



## 1 Title: Using spatial Markovian chain for the statistical analysis of seismic occurrences

## 2 in the Azores Region

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20



21 **Abstract**

22 The objective of this paper is to study the spatial sequence of the epicentral locations of  
23 seismic occurrences (Space variable) in the Azores region. In a previous investigation  
24 based on geological considerations and statistical criteria that addresses the existing  
25 historical and instrumental information, the epicentral locations were assigned to seven  
26 seismic zones.

27 This paper focuses on the analysis of occurrences in the seven seismic zones using  
28 Markovian chains.

29 The probability of occurrence of an earthquake in one of the seven adopted zones is  
30 estimated, revealing great differences among the seismic zones.

31 Additionally, the one-step transitions of this variable (seismic zone for the next  
32 occurrence in time) are explored and show an evident dependence between consecutive  
33 earthquake locations. Assuming that the process is stationary, N-step transitions are also  
34 discussed. Based on the developed Markovian model, this study also simulates the  
35 sequence of epicentral zones where occurrences can take place, which is an important  
36 component of modelling the entire process of seismic occurrences in the Azores region.

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40 **1 Introduction**

41 The aim of this study is to estimate the probability of occurrence of an earthquake in  
42 each of the seven distinct seismic zones in the Azores region (as explained later) based  
43 on the existing historical and instrumental information and also on geological data with  
44 special emphasis on spatial location “memory”. This goal also includes evaluation of  
45 the influence of the location of an earthquake on the location of the next earthquake,  
46 i.e., the first order (or one-step) dependence of the Space variable. N-step transitions are  
47 also analyzed, and Markovian chains are applied for this purpose.

48 This study also simulates the sequence of epicentral seismic zones where occurrences  
49 can take place, which is an important component of the entire process of seismic  
50 occurrences in the Azores region and a topic of ongoing study.

51 Traditionally, seismic phenomena have been described using Poisson models, but these  
52 models do not have “memory”, a fact that contradicts the reality.

53 After an earthquake, it is common to ask where the next earthquake will occur. This  
54 study attempts to give a statistically sound answer to this question.

55 The Azores Archipelago is renowned due its intense seismicity, a characteristic that can  
56 be explained by its location at the triple junction of the Mid-Atlantic Rift, where the  
57 Eurasian, Nubian, and American Plates meet. The consequent seismic activity in this  
58 region is the result of the existence of active complex geological structures such as rifts,  
59 trenches, volcanoes, banks and faults.

60 This intense seismic activity has been studied by several authors, including Bezzeghou  
61 [et al. \(2008\)](#), Borges [et al. \(2008\)](#), Carvalho [et al. \(2001\)](#) and Nunes [et al. \(2000\)](#). Other  
62 authors such as Kagan [et al. \(2010\)](#) and Reiter (1991) also studied this particular region.



63 The Azores Archipelago consists of nine islands distributed among three different  
64 groups: the islands of Flores and Corvo, which constitute the Western Group; the  
65 islands of Terceira, Graciosa, São Jorge, Faial and Pico, which are components of the  
66 Central Group; and the islands of São Miguel and Santa Maria that form the Eastern  
67 Group.

68 Modelling of natural phenomena, especially seismic processes, is a complex task that  
69 has been attempted by several authors in different areas of the world. As examples,  
70 Nanjo et al. (2011) presented selected models for Japan that are still undergoing testing  
71 and development. Other authors focused on tectonic aspects, such as Burford et al.  
72 (2000), who built a 3-D subsurface model, and still others have focused on prediction of  
73 damages caused by earthquakes (Sopra and Patrizi 1987) to better understand  
74 consequences to building

75 Other models appeal to “memory” such as Markovian models, but these models have  
76 not experienced great development. Kirimidjian and Anagnos (1984) first attempted to  
77 implement such models in the framework of California, but these studies were restricted  
78 to the same seismic region, and the results obtained were never transposed to practice.

79 Memory is present in several natural phenomena and is an important aspect in  
80 simulation of natural processes that are not independent. For example, Russo and Soares  
81 (2014) used conditional space simulations in the context of urban air pollution  
82 forecasting.

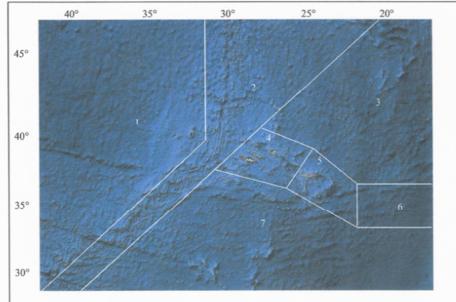
83 Recently, Cavers and Vasudevan (2015) presented a space-time Markovian chain to  
84 represent a global model for earthquakes sequences. These researchers recognized that  
85 the sequence of epicenters has “memory”, and this fact is of fundamental importance.



