1 Statistical correlation between meteorological and rockfall

databases

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Abstract

Rockfalls are major and essentially unpredictable sources of danger, particularly along transportation routes (roads and railways). Thus, the assessment of their probability of occurrence is a major challenge for risk management. From a qualitative perspective, it is known that rockfalls occur mainly during periods of rain, snowmelt, or freeze-thaw. Nevertheless, from a quantitative perspective, these generally assumed correlations between rockfalls and their possible meteorological triggering events are often difficult to identify because i) rockfalls are too rare for the use of classical statistical analysis techniques and ii) all intensities of triggering factors do not have the same probability. In this study, we propose a new approach to investigate the correlation of rockfalls with rain, freezing periods, and strong temperature variations. This approach is tested on three French rockfall databases, the first of which exhibits a high frequency of rockfalls (approximately 950 events over 11 years), whereas the other two databases are more typical (approximately 140 events over 11 years). These databases come from (1) the national highway RN1 on La Réunion Island, (2) a railway in the Bourgogne region, and (3) a railway in the Auvergne region. Whereas a basic correlation analysis is only able to highlight an already obvious correlation in the case of the "rich" database, the newly suggested method appears to detect correlations even in "poor" databases. Indeed, the use of this method confirms the positive correlation between rainfalls and rockfalls in the La Réunion database. This method highlights a correlation between cumulative rainfalls and rockfalls in the Bourgogne region, and it detects a correlation between the daily minimum temperature and rockfalls in the Auvergne database. This new approach is easy to use and also serves to determine the conditional probability of rockfall according to a given meteorological factor. The approach will help to optimize risk management in the studied areas based on their meteorological conditions.

Keywords: Rockfall; Hazard assessment; Database; Triggering factor

1 Introduction

- 2 Rockfall hazard is defined as the probability that a rockfall of a given volume occurs in a
- 3 given area within a specified time interval (Varnes, 1984). This definition considers three
- 4 different components of hazard: space, time (rockfall frequency), and the intensity (volume)
- of the event. Numerous studies on hazard mapping (e.g., Baillifard et al., 2003; Jaboyedoff et
- 6 al., 2005) and rockfall frequency (e.g., Brunetti et al., 2009; Dussauge et al., 2003) are
- 7 available in the literature, but little work has been conducted to quantify the influence of
- 8 meteorological factors on rockfall frequency.
- 9 Temporal probability can be estimated through the study of triggering factors, which are
- external causes that are principally climatic in origin. These factors, which appear only at
- discrete times, induce changes in the forces acting on rock blocks (Hoek, 2007) and cause the
- blocks to fall. The most common triggering factors are intense rainfall episodes (André, 1997;
- Berti et al., 2012; Ilinca, 2008; Rapp, 1960), the freeze and thaw of water-filled fractures
- 14 (Ilinca, 2008; Matsuoka and Sakai, 1999), and repeated rock surface temperature variations
- 15 (Frayssines and Hantz, 2006; Gunzburger et al., 2005; Luckman, 1976). Furthermore, seismic
- activity has been shown to influence rockfall events (Bull et al., 1994; Vidrih et al., 2001;
- 17 Zellmer, 1987).
- Rockfall inventories can be used to quantify the statistical correlation between rockfall events
- and their triggering factors (Chau et al., 2003; Helmstetter and Garambois, 2010). However, it
- 20 is generally difficult to identify such a correlation because: i) rockfalls are too rare for the use
- of classical statistical analysis techniques and ii) all intensities of triggering factors do not
- 22 have the same probability. More precisely, as the occurrence or action of a triggering factor
- does not necessarily result in a rockfall, it is necessary to distinguish the rockfall probability
- 24 itself from the frequency of its potential triggering factors.
- In this paper, we present a new approach to investigate the correlation of rockfalls with rain,
- 26 freezing periods, and strong temperature variations. This approach is tested on three French
- 27 rockfall databases, the first of which exhibits a high rockfall frequency (approximately 950
- events over 11 years). The two other databases contain approximately 140 events over 11
- years. The three databases came from the following sources: (1) national highway RN1 on La
- Réunion Island (Indian Ocean), (2) a railway in the Bourgogne region, and (3) a railway in the
- 31 Auvergne region, <u>France</u> (<u>Figure 1 and Table 1</u>). The spatial location and intensity <u>of the</u>
- 32 events are not studied in this paper; only the number of rockfalls during the period of

- 1 monitoring is considered. However, the volume range and the mean height of the source rock
- walls are given for each sector (cf. Part 2).

- 3 The classical time series approach (Helmstetter and Garambois, 2010) is able to highlight an
- 4 already obvious correlation only in the case of the "rich" database. The newly suggested
- 5 method also appears to detect correlations in the "poor" databases. This approach will help to
- 6 optimize risk management in the areas considered in terms of the meteorological conditions.

