher densities, water	debris-flow mixtures) on scour depth was
	content variations)	added in lines 135-141, page 7.
13.	I miss information on the LRF. What is the	The information on the LRF was given in
	sampling rate (in Hz) of the device? How are	lines 89-90, page 5 and the sampling rate
	bris-flow mixtures (e.g. higher densities, water content variations) I miss information on the LRF. What is the	The variation of debris-flow density (different debris-flow mixtures) on scour depth wa added in lines 135-141, page 7. The information on the LRF was given in

	splashing effects handled?	(Frequency) was added in line 90, page 5.
14	What would have if there is driftwood in	Debrie flowe with driftmond will eread up the
14.	What would happen, if there is driftwood in-	Debris flows with driftwood will speed up the
	volved? Did you test that or what do you ex-	blockage and jamming of a check dam. Pro-
	pect in such a case?	vided that driftwood is involved in our ex-
		periments, the check dam will capture
		driftwood when it passed through the spill-
		way with debris flows. The subsequent de-
		bris flows will overflow from the check dam
		crest once the spillway is blocked by the
		driftwood, which will cause scour downriver
		of a check dam. The debris flows with
		driftwood was not considered in the current
		experiments, but definitely the reviewer has
		raised a very important question. The related
		experiments will be carried out to investi-
		gate the behaviour of debris flows with
		driftwood and its scour feature in the future.
15.	Can you say something about abrasion rates	Abrasion occurs due to the interaction be-
	and the expected life time of such structures?	tween solid particles in debris flows and the
		boundary of hydraulic structures. For a spill-
		way with curved bottom, the reaction of cen-
		trifugal force exerting on spillway bottom
		enhance the interaction between the solid par-
		ticles and the bottom (a component of the re-
		action force has the same direction as the
		gravitational force of debris flows near the
		outlet of the spillway). Although abrasion
		phenomenon is common, it is difficult to
		quantify the abrasion rate during an episode
		of debris flows.
		Abrasion may be one of the factors lead to the
3		,

damage of spillway with lateral contraction.However, some methods can be taken to mitigate the abrasion damage of such structuresby using anti-abrasion materials, or add theprotecting layer. The check dam with lateralcontracted spillway, like other check dams,the expected life time mainly depends on thedebris-flow scales, flow velocity, particleconcentration, etc.

Effects of Y-type spillway lateral contraction ratios on debris flow patterns 1 and scour features downriver of a check dambehind a check dam 2 Huayong Chen^{1,2}, Jinfeng Liu^{1,2}, and Wanyu Zhao^{1,2} 3 4 ¹Key Laboratory of Mountain Hazards and Earth Surface Process Chinese Academy of Sciences (CAS), Chengdu 610041, China 5 ²Institute of Mountain Hazards and Environment, CAS, Chengdu 610041, China 6 Correspondence to: Huayong Chen (hychen@imde.ac.cn) 7 Abstract. Debris flows often cause devastating damage to property and can injure or kill residents in 8 mountainous areas. The construction of check dams in debris-debris-flow valleys is considered a useful strategy 9 for mitigating the damages downstream. In this paper, a new type of spillway structure with lateral contraction 10 was proposed to distribute debris flows after the check dam storage filled up. Four different lateral contraction 11 ratios of the spillway were considered in experiments that investigated debris-debris-flow patterns, scour 12 characteristics, and energy dissipation rates when debris flows passed through the spillway. The results indicated 13 that lateral contraction considerably influenced the extension of debris-debris-flow nappes. The drop length of 14 the nappe at $\eta=0.7$ (η means lateral contraction ratio) was approximately 1.4 times larger than at $\eta=0.4$. The 15 collision, friction, and mixing forces between the debris-debris-flow nappes and debris flows in downstream plunge pools dissipated much of the debris-debris-flow kinetic energy, ranging from 42.03% to 78.08% at 16 17 different contraction ratios. Additionally, based on a dimensionless analysis, an empirical model was proposed to 18 predict the maximum scour depth behind the check damdownriver of a check dam. It indicated that the results 19 calculated by the model exhibited good agreement with the experimental results. 20 Introduction 1 21 Debris flows are formed by poorly sorted, water-saturated materials that mobilize in upstream regions of 22 valleys and surge down slopes in response to gravitational attraction (Iverson, 1997). Large scale debris flows

23 were triggered by intensive rainfalls after the "5.12" Wenchuan Earthquake, including the Zhouqu debris flow,

the Wenjia gully debris flow, and the Hongchun gully debris flow (Wang, 2013; Yu et al., 2013; Tang et al., 2015). On August 8, 2010, a large debris flow occurred in the Luojiayu gully, northern Zhouqu County, Gansu Province. The flow destroyed six villages, blocked the Bailongjiang River, resulting in the formation of a lake that inundated over half of Zhouqu County, and displaced or killed 1765 people (Cui et al., 2013). Usually, large-scale debris flow events involve substantial erosion upstream (Ni et al., 2012; Yu et al., 2013), and large volumes of solid materials are transported from the <u>initiation zoneformation region</u> to downstream areas by debris flows.

31 The construction of check dams is considered one of the most effective ways to store solid materials and 32 control soil erosion in a valley. This structural counter-measure is commonly used to stabilize bank slopes, 33 flatten the gradients of valleys, reduce flow velocity, and decrease the peak-discharge of debris flows (Lenzi, 34 2002; Mizuyama, 2008; Remaître et al., 2008; Remaitre and Malet, 2010). Two main types of check dams are 35 applied to control debris flows (i.e., closed-type and opened-type). Opened-type dams trap boulders, cobble, and 36 gravel, allowing small particles, fine sediments, and water to pass through the dams (Abedini et al., 2012). 37 Closed-type damns not only trap the coarse particles but also retain most small particle materials (Heumader, 38 2000; Lien, 2003). Generally, the dam storage volume of a closed-type check dam is quickly filled with debris 39 debris-flow material when a large debris flow occurs. The sequent debris flows directly overflow the check dam, 40 which can lead to serious scour on and around the foundation of the check dam (Figure 1).

