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Setting up the critical rainfall line for debris flows via support vector machines

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Setting up the critical rainfall line for debris flows via support vector machines

Y. F. Tsai et al.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)



[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)



al. (2009), it showed that the numerous landslides triggered by Chi-Chi Earthquake caused a lot of debris-flows and lowered the rainfall threshold of these debris-flows in subsequent years. Nakamura et al. (2000) also indicated that there was a huge number of landslides for about 42 years after the Kanto earthquake in Japan, and almost every landslides during that time induced server debris-flow disasters, presented in Fig. 1.

Thus, in order to prevent the disaster of debris flow, setting a critical rainfall line for each debris-flow stream is necessary. In this research, we aims to setting a critical rainfall line for each debris-flow stream via a series of statistical method. Firstly, 377 debris-flow streams in the center of Taiwan affected by Chi-Chi earthquake was considered. Then, 8 predisposing factors of debris flow were used to cluster streams into 7 groups via the genetic algorithm. After streams with similar characteristics were clustered together, support vector machines (SVMs) were applied to setup the critical rainfall line for each debris-flow clusters. Finally, the experimental result shows that SVM method performs well in setting a critical rainfall line for each group of debris-flow streams.

2 Study area

The Chi-Chi earthquake occurred in 1999 in Taiwan caused numerous landslides, the blocks of these landslides were up to 2365 units and the area were approximate 14347 ha, represented in Fig. 2a. These landslides mostly located in the mountains of central Taiwan. The debris flow streams triggered by the landslides which affected seriously by the Chi-Chi earthquake were studied in the experiments. 377 debris flow streams were chosen from 7 counties included Nan-Tou county, Maio-Li county, Taichung City, Taichung county, Chun-Chua county, Yun-Lin county and Chia-Yi county, represented in Fig. 2b.

According to Shieh and Tsai (2001), 8 important characteristics of the 377 debris-flow streams including rock type (R), watershed area (A), effective watershed area (A_{15}), landslide area (A_s), landslide ratio (A_s/A), length of channel in the effec-

Setting up the critical rainfall line for debris flows via support vector machines

Y. F. Tsai et al.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

[⏪](#)

[⏩](#)

[◀](#)

[▶](#)

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)



tive watershed area (L), mean surface slope of the effective watershed area (S_s) and mean channel slope of the effective watershed area (S_c). Table 1 shows the eight characteristics of the 377 streams.

3 Data processing

In order to cluster the 377 debris flow streams into different groups, the statistical data including geographical information, hydrological information, historical data of disaster and statistical tables of eight predisposing factors have to be preprocessed. The preprocessing involved presentation of the data, normalization of the data and the measurement of the distance between two debris-flow streams. Equation (1) represents the normalization of the data (Z -score).

$$Z_{ij} = \frac{x_{ij} - \bar{X}_i}{\sigma_i} \text{ where } 1 \leq j \leq K, 1 \leq i \leq M, \quad (1)$$

where M represents the 377 debris-flow streams and K is the eight attributes of each stream. Let F_i represent the i th debris flow where $1 \leq j \leq K$, and F_j represent the j th attribute of 8 predisposing factors where $1 \leq i \leq M$. The corresponding attribute vector for the debris flow F_i is represented as X_{ij} . The \bar{X} and σ_i are the mean and mean absolute deviation of X_{ij} , respectively.

After the data were normalized, the distance between two debris-flows could be calculated. The centered Person correlation was used to define the distance $D(F_i, F_j)$. Let $F_i = (X_{i1}, X_{i2}, \dots, X_{ik})$ and $F_j = (X_{j1}, X_{j2}, \dots, X_{jk})$ be normalized attribute vectors of two flows over a series of K attributes. The distance between flows F_i and F_j was defined as Eq. (2).

$$S_{i,j} = \frac{1}{K} \sum_{l=1}^k \left[\frac{X_{il} - \bar{X}_i}{\sigma_{X_i}} \right] \left[\frac{X_{jl} - \bar{X}_j}{\sigma_{X_j}} \right], \text{ where } -1 \leq S_{i,j} \leq 1 \quad (2)$$

Setting up the critical rainfall line for debris flows via support vector machines