2 Rockfall databases

- 2 There is a significant difference between the three databases: for La Réunion Island, 13% of
- 3 the days have at least one rockfall (529 days out of 4,008 days in the entire database),
- 4 compared with 3% for the Auvergne and Bourgogne databases. The high frequency of events
- 5 makes the first database particularly unique. Rockfall databases typically have an event
- 6 frequency of approximately 3% (Hungr et al., 1999; Jeannin, 2001; RTM Isère, 1996;
- Wieczorek et al., 1992).
- 8 The daily rockfall hazard, which is the probability of a fall on each day, regardless of the
- 9 meteorological factors, is similar to these frequencies under the assumption of spatial and
- 10 temporal homogeneity.

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2.1 Highway RN1 on La Réunion Island

- National Road #1 (RN1) on La Réunion Island (Indian Ocean, latitude: 21°10 S, longitude:
- 14 55°30 E) runs along the coast at the base of a 10-km long and up to 200-m high cliff
- 15 composed of basaltic lava strata alternating with pyroclastic layers. This region has a tropical
- climate. In the studied area, the precipitation can reach 372 mm in one day, and temperatures
- 17 typically vary from 16°C to 35°C over the year, with an average amplitude of 9.2°C in one
- 18 day.

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- 19 Daily rockfall data are available due to the regular patrols conducted by the local Public
- Works authorities (DDE). A total of 949 rockfalls were recorded within the 11-year span
- between 1998 and 2009. The volumes of the rockfalls range between 2.10⁻³ and 27.10³ m³.
- 22 Previous studies (Durville, 2004; Rat, 2006) that considered only a portion of the database
- 23 (352 rockfalls recorded between 1998 and 2002) have shown that rockfalls are mainly
- 24 correlated with intense rainfall episodes. We repeated this study with a more exhaustive
- database and also evaluated the influence of temperature on rockfalls.

2.2 Railway in the Bourgogne region, France

- 27 The altitude of the study area is between 300 and 400 m. It consists of limestone marl
- 28 alternations. Its climate is oceanic to semi-continental. The oceanic influence is responsible
- 29 for frequent rainfall in any season, with a maximum in autumn (up to 89 mm daily). The

- semi-continental influence produces cold winters (minimum temperature down to -20°C) and
- 2 hot summers (maximum temperature up to 36°C). The daily temperature amplitude may be up
- 3 to 24°C.
- 4 Technicians from the French National Railway Company (SNCF), working on the railroads to
- 5 ensure their safety, are in charge of the rockfall inventory. Daily data are available, and 135
- 6 rockfalls were recorded within a 13-year span (1999-2012) along the 100 km of the studied
- 7 railroad. The average height of the rock walls is 20 meters. The volumes of the rockfalls range
- 8 between 8.10⁻³ and 80 m³.

9 2.3 Railway in the Auvergne region, France

- The altitude of the study area is between 700 and 900 m. It consists of volcanic (basalt) and
- plutonic (granite) magmatic rocks. Its climate is similar to that of the Bourgogne region. The
- rainfall can reach 125 mm in one day. Temperatures range between -18°C and 36°C, with a
- daily temperature amplitude of up to 23°C.
- 14 The Auvergne database provides daily data based on a rockfall inventory maintained by
- 15 technicians from SNCF. Overall, 40 km of railroads are included in this database, and the
- mean height of the cliffs is 15 meters. The database includes 142 rockfalls, which were
- 17 recorded over an 11-year span (2001-2012). The volumes of the rockfalls range between 2.10
- 3 and 6 m 3 .

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The following analyses were conducted for the three <u>study sites</u> taken separately.

3 Preliminary analysis using a classical time-series approach

3.1 Possible triggering factors considered in this study

- 3 Possible triggering factors include the following:
- 4 $\underline{P_{Di}}$, the amount of precipitation (or rainfall) of the considered day (D_0) , or n days before (D_n) , with n varying from 1 to 10;
- 6 $\underline{P_{cN_2}}$ the amount of precipitation (or rainfall) accumulated over N days (up to 10 days): $P_{cN} = P_{D0} + P_{D1} + ... + P_{DN_2}$;
 - The day's temperature <u>range</u>, indicated by the minimum temperature (T_{min}) , maximum temperature (T_{max}) , and temperature amplitude $(T_{amp} = \underline{T_{max} T_{min}})$;
 - The daily duration of freezing. This factor was considered only for the Bourgogne and Auvergne regions because the temperatures on La Reunion Island are never below 0°C.
- 13 These meteorological parameters were provided by Météo France (the French National
- Weather Service) for each sector on a daily basis. The weather stations selected for this
- purpose were located no more than 30 km away from the studied area. The stations used in
- the study of the highway on La Réunion Island have a mean altitude of 100 meters. Those
- used for the Bourgogne region have a mean altitude of 310 meters, and those used for the
- 18 Auvergne region have a mean altitude of 700 meters.