86 We aim to estimate the probability of earthquake occurrence in a target seismic zone  
87 using knowledge of the seismic zone of the previous event. The process can be repeated,  
88 thus allowing the simulation of the sequence of seismic locations.  
89 Cavers and Vasudevan (2015) used a different methodology for macro-earthquake  
90 zonation (i.e., active continent, trenches, etc.,) and applied weights for the state-to-state  
91 transition probabilities.  
92 Each earthquake occurrence can be characterized by the three variables of Time, Size  
93 and Space. The variable Time (Dt) is defined by the time intervals between consecutive  
94 events, the variable Size (S) is the Richter magnitude ( $M_L$ ) associated with an  
95 earthquake, and the Space variable (Sp) represents the zone in which the epicenter of  
96 the earthquake is located.  
97 Rodrigues and Oliveira (2013) defined 7 distinct seismic zones in the Azores Region  
98 based on statistical and geological information and verified that the magnitude and time  
99 between consecutive earthquakes differ significantly among these seismic zones. Figure  
100 1 shows the seven defined zones together with the epicenter locations.

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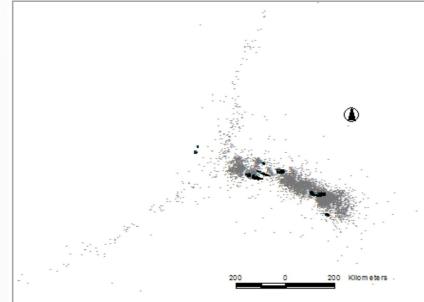
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**Fig. 1** (a) Schematic representation of the 7 defined seismic zones proposed by  
109 Rodrigues and Oliveira (2013), (b) Epicentral locations.

110



111 This 7-zone definition is adopted in this work, and the Space variable is represented as  
112  $Sp \in \{1, 2, 3, 4, 5, 6, 7\}$ .

113

## 114 **2 Data**

115 For the Azores region, the available data are collected from two different sources. The  
116 catalogue of Nunes et al. (2004) is the source of data for the period 1915-1998, and for  
117 the period 1999-2011, the data are directly obtained from the site of Instituto Português  
118 do Mar e da Atmosfera (I.P.M.A. - 2011).

119 The first period covers the area encompassed by longitude  $11.50^\circ$  W –  $42.86^\circ$  W and  
120 latitude  $10.80^\circ$  N –  $47.54^\circ$  N. A total of 9214 records are available, of which 5456  
121 contain information on magnitude according to the Richter scale ( $M_L$ ).

122 The catalogue of the second period covers an area delimited by longitude  $21.31^\circ$  W –  
123  $35.42^\circ$  W and latitude  $34.3^\circ$  N –  $45.57^\circ$  N containing 9608 events, all of which contain  
124 magnitude information ( $M_L$ ).

125 A total of 18822 seismic records are available with information on Time and Space,  
126 15064 of which contain information on magnitude according to the Richter scale.

127 Data are not constrained to “completeness of data for the low magnitude values” or to  
128 “filtration of aftershocks”.

129

## 130 **3 Methodology**

131 The current study is performed in the following stages:

132 1. The Space variable is characterized ~~among~~ the seven defined seismic zones,  
133 and the main statistics of  $Sp$  are determined.

134 2. The “memory” effect is analyzed. The influence of the seismic zone of an  
135 earthquake ~~in~~ the location (seismic zone) ~~on~~ the next seismic event is quantified



136 by estimating the conditioned probability of occurrence of an event in each one  
137 of the seven seismic zones and knowing the location of the epicenter (seismic  
138 zone) of the last occurrence. This step includes the definition of seven statistical  
139 conditioned distributions:

140  $P [ Sp_{t+1} = i | Sp_t = 1 ],$

141  $P [ Sp_{t+1} = i | Sp_t = 2 ],$

142  $P [ Sp_{t+1} = i | Sp_t = 3 ],$

143  $P [ Sp_{t+1} = i | Sp_t = 4 ],$

144  $P [ Sp_{t+1} = i | Sp_t = 5 ],$

145  $P [ Sp_{t+1} = i | Sp_t = 6 ],$

146  $P [ Sp_{t+1} = i | Sp_t = 7 ], i \in \{1, 2, 3, 4, 5, 6, 7\}.$

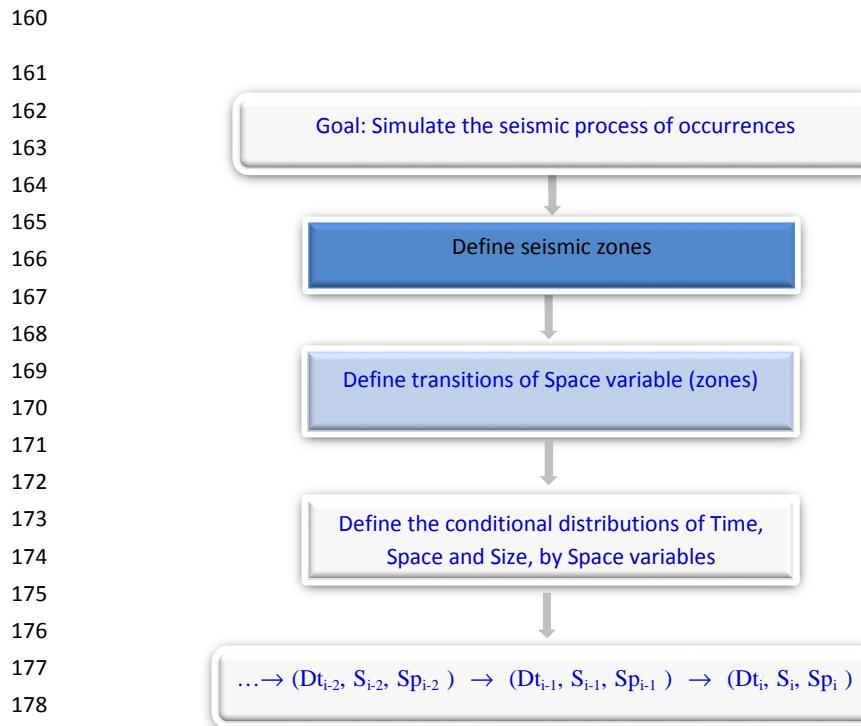
147 These formulations represent the “one-step” transition probabilities. The “N-  
148 step” transitions are also referred.

149 3. Assuming that the sequence of epicentral locations is stationary in time, a  
150 simulation model for the Space sequence is built and generated according to the  
151 corresponding  $P [ Sp_{t+1} = j | Sp_t = i ], i, j \in \{1, 2, 3, 4, 5, 6, 7\}.$

152 To evaluate the quality of the generated Space sequence, samples of generated  
153 sequences are compared with the Space data using goodness-of-fit statistical  
154 tests.

155

156 This methodology is a component of an ongoing study for modelling the seismic  
157 process of occurrences in the Azores region, and the main steps are represented in Fig.  
158 2.  
159



181 **Fig. 2** Schematic representation of the global process of occurrences. The dark blue box  
182 indicates previous achievements, the light blue box denotes the subject of this paper,  
183 and the white boxes portray work in progress.

184  
185 The statistical software R® (see, e.g., Dalgaard 2008 or Venables et al. 2011) and the  
186 Turbo Pascal® language are used to implement the procedure described above.

#### 188 **4 Space data analysis**

##### 189 **4.1 Space variable analysis**

190 Based on the data, the main statistics of Sp are computed and presented in Table 1, and  
191 the corresponding histogram is shown in Fig. 3.

192

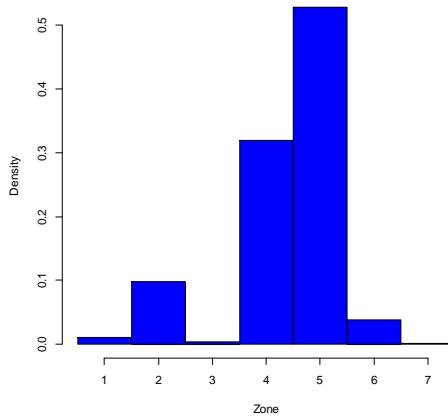


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194 **Table 1.** Statistics of Sp

Statistics of Sp	
Mean	4.38
Standard deviation	1.02
Skewness	-1.35
Kurtosis	4.55
Minimum	1
quantile	
0.1	2
0.2	4
0.3	4
0.4	4
0.5	5
0.6	5
0.7	5
0.8	5
0.9	5
1 (max.)	7
Total number of records	18 822

195



196

197 **Fig. 3** Histogram of Sp

198

199 As shown, the frequency of seismic events in each one of the seven adopted zones is  
200 quite different, highlighting the great dispersion of Sp among the seven zones.



201 Additionally, zones 1, 3 and 7 include small numbers of events compared with the other  
202 seismic zones, and for this reason, they are considered to be background zones of  
203 seismicity.

204 Zones 4 and 5 have the highest number of occurrences, followed by zone 2.

205 Zone 2 is a maritime zone corresponding to the Mid-Atlantic Ridge and its transform  
206 faults to the north. This zone also includes the North Azores Fracture Zone.

207 Zone 5 consists of the Eastern Group of the Archipelago, the Hirondelle Trench, the D.  
208 João de Castro Bank and the two islands of São Miguel and Santa Maria.

209 Zone 4 encompasses the Central Group of the Archipelago west of Capelinhos and the  
210 Terceira Rift central sector with five islands.

211 Zone 6 is a maritime zone and includes the Gloria Fault to the East. The number of  
212 seismic events is moderate, but this zone has the highest magnitude of all zones:  $M_L 8.2$ .

213 The number of seismic events is not high but the magnitudes can be high. (For details  
214 on these morphological structures, see Madeira et al., 2015).