Y. F. Tsai et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

⏪

⏩

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



$$\bar{X}_i = \frac{\sum_{l=1}^k F_{il}}{k} \quad (3)$$

$$\sigma_{x_i} = \sqrt{\frac{1}{k} \sum_{l=1}^k (X_{il} - \bar{X}_i)^2} \quad (4)$$

Since this term measured distance, the following was defined as Eq. (5)

$$D(F_i, F_j) = 1 - S_{i,j}, \text{ where } -1 \leq D(F_i, F_j) \leq 1. \quad (5)$$

4 Clustering analysis of debris-flow stream

This section aims to cluster 377 debris-flow streams into seven groups via clustering analysis such that streams in each group have similar characteristics. An efficient clustering algorithm was considered for describing debris flows in order to illustrate the relationships by constructing a binary hierarchical tree. This approach was employed to group 377 debris flow streams into seven groups such that the critical rainfall line in the same group could be set. Many approaches to constructing binary hierarchical trees have been proposed. For example, Ward's method (Ward, 1963), the single-linkage method (Sibson, 1973), the average-linkage method (Defays, 1977), and the average-linkage (Voorhees, 1986) hierarchical clustering approach have been extensively applied in various fields to approximate such trees, including the fields of document clustering (Willet, 1988) and bioinformatics (Eisen et al., 1998; Alizadeh et al., 2000).

In this study, a means of family competition genetic algorithm (FCGA) was presented to construct a hierarchical tree of streams. The FCGA combines family competition, neighbor-join mutation (NJ) and edge assembly crossover (EAX) (Nagata

Setting up the critical rainfall line for debris flows via support vector machines

Y. F. Tsai et al.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

[⏪](#)

[⏩](#)

[◀](#)

[▶](#)

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)



and Kobayashi, 1997). The concepts of family competition have been successfully applied to solve numerous continuous parameter optimization problems, including protein docking (Yang and Kao, 2000). In the authors' earlier work (Tsai et al., 2001), family competition and EAX were successfully integrated to solve traveling salesman problems (TCPs). Neighbor-join mutation (Tsai et al., 2002) was developed to coordinate with the EAX and thus balance exploration and exploitation. The primary difference between the method in this study and that in our previous work is in the integration of these three mechanisms.

The experimental results revealed that the FCGA is a promising method for constructing the optimal tree of streams. Figure 3 presents the seven groups of 377 debris-flow streams. In Fig. 3a–g, the x axis represents the eight important characteristics and the y axis is the normalized values of each characteristics. Each groups include 39, 58, 61, 42, 67, 47 and 63 streams respectively. Each groups all exhibited different trends in their characteristics and the characteristics in the same group were similar. Additionally, it should be noted that Fig. 3f and g use different scales. The clustering results showed that the proposed method was able to cluster streams into separate groups with similar characteristics. As a result, this method represents a possible means of establishing a critical rainfall line for debris flow streams in each group. The critical rainfall lines of each groups could be set according to the characteristics.

5 Establishing the critical rainfall line for debris flows

When the streams with similar characteristics have clustered together, the critical rainfall line of debris flow could be set via SVM. SVM is a new machine learning approach proposed by Vapnic (1998) based on statistical learning theory. The advantage of SVM is that this theory raises the generalized ability of learning mechanisms according to minimize the structural risk. Therefore, we can obtain the results with minimum error rates and without many training samples. Otherwise, SVM is an optimized algorithm which can rapidly performed by a standard programming algorithm and obtained the

Setting up the critical rainfall line for debris flows via support vector machines

Y. F. Tsai et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



global optima. The SVM has been widely applied in many disciplines to solve the problems of classification and regression in the field of hydrological engineering (Yu et al., 2011; Lin and Chen, 2011; Shen et al., 2011). This study tried to establish the critical rainfall line of debris flow via SVM.

In this study, each data of debris flow stream were consider as a vector or a point in a multidimensional space. The destination of this research is to find a hyper-plane which can separate the vectors into two parts, according to the occurrence of debris flow, represented in Fig. 4.

However, two problems have encountered frequently in most cases during the process of classification. Figure 5 shows the two problems, it is likely that there are many hyper-planes existed in the multidimensional space, or it does not have any hyper-plane could separate the training data into two parts exactly.