3.2 Results

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- First, a qualitative analysis of the three databases was performed. Figure 2 shows the visual
- 21 correlation between the rockfalls and meteorological factors over a three-year period. The
- 22 graphs were obtained by calculating a 30-day moving average to smooth the data and to focus
- on the trend. From a purely qualitative perspective, the graphs shed light on the following:
- A good correlation between rockfalls and rainfalls and between rockfalls and minimum temperatures for La Réunion Island;
- No noticeable correlation between rockfalls and meteorological factors in the Bourgogne region;
- A low correlation between rainfalls and rockfalls in the Auvergne region but no noticeable correlation between temperatures and rockfalls.

- 1 Table 2 presents the distribution of the total number of rockfalls per day as a function of the
- 2 daily amount of rain for the three studied areas. The maximum frequency of rockfalls occurs
- 3 for the lowest daily amount of rainfall. This rainfall interval is also the most frequent. Low
- 4 levels of rain are more frequent than high levels. This difference in frequency tends to conceal
- 5 the effect of rain on triggering rockfall events.
- 6 The cross-correlation between the daily number of rockfalls (R) and the amount of
- 7 precipitation (P), both expressed as time series, was investigated by calculating

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$$C_{k}(R,P) = \frac{\sum (R_{t} - \bar{R})(P_{t-k} - \bar{P})}{\sqrt{\sum (R_{t}} - \bar{R})^{2} \sqrt{\sum (P_{t}} - \bar{P})^{2}}},$$
 (1)

- 9 with k corresponding to the time delay between the rain episode and the rockfalls that it may
- 10 have triggered (Hipel and McLeod, 2005).
- 11 Figure 3 presents the cross-correlation function of Eq. (1) for La Réunion Island by
- 12 considering various delays. A maximum value of 0.563 is reached for a delay of one day; this
- value is statistically significant in terms of the significance threshold applied to the data. If the
- 14 cross-correlations are larger than $1.96/\sqrt{n}$ in magnitude, with n as the number of pairs of
- 15 (R_t,P_t) available (equal to the number of days in the databases), then they are deemed
- significant. Similar cross-correlation analyses were performed for the other two study sites
- and two meteorological parameters (the daily temperature and the daily freezing duration), but
- none of these yielded satisfactory results (maximum value of 0.07 with a significant threshold
- 19 of 0.031).

3.3 Limitations of the classical approach

- 21 The preliminary analysis presented here only confirms the visual correlation between rainfalls
- 22 and rockfalls for La Réunion Island. Although meteorological factors are frequently
- 23 mentioned in the literature as an explanation of rockfalls, no other correlations were identified
- for the two other databases.
- 25 This lack of significant results can be explained by the nature of databases: using only 3% of
- 26 the days in the database resulted in a relatively weak time series analysis. Furthermore, these
- 27 days typically contain only one event (1% of days with rockfalls are days with several events
- in the railway databases). These characteristics lead to a smoothing of the results and do not
- 29 permit us to draw any conclusions regarding the potential correlations.

- 1 Our proposed method does not consider the delay in time, only the influence of the intensity
- 2 of the parameters on rockfalls.

4 Suggested new methodology of analysis

4.1 Principle

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- 3 The objective of the new methodology is to weight the number of rockfalls by the probability
- 4 of occurrence of the studied triggering factor (rainfall, temperatures, and freezing period). To
- 5 this end, three steps are required. These steps will now be detailed for the case of rainfall.
- 6 First, rainfall intervals $[P_i, P_{i+1}]$ are defined, where P designates the daily or cumulated
- 7 rainfall. Theses intervals are defined such that i) the number of days within this rainfall
- 8 interval is equal or greater to five (to avoid non-statistically significant intervals) and ii) at
- 9 least one event occurs within this rainfall interval.
- 10 Second, the following ratio is calculated for each interval:

$$E_i = Nr_i/Nd_i, (2)$$

- where Nr_i is the number of rockfall(s) that occurred within the given rainfall interval and Nd_i
- is the number of days in this interval. Thus, E_i corresponds to the daily rockfall frequency for
- each interval.
- Third, a linear regression analysis of the values E_i is performed with respect to P_i to search for
- a possible linear relationship between the <u>magnitude</u> of the triggering factor and the
- 17 corresponding average number of rockfalls. To validate the correlation, we have considered
- the squared correlation coefficient R² and the p-value of the linear regression. If the p-value
- was less than 0.05 (significance level), the linear model was considered satisfactory, and the
- 20 R² value corresponds to the best correlation.