Flow patterns and scour caused by the discharge of clear water or sediment flows has been well studied in hydraulic engineering. The characteristics of free-falling nappes behind the spillway of a gravity dam were investigated and the drop length of the free jet was predicted based on the energy equation in which the energy dissipation was neglected at two chosen cross-section (Toombes et al., 2008). Experimental investigations of aeration associated with overflow dams with curved surfaces were carried out, and empirical correlations

46	predicting the aeration efficiencies of these differently shaped spillways were developed (Chu et al., 2014). An
47	interpolation formula for predicting scour depth was proposed based on experimental data. It indicated that the
48	maximum scour increased with increasing discharge and decreased with increasing downstream tail water depth
49	(Adduce et al., 2005). In addition to the discharge and downstream tail water depth, the characteristic grain size
50	and the plunge angle were also considered for scour depth prediction (Bormann and Julien, 1991). Considerable
51	attention has been given to the flow patterns and scour caused by clear flows or sediment flows behind dams.
52	However, few studies have investigated the debris-debris-flow patterns and scour features behind check dams
53	(Pan et al., 2013), especially for spillway structures with lateral contraction. The flow patterns and scour features
54	caused by debris flows are different from those caused by clear water or sediment flows due to different flow
55	densities, cohesion, and particle volume concentrations. The investigation on characteristics of debris flows
56	discharging and scouring with the new spillway (Y-type spillway) can help us better understand the enrich our
57	knowledge of scour control for debris-flow mitigation.interaction between debris flows and the erodible solid
58	materials, which can also help us to find out better methods for debris flow mitigation in some serious geology
59	conditions.
60	In this paper, a new spillway structure with lateral contraction was-is proposed. Experiments with different
61	spillway contraction ratios were conducted to study the characteristics of debris-debris-flow nappes and scour
62	after debris flows overflowed the check dam. For each experimental test, video cameras were used to record the
63	trajectories of debris-debris-flow nappes. The energy dissipation rate was analyzed due to the varying lateral
64	contraction ratios. Finally, an empirical model based on dimensionless analysis was proposed to predict the
65	maximum scour depth behind the check damdownriver of a check dam.
66	2 Experimental setup

67 The experiments were performed at the Dongchuan Debris Flow Observation and Research Station (DDFORS)

in Dongchuan District, Yunnan Province, China. Generally, the experimental flume consisted of a hopper, a gate, a rectangular channel, and the downstream erodible bed (Figure 2a). The rectangular channel was approximately 4.0 m long, 0.4 m wide, and 0.4 m high, with a slope of 8° (Figure 2b). A check dam made of steel material was located at the end of the rectangular channel. The shape of the spillway inlet was a 0.20 m wide by 0.10 m high rectangle. The outlet was shaped like a capital letter 'Y'. The top width of the outlet was equal to that of the inlet. The bottom width ranged from 0.06 m to 0.12 m due to the different contraction ratios of the spillway. The dimensions of the spillway are shown in Figure 2c.

75 The lateral contraction ratio η is defined as follows:

$$\eta = \frac{B-b}{B} \tag{1}$$

76 where *B* is the width of the spillway inlet and *b* is the width of the spillway outlet. When b=B, $\eta=0$.

77 The storage of the check dam was filled with the solid materials from Jiangjia ravine, with a slope of 3°. The 78 diameter of the solid material was smaller than 20.0 mm. Its particle size distribution is shown in Fig. 3. Particle 79 size distribution may affect the debris-debris-flow density and flow motion along the channel. The solid 80 materials used in this experiment was prepared according to the sample of typical debris flows and excluded 81 particles larger than 20.0 mm due to the limitations of the experimental conditions. The diameter of the solid 82 materials in the erodible bed was also smaller than 20.0 mm. In addition, the clay and fine particles (smaller than 83 1.0 mm) were excluded to avoid the effects of matric suction on the development of the scour hole. The particle 84 size distribution of the erodible bed materials is also shown in Figure 3.

In each experimental test, a laser range finder (LRF) was set at the end of the erodible bed to monitor the depth of the debris flow during the entire process, as shown in Figure 4. The LRF measured the distance between the original bottom and the laser receiver. When debris flows flowed over the channel bottom, the LRF measured the distance between the <u>debris-debris-flow</u> surface and the laser receiver. The distance

89	difference was the flow depth. The measurement range of the LRF was up to 30.0 m, with an accuracy of
90	±0.001 m. The sampling frequency of the LRF was about 31.0 Hz. The elevation difference between the initial
91	position and the flow surface was the measured flow depth. The Froude number in our experiment ranged from
92	1.14 to 1.16. It meant that the debris flows in the experiments were supercritical flow. An example of the
93	measured results is shown in Figure 5. It reveals that although the debris-debris-flow process is not steady over
94	time, the debris flow over a short period can be considered steady flow. Therefore, the energy conservation
95	equation derived based on the steady flow assumption can be applied to analyze the energy dissipation rate of a
96	debris flow.
97	3 Experimental results and analysis
98	4.1 Flow patterns of different contraction ratios
99	When debris flows overflowed the spillway with a high lateral contraction ratio (η =0.7), the flow depth and
100	velocity increased dramatically. The debris-debris-flow nappe clearly extended in the flow direction.
101	Furthermore, the debris flows near both side wall, which were forced to change direction by the walls, collided
102	at the outlet when the debris flows overflowed from the spillway (Figure 6a). Decreasing the lateral contraction
103	ratio caused the flow depth and velocity to decrease at the same flow discharge. Therefore, the drop length of the
104	debris-debris-flow nappe decreased in the flow direction. The drop length at η =0.7 was approximately 1.4 times
105	than at η =0.4 (Table 1). Lateral contraction not only affected the drop length but also broadened the nappe width
106	due to the collision of debris flows at the outlet (Figure 6b-d). When η =0.5, the broadening ratio κ (κ is the ratio
107	of nappe width to the outlet width) reached its maximum value (κ =2.93 in Table 1). The nappe width was equal
108	to that of the spillway (κ =1.0) when there was no lateral contraction at the spillway.
109	If debris flows flowing out of the spillway are considered free-motion point masses under the influence of
110	gravity, the trajectory of a debris-debris-flow nappe can be expressed as follows (Figure 7):

$$y = xtg\varphi + \frac{g}{2v_1^2 \cos\varphi^2} x^2$$
⁽²⁾

$$x = \frac{v^2}{g} \cos \varphi \left(\sqrt{\sin^2 \varphi + \frac{2gy}{v^2}} - \sin \varphi \right) \varphi \ge 0$$
(3)

112 When $\varphi = 0$, equation (2) simplifies to equation (3):

111

128

$$x = \sqrt{\frac{2v^2 y}{g}} \tag{4}$$

113 where v is the initial velocity of the debris flow flowing out of the spillway, φ represents the angle of the 114 initial velocity in the horizontal direction, and y is the water elevation difference.

115 Equation (3) indicates that the nappe extension in the horizontal direction 'x' is proportional to the initial 116 velocity v and square root of the water elevation difference y. From Fig. 6 and Table 1, we found that when 117 $\eta=0.7$, the nappe extension was longest in the flow direction. From this point of view, a high lateral contraction 118 ratio increased the distance between the plunge point and the dam toe, which effectively protected the dam 119 foundation from scouring. The hydraulic characteristics of the nappe away from the spillway at different lateral 120 contraction ratios were shown in Figure 8 and Figure 9. Figure 8 indicates that increasing the lateral contraction 121 ratio decreased the width of the debris-debris-flow nappe. Furthermore, the higher lateral contraction of the 122 spillway strengthened the collision between flows at the spillway outlet. Air bubbles were entrained in the debris 123 flows when the continuum of the debris flows was broken. Figure 9 shows the extent of the debris-debris-flow 124 nappes. The distribution of the flow velocity in the vertical direction at the outlet increased with increasing flow 125 depth due to the effects of boundary friction. Therefore, the longest flow nappes were formed by the debris flows 126 with relatively large velocities at the flow surface.

