



1 **Development of fragility curves for railway ballast and embankment**
2 **scour due to overtopping flood flow**

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11 **Abstract**

12 Fragility curves evaluating risk of railway track ballast and embankment fill scour were developed. To develop
13 fragility curves, two well-documented single-track railway washouts during two recent floods in Japan were
14 investigated. Type of damage to the railway was categorized into no damage, ballast scour, and embankment
15 scour, in order of damage severity. Railway overtopping surcharge for each event was estimated via hydrologic
16 and hydraulic analysis. Normal and log-normal fragility curves were developed based on failure probability
17 derived from field records. A combined ballast and embankment scour model was validated by comparing the
18 spatial distribution of railway scour with the field damage record.

19

20 **Key Words:** railway embankment, fragility curve, overtopping, ballast scour, embankment scour

21

22 1. Introduction

23 Railway lines consist of components including tracks, power supply, and signaling infrastructure, all of which
24 can suffer damage during river floods, hurricane storm surge, and tsunamis, leading to interruption of
25 transportation service (see Figure 1 for two examples for damage due to surge in the USA). The most common
26 mechanism of track damage occurs when tracks are overtopped by floodwaters, leading to scouring of the
27 ballast and/or the embankment fill upon which the rail tracks are built. Even when only a short section of
28 track is washed out, the entire railway system can experience serious delays or malfunction due to a ripple
29 effect on the dispatch of engines and cars until the damaged section is repaired.

30 Since railcars (except those specialized for steep slopes like cable cars or rack railways) cannot handle
31 steep gradients in topography, railways are often built in areas of mild slopes, such as rivers, floodplains, and



32 coasts. Due to this, railway damage is a common occurrence during flood events (e.g. Changnon 2009,
33 Polemio et al. 2011, Tsubaki et al. 2012b). Furthermore, railways utilize many bridges, which are often built
34 with low clearance over waterways in order to minimize construction time, cost, and track slope. Many
35 examples exist of such bridges collapsing during large river flood and tsunami events (e.g. Wardhana and
36 Hadipriono 2003, Reed et al. 2004, Kaneko 2010).

37 As such, railways are seen to exhibit significant vulnerability when tracks are inundated or overtopped.
38 Climate change projections show that in some locations, the frequency and intensity of river flood and storm
39 surge events will increase (IPCC 2014), further exacerbating risk to railway damage due to overtopping and
40 inundation. Predictive evaluation of railway damage due to flood is essential for concrete assessment of socio-
41 economic impact of large flood events.

42 HAZUS is a software package for estimating potential losses caused by earthquakes, floods and hurricanes
43 used in the USA. Within the framework of HAZUS, a railway system consists of railway track/embankments,
44 bridges, tunnels, stations, and other facilities (FEMA 2010a, 2010b, 2010c, see Table 1 for the items accounted
45 in the flood sub-model in HAZUS). In HAZUS, damage to railway tracks due to earthquakes is evaluated
46 based on permanent ground deformation (p.7-25, FEMA 2010a), and the damage functions developed for
47 major roads are adopted for damage estimation for railway tracks/roadbeds (p.7-32, FEMA2010a). However,
48 there is no guideline to estimate damage to railway tracks due to floods or hurricanes in the HAZUS
49 framework. There have been several attempts to establish failure prediction of railway components (e.g.
50 Argyroudis and Kaynia 2014) and river embankments (e.g. Hata et al. 2015) for damage due to seismic
51 motion; however railway track/embankment fragility due to flood overtopping is not yet implemented
52 in practice (FEMA 2010b). Fundamental research on the processes responsible for railway embankment
53 failure during floods has recently begun. For example, Polemio and Lollino 2011 reported a case of
54 seepage failure of railway embankment. Tsubaki et al. 2012a experimentally investigated the process
55 and critical condition of ballast breaching.

56 In Japan, rapid population decline is another factor exacerbating risk to railways in many regions, as the
57 amount of money available for maintenance and upgrade of these railroads is shrinking together with the
58 amount of customers and goods they serve to transport. Therefore, in order to prevent the need for expensive
59 repairs after damage during future events, it is essential to evaluate which sections of railroads are most
60 vulnerable to washout during floods and to strengthen these sections before damage occurs.

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Table 1 Railway System Classifications in HAZUS (2010b)

Occupancy	HAZUS valuation in thousands of dollars
Railway Tracks (per km)	1,500
Railway Bridge (Concrete, steel, wood and unknown types)	5,000
Railway Tunnel	10,000
Railway Urban Station (Concrete, steel, wood and brick made)	2,000
Railway Fuel Facility (Tanks)	3,000
Railway Dispatch Facility (Equip)	3,000
Railway Maintenance Facility (Concrete, steel, wood and brick made)	2,800

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67 This paper focuses on fragility estimation of railway track/embankment scour due to overtopping. Even
 68 though railway embankments are geometrically similar to roadway embankments and levees, the structures
 69 atop railway embankments are very different from those atop these other embankments, as are the mechanisms
 70 by which overtopping can cause damage. As Figure 2 shows, floods can cause damage to railroad
 71 embankments via three processes: (a) scour of ballast induced by overtopping, (b) scour of both ballast and
 72 embankment fill by overtopping, and (c) piping/seepage failure of embankment fill. Though piping/seepage
 73 failure of fill is more likely to occur in high embankments, most railway embankments are relatively low, and
 74 most observed railway embankment failures appear to have been the result of overtopping-induced scour of
 75 fill and/or ballast (Kaneko 2010, Tsubaki et al. 2012b, Onoda et al. 2015). In the cases of ballast scour only,
 76 repair of the ballast layer is relatively straightforward, but in cases of embankment fill scour, repairs can be
 77 costly and take a long time. Repair of damage to an embankment is less expensive than repair of damage to
 78 bridges and other facilities (see Table 1), but ballast and embankment damage occurs much more frequently
 79 than bridge damage. Furthermore, river floods or tsunamis large enough to damage bridges usually also cause
 80 severe flooding which leads very long sections of embankment to wash out (e.g. Shimoazono and Sato 2016).
 81 Therefore, the development of fragility curves for scour of railroad ballast and embankments is crucial for
 82 assessment of railroad vulnerability and resilience.