Therefore, we switched these training data to a higher dimensional space called feature space via a non-linear function $\varphi(x)$. In the feature space, we could still find several hyper-planes can separate the training data into two groups successfully. However, the method of SVM we applied can choose a particular plane from those hyper-planes named maximum margin hyper-plane. Figure 6 shows that with the advantage of SVM, a maximum margin hyper-plane could be selected from several hyper-planes. This maximum margin hyper-plane represents the inner product of the vector in the feature space. This inner product generally made by a kernel function, hence we can easily find the maximum margin hyper-plane with a suitable kernel function. Under the situation of maximum margin hyper-plane, the sum of distance from those training data closest to the plane would be maximum. The decision-making hyper-plane for classification could be illustrated with less training data near the hyper-plane called support vector. Therefore, these training data can classified easily and efficiently.

This section describes the result of the proposed method SVM to establish the critical rainfall line for each group of debris flows. When the debris flow streams with similar characteristics have clustered together into seven group, the critical rainfall line of each debris-flow group could be set via SVM. Figure 7a–g shows the critical rainfall line of

Setting up the critical rainfall line for debris flows via support vector machines

Y. F. Tsai et al.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

[⏪](#)

[⏩](#)

[◀](#)

[▶](#)

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)



future, the weights and the interactions of the predisposing characteristics would be the focus of research.

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Setting up the critical rainfall line for debris flows via support vector machines

Y. F. Tsai et al.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

[◀](#)

[▶](#)

[◀](#)

[▶](#)

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)



Setting up the critical rainfall line for debris flows via support vector machines

Y. F. Tsai et al.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

[⏪](#)

[▶⏩](#)

[◀](#)

[▶](#)

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)



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Setting up the critical rainfall line for debris flows via support vector machines

Y. F. Tsai et al.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

[⏪](#)

[⏩](#)

[◀](#)

[▶](#)

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)



Table 1. The statistical table of 8 characteristics with 377 streams.

R		A_s/A (%)		S_c (degree)		S_s (degree)	
Type	Stream no.	Range	Stream no.	Range	Stream no.	Range	Stream no.
Alluvion	4	0–5	3	0–10	3	0–0.5	81
Conglomerate	30	5–10	9	10–15	11	0.5–1.0	35
Sand stone	35	10–15	67	15–20	42	1.0–2.0	65
Sand and shale	191	15–20	115	20–25	80	2.0–3.0	39
Shale	5	20–25	99	25–30	103	3.0–5.0	45
Slate	55	25–30	56	30–35	93	5.0–10.0	49
Metamorphic sand	57	> 30	28	> 35	45	> 10.0	63

A (ha)		A_{15} (ha)		A_s (ha)		L (km)	
Range	Stream no.	Range	Stream no.	Range	Stream no.	Range	Stream no.
0–10	13	0–10	23	0–0.1	59	0–0.5	54
10–20	19	10–20	34	0.1–0.5	45	0.5–1.0	88
20–30	18	20–30	22	0.5–1.0	37	1.0–1.5	78
30–40	32	30–40	30	1.0–2.0	53	1.5–2.0	44
40–50	17	40–50	28	2.0–3.0	25	2.0–3.0	53
50–60	19	50–60	23	3.0–4.0	30	3.0–4.0	19
60–70	18	60–70	18	4.0–5.0	23	4.0–5.0	10
70–80	13	70–80	13	5.0–10.0	38	5.0–6.0	11
80–90	19	80–90	19	10.0–20.0	29	6.0–7.0	4
90–100	14	90–100	12	20.0–30.0	15	7.0–8.0	4
100–200	91	100–200	71	30.0–40.0	9	8.0–9.0	1
200–300	30	200–300	27	40.0–100.0	8	9.0–10.0	4
300–500	36	300–500	25	> 100.0	6	> 10.0	7
> 500	38	> 500	32				

Setting up the critical rainfall line for debris flows via support vector machines

Y. F. Tsai et al.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

[|◀](#)

[▶|](#)

[◀](#)

[▶](#)

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)



Table 2. The value of critical rainfall line of each debris flow groups.