127 **4.2 Debris**-<u>flow scour features behind the check damdownriver of a check dam</u>

The scour features of debris flows behind the check damdownriver of a check dam represent one of the most

129	important indexes, which determines the scour depth at the dam foundation. Figure 10 shows the effects of
130	lateral contraction on the formation of scour holes in an erodible bed. For the same curvature of the spillway
131	surface, decreasing the contraction ratio decreased the maximum scour depth and caused the location of the
132	maximum scour point to shift toward the dam toe due to the decreased debris debris flow velocity. The
133	maximum scour depth and its location farther from the dam toe for η =0.7 were approximately 1.3 and 1.4 times,
134	respectively, larger than for η =0.4. Although a high lateral contraction ratio extended the debris-debris-flow
135	nappe, it also increased the scour depth in the erodible bed to some extent. In addition, debris-flow density has
136	some effects on the scour depth. Figure 11 indicates the scour depth caused by debris flow with density of
137	1200kg/m ³ is a bit larger than that caused by debris flow with density of 1500kg/m ³ at a certain lateral
138	contraction ratio (Figure 11). It was explained that the debris flow with lower particle concentration (Lower
139	debris-flow density) initialized and carried more bed materials than that with higher particle concentration
140	(Higher debris-flow density) when the other factors were fixed (Such as longitudinal slope of gully, debris-flow
141	scale, lateral contraction ratio of the spillway).

142 **4.3** Energy dissipation at different contraction ratios

Generally, different energy dissipaters such as the plunge pool (Pagliara et al., 2010; Duarte et al., 2015) or step-pool systems (Yu, 2007; Wang et al., 2009; Wang et al., 2012) are required to dissipate the kinetic energy of the surplus flow and prevent the dam foundation and riverbed from scouring when sudden changes to the channel slope occur. The energy dissipation process of the check dam was estimated using the Bernoulli equation (4). The rationale behind using this equation was previously mentioned.

148 The Bernoulli equation between two reference cross-sections is written as follows:

$$Z_1 + h_1 + \alpha_1 \frac{v_1^2}{2g} = Z_2 + h_2 + \alpha_2 \frac{v_2^2}{2g} + h_w$$
(5)

149 If $\Delta Z = Z - Z$, then equation (4) can be transformed into equation (5):

$$\Delta Z + h_1 + \alpha_1 \frac{v_1^2}{2g} = h_2 + \alpha_2 \frac{v_2^2}{2g} + h_w$$
(6)

150 The energy dissipation coefficient ζ can be expressed as follows:

$$\zeta = 1 - \frac{h_2 + \frac{v_2^2}{2g}}{\Delta z + h_1 + \frac{v_1^2}{2g}}$$
(7)

where Z_1 and Z_2 are the elevations of reference cross-sections #1 and #2 (Figure. 2b), respectively; h_1 and h_2 are the depths of debris flows at reference cross-sections #1 and #2, respectively; v_1 and v_2 are the velocities of the debris flows at references cross-sections #1 and #2, respectively; α_1 and α_2 are the kinetic energy correction coefficients ($\alpha_1 = \alpha_2 = 1$) (Adamkowski et al., 2006); ΔZ is the elevation difference between the two reference cross-sections; and h_w is the water head loss.

Table 2 indicates that the collision and friction forces between the debris-debris-flow nappes and debris flows 156 157 in the plunge pool dissipated the kinetic energy of the flows, ranging from 42.03% to 78.08% at different 158 contraction ratios. In the case of $V=0.16 \text{ m}^3$, the energy dissipation rate decreased gradually when the contraction 159 ratio changed from 0.7 to 0.4 because the high contraction ratio increased the number of debris-debris-flow collisions when it passed through the spillway. In the cases of $V=0.10 \text{ m}^3$ and $V=0.06 \text{ m}^3$, the energy dissipation 160 161 rate also decreased with decreasing the contraction ratios except at $\eta=0.4$. The mean value of the energy 162 dissipation rate demonstrated a good positive correlation between the energy dissipation rate and the lateral 163 contraction ratio. In addition, for the same contraction ratio, the energy dissipation rate increased gradually with 164 decreasing debris-debris-flow scale.

165 4.4 The empirical equation for estimating the maximum scour depth

166 Many empirical equations have been proposed to predict the maximum scour depth over the last several

decades (Bormann and Julien, 1991; Zhou, 1991; Adduce et al., 2005; Pan et al., 2013). The main parameters include the unit discharge, characteristic particle size of the erodible bed, water elevation difference and clear water and <u>debris-debris-</u>flow densities. However, most of the empirical equations (Li and Liu, 2010) neglect dimensional homogeneity (the empirical equations should be dimensionally homogeneous). For new type of spillway, the lateral contraction ratio is an important parameter for predicting the maximum scour depth. For a debris flow, the maximum scour depth is mainly determined by the following parameters:

$$h_{d} = f(q, g, \rho_{d}, \rho_{w}, d_{90}, \eta....)$$
(8)

where h_d is the maximum scour depth, q is the unit discharge of the debris flow, g is the acceleration due to gravity, ρ_d and ρ_w are the <u>debris-debris-flow</u> density and clear water density, respectively (two <u>debris-debris-flow</u> densities were considered, including, $\rho_d=1200$ kg/m³ and $\rho_d=1500$ kg/m³), d_{90} is the characteristic particle size for erodible bed materials , and η is the lateral contraction ratio.

Based on a dimensional analysis, the dimensionless parameters with clear physical meanings are developed asfollows:

$$\frac{h_s}{d_{90}} = k \left(\frac{q}{d_{90}\sqrt{gd_{90}}}\right)^{a_1} \left(\frac{\rho_d}{\rho_w}\right)^{a_2} \left(1-\eta\right)^{a_3}$$
(9)

179 where h_s/d_{90} is dimensionless scour depth, k is a coefficient, at is an index (i=1, 2, 3), $\frac{q}{d_{90}\sqrt{gd_{90}}}$ is the

180 dimensionless discharge, and ρ_d / ρ_w is the dimensionless density.