215

#### 216 **4.2 One-step transitions of space variable analysis**

217 It is known that the zone of an epicenter might constrain the zone of the next earthquake  
218 (see for example, Cavers and Vasudevan 2015).

219 The objective is to analyze the statistical distribution of the Space variable (Sp) and the  
220 one-step transitions of this variable. If an earthquake takes place in a seismic zone, the  
221 aim is to answer the question: “which is likely to be the next seismic zone?”

222 Markovian chains are suitable for modelling this phenomenon (see, for example  
223 Ravindran et al. 1987).



224  The possible values of  $Sp$  are considered “states”, and each change of state is a  
225 transition. The points in time at which the system is observed (in this case, the seismic  
226 events) are the epochs.

227  $Sp_{t+1} = j$  signifies that at epoch  $t+1$ , an event took place in zone  $j$ , and  $Sp_t = i$  represents  
228 that at epoch  $t$ , an event took place in zone  $i$ .

229 Let  $p_{ij}$  be the conditional probability  $P [ Sp_{t+1} = j | Sp_t = i ]$ , i.e., the one-step transition  
230 probability,  $i, j \in \{1, 2, 3, 4, 5, 6, 7\}$ .

231 Based on the data, the one-step transition matrix  $T$  was computed for estimation of the  
232 seven empirical conditioned distribution functions  $Sp_{t+1}|Sp_t = i, i \in \{1, 2, 3, 4, 5, 6, 7\}$ .

233 Figures 4(a) to (g) display the corresponding histograms.

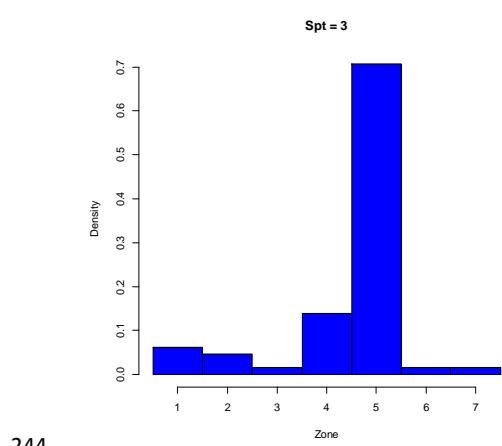
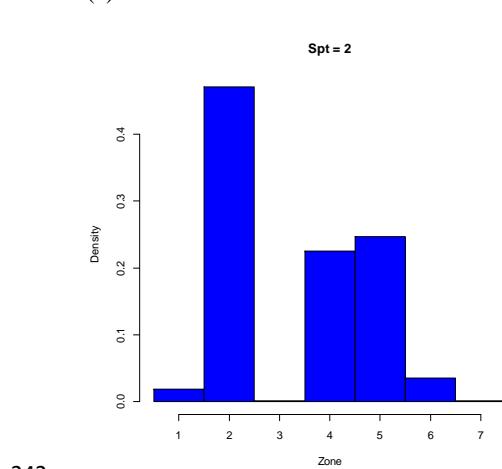
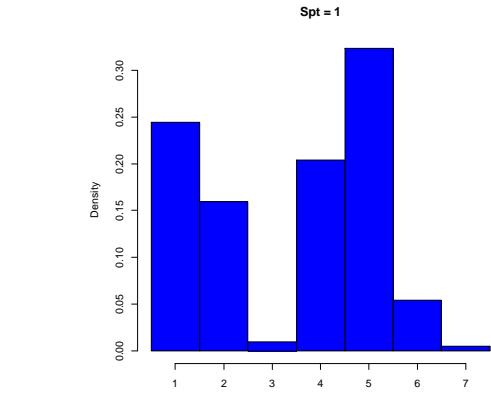
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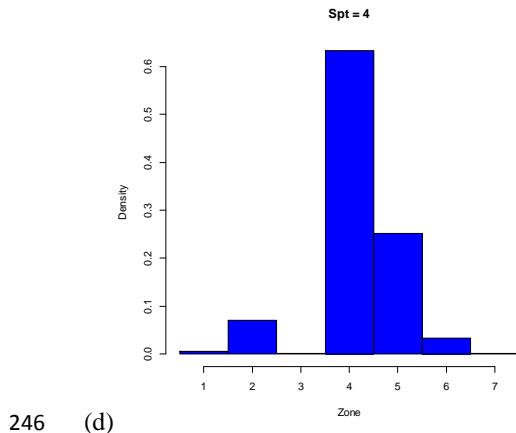
$$235 T = \begin{bmatrix} 0.244 & 0.159 & 0.01 & 0.204 & 0.323 & 0.055 & 0.005 \\ 0.019 & 0.472 & 0.001 & 0.225 & 0.247 & 0.035 & 0.001 \\ 0.062 & 0.046 & 0.015 & 0.138 & 0.709 & 0.016 & 0.015 \\ 0.006 & 0.072 & 0.002 & 0.633 & 0.251 & 0.034 & 0.002 \\ 0.007 & 0.045 & 0.005 & 0.154 & 0.753 & 0.035 & 0.001 \\ 0.011 & 0.094 & 0 & 0.273 & 0.508 & 0.114 & 0 \\ 0 & 0.12 & 0.04 & 0.32 & 0.48 & 0.04 & 0 \end{bmatrix} \quad (1)$$

236 For example, Fig. 4(a) shows the probability of an earthquake occurring in each one of  
237 the seven seismic zones knowing that the last earthquake took place in zone 1.