83 Fragility curves are widely used to evaluate the vulnerability of structures in terms of probability
 84 (Shinozuka et al. 2000). This approach was initially applied for seismic damage to bridges and other structures
 85 (Shinozuka et al. 2000, Ichii 2002, Hata et al. 2015), and application to water related hazards has followed
 86 (e.g. Hall et al. 2003 for national-scale flood risk assessment, Vorogushyn et al. 2009 for embankment piping



87 failure, Suppasri et al. 2012 for building damage due to tsunami).

88 The manner in which earthquakes damage earthen embankments is relatively simple and understood, even
89 though the exact physical/dynamic properties of earth fill, especially the spatial distribution, are usually
90 uncertain. Floods, on the other hand, interact with and are controlled by the presence of embankments. There
91 are even many locations in which transportation embankments serve as de facto river and coastal levees (e.g.
92 Brammer 1990, Ueda and Nakatsuka 2014). In such a location, if a flood causes an embankment breach, the
93 flood will spread to previously protected areas. Therefore, in evaluating the risk of damage due to a railway
94 embankment breach, it's important to evaluate the effect of that breach on the spread of the flood itself.
95 Predicting the location of the railway embankment having significant potential to scour is essential to
96 precisely evaluate the effect of the embankment breaching on the flood propagation during catastrophic flood
97 events.

98 This paper investigates the conditions responsible for washout of track ballast and embankment fill for
99 single-track, unelectrified railroads, which are quite common in rural areas where the level of flood protection
100 is relatively limited. The fragility curves for this kind of railway embankment are developed based on two
101 well-documented rail track washout events during the recent floods in Japan. To develop fragility curves,
102 damage from each of these events is compared with embankment overtopping surcharge, which is estimated
103 via hydrologic and hydraulic analysis. The spatial distribution of railway embankment scour evaluated using
104 developed fragility curves is then compared with damage recorded in the field. Finally, the validity, limitations,
105 and required further research regarding the development of fragility curves for railway embankment scour are
106 discussed.

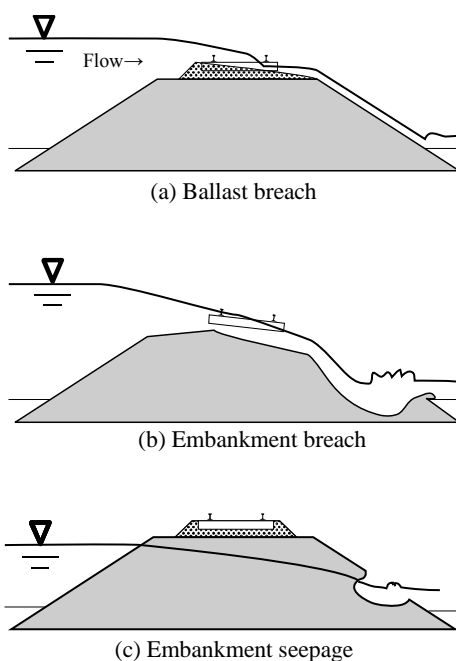
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109 Figure 1 Railway embankment scour failures (left: New Jersey Transit tracks in New Jersey, USA after
110 Hurricane Sandy in 2012; right: CSX railroad tracks in Mississippi, USA after Hurricane Katrina in 2005)

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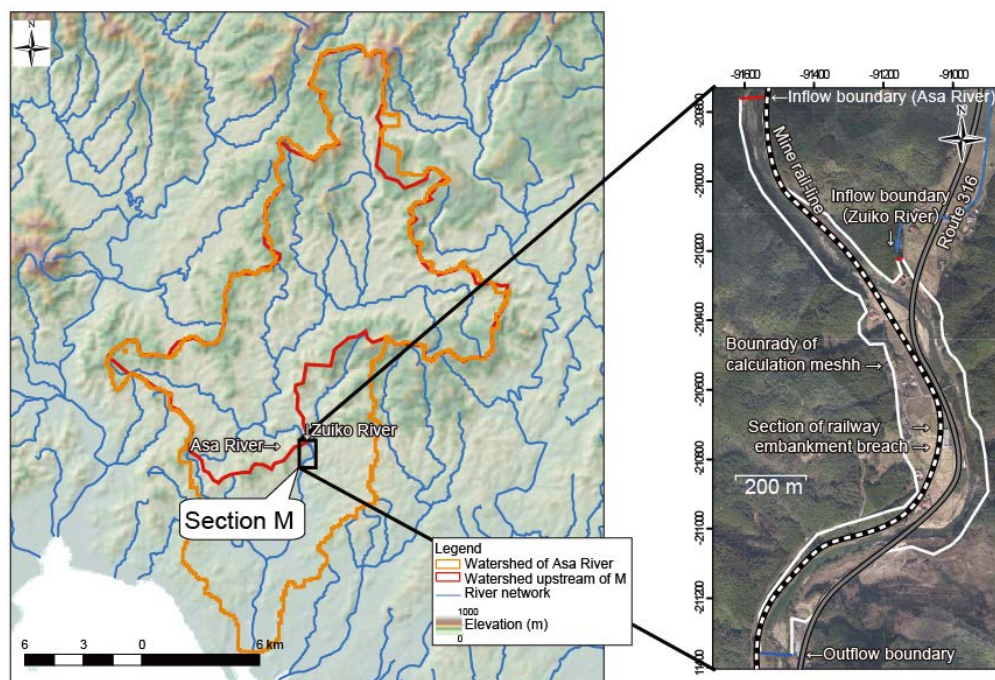
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116 2. Target events

117 2.1 Asa River flood of July, 2010

118 In June 2010, a large flood occurred in the Asa River including section M in the basin, causing inundation of
119 homes and a factory, as well as washout of a railroad embankment (Tsubaki et al. 2014). The left-hand map
120 in Figure 3 outlines the watershed upstream of section M of the Asa River in red, while the watershed of the
121 entire reach of the Asa River is outlined in orange. A hydrologic model calculated the maximum flow rate in
122 the Asa River to be 811 m³/s (personal communication with Yamaguchi Prefecture), while the inflow from
123 the Zuiko River was 110 m³/s. Though it's possible that the peak flow in each river would reach their
124 confluence at slightly different times, the same hydrologic model showed that the maximum flow at a point 3
125 km downstream of the confluence was 967 m³/s. This flow rate closely matches that calculated from high
126 water marks measured in the field. Since no major tributaries exist between the confluence of the two rivers
127 and this measurement point, flow rates of 811 m³/s for the Asa River and 110 m³/s for the Zuiko River are
128 adopted as steady inflow boundary conditions of the hydraulic model of section M.