Group	Group A	Group B	Group C	Group D	Group E	Group F	Group G
Rainfall intensity	31.5	23	18	23.5	40.5	22.5	18.5
Rainfall accumulation	235.5	195	195	70	218	50	280

Setting up the critical rainfall line for debris flows via support vector machines

Y. F. Tsai et al.

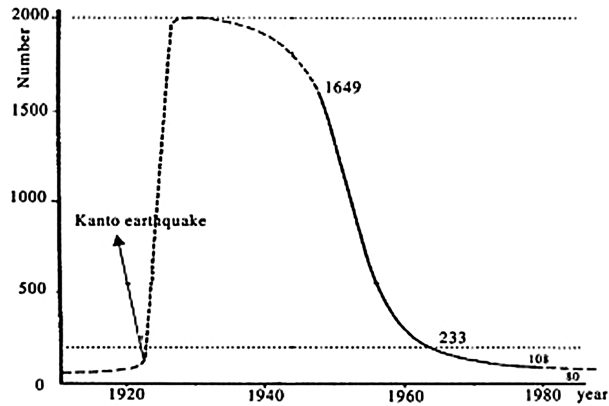


Figure 1. The statistical information of the landslides after the Kanto earthquake in Japan (Nakamura et al., 2000).

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

⏪

⏩

◀

▶

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)



Setting up the critical rainfall line for debris flows via support vector machines

Y. F. Tsai et al.

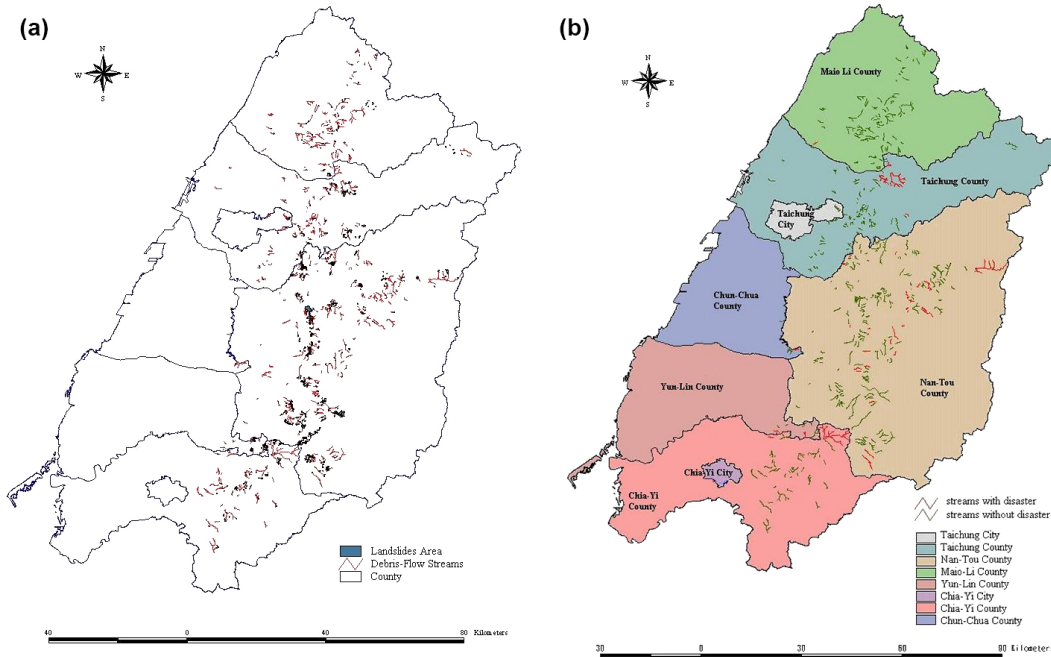


Figure 2. (a) The position and landslide area of 377 debris-flow streams in central Taiwan and (b) the historical disaster and position of 377 debris-flow streams in central Taiwan.