181 According to the experimental data, the regression equation can be expressed as follows:

$$\frac{h_s}{d_{90}} = 3.15 \left(\frac{q}{d_{90}\sqrt{gd_{90}}}\right)^{0.51} \left(\frac{\rho_d}{\rho_w}\right)^{-0.1363} \left(1-\eta\right)^{0.7583}$$
(10)

The regression equation suggests that the flow density had relatively small effects on the depth of the scour hole. However, the <u>debris-debris-</u>flow discharge and the lateral contraction had strong effects on the maximum depth of the scour hole, which directly determined the kinetic energy of the flow in the downstream erodible bed. The validation tests were also performed using the physical experimental model shown in Figure 2, but under different conditions. Additional experimental data provided in the literature (Ben and Mossa, 2006) were used to verify the reliability of the regression equation. The predicted results exhibited good agreement with the experimental results. The absolute error was smaller than 15.0% in most cases, as shown in Figure <u>112</u>.

189 4 Conclusions and Discussions

190 <u>4.1 Conclusions</u>

The characteristics of debris flows overflowing the new type of spillway were analyzed at different lateral contraction ratios. The energy dissipation rate and an empirical model for predicting the maximum scour depth were also studied in this paper. The following conclusions were drawn from this analysis:

- 1) Flow patterns were mainly determined by the lateral contraction ratio. At a high lateral contraction ratio, the spillway effectively extended the <u>debris-debris-</u>flow nappe and increased the distance between the plunge point and the dam toe. The drop length of the nappe at η =0.7 was approximately 1.4 times higher than that
- 197 at η =0.4.
- The plunge pool behind the check dam<u>downriver of a check dam</u> inevitably dissipated the kinetic energy of
 the debris flow after overflowing the check dam. The collision and friction between the debris-flow
- 200 nappe and the debris flow in the plunge pool dissipated the kinetic energy of the flow, ranging from 42.03%
- 201 to 78.08% at different contraction ratios. Generally, increasing the contraction ratio increased the energy
 202 dissipation rate at the same debris debris-flow scale.
- An empirical model was proposed to predict the maximum scour depth behind the check damdownriver of
 a check dam. The results indicated that the predicted results exhibited good agreement with the
 experimental results. The absolute error was smaller than 15.0% in most cases.
- 206 <u>4.2 Discussions</u>
- 207 The characteristics of debris flow nape and scour downriver of a check dam with different spillway were

i	
208	experimentally investigated in this article. When the experimental data are used to predict debris-flow motion
209	and scour feature downriver of a check dam in prototype, the effects of physical model scale should be
210	considered. Scaling effect is mainly induced by dissatisfaction of mobility similitude of model sediment in
211	physical model experiments and it leads to discrepancies between the estimated and actual scour results. Just like
212	the experimental investigation on the scale effect in pier-scour experiments, the bed-particle mobility similitude
213	(Ettema et al ,1998; Ettema and Melville,1999) or the flow-strength similitude (Lee and Sturm,2009) should be
214	satisfied to weaken or eliminate the scaling effect for debris-flow scour when the experimental results are
215	extrapolated to predict prototype performance in the future.
216	When debris flows occur in the mountainous areas with forest the driftwood carried by debris flows is a
217	common phenomenon. The debris flows combined with driftwood will speed up blockage and jamming of a
218	check dam. Once the spillway is blocked by the driftwood the subsequent debris flows will overflow from the
219	crest of a check dam, which will cause extensive scour downriver of a check dam. Therefore, it is also necessary
220	to investigate the behavior of debris flows with driftwood and propose some reasonable structural or non-
221	structural countermeasures to mitigate the effects of debris flows with driftwood on the operation of a check dam
222	in the future.
223	Acknowledgments
224	The study results presented in this paper were supported by the Key Research Program of the Chinese
225	Academy of Sciences (Grant No. KZZD-EW-05-01), the National Natural Science Foundation of China (Grant
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227	KFJ-EW-STS-094), and the Key Laboratory of Mountain Hazards and Earth Surface Process, Chinese Academy
228	of Sciences.

229 List of symbols

- ai = The index for the dimensionless parameter (-)
- b = The width of the spillway outlet(m)
- B = The width of the spillway inlet (m)
- d_{90} = The characteristic particle size for erodible bed materials (m)
- k = The coefficient for the dimensionless equation (-)
- h_1 = The depth of debris flows at reference cross-sections #1 (m)
- h_2 = The depth of debris flows at reference cross-sections #2 (m)
- $h_{\rm d}$ = The maximum scour depth (m)
- h_w = The water head loss (m)
- g = The acceleration of gravity (m/s²)
- q = The unit discharge of the debris flow (m³/s)
- v = The initial velocity of the debris flow flowing out of the spillway(m/s)
- v_1 = The velocity of debris flows at reference cross-sections #1 (m/s)
- v_2 = The velocity of debris flows at reference cross-sections #2 (m/s)
- V = The scale of debris flow in the experiments (m⁵)
- x = Trajectory in the horizontal direction (m)
- y = The water elevation difference (m)
- Z_1 = The elevation of reference cross-sections at #1 (m)
- Z_2 = The elevation of reference cross-sections at #2 (m)
- Δz = The elevation difference between the two reference cross-sections (m) eek letters

Greek letters

- α_1 = The kinetic energy correction coefficient for v_1 (-)
- α_2 = The kinetic energy correction coefficient for v_2 (-)
- ρ_d = The density of debris flows (kg/m³)
- ρ_w = The density of clear water (kg/m³)
- ζ = The energy dissipation coefficient(-)
- η = The lateral contraction ratio(-)
- φ = The angle of the initial velocity in the horizontal direction(°)

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Fig. 1. An example of foundation scour <u>downriver of behind</u> a check dam



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299 (c) The structure and dimensions of the spillway (unit: mm). Four different lateral contraction ratios were 300 considered in the experiments: (a) B=200.0 mm, b=60.0 mm, $\eta=0.7$; (b) B=200.0 mm, b=80.0 mm, $\eta=0.6$; (c) B301 =200.0 mm, b=100.0 mm, $\eta=0.5$; (d) B=200.0 mm, b=120.0 mm, $\eta=0.4$. The bottom of the spillway was 302 formed by a compound curve surface (a simple curved segment and a circular segment: radius R=100.0 mm, 303 radius angle $\delta=75^{\circ}$).