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Figure 3 Watershed of the Asa River (left) and aerial photo of section M (right).

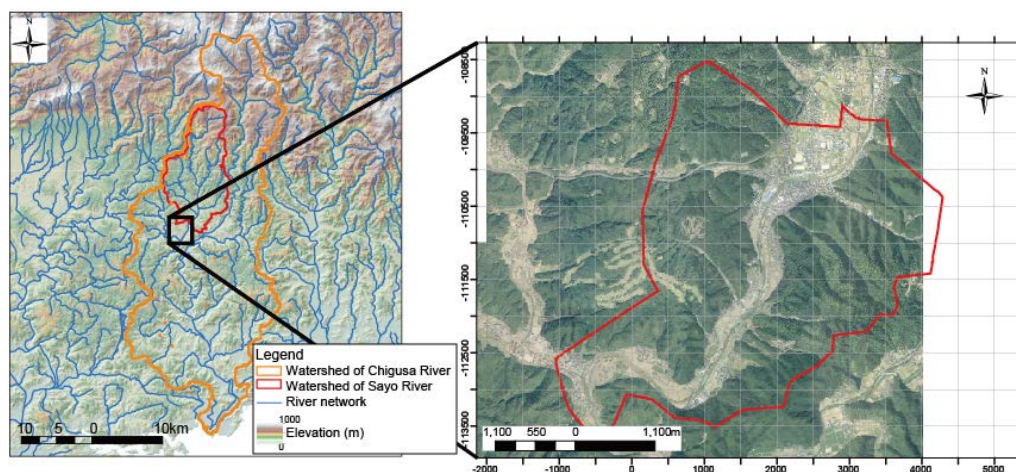
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133 2.2 Sayo River flood of August, 2009

134 On August 8-11, 2009, Typhoon Etau generated record rainfall over the mid-west region of Japan including
135 Sayo Town, Hyogo Prefecture. The previous 24-hour record rainfall in Sayo Town had been 187 mm, but
136 Typhoon Etau set a new record at 327 mm. This caused record flooding in the Chigusa River, the watershed
137 of which includes Sayo Town and much of western Hyogo Prefecture, resulting in a large number of casualties,
138 as well as extensive damage to river and slope protection works (Tsubaki et al. 2012b).

139 Figure 4 (left panel) illustrates the watershed upstream of section S of the Sayo River, together with that of
140 its primary river, the Chigusa River. Figure 4 (right panel) depicts the domain in which the hydraulic flood
141 model was evaluated. The highest flow rate that passed through here during the August 2009 storm was
142 calculated to be 750 m³/s by hydrologic and hydraulic analysis conducted in Fujita et al. 2012.

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Figure 4 Watershed of Sayo River section S (left) and hydraulic flood model domain (right).

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148 3. Methods

149 3.1 Fragility curve

150 In this paper, we use upstream flood water level (surcharge) as an explanatory variable for railway breaching
151 failures. Under the situation of water overtopping an embankment, critical flow occurs on the embankment
152 and the upstream water level correlates almost directly to the overtopping discharge. The upstream water has
153 less velocity head and the surface is relatively flat, whereas the overtopping flow atop the embankment is
154 rapidly-varied flow and quite sensitive to small differences and uncertainty in the local elevation of the
155 embankment crest. The local flow rate over complex topography (i.e., an embankment crest) estimated by an
156 inundation simulation has non-negligible uncertainty even though a fine calculation grid (one to few meters
157 spacing) was used, but the estimated upstream water level has a smaller relative uncertainty (Tsubaki and
158 Kawahara 2013). For these reasons we use the upstream water level to explain the probability of embankment
159 failure.

160 Properties of ballast, embankment fill and surface cover of the embankment vary depending on the
161 region/country/design standard of the railway being investigated, as well as on the characteristics of the
162 specific cross sections of interest. The two railway lines focused on in this paper are single-track, unelectrified
163 railroads running through mountainous regions, and which started operation about 90 years ago. In this regard,
164 the material properties of the railways are relatively homogeneous.

165 In the fragility curve approach, a probabilistic damage function can be expressed by a two parameter normal



166 distribution function (Shinozuka et al. 2000, Suppasri et al. 2012),

$$167 \quad F(a) = \Phi \left[\frac{a - \mu}{\sigma} \right] \quad (1)$$

168 or log-normal distribution function

$$169 \quad F(a) = \Phi \left[\frac{\ln(a/c)}{\zeta} \right] \quad (2)$$

170 where $F(\)$ represents the conditional probability of occurrence for the specific state of damage; Φ is the
171 normal error function; a represents the hazard level; μ and σ are the median and standard deviation of hazard
172 level; and c and ζ are the median and log-standard deviation, respectively. The deviation parameters σ or ζ
173 represent both uncertainty in hazard level a and variation in fragility among data points. The estimation of
174 the two model parameters (median and deviation) is carried out by maximizing the likelihood function. The
175 likelihood function for binary damage (damage / no damage) is

$$176 \quad L = \prod_{i=1}^N [F(a_i)]^{x_i} [1 - F(a_i)]^{1-x_i} \quad (3)$$

177 where a_i is the damage level (overtopping water depth in this study); $x_i=1$ or 0 indicates embankment breach
178 or no breach, respectively, under the corresponding damage level; and N is the total number of case histories.

179

180 3.2 Railway damage record

181 3.2.1 Asa River flood of 2010

182 Locations of ballast and embankment fill scour are determined by investigating photos taken from the factory
183 beside the railway (personal communication with the factory and downloaded from the internet) as well as
184 aerial photos of the area obtained in February 2012.

185

186 3.2.2 Sayo River flood of 2009

187 Kaneko (2010) reported damage to the railway as a function of kilometer post along the track. Site survey
188 data (personal communication with I. Ario), photos from the internet, and aerial photos from October 2009
189 (immediately after the flood) were also utilized to detail damage along the length of the section of railway.