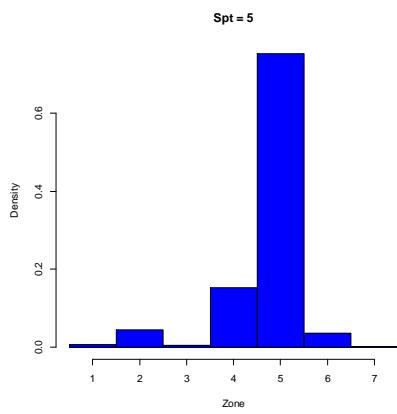
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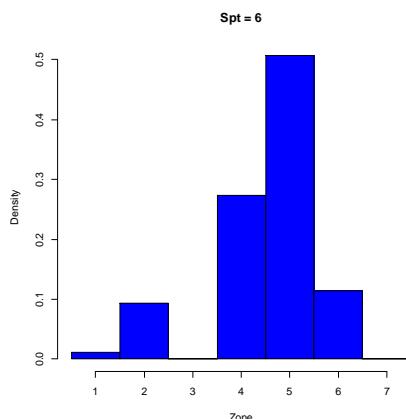


246 (d)



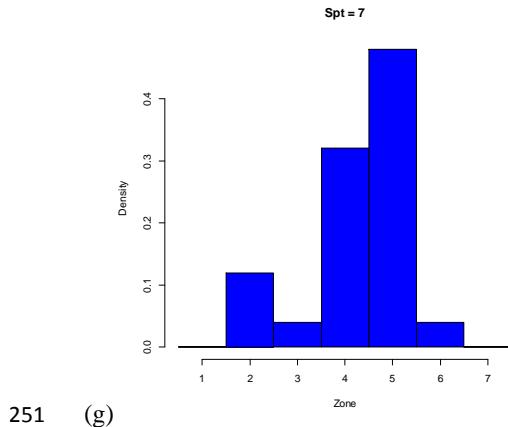
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248 (e)



249

250 (f)



251 (g)

252 **Fig. 4** Histogram of: (a)  $S_{pt+1}|S_{pt}=1$ , (b)  $S_{pt+1}|S_{pt}=2$ , (c)  $S_{pt+1}|S_{pt}=3$ , (d)  $S_{pt+1}|S_{pt}=4$ , (e)  
253  $S_{pt+1}|S_{pt}=5$ , (f)  $S_{pt+1}|S_{pt}=6$ , (g)  $S_{pt+1}|S_{pt}=7$ .

254

255 The seven conditioned distributions are highly different. The most similar to the Sp  
256 distribution function is the distribution of  $S_{pt+1}|S_{pt}=5$ , which is not surprising given that  
257 zone 5 contains the greatest number of seismic occurrences.

258 If a seismic event occurs in zone 1, the most likely target zone is zone 5, which means  
259 that the next earthquake will not be an aftershock. Zone 1 is a background zone with  
260 few seismic events.

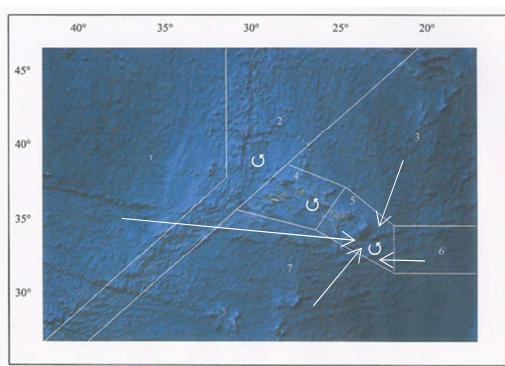
261 If a seismic event occurs in zone 2, the most likely target zone is the same zone, which  
262 means that in zone 2, a great probability exists that the next earthquake will be an  
263 aftershock.

264 If a seismic event occurs in zone 3, the most likely target zone is zone 5, which means  
265 that the next earthquake will probably not be an aftershock. Zone 3 is a background  
266 zone with a small number of earthquakes.

267 If a seismic event occurs in zone 4, the most likely target zone is the same zone. Again,  
268 in zone 4, a great possibility exists that the next earthquake will be an aftershock.