Fig. 2. Experimental setup





309 Fig. 3. The particle size distribution of samples for the debris flows and erodible bed



Fig. 4. Photograph of the LRF system (the photograph was taken in the downstream direction)



Fig. 5. An example of a <u>debris-flow hydrograph</u> debris flow duration monitored by the LRF
318



- 321 Fig. 6. Various debris flow patterns at different lateral contraction ratios (the pictures on the left were taken
- 322 from a downstream view)



Fig. 7. A diagram of dynamic parameters of debris flows



Fig. 8. The transverse expansion of a debris flow nappe at different lateral contraction ratios



335 Fig. 9. The trajectory of a debris flow nappe





Fig. 10. The shapes of the scour hole behind the check damdownriver of a check dam ($V=0.16 \text{ m}^3, \rho=1.50 \text{ g/cm}^3$)





Fig. <u>1112</u>. Comparison between predicted data and experimental ones

Table 1. The main parameters of the debris flow nappe for different contraction ratios

Items	(a)	(b)	(c)	(d)
Width of the outlet <i>b</i> /mm	60.0	80.0	100.0	120.0
Lateral contraction ratio η	0.7	0.6	0.5	0.4
Width of the nappe W_{Nappe} /mm	137.2	231.6	292.6	320.6
Broadening ratio $\kappa(\kappa = W_{\text{Nappe}}/b)$	2.29	2.90	2.93	2.67
Length of the nappe away from the outlet x_a/m	0.43	0.34	0.33	0.31
Length of the nappe close to the outlet x_c/m	0.25	0.21	0.21	0.18

350 Notes: B is constant for each spillway type (B =200.0 mm)

 Table 2. The energy dissipation rates at different contraction ratios
 Density (p=1.50 g/cm³) Scales η=0.4 η=0.7 η=0.6 $\eta = 0.5$ $V=0.16 \text{ m}^3$ 66.43%57.48%52.34%42.03% $V=0.10 \text{ m}^3$ 60.58% 67.97% 75.37% 72.94% $V=0.06 \text{ m}^3$ 78.08% 73.70% 63.61% 71.75% Mean value 73.29% 68.04% 60.58% 58.84%

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Effects of Y-type spillway lateral contraction ratios on debris flow patterns 1 and scour features downriver of a check dam 2 Huayong Chen^{1,2}, Jinfeng Liu^{1,2}, and Wanyu Zhao^{1,2} 3 4 ¹Key Laboratory of Mountain Hazards and Earth Surface Process Chinese Academy of Sciences (CAS), Chengdu 610041, China 5 ²Institute of Mountain Hazards and Environment, CAS, Chengdu 610041, China 6 Correspondence to: Huayong Chen (hychen@imde.ac.cn) 7 Abstract. Debris flows often cause devastating damage to property and can injure or kill residents in 8 mountainous areas. The construction of check dams in debris-flow valleys is considered a useful strategy for 9 mitigating the damages downstream. In this paper, a new type of spillway structure with lateral contraction was 10 proposed to distribute debris flows after the check dam storage filled up. Four different lateral contraction ratios 11 of the spillway were considered in experiments that investigated debris-flow patterns, scour characteristics, and 12 energy dissipation rates when debris flows passed through the spillway. The results indicated that lateral 13 contraction considerably influenced the extension of debris-flow nappes. The drop length of the nappe at $\eta=0.7$ 14 (η means lateral contraction ratio) was approximately 1.4 times larger than at $\eta=0.4$. The collision, friction, and 15 mixing forces between the debris-flow nappes and debris flows in downstream plunge pools dissipated much of 16 the debris-flow kinetic energy, ranging from 42.03% to 78.08% at different contraction ratios. Additionally, 17 based on a dimensionless analysis, an empirical model was proposed to predict the maximum scour depth 18 downriver of a check dam. It indicated that the results calculated by the model exhibited good agreement with 19 the experimental results. 20 Introduction 1

Debris flows are formed by poorly sorted, water-saturated materials that mobilize in upstream regions of valleys and surge down slopes in response to gravitational attraction (Iverson,1997). Large scale debris flows were triggered by intensive rainfalls after the "5.12" Wenchuan Earthquake, including the Zhouqu debris flow, the Wenjia gully debris flow, and the Hongchun gully debris flow (Wang, 2013; Yu et al., 2013; Tang et al., 2015). On August 8, 2010, a large debris flow occurred in the Luojiayu gully, northern Zhouqu County, Gansu Province. The flow destroyed six villages, blocked the Bailongjiang River, resulting in the formation of a lake that inundated over half of Zhouqu County, and displaced or killed 1765 people (Cui et al., 2013). Usually, large-scale debris flow events involve substantial erosion upstream (Ni et al., 2012; Yu et al., 2013), and large volumes of solid materials are transported from the initiation zone to downstream areas.

30 The construction of check dams is considered one of the most effective ways to store solid materials and 31 control soil erosion in a valley. This structural counter-measure is commonly used to stabilize bank slopes, 32 flatten the gradients of valleys, reduce flow velocity, and decrease the peak-discharge of debris flows (Lenzi, 33 2002; Mizuyama, 2008; Remaître et al., 2008; Remaitre and Malet, 2010). Two main types of check dams are 34 applied to control debris flows (i.e., closed-type and opened-type). Opened-type dams trap boulders, cobble, and 35 gravel, allowing small particles, fine sediments, and water to pass through the dams (Abedini et al., 2012). 36 Closed-type damns not only trap the coarse particles but also retain most small particle materials (Heumader, 37 2000; Lien, 2003). Generally, the dam storage volume of a closed-type check dam is quickly filled with 38 debris-flow material when a large debris flow occurs. The sequent debris flows directly overflow the check dam, 39 which can lead to serious scour on and around the foundation of the check dam (Figure 1).

Flow patterns and scour caused by the discharge of clear water or sediment flows has been well studied in hydraulic engineering. The characteristics of free-falling nappes behind the spillway of a gravity dam were investigated and the drop length of the free jet was predicted based on the energy equation in which the energy dissipation was neglected at two chosen cross-section (Toombes et al., 2008). Experimental investigations of aeration associated with overflow dams with curved surfaces were carried out, and empirical correlations predicting the aeration efficiencies of these differently shaped spillways were developed (Chu et al., 2014). An 46 interpolation formula for predicting scour depth was proposed based on experimental data. It indicated that the 47 maximum scour increased with increasing discharge and decreased with increasing downstream tail water depth 48 (Adduce et al., 2005). In addition to the discharge and downstream tail water depth, the characteristic grain size 49 and the plunge angle were also considered for scour depth prediction (Bormann and Julien, 1991). Considerable 50 attention has been given to the flow patterns and scour caused by clear flows or sediment flows behind dams. 51 However, few studies have investigated the debris-flow patterns and scour features behind check dams (Pan et al., 52 2013), especially for spillway structures with lateral contraction. The flow patterns and scour features caused by 53 debris flows are different from those caused by clear water or sediment flows due to different flow densities, 54 cohesion, and particle volume concentrations. The investigation on characteristics of debris flows discharging 55 and scouring with the new spillway (Y-type spillway) can enrich our knowledge of scour control for debris-flow 56 mitigation.