190

191 3.3 Estimation of overtopping water stage

192 3.3.1 Hydraulic model for flood flow simulation (Tsubaki et al. 2012b)

193 The river and floodplain flows were calculated by solving the shallow water equations. The basic equations solved
194 here are as follows:

$$195 \quad \frac{\partial U}{\partial t} + \frac{\partial E}{\partial x} + \frac{\partial F}{\partial y} = S \quad (4)$$



$$\begin{aligned}
 U &= (h \quad hu \quad hv)^T, \\
 E &= (hu \quad hu^2 + 0.5gh^2 \quad huv)^T, \\
 F &= (hv \quad huv \quad hv^2 + 0.5gh^2)^T, \\
 S &= (q_s \quad gh(S_{0x} - S_{fx} - S_{Hx}) \quad gh(S_{0y} - S_{fy} - S_{Hy}))^T.
 \end{aligned} \tag{5}$$

where t is the time, x and y are the horizontal coordinates, h is the water depth, u and v are the depth-averaged velocities in the x - and y - directions, g is the gravitational acceleration, q_s is the source water mass due to rainfall, S_{0x} and S_{0y} are the bed slopes in the x - and y - directions calculated using the ground elevation z as

$$S_{0x} = -\frac{\partial z}{\partial x}, S_{0y} = -\frac{\partial z}{\partial y}. \tag{6}$$

S_{fx} and S_{fy} are the friction slopes evaluated by using the Manning's roughness coefficient n as follows.

$$S_{fx} = \frac{n^2 u \sqrt{u^2 + v^2}}{h^{4/3}}, S_{fy} = \frac{n^2 v \sqrt{u^2 + v^2}}{h^{4/3}}. \tag{7}$$

S_{Hx} and S_{Hy} are the energy slope due to the bridge with piers. These terms are effective only at the cell interface located in the bridge cross-section.

$$S_{Hx} = -\frac{\partial H_b}{\partial x}, S_{Hy} = -\frac{\partial H_b}{\partial y} \tag{8}$$

where H_b is the head loss due to the bridge. The amount of head loss was calculated by using D'Aubuisson's empirical formula (Chow 1959, Sakano 2003, Tsubaki et al. 2012b).

The equations were solved by means of the finite volume method on an unstructured triangular grid. The flux difference scheme (FDS) was used to evaluate fluxes through the boundaries of each triangular cell.

210

211 (a) Sayo River model (Tsubaki et al. 2012b)

212 The domain represented in the inundation simulation (Figure 4, right panel) was about 15 km² in area. The
 213 Sayo River flows through this section, and no major tributaries are present here. Elevation data for the
 214 calculation grid was configured using aerial LiDAR (Light Detection and Ranging) for the riverside region,
 215 and a 50-m grid DEM (Digital Elevation Model) was utilized for the intermountain area. A comparatively
 216 small grid size (3 m for the length of a side of a triangle) was used around the river and the railway to represent
 217 the details of the topography (Bates et al. 2003, Cobby et al. 2003, Rath and Bajat 2004). In the mountain
 218 area, a larger grid size (40 m in length) was used to reduce computational load. Manning's roughness
 219 parameter n was set to 0.02 for the river bed and the floodplain, 0.1 for vegetated areas of the river course
 220 and floodplain as well as for residential areas, and 0.3 for mountainous areas. The discharge estimated by
 221 using a hydrological model with the ground rain gauge data (Fujita et al. 2012) was used as the inflow
 222 boundary condition. The rating curve at the outflow cross-section was estimated and the flow rate at the
 223 outflow cross-section calculated by the hydrological model was converted to water stage. The source term in



224 the mass conservation equation (q_s in Equation (5)) represents the precipitation in this area; the observed gross
225 precipitation is multiplied by a runoff ratio of 0.85 to account for the amount of net surface runoff in this area.

226

227 (b) Asa River model

228 Due to the short length of the river reach (2 km) focused on in this study, and the relatively steep riverbed
229 slope (1/240), the flood was evaluated using a steady peak flow simulation. The inflow rates, based on the
230 flow simulation conducted by Yamaguchi Prefecture, were used as constant inflow boundary conditions for a
231 2-dimensional unsteady flow model. Resolution of the triangular mesh was 2 m in the area of railway
232 embankment fill, and 5 m elsewhere. Manning's n was set to 0.03 in the river channel and floodplain, and 0.1
233 in vegetated and built-up areas. This river channel roughness equals that used by Yamaguchi Prefecture in
234 historical analyses. The downstream boundary condition was water level as determined by Yamaguchi
235 Prefecture's calculation (personal communication).

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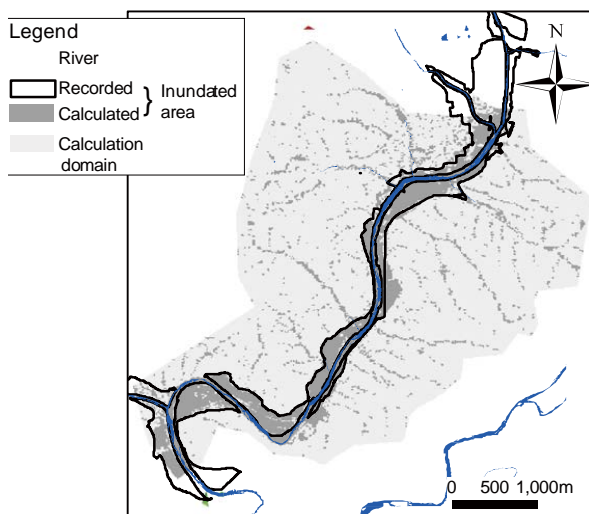
237 3.3.2 Validation of inundation flow models

238 To validate the inundation flow models, calculated results are compared with inundation records.

239 (a) Sayo River model

240 As shown in Figure 5, the calculated inundation area corresponds closely to the recorded inundation area. In
241 Figure 6, calculated and recorded inundation water stages and water depths are compared. The calculated
242 water stage is represented by $h + z$. The mean absolute error is 0.28 m, and the magnitude of the error is
243 smaller than, but comparable to, the magnitude of inundation water depth, 1 m.