269 If a seismic event occurs in zone 5, the most probable target zone is the same zone.  
270 Again, in zone 5, a great possibility exists that the next earthquake will be an  
271 aftershock.  
272 If a seismic event occurs in zone 6, the most likely target zone is zone 5, which signifies  
273 that the next earthquake will probably not be an aftershock.  
274 If a seismic event occurs in zone 7, the most likely target zone is zone 5, which signifies  
275 that the next earthquake will probably not be an aftershock. Zone 7 is a background  
276 zone with a small number of earthquakes.  
277 Fig. 5 presents these data in the form of “arrows” and loops” or a scheme of the most  
278 likely one-step transitions for each seismic zone.  
279



280  
281 **Fig. 5** Scheme of the most likely one-step transitions for each seismic zone.  
282

283 It can be noted that in zones with great number of occurrences (zones 2, 4 and 5), the  
284 most probable case is that the next seismic event (event) will take place in the same  
285 zone.  
286 In zones with few earthquakes, the most probable case is that the next seismic event will  
287 occur in a different zone because zones 1, 3, 6, and 7 are located far from the islands,  
288 and if the aftershocks were weak, they might not be recorded.



289 These results show that the sequence of events is not independent of the preceding  
290 earthquake. 

291 We note that the current results represent only one-step transitions, and we must  
292 quantify the N-step transitions.

293 We assume that the transition probabilities do not change with the passage of time. In  
294 this situation, if we use Markovian chains to model the sequence of epicenters, the  
295 Markovian chain will be stationary.

296 For a stationary Markovian chain, the matrix  $T$  creates the one-step transition  
297 probabilities for any time and is sufficient to describe the entire process, i.e., the entire  
298 sequence of epicentral seismic zones.

299 For example, if a seismic event has occurred in zone 2 at epoch  $t$ , i.e.,  $Sp_t = 2$ , and we  
300 desire to estimate the probability of  $Sp_{t+2} = 5$ , this is a two-step transition,  $p_{ij}^{(2)}$ . Using  
301 matrix  $T$ ,  $p_{52}^{(2)}$  can be computed.

302

$$303 p_{52}^{(2)} = p_{51} \cdot p_{12} + p_{52} \cdot p_{22} + p_{53} \cdot p_{32} + p_{54} \cdot p_{42} + p_{55} \cdot p_{52} + p_{56} \cdot p_{62} + p_{57} \cdot p_{72} \quad (2)$$

304

305 By generalizing, it is possible to obtain the N-step transition matrix (see, for example,  
306 Ravindran and Dolberg, 1987). Given that the Markovian chain is stationary:

$$307 TM^{(n)} = TM^n. \quad (3)$$

308 This procedure allows reproduction of the seismic epicentral sequence.

309

### 310 **5 Space generation**

311 Space variables can be generated, i.e., a sample of values of the random variable can be  
312 produced and compared with the data sample. First, the aim is to only test whether the  
313 proportion of the number of generated events in each zone matches the corresponding



314 proportion in the data. Subsequently, the sequence of the generated sample must be  
315 checked.

316

317 **5.1 Generation of Space variable**

318 The number of earthquakes in each seismic zone was computed based on the data,  
319 allowing estimation of the probability of a seismic event occurring in each one of the  
320 seismic zones.

321 The inverse-transform method and the statistical distribution function of Space were  
322 used to generate pseudo-random values of Space (see, for example, Pidd (1994) or  
323 Rubinstein and Melamed (1998)).

324 We use Spg as the random variable that represents the generated values of Space.

325 Table 2 shows the number of seismic events for each zone in the data and in sample of  
326 size 19 000. Fig. 6 presents the histogram of Spg.

327

328 **Table 2** Number of generated seismic events for each seismic zone in the data and in a  
329 generated sample.

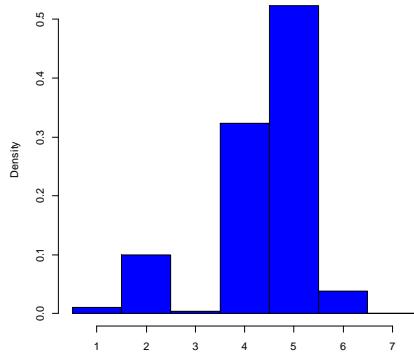
Zone	1	2	3	4	5	6	7	Totals
Data	201	1847	65	6009	9948	727	25	18822
Sample	204	1892	60	6148	9953	730	13	19000

330

331 The generated sample and the data samples should exhibit the same features. A  
332 goodness-of-fit test was used to check whether the generated random values of Space fit  
333 the corresponding data values.

334

335



336  
337 **Fig. 6** Histogram of Sp

338

339 The Chi-square test for two independent samples (see, e.g., Siegel and Castellan, 1988)  
340 was used to verify whether the samples formed by Sp and Spg can be considered to  
341 come from the same population. Table 3 summarizes the results obtained.

342

343 **Table 3.** Summary of results obtained in the Chi-square two-sample test (Space  
344 variable).