Title Page	
Abstract	Introduction
Conclusions	References
Tables	Figures
◀	▶
◀	▶
Back	Close
Full Screen / Esc	
Printer-friendly Version	
Interactive Discussion	



Setting up the critical rainfall line for debris flows via support vector machines

Y. F. Tsai et al.

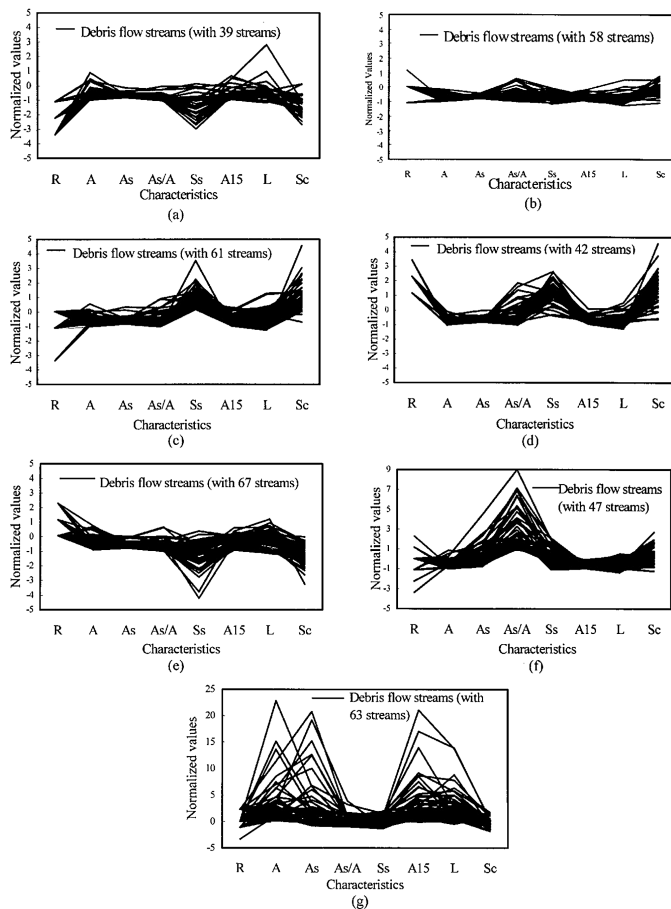


Figure 3. The results of clustering analysis on 377 debris-flow streams.

[Title Page](#)
[Abstract](#) [Introduction](#)
[Conclusions](#) [References](#)
[Tables](#) [Figures](#)

⏪ ⏩
◀ ▶
[Back](#) [Close](#)

[Full Screen / Esc](#)
[Printer-friendly Version](#)
[Interactive Discussion](#)



Setting up the critical rainfall line for debris flows via support vector machines

Y. F. Tsai et al.

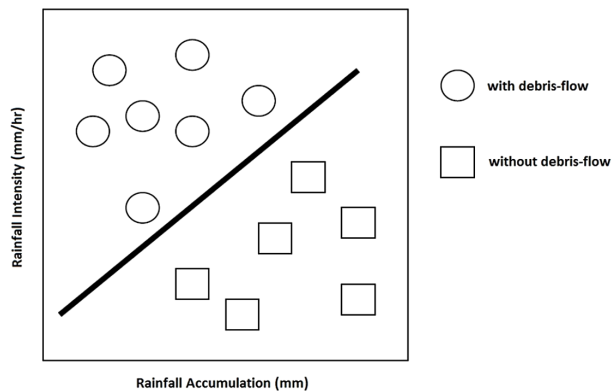


Figure 4. The multidimensional space with vector of debris-flow.

[Title Page](#)[Abstract](#)[Introduction](#)[Conclusions](#)[References](#)[Tables](#)[Figures](#)[⏪](#)[⏩](#)[◀](#)[▶](#)[Back](#)[Close](#)[Full Screen / Esc](#)[Printer-friendly Version](#)[Interactive Discussion](#)

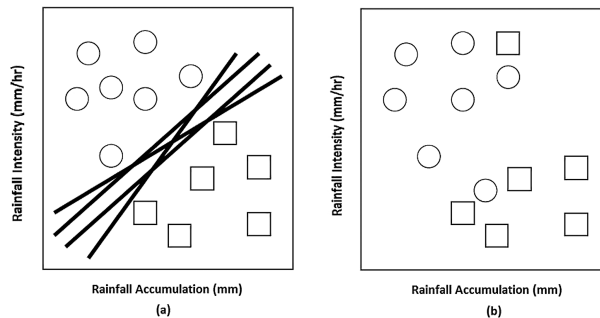


Figure 5. The examples of problems encountered in most cases.