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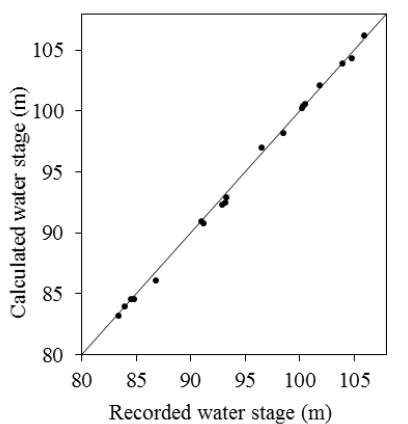


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Figure 5 Comparison of calculated and recorded inundated areas (Tsubaki et al. 2012b).

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248

249

Figure 6 Comparison of calculated and recorded flood stages and depths (Tsubaki et al. 2012b).

250

251 (b) Asa River model

252 Water levels hindcast by the flood simulation are compared with measured water level traces from two
253 locations (Figure 3). Steady flow boundary conditions were used for model inflow and outflow, though the
254 presence of vortices over the floodplain and near the riverbanks prevented perfectly steady flow from forming.

255 Due to these fluctuations, modeled water levels were assessed via both 20-minute running averages
256 representing each minute of model output, as well as maximum water levels during these same intervals.

257 Flood elevation trace #1, on the inner wall of the factory, was measured to be 25.98 m. The average modeled



258 flood elevation here was 25.79 m, and the maximum modeled flood elevation at this location was 25.90 m.
259 At location #2, the recorded trace elevation was 25.81 m, model average elevation was 25.61 m, and model
260 maximum elevation was 25.67 m. Modeled average elevation is about 19 cm too low, and maximum elevation
261 is about 11 cm too low, compared to measured trace elevations.

262

263 (c) Uncertainty in flood water stage

264 According to the benchmarking of a two-dimensional high-resolution (~2 m grid spacing, LiDAR topography
265 based) urban flood model reported by Hunter et al. (2008), the uncertainty in predicted water level among six
266 hydraulic models was assessed as 0.05 m. This is same order of RMSE error in the terrain data they used.

267 The difference between calculated and recorded water stages in our simulation was 0.1~0.3 m, and
268 this is larger than the water level uncertainty estimated by numerical models reported by Hunter et al. (2008).
269 This discrepancy may be related to larger inaccuracy in the LiDAR data we used due to very uneven terrain
270 and quite complex surface cover, including rails on the railway embankment and vegetation cover on the
271 embankment slope. Moreover, there is a difference in the definitions of calculated and recorded water depths,
272 namely the calculated water depth is a cell averaged quantity but the recorded water depth denotes the local
273 water depth around obstacles; this caused an underestimation of the calculated water depth as shown on the
274 right side of Figure 6.

275 In summary, the magnitude of uncertainty in flood water stage in this study was non-negligible but
276 inevitable in practice because of the complexity of the topography and uncertainty in the topographic data
277 available. The fragility curve concept can account for the uncertainty in the explanatory variable, surcharge
278 water depth in this study. The effect of uncertainty in water level prediction on the fragility curve will be
279 discussed later.

280

281 4. Results

282 The difference between H and the elevation z of the railroad track is surcharge Δh , which is correlated with
283 the recorded state of damages categorized into “no damage”, ballast scour and embankment scour
284 (Appendix), and fragility curves were developed based on this correlation. Both upstream water depth H
285 and rail track elevation z are derived from the cell-averaged quantities used in the model described in
286 section 3.3.

287 The elevation of water overtopping the tracks was taken as water surface elevation H averaged over
288 a 2 m diameter area at a distance of 5 m from the center line of the tracks. For the generation of fragility
289 curves “no damage” was defined as cases where the model result showed the tracks were indeed overtopped

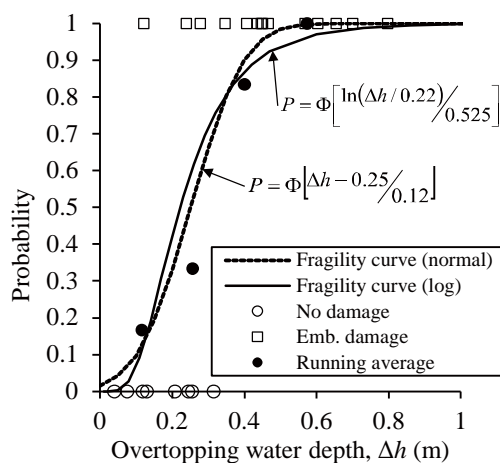


290 but where no damage was observed in reality. Accordingly, the point where neither overtopping was observed
 291 nor track damage was recorded was excluded. As such, 10 data points were obtained for the Asa River, and
 292 24 data points for the Sayo River.

293 Figure 7 displays the fragility curves for the embankment fill scour using the normal distribution
 294 (depicted by the dashed line and the log-likelihood = -7.3) and the log-normal distribution (the solid line and
 295 log-likelihood = -7.9) resulting from data points at which either no damage (the number of sample was $n=8$)
 296 or embankment fill scour ($n=16$) were observed. In Figure 7, open symbols represent individual data points,
 297 while filled figures represent overtopping surcharge and damage data which have been put through a 5-point
 298 running average after ordering by surcharge. Though both normal and log-normal distribution models (solid
 299 and dashed lines, respectively) represent well the trend of damage probability based on the field record (filled
 300 circles), the normal distribution has a slightly better fit.

301 Figure 8 shows a normal fragility curve for ballast scour (dashed line, log-likelihood = -2.6) and a
 302 log-normal curve for the combination of ballast and embankment scour (thick line, log-likelihood = -8.9). For
 303 the case of ballast scour, the fits of the normal distribution and the log-normal distribution were almost
 304 identical. As shown in Figure 8, the fragility curve for ballast scour has a larger mean and smaller standard
 305 deviation compared with the curve for embankment scour and the curve for combined ballast and embankment
 306 scour. The failure probability at medium surcharge depth $0.2 \text{ m} < \Delta h < 0.6 \text{ m}$ for the combined ballast and
 307 embankment scour is slightly larger than the probability for embankment scour only.

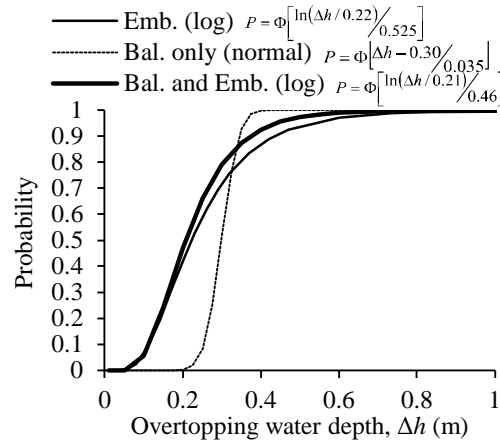
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310 Figure 7 Fragility curves for embankment scour damage described by normal and log-normal distributions.