In this paper, a new spillway structure with lateral contraction is proposed. Experiments with different spillway contraction ratios were conducted to study the characteristics of debris-flow nappes and scour after debris flows overflowed the check dam. For each experimental test, video cameras were used to record the trajectories of debris-flow nappes. The energy dissipation rate was analyzed due to the varying lateral contraction ratios. Finally, an empirical model based on dimensionless analysis was proposed to predict the maximum scour depth downriver of a check dam.

63 2 Experimental setup

The experiments were performed at the Dongchuan Debris Flow Observation and Research Station (DDFORS) in Dongchuan District, Yunnan Province, China. Generally, the experimental flume consisted of a hopper, a gate, a rectangular channel, and the downstream erodible bed (Figure 2a). The rectangular channel was approximately 4.0 m long, 0.4 m wide, and 0.4 m high, with a slope of 8° (Figure 2b). A check dam made of steel material was
located at the end of the rectangular channel. The shape of the spillway inlet was a 0.20 m wide by 0.10 m high rectangle. The outlet was shaped like a capital letter 'Y'. The top width of the outlet was equal to that of the inlet. The bottom width ranged from 0.06 m to 0.12 m due to the different contraction ratios of the spillway. The dimensions of the spillway are shown in Figure 2c.

72 The lateral contraction ratio η is defined as follows:

$$\eta = \frac{B-b}{B} \tag{1}$$

73 where *B* is the width of the spillway inlet and *b* is the width of the spillway outlet. When b=B, $\eta=0$.

74 The storage of the check dam was filled with the solid materials from Jiangjia ravine, with a slope of 3°. The 75 diameter of the solid material was smaller than 20.0 mm. Its particle size distribution is shown in Fig. 3. Particle 76 size distribution may affect the debris-flow density and flow motion along the channel. The solid materials used 77 in this experiment was prepared according to the sample of typical debris flows and excluded particles larger 78 than 20.0 mm due to the limitations of the experimental conditions. The diameter of the solid materials in the 79 erodible bed was also smaller than 20.0 mm. In addition, the clay and fine particles (smaller than 1.0 mm) were 80 excluded to avoid the effects of matric suction on the development of the scour hole. The particle size 81 distribution of the erodible bed materials is also shown in Figure 3.

In each experimental test, a laser range finder (LRF) was set at the end of the erodible bed to monitor the depth of the debris flow during the entire process, as shown in Figure 4. The LRF measured the distance between the original bottom and the laser receiver. When debris flows flowed over the channel bottom, the LRF measured the distance between the debris-flow surface and the laser receiver. The distance difference was the flow depth. The measurement range of the LRF was up to 30.0 m, with an accuracy of ± 0.001 m. The sampling frequency of the LRF was about 31.0 Hz. The elevation difference between the initial position and the flow surface was the measured flow depth. The Froude number in our experiment ranged from 1.14 to 1.16. It 89 meant that the debris flows in the experiments were supercritical flow. An example of the measured results is 90 shown in Figure 5. It reveals that although the debris-flow process is not steady over time, the debris flow over a 91 short period can be considered steady flow. Therefore, the energy conservation equation derived based on the 92 steady flow assumption can be applied to analyze the energy dissipation rate of a debris flow.

93 **3**

Experimental results and analysis

94 **4.1** Flow patterns of different contraction ratios

95 When debris flows overflowed the spillway with a high lateral contraction ratio (η =0.7), the flow depth and 96 velocity increased dramatically. The debris-flow nappe clearly extended in the flow direction. Furthermore, the 97 debris flows near both side wall, which were forced to change direction by the walls, collided at the outlet when 98 the debris flows overflowed from the spillway (Figure 6a). Decreasing the lateral contraction ratio caused the 99 flow depth and velocity to decrease at the same flow discharge. Therefore, the drop length of the debris-flow 100 nappe decreased in the flow direction. The drop length at $\eta=0.7$ was approximately 1.4 times than at $\eta=0.4$ 101 (Table 1). Lateral contraction not only affected the drop length but also broadened the nappe width due to the 102 collision of debris flows at the outlet (Figure 6b-d). When $\eta=0.5$, the broadening ratio κ (κ is the ratio of nappe 103 width to the outlet width) reached its maximum value (κ =2.93 in Table 1). The nappe width was equal to that of 104 the spillway (κ =1.0) when there was no lateral contraction at the spillway.

If debris flows flowing out of the spillway are considered free-motion point masses under the influence ofgravity, the trajectory of a debris-flow nappe can be expressed as follows (Figure 7):

107
$$y = xtg\phi + \frac{g}{2v_1^2 \cos\phi^2} x^2$$
 (2)

$$x = \frac{v^2}{g} \cos \varphi \left(\sqrt{\sin^2 \varphi + \frac{2gy}{v^2}} - \sin \varphi \right) \varphi \ge 0$$
(3)

108 When $\varphi = 0$, equation (2) simplifies to equation (3):

$$x = \sqrt{\frac{2v^2 y}{g}} \tag{4}$$

109 where v is the initial velocity of the debris flow flowing out of the spillway, φ represents the angle of the 110 initial velocity in the horizontal direction, and y is the water elevation difference.

111 Equation (3) indicates that the nappe extension in the horizontal direction 'x' is proportional to the initial 112 velocity v and square root of the water elevation difference y. From Fig. 6 and Table 1, we found that when 113 $\eta=0.7$, the nappe extension was longest in the flow direction. From this point of view, a high lateral contraction 114 ratio increased the distance between the plunge point and the dam toe, which effectively protected the dam 115 foundation from scouring. The hydraulic characteristics of the nappe away from the spillway at different lateral 116 contraction ratios were shown in Figure 8 and Figure 9. Figure 8 indicates that increasing the lateral contraction 117 ratio decreased the width of the debris-flow nappe. Furthermore, the higher lateral contraction of the spillway 118 strengthened the collision between flows at the spillway outlet. Air bubbles were entrained in the debris flows 119 when the continuum of the debris flows was broken. Figure 9 shows the extent of the debris-flow nappes. The 120 distribution of the flow velocity in the vertical direction at the outlet increased with increasing flow depth due to 121 the effects of boundary friction. Therefore, the longest flow nappes were formed by the debris flows with 122 relatively large velocities at the flow surface.