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- To test the relevance of the method, virtual rockfalls and rainfall databases were created. To
- confirm the importance of the number of events in the database, "rich" and "poor" databases
- 24 were generated such that the correlation between the rainfall and the number of events could
- be determined in advance. The method was then applied to determine the correlations for
- different cases.

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4.2 Case study on virtual databases

4.2.1 Generation of virtual databases

- 3 For the first case study, the virtual databases were generated using Mathematica software (V9,
- 4 Wolfram Research, Champaign, Illinois, USA). The following parameters were used as fixed
- 5 components of the databases:

- the number of days in the entire database (*N*). *N* is taken equal to 4,015 days (11 years), similar to the real databases;
 - the type of triggering meteorological factor and its distribution. The chosen factor is rainfall, which follows the same distribution as the measured rainfall of La Réunion Island (Figure 4). Overall, 43% of the days were rainy;
 - the ratio between the rainfall and the number of events, which gives the number of rockfalls given the amount of rain for each day, is taken to be equal to 0.1 in the case of the virtual databases (a rainfall of 10 mm on one day is assumed to trigger one rockfall on the same day; in the case of a day without rainfall, zero rockfall occurs on this day);
 - k, the time delay (in days) between a rain episode and the rockfalls that it may have triggered. k is always equal to zero in the virtual databases (because all rockfalls are assumed to occur within the same day of the rain episode).
 - Two other parameters will vary depending on the databases:
 - the "correlation rate" C_r between the rainfalls and number of events. For example, a perfect correlation (correlation rate of 100%) indicates that all rainy days are days with rockfalls, in accordance with the fixed proportionality coefficient. A correlation rate of 50% means that half of the events are perfectly correlated with the rain, whereas the others are randomly distributed throughout the database;
 - the proportion x of days with events. Three cases were tested: (1) x = 43%, corresponding to the proportion of rainy days in the La Réunion Island database;
 (2) x = 13%, corresponding to the proportion of days with events in the La Réunion database; and (3) x = 3%, corresponding to the proportion of days with events in the railway databases.
- The cross-correlation approach and the method developed were used on the virtual databases, and the results are presented in the next section. The comparison of the results allows for the

- detection and verification of correlations by the proposed method even in the case of the
- 2 railway databases.

3 4.2.2 Results

- 4 Figure 4 shows the different cases tested and the correlations from a graphical perspective.
- 5 The correlation is noticeable regardless of the proportion x of days with events if $C_r = 100\%$.
- 6 If this value decreases, the proportion of days with events has a stronger influence.
- 7 Table 3 presents the values of the cross-correlation function for all of the databases, obtained
- 8 for a time delay k = 0. In the case of a high-frequency database (x = 43%), the correlation was
- 9 detected for $C_r = 50\%$. However, the cross-correlation did not permit the establishment of a
- 10 correlation between the rainfalls and rockfalls for $C_r = 25\%$. The same negative conclusion
- applies to the case of a database with 13% of days with events when $C_r = 50\%$ and 75% for a
- "typical" database (x = 3%). Thus, by analogy, the value of the maximum of the cross-
- 13 correlation function (0.563) for the La Réunion database indicated that at least 75% of the
- events were correlated with rain.

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- 15 Table 4 presents the results obtained with the proposed method, allowing us to identify the
- 16 correlation between the rainfalls and number of rockfalls, provided that the number of
- 17 rockfalls and rainfall events are 100% correlated.
- 19 Similar tests were also performed with the rainfall distribution for the Bourgogne region
- 20 (Figure 6), and the results were found to be similar to those presented here.

Application of the proposed method to the three real databases 5

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2 Table 5 summarizes the correlations identified using the proposed method. Only the 3 4 maximum correlation values are presented in the table. The new method confirms the existence of a positive correlation between rainfalls and rockfalls on La Réunion Island. This 5 6 correlation exists with the daily rainfall and with the cumulative daily rainfall (Figure 7) but is 7 more significant in the case of the accumulated rains. The method also detects a correlation 8 between the minimum and maximum temperatures and the rockfalls in the same region, 9 which is not surprising because the rainy season is characterized by both high temperatures and intense rainfalls. These correlations are maximal for a time delay of one day. 10 Whereas the classical analysis did not identify any correlation for the two other databases, the 12 new approach detected several correlations. Indeed, the new approach detected a correlation between the accumulated rainfall and rockfalls for the Bourgogne region. More precisely, the 13 14 method indicates that the occurrence of two successive days with intense rainfall is the most 15 favorable meteorological factor, among those studied, for triggering rockfall events (Figure 16 8). 17 A correlation between the daily minimum temperature and number of rockfalls was also 18 identified for the Auvergne database. The maximal correlation occurred for the minimum 19 temperature recorded two days before the event (D_2) (Figure 9). Temperatures lower than 0° C 20 also triggered rockfall events