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312

313 Figure 8 Fragility curves for ballast scour (Bal. only), embankment scour (Emb.) and
 314 embankment scour (Bal. and Emb.)

315

316 5. Discussion

317 5.1 Consistency in lower limit of failure probability with experimental result

318 Ballast damage is a transitional type of damage, falling between "no damage" and embankment fill scour in
 319 its severity. The number of samples with ballast damage available in this study is limited ($n=7$) because this
 320 type of damage occurred in between sections with embankment fill scour and "no damage". During a full-
 321 scale experiment of ballast scour (Tsubaki et al. 2012a), steady scour was observed beginning at a flow rate
 322 per unit length of $q_c=0.045 \text{ m}^2/\text{s}$. Figures 7 and 8 show surcharge depth on the x-axis, but there is a relation
 323 between surcharge depth and overtopping flow rate. By adopting the broad-crested weir concept, the
 324 overtopping discharge per unit length can be estimated as

325
$$q = \alpha \Delta h^{3/2} \quad (9)$$

326 where $\alpha = 2.46$ to 3.47 and Δh is the surcharge water depth above the weir crest (Chow, 1959). Using
 327 equation (9) and $\alpha = 2.46$, the overtopping water depth is converted to the overtopping flow rate per unit
 328 length in Figure 9. In this figure, the critical flow rate for ballast scour is depicted as a vertical dashed
 329 line. This critical flow rate corresponds well to the initial rise of the log-normal fragility curve for
 330 embankment and ballast scour. The agreement of the initial rise of the fragility curve of
 331 embankment/ballast scour and critical flow rate to initiate ballast scour indicates that railway
 332 overtopping damage begins with ballast scour and progresses to embankment scour. This also implies
 333 that the critical flow rate for initiation of ballast scour based on the full-scale experiment of ballast
 334 scouring conducted by Tsubaki et al. (2012a) can be used as a critical condition for initiation of railway



335 ballast damage in the field.

336

337 5.2 Upper limit of failure probabilities

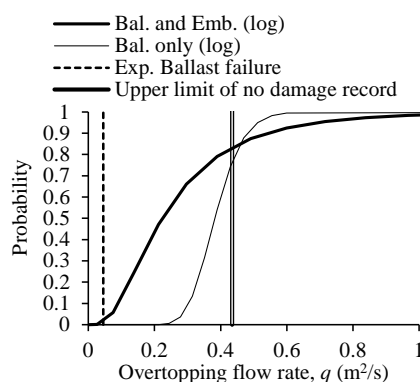
338 The upper limit of the overtopping flowrate at which no-damage was observed in the assessment in
339 previous sections is depicted as a double line in Figure 9. The damage probability is almost identical for
340 both models at this upper limit. Above this flow rate, the probability of combined ballast and
341 embankment scour increases slowly due to the assumed shape of the distribution and uncertainty at lower
342 flow conditions ($q < 0.2 \text{ m}^2/\text{s}$ and $\Delta h < 0.2 \text{ m}$). Actually, an overtopping flow rate of $0.5 \text{ m}^2/\text{s}$
343 (corresponding to a surcharge of 0.4 m) is quite an intense flow from the viewpoint of earthen
344 embankment overtopping, and it is very unlikely that no scour will occur during such an intense flow.

345

346 5.3 On the deviation of probabilities

347 In Figure 8, the fragility curve for ballast scour has a median surcharge of $\Delta h = 0.29 \text{ m}$, and its variance $\sigma =$
348 0.035 m is smaller than those for the embankment scour model and the fragility curve for combined damage.
349 It must be kept in mind that the LiDAR topography used in the flood model has a RMSE on the order of 0.1
350 m , and the uncertainty in hindcast flood levels was on the order of 0.2 m , so the standard deviation $\sigma = 0.035$
351 m of the ballast scour model is very small compared with expected uncertainty in the estimated surcharge
352 level. The experiment of Tsubaki et al. (2012a) showed ballast scour to begin at $q_c = 0.045 \text{ m}^2/\text{s}$, which is an
353 order of magnitude smaller than the median ($q = 0.4 \text{ m}^2/\text{s}$) or lower limit ($q = 0.25 \text{ m}^2/\text{s}$) of the fragility curve
354 for ballast scour shown in Figure 9. Therefore, it appears the calculated fragility curve for ballast breach in
355 this study may overestimate the condition experimentally evaluated in Tsubaki et al. (2012). This may partially
356 be explained by the fact that the ballast embankment in the field had been consolidated due to periodical
357 loading by railcars, and because actual ballast may have greater resiliency than in the experiment conducted
358 by Tsubaki et al. (2012a). Even so, ballast should be more vulnerable to overtopping scour than embankment
359 fill is, but the fragility curves shown in Figure 9 did not correspond to such a relation. It is also possible that,
360 in the field cases studied, ballast scour at smaller overtopping flowrates always coincided with combined
361 ballast and embankment scour, not ballast scour alone. Future work is needed to improve the fragility curve
362 for ballast scour by acquiring more sample data points in the field and running more hydraulic experiments.

363



364

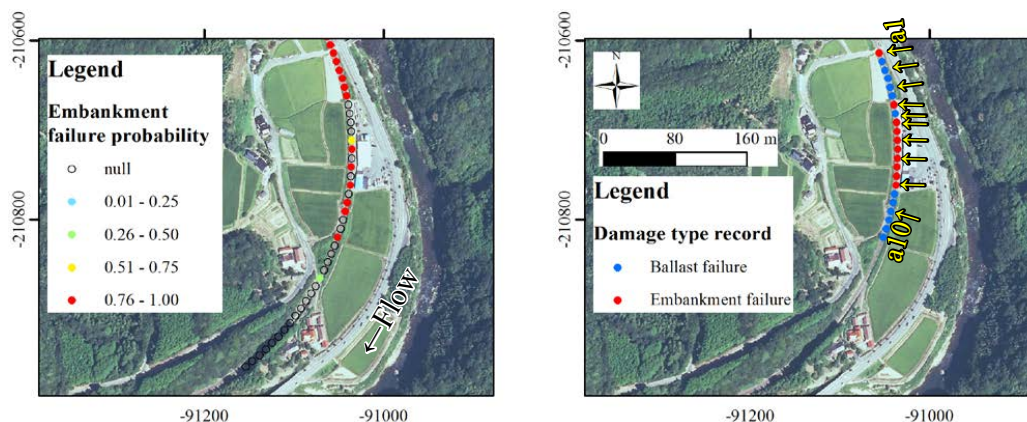
365 Figure 9. Fragility curve for ballast failure using overtopping flow rate per unit length. The dashed line
366 indicates the experimental bound at which the onset of ballast scour occurs (Tsubaki et al. 2012a). The
367 double line corresponds to the upper limit of the flow condition where no-damage was observed.