123 4.2 Debris-flow scour features downriver of a check dam

The scour features of debris flows downriver of a check dam represent one of the most important indexes, which determines the scour depth at the dam foundation. Figure 10 shows the effects of lateral contraction on the formation of scour holes in an erodible bed. For the same curvature of the spillway surface, decreasing the contraction ratio decreased the maximum scour depth and caused the location of the maximum scour point to shift toward the dam toe due to the decreased debris-flow velocity. The maximum scour depth and its location

129 farther from the dam toe for $\eta=0.7$ were approximately 1.3 and 1.4 times, respectively, larger than for $\eta=0.4$. 130 Although a high lateral contraction ratio extended the debris-flow nappe, it also increased the scour depth in the 131 erodible bed to some extent. In addition, debris-flow density has some effects on the scour depth. Figure 11 indicates the scour depth caused by debris flow with density of 1200kg/m^3 is a bit larger than that caused by 132 debris flow with density of 1500kg/m³ at a certain lateral contraction ratio (Figure 11). It was explained that the 133 134 debris flow with lower particle concentration (Lower debris-flow density) initialized and carried more bed 135 materials than that with higher particle concentration (Higher debris-flow density) when the other factors were 136 fixed (Such as longitudinal slope of gully, debris-flow scale, lateral contraction ratio of the spillway).

137 4.3 Energy dissipation at different contraction ratios

Generally, different energy dissipaters such as the plunge pool (Pagliara et al., 2010; Duarte et al., 2015) or step-pool systems (Yu, 2007; Wang et al., 2009; Wang et al., 2012) are required to dissipate the kinetic energy of the surplus flow and prevent the dam foundation and riverbed from scouring when sudden changes to the channel slope occur. The energy dissipation process of the check dam was estimated using the Bernoulli equation (4). The rationale behind using this equation was previously mentioned.

143 The Bernoulli equation between two reference cross-sections is written as follows:

$$Z_1 + h_1 + \alpha_1 \frac{v_1^2}{2g} = Z_2 + h_2 + \alpha_2 \frac{v_2^2}{2g} + h_w$$
(5)

144 If $\Delta z = z_1 - z_2$, then equation (4) can be transformed into equation (5):

$$\Delta Z + h_1 + \alpha_1 \frac{v_1^2}{2g} = h_2 + \alpha_2 \frac{v_2^2}{2g} + h_w \tag{6}$$

145 The energy dissipation coefficient ζ can be expressed as follows:

$$\zeta = 1 - \frac{h_2 + \frac{v_2^2}{2g}}{\Delta z + h_1 + \frac{v_1^2}{2g}}$$
(7)

where Z_1 and Z_2 are the elevations of reference cross-sections #1 and #2 (Figure. 2b), respectively; h_1 and h_2 are the depths of debris flows at reference cross-sections #1 and #2, respectively; v_1 and v_2 are the velocities of the debris flows at references cross-sections #1 and #2, respectively; α_1 and α_2 are the kinetic energy correction coefficients ($\alpha_1 = \alpha_2 = 1$) (Adamkowski et al., 2006); ΔZ is the elevation difference between the two reference cross-sections; and h_w is the water head loss.

151 Table 2 indicates that the collision and friction forces between the debris-flow nappes and debris flows in the 152 plunge pool dissipated the kinetic energy of the flows, ranging from 42.03% to 78.08% at different contraction 153 ratios. In the case of V=0.16 m³, the energy dissipation rate decreased gradually when the contraction ratio 154 changed from 0.7 to 0.4 because the high contraction ratio increased the number of debris-flow collisions when 155 it passed through the spillway. In the cases of $V=0.10 \text{ m}^3$ and $V=0.06 \text{ m}^3$, the energy dissipation rate also 156 decreased with decreasing the contraction ratios except at η =0.4. The mean value of the energy dissipation rate 157 demonstrated a good positive correlation between the energy dissipation rate and the lateral contraction ratio. In 158 addition, for the same contraction ratio, the energy dissipation rate increased gradually with decreasing 159 debris-flow scale.

160 **4.4** The empirical equation for estimating the maximum scour depth

Many empirical equations have been proposed to predict the maximum scour depth over the last several decades (Bormann and Julien, 1991; Zhou, 1991; Adduce et al., 2005; Pan et al., 2013). The main parameters include the unit discharge, characteristic particle size of the erodible bed, water elevation difference and clear water and debris-flow densities. However, most of the empirical equations (Li and Liu, 2010) neglect dimensional homogeneity (the empirical equations should be dimensionally homogeneous). For new type of spillway, the lateral contraction ratio is an important parameter for predicting the maximum scour depth. For a

167 debris flow, the maximum scour depth is mainly determined by the following parameters:

$$h_{d} = f(q, g, \rho_{d}, \rho_{w}, d_{90}, \eta.....)$$
(8)

where h_d is the maximum scour depth, q is the unit discharge of the debris flow, g is the acceleration due to gravity, ρ_d and ρ_w are the debris-flow density and clear water density, respectively (two debris-flow densities were considered, including, $\rho_d=1200$ kg/m³ and $\rho_d=1500$ kg/m³), d_{90} is the characteristic particle size for erodible bed materials , and η is the lateral contraction ratio.

Based on a dimensional analysis, the dimensionless parameters with clear physical meanings are developed asfollows:

$$\frac{h_s}{d_{90}} = k \left(\frac{q}{d_{90}\sqrt{gd_{90}}}\right)^{a_1} \left(\frac{\rho_d}{\rho_w}\right)^{a_2} \left(1-\eta\right)^{a_3}$$
(9)

174 where h_s/d_{90} is dimensionless scour depth, k is a coefficient, ai is an index (i=1, 2, 3), $\frac{q}{d_{90}\sqrt{gd_{90}}}$ is the

175 dimensionless discharge, and ρ_d/ρ_w is the dimensionless density.

According to the experimental data, the regression equation can be expressed as follows:

$$\frac{h_s}{d_{90}} = 3.15 \left(\frac{q}{d_{90}\sqrt{gd_{90}}}\right)^{0.51} \left(\frac{\rho_d}{\rho_w}\right)^{-0.1363} \left(1-\eta\right)^{0.7583}$$
(10)

The regression equation suggests that the flow density had relatively small effects on the depth of the scour hole. However, the debris-flow discharge and the lateral contraction had strong effects on the maximum depth of the scour hole, which directly determined the kinetic energy of the flow in the downstream erodible bed. The validation tests were also performed using the physical experimental model shown in Figure 2, but under different conditions. Additional experimental data provided in the literature (Ben and Mossa, 2006) were used to verify the reliability of the regression equation. The predicted results exhibited good agreement with the experimental results. The absolute error was smaller than 15.0% in most cases, as shown in Figure 12.

184 4 Conclusions and Discussions

185 4.1 Conclusions

186 The characteristics of debris flows overflowing the new type of spillway were analyzed at different lateral 187 contraction ratios. The energy dissipation rate and an empirical model for predicting the maximum scour depth

- 188 were also studied in this paper. The following conclusions were drawn from this analysis:
- 189 1) Flow patterns were mainly determined by the lateral contraction ratio. At a high lateral contraction ratio, the

spillway effectively extended the debris-flow nappe and increased the distance between the plunge point

- 191 and the dam toe. The drop length of the nappe at $\eta=0.7$ was approximately 1.4 times higher than that at
- 192 $\eta=0.4$.