Chi-square two-sample test	
Test statistic	5.31
Critical value ( $\alpha = 0.05$ )	12.59
Conclusion	Do not reject H <sub>0</sub>

345

346 Therefore, it can be considered that Sp and Spg have the same distribution.

347

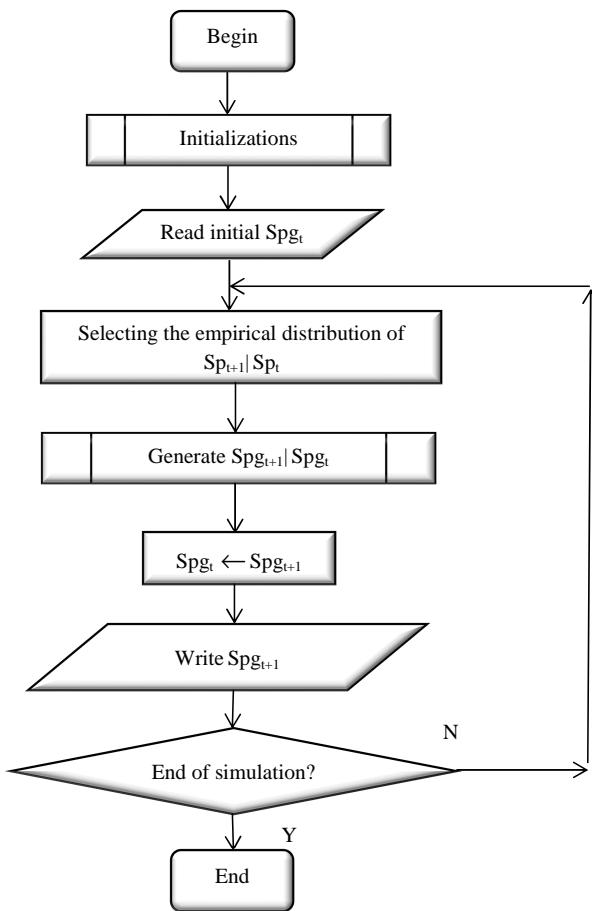
## 348 **5.2 Generation of conditioned Space variable**

349 Given an initial value of Sp<sub>g<sub>t</sub></sub>, it is possible to generate the next value Sp<sub>g<sub>t+1</sub></sub> according  
350 to the respective conditioned distribution functions.

351 If the procedure is repeated, it generates a sample of pseudo-random values. Figure 7  
352 displays the flowchart for Space generation.



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386 **Fig. 7** Flowchart of Space generation.

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388 To check the first-order transitions of Space, a sample of data and the generated one-  
389 step transitions were compared.  
390 Based on the generated sample (of size 19000), the number of one-step transitions of the  
391 variable Space was also generated, and the results are presented in the transition  
392 frequency matrix TG:  
393



$$394 \quad \text{TG} = \begin{bmatrix} 72 & 27 & 3 & 42 & 79 & 9 & 0 \\ 41 & 999 & 3 & 432 & 455 & 54 & 2 \\ 5 & 5 & 2 & 11 & 38 & 3 & 3 \\ 35 & 433 & 10 & 3882 & 1515 & 207 & 6 \\ 73 & 444 & 50 & 1519 & 7466 & 357 & 8 \\ 6 & 73 & 0 & 197 & 354 & 63 & 0 \\ 0 & 4 & 0 & 6 & 9 & 0 & 0 \end{bmatrix} \quad (4)$$

395 The generated and data conditioned distribution functions must be compared, which  
 396 means comparison of 7 conditional distributions. The variables

397  $\text{Sp}_{t+1} | \text{Sp}_t = i$  and  $\text{Spg}_{t+1} | \text{Spg}_t = i$ ,  $i = 1, 2, \dots, 7$  (5)

398 were compared using the Chi-square test for two independent samples (see, e.g., Siegel  
 399 and Castellan 1988). Table 4 condenses the results.

400

401 **Table 4.** Summary of results obtained in the Chi-square two-sample test (conditioned  
 402 distribution functions of Space).

403

Samples compared	Test statistic	C. V. ( $\alpha = 0.05$ )	Conclusion
$\text{Sp}_{t+1}   \text{Sp}_t = 1$			
$\text{Spg}_{t+1}   \text{Spg}_t = 1$	5.31	9.49	NR
$\text{Sp}_{t+1}   \text{Sp}_t = 2$			
$\text{Spg}_{t+1}   \text{Spg}_t = 2$	5.56	9.49	NR
$\text{Sp}_{t+1}   \text{Sp}_t = 3$			
$\text{Spg}_{t+1}   \text{Spg}_t = 3$	0.88	5.99	NR
$\text{Sp}_{t+1}   \text{Sp}_t = 4$			
$\text{Spg}_{t+1}   \text{Spg}_t = 4$	1.41	12.59	NR
$\text{Sp}_{t+1}   \text{Sp}_t = 5$			
$\text{Spg}_{t+1}   \text{Spg}_t = 5$	1.37	12.59	NR
$\text{Sp}_{t+1}   \text{Sp}_t = 6$			
$\text{Spg}_{t+1}   \text{Spg}_t = 6$	2.71	9.49	NR
$\text{Sp}_{t+1}   \text{Sp}_t = 7$			
$\text{Spg}_{t+1}   \text{Spg}_t = 7$	0.20	5.99	NR

404 C.V. = Critical value; NR = Do not reject  $H_0_i$ ; R = Reject  $H_0_i$

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406



407 According to the statistical tests, it can be assumed that one-step transitions in the  
 408 generated sample fit the one-step transitions in the data.