368

369 5.4 Validation of railway fragility curve

370 A validation of the combined damage fragility curve, of which feasibility was discussed in sections 5.1 to 5.3,
371 was conducted by comparing its calculated probabilities to the actual damage record. The log-normal
372 distribution for ballast and embankment scour was determined to be the most feasible model. Via the model,
373 the failure probability along the rail-track in the Asa River floodplain at 10 m intervals was calculated and
374 plotted in Figure 10 (left). Failure probability in Figure 10 (left) is calculated without regard to type of failure
375 (embankment fill or ballast), but is calculated with the lumped damage curve; however, the actual damage
376 record of the right figure distinguishes the type of damage. In Figure 10, there is variability in the calculated
377 result, but it generally agrees with recorded damage. The points at which no damage was calculated are points
378 at which the flood model calculated either a very shallow overtopping surcharge, or no overtopping at all. The
379 railway crest in this section is almost horizontal, with little large-scale topographic variation. Since the crest
380 of the railway embankment consists of both rail and railway ties (sleepers), the 1 m² resolution LiDAR data
381 cannot resolve this, and the 1.7 m² triangular mesh carries forward this variation, leading to an unavoidable
382 difference between modeled and actual topography. Since actual railroad crest elevation does not experience
383 spurious variations at 10 m intervals, topography based on LiDAR data of limited resolution and accuracy
384 might be improved by application of a spatial filter along the railway.

385



386
387 Figure 10 Estimated damage probability (left) and damage record (right) at Asa River section M. The yellow
388 symbols in the right map depict data points listed in Table A.1.