Setting up the critical rainfall line for debris flows via support vector machines

Y. F. Tsai et al.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

[⏪](#)

[⏩](#)

[◀](#)

[▶](#)

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)



Setting up the critical rainfall line for debris flows via support vector machines

Y. F. Tsai et al.

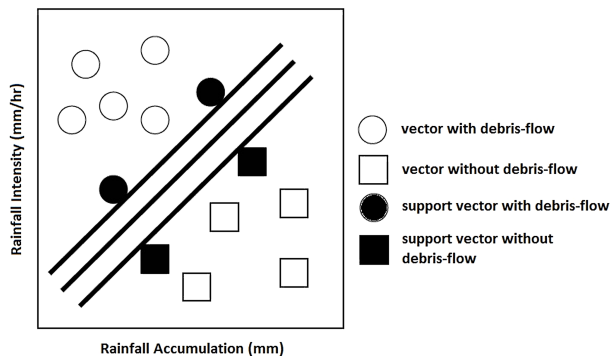


Figure 6. An example of maximum margin hyper-plane and support vector.

[Title Page](#)
[Abstract](#) [Introduction](#)
[Conclusions](#) [References](#)
[Tables](#) [Figures](#)
[⏪](#) [⏩](#)
[◀](#) [▶](#)
[Back](#) [Close](#)
[Full Screen / Esc](#)
[Printer-friendly Version](#)
[Interactive Discussion](#)



Setting up the critical rainfall line for debris flows via support vector machines

Y. F. Tsai et al.

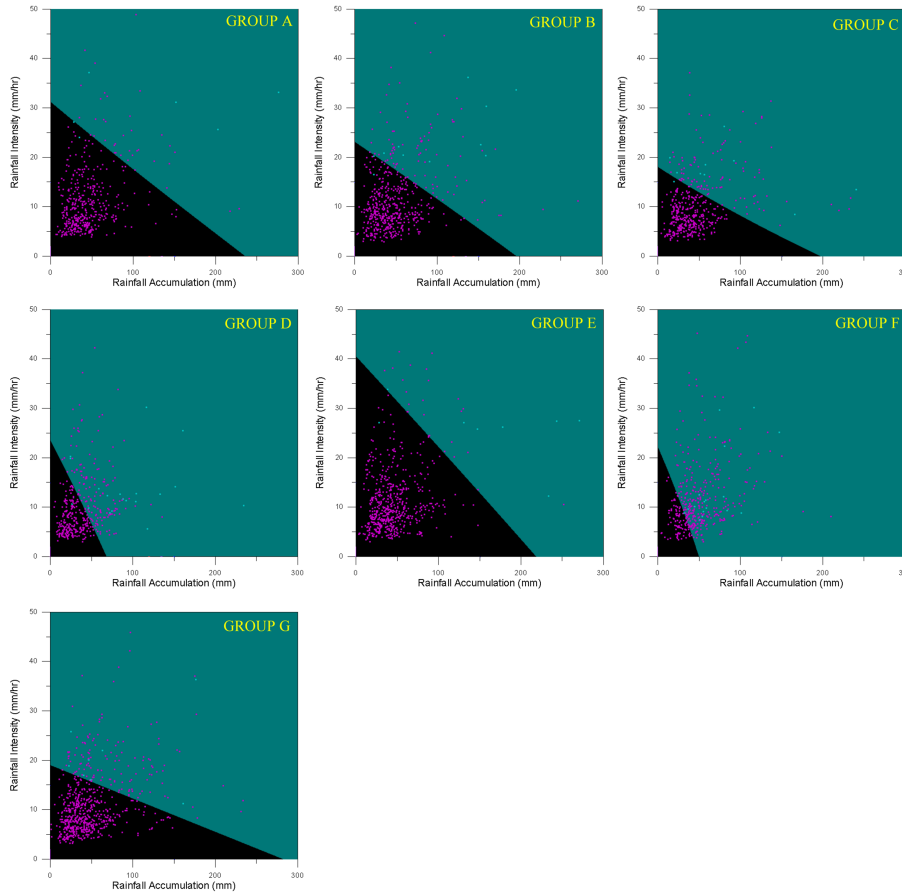


Figure 7. The result of our research tested on 7 groups.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

⏪

⏩

◀

▶

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)