409 Assuming that the sequence of epicenters is stationary in time (which makes sense, in  
 410 our opinion), it is possible to properly generate the entire sequence using the one-step  
 411 transition matrix.

412 As an example, the matrixes of the second and sixth order are presented below. Note  
 413 that in the 6<sup>th</sup> order matrix, the columns are nearly equal. As anticipated, the transition  
 414 matrices are expected to have equal columns when the order increases, and each line  
 415 tends to be equal to the Space distribution function.

416

$$417 \quad T^{(2)} = T^2 = \begin{bmatrix} 0.07 & 0.149 & 0.005 & 0.282 & 0.500 & 0.044 & 0.002 \\ 0.017 & 0.257 & 0.002 & 0.301 & 0.384 & 0.038 & 0.001 \\ 0.023 & 0.078 & 0.005 & 0.231 & 0.626 & 0.037 & 0.002 \\ 0.009 & 0.095 & 0.003 & 0.467 & 0.387 & 0.037 & 0.002 \\ 0.009 & 0.071 & 0.004 & 0.236 & 0.641 & 0.038 & 0.001 \\ 0.011 & 0.099 & 0.003 & 0.306 & 0.536 & 0.044 & 0.001 \\ 0.010 & 0.107 & 0.004 & 0.320 & 0.520 & 0.037 & 0.002 \end{bmatrix} \quad (6)$$

418 This result means that the seismic process of occurrences loses “memory” with time.  
 419 After several events, the probability of an occurrence among the seismic zones is nearly  
 420 independent of the location of a far event.

421

$$422 \quad T^{(6)} = T^6 = \begin{bmatrix} 0.011 & 0.102 & 0.004 & 0.320 & 0.525 & 0.038 & 0.001 \\ 0.011 & 0.105 & 0.004 & 0.323 & 0.519 & 0.038 & 0.001 \\ 0.011 & 0.098 & 0.004 & 0.314 & 0.535 & 0.037 & 0.001 \\ 0.011 & 0.100 & 0.004 & 0.327 & 0.519 & 0.038 & 0.001 \\ 0.011 & 0.097 & 0.004 & 0.314 & 0.536 & 0.038 & 0.001 \\ 0.011 & 0.099 & 0.004 & 0.318 & 0.529 & 0.038 & 0.001 \\ 0.011 & 0.099 & 0.004 & 0.319 & 0.528 & 0.038 & 0.001 \end{bmatrix} \quad (7)$$



423

424 **6 Conclusions**

425 In this work, the sequence of Space locations of the epicenters (seismic zones) in the  
426 Azores region was analyzed. The seismic zones were defined in a previous study  
427 (Rodrigues and Oliveira 2013), and based on the existing historical and instrumental  
428 information, this paper focuses on the analysis of the Space variable using Markovian  
429 chains. The one-step transitions of this variable were explored and showed an evident  
430 dependence on consecutive earthquake locations.

431 It can be noted that in zones with greater number of occurrences, (zones 2, 4 and 5) the  
432 most probable event is that the next seismic event will take place in the same zone. The  
433 next event should be an aftershock. In zones with few earthquakes, the most probable  
434 event is that the next seismic event will occur in a different zone. This observation can  
435 be explained because zones 1, 3, 6, and 7 are located far from the islands, and if the  
436 aftershocks were weak, they might not be recorded.

437 These results confirm that the spatial sequence of events is not independent of the  
438 preceding earthquakes.

439 These results make sense assuming that the transition probabilities do not change with  
440 time, i.e., the Markovian chain is stationary. With this assumption, it is possible to  
441 obtain the N-step transitions of Space, which allows estimation of the probability of  
442 occurrence of a seismic event in a specific zone based on the “recent seismological  
443 past”.

444 Using simulation techniques, the sequence of epicentral zones was reproduced. The  
445 current simulation is a component of ongoing work aimed at modelling the process of  
446 seismic occurrences in the Azores region. This project will include a visual computer  
447 simulation of the entire process of seismic occurrences in the Azores region.



448 The Markov chain developed here ~~in~~ can be easily exported to the analyses of time  
449 ~~in~~ events of other natural phenomena such as temperature, precipitation, etc.  
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