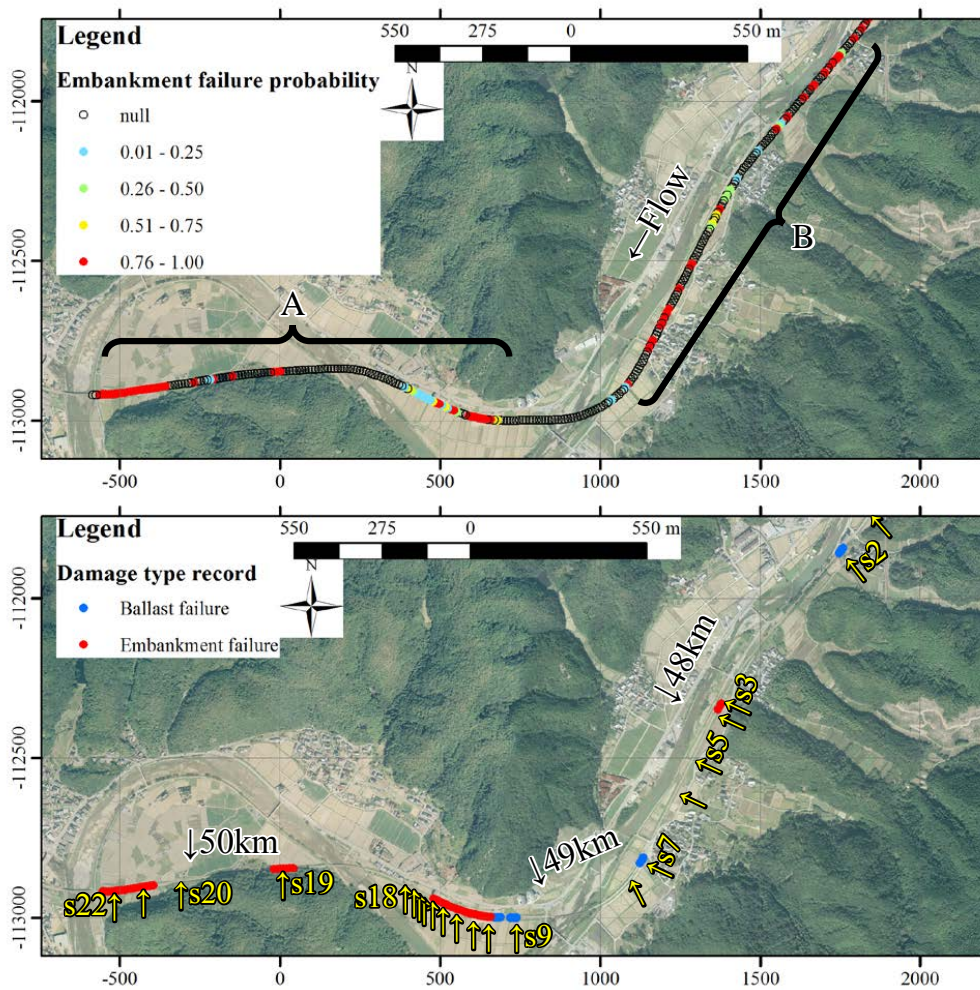
389

390 Figure 11 shows calculated and observed damage to the railway along the Sayo River. The domain is
391 decomposed into two segments (A and B) in the discussion below. Continuous damage was recorded along a
392 portion of Segment A, and this damage was reproduced well in the fragility curve calculation. In this segment,
393 damage occurred in locations at which relatively steep slopes existed in the railway crest elevation profile
394 (Figure 12). Since the locations of railway embankment overtopping were governed by longitudinal slope of
395 the railway and large-scale topography in this segment A, the flood model was able to simulate actual
396 overtopping location and flow rate with good accuracy, and damage probability resulting from the fragility
397 curve matched recorded damage well. In Segment B, estimated damage probability was high at points that
398 experienced actual damage, but many other points with high damage probability experienced no actual
399 damage. In regions such as this, where spatially sporadic damage is calculated, fragility curves are still useful
400 for predicting whether damage will occur, but they cannot predict the specific locations at which the damage
401 should be expected. In this segment, elevation of the railway embankment crest was very smooth, with no
402 steep slopes in crest elevation. Therefore, the entire segment was overtopped with shallow surcharge. However,
403 small errors in topography at the size of each model grid cell caused errors in the overtopping surcharge depth,
404 resulting in different damage probabilities at the 10 m intervals at which damage was assessed. The fragility
405 curve concept can also account for uncertainty in hazard level; in segments within which sporadic damage is
406 predicted, the level of damage can be estimated by averaging the damage predicted for points within the
407 segment. However, the reason damage in Segment B of Figure 11 was not evaluated as such an average is that
408 the error in grid-scale model topography was too large to just cause variations in overtopping surcharge depth;
409 rather, the error caused many points within the segment to not experience any overtopping at all. Therefore,



410 the model predicted scattered damage for Segment B.

411



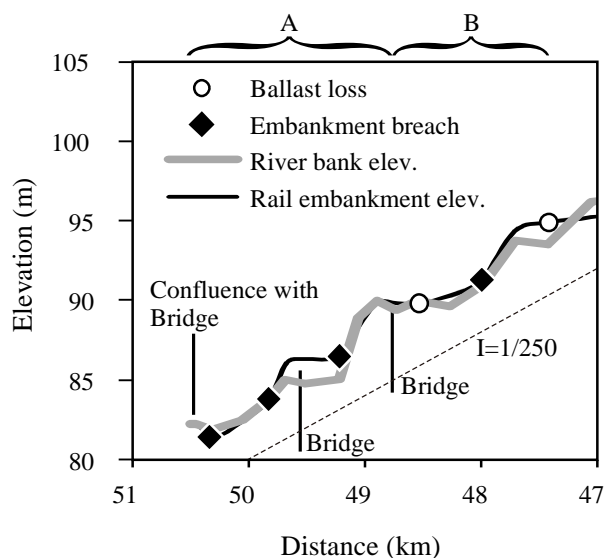
412

413 Figure 11 Estimated damage probability (top) and damage record (bottom) at Sayo River section S. The

414

yellow symbols in the bottom figure depict data points listed in Table A.2.

415



416

417 Figure 12 Longitudinal profiles of railway and riverbank elevation. The cross-sections where the river and
418 railway intersect are indicated as 'bridge' (Tsubaki et al. 2012b).

419

420 6. Conclusion

421 This paper shows the significance of evaluating the likelihood of damage to railway embankments due to
422 overtopping. Fragility curves were developed to relate damage probability to overtopping surcharge depth,
423 itself calculated via the use of a hydraulic flood model. Fragility curves were generated based on recorded
424 observations of railway damage types, simulated overtopping surcharge and types of curve. Each fragility
425 curve was validated by comparison between modeled damage probability and records of observed damage.
426 The fragility curve for ballast scour, the least serious type of damage investigated, did not match the criteria
427 revealed through laboratory experiments of ballast scour, and may underestimate actual damage probability.
428 However, the fragility curve for combined damage including embankment fill and ballast scour well represents
429 the laboratory experiment result for the onset of scour. Field validation of the combined damage fragility
430 curve was carried out by comparing modeled damage probability with recorded damage at two different river
431 sections. At one location, where recorded damage indicated continuous railway washout over stretches,
432 fragility curve damage probability agreed with observed damage quite well. On the other hand, the model did
433 not well represent observed damage in locations of relatively flat and level railway crest, where variations in
434 the simulated overtopping surcharge depth were affected by small errors in the topographic data, resulting in
435 sporadic flood overtopping where no damage existed in reality.

436 Though the fragility curves developed here are useful for estimation of damage probability for



437 single-track non-electrified railroad embankments, the limited number of data points used to generate these
 438 curves prevents them from being applicable to a variety of situations. To make these curves more robust, more
 439 field records are needed in different types of environments. Furthermore, the fit of modeled ballast scour
 440 probability to observed ballast damage was unsatisfactory, indicating the necessity for further laboratory
 441 experiments and field data collection. In addition, the role of small errors in the hydraulic flood model result
 442 on predicted damage probability has become clear, and the application of spatial filtering to improve model
 443 accuracy needs to be investigated in the future.

444

445 Appendix

446 Table A.1 Pointwise estimated overtopping water depth Δh and damage record for the Asa River flood. (In
 447 status row, emb: embankment breaching, bal: ballast breaching and no: no damage, accordingly.)

point	calc z(m)	calc H(m)	Δh (m)	status
a1	26.89	27.36	0.47	emb
a2	26.94	27.35	0.41	bal
a3	26.94	27.35	0.41	bal
a4	26.90	27.35	0.45	emb
a5	26.99	27.34	0.35	bal
a6	27.00	27.35	0.35	emb
a7	26.94	27.35	0.41	emb
a8	26.90	27.35	0.45	emb
a9	26.91	27.35	0.44	emb
a10	26.93	27.34	0.41	bal

448

449

450 Table A.2 Pointwise estimated overtopping water depth Δh and damage record for the Sayo River flood.

point	calc z(m)	calc H(m)	Δh (m)	status
s1	95.56	95.88	0.31	no
s2	94.96	95.30	0.34	bal
s3	91.55	91.83	0.28	emb
s4	91.12	91.36	0.24	emb
s5	90.85	90.98	0.13	no
s6	90.50	90.98	0.48	no
s7	89.88	90.37	0.49	bal
s8	89.85	90.10	0.25	no
s9	87.65	87.93	0.28	bal
s10	87.37	87.94	0.57	emb
s11	85.82	87.27	1.46	emb
s12	86.04	87.35	1.31	emb
s13	86.52	87.31	0.80	emb
s14	86.36	86.48	0.12	emb
s15	86.17	86.21	0.04	no
s16	86.24	86.31	0.08	no
s17	86.16	86.27	0.12	no
s18	82.34	82.55	0.21	no
s19	81.87	82.57	0.70	emb
s20	82.31	82.55	0.25	no
s21	81.91	82.57	0.66	emb
s22	81.96	82.56	0.60	emb

451



452

453

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461

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