193 2) The plunge pool downriver of a check dam inevitably dissipated the kinetic energy of the debris flow after 194 overflowing the check dam. The collision and friction between the debris-flow nappe and the debris flow in 195 the plunge pool dissipated the kinetic energy of the flow, ranging from 42.03% to 78.08% at different 196 contraction ratios. Generally, increasing the contraction ratio increased the energy dissipation rate at the 197 same debris-flow scale.

An empirical model was proposed to predict the maximum scour depth downriver of a check dam. The
 results indicated that the predicted results exhibited good agreement with the experimental results. The
 absolute error was smaller than 15.0% in most cases.

201 4.2 Discussions

The characteristics of debris flow nape and scour downriver of a check dam with different spillway were experimentally investigated in this article. When the experimental data are used to predict debris-flow motion and scour feature downriver of a check dam in prototype, the effects of physical model scale should be considered. Scaling effect is mainly induced by dissatisfaction of mobility similitude of model sediment in physical model experiments and it leads to discrepancies between the estimated and actual scour results. Just like the experimental investigation on the scale effect in pier-scour experiments, the bed-particle mobility similitude (Ettema et al ,1998; Ettema and Melville,1999) or the flow-strength similitude (Lee and Sturm,2009) should be satisfied to weaken or eliminate the scaling effect for debris-flow scour when the experimental results are extrapolated to predict prototype performance in the future.

When debris flows occur in the mountainous areas with forest the driftwood carried by debris flows is a common phenomenon. The debris flows combined with driftwood will speed up blockage and jamming of a check dam. Once the spillway is blocked by the driftwood the subsequent debris flows will overflow from the crest of a check dam, which will cause extensive scour downriver of a check dam. Therefore, it is also necessary to investigate the behavior of debris flows with driftwood and propose some reasonable structural or nonstructural countermeasures to mitigate the effects of debris flows with driftwood on the operation of a check dam in the future.

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224 List of symbols

- ai = The index for the dimensionless parameter (-)
- b = The width of the spillway outlet(m)
- B = The width of the spillway inlet (m)
- d_{90} = The characteristic particle size for erodible bed materials (m)
- k = The coefficient for the dimensionless equation (-)
- h_1 = The depth of debris flows at reference cross-sections #1 (m)
- h_2 = The depth of debris flows at reference cross-sections #2 (m)
- $h_{\rm d}$ = The maximum scour depth (m)

- h_w = The water head loss (m)
- g = The acceleration of gravity (m/s²)
- q = The unit discharge of the debris flow (m³/s)
- v = The initial velocity of the debris flow flowing out of the spillway(m/s)
- v_1 = The velocity of debris flows at reference cross-sections #1 (m/s)
- v_2 = The velocity of debris flows at reference cross-sections #2 (m/s)
- V = The scale of debris flow in the experiments (m³)
- x = Trajectory in the horizontal direction (m)
- y = The water elevation difference (m) Z_1 = The elevation of reference cross-sections at #1 (m)
- Z_2 = The elevation of reference cross-sections at #2 (m)
- Δz = The elevation difference between the two reference cross-sections (m)

Greek letters

- α_1 = The kinetic energy correction coefficient for v_1 (-)
- α_2 = The kinetic energy correction coefficient for v_2 (-)
- ρ_d = The density of debris flows (kg/m³)
- ρ_w = The density of clear water (kg/m³)
- ζ = The energy dissipation coefficient(-)
- η = The lateral contraction ratio(-)
- φ = The angle of the initial velocity in the horizontal direction(°)

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- **Fig. 1.** An example of foundation scour downriver of a check dam



292

(c) The structure and dimensions of the spillway (unit: mm). Four different lateral contraction ratios were considered in the experiments: (a) B=200.0 mm, b=60.0 mm, $\eta=0.7$; (b) B=200.0 mm, b=80.0 mm, $\eta=0.6$; (c) B=200.0 mm, b=100.0 mm, $\eta=0.5$; (d) B=200.0 mm, b=120.0 mm, $\eta=0.4$. The bottom of the spillway was formed by a compound curve surface (a simple curved segment and a circular segment: radius R=100.0 mm, radius angle $\delta=75^{\circ}$).

Fig. 2. Experimental setup





304 Fig. 3. The particle size distribution of samples for the debris flows and erodible bed



Fig. 4. Photograph of the LRF system (the photograph was taken in the downstream direction)



Fig. 5. An example of a debris-flow hydrograph





- 316 Fig. 6. Various debris flow patterns at different lateral contraction ratios (the pictures on the left were taken
- 317 from a downstream view)



- 320 Fig. 7. A diagram of dynamic parameters of debris flows



Fig. 8. The transverse expansion of a debris flow nappe at different lateral contraction ratios



Fig. 9. The trajectory of a debris flow nappe





(c) η =0.5, V=0.16 m³, ρ =1.50 g/cm³, b=0.10 m (d) η =0.4, V=0.16 m³, ρ =1.50 g/cm³, b=0.12 m **Fig. 10.** The shapes of the scour hole downriver of a check dam (V=0.16 m³, ρ =1.50 g/cm³) 334



Fig. 11. Comparison of scour depth at different debris-flow densities



Fig. 12. Comparison between predicted data and experimental ones

Table 1. The main parameters of the debris flow nappe for different contraction ratios

Items	(a)	(b)	(c)	(d)
Width of the outlet <i>b</i> /mm	60.0	80.0	100.0	120.0
Lateral contraction ratio η	0.7	0.6	0.5	0.4
Width of the nappe W_{Nappe} /mm	137.2	231.6	292.6	320.6
Broadening ratio $\kappa(\kappa = W_{\text{Nappe}}/b)$	2.29	2.90	2.93	2.67
Length of the nappe away from the outlet x_a/m	0.43	0.34	0.33	0.31
Length of the nappe close to the outlet x_c/m	0.25	0.21	0.21	0.18

344 Notes: B is constant for each spillway type (B =200.0 mm)

Table 2. The energy dissipation rates at different contraction ratios Scales p=0.7 p=0.6 p=0.5

Density (ρ =1.50 g/cm ³)					
Scales $\eta=0.7$	η=0.6	η=0.5	η=0.4		
66.43%	57.48%	52.34%	42.03%		
75.37%	72.94%	60.58%	67.97%		
78.08%	73.70%	63.61%	71.75%		
73.29%	68.04%	58.84%	60.58%		
	66.43% 75.37% 78.08%	η=0.7 η=0.6 66.43% 57.48% 75.37% 72.94% 78.08% 73.70%	$\eta=0.7$ $\eta=0.6$ $\eta=0.5$ 66.43%57.48%52.34%75.37%72.94%60.58%78.08%73.70%63.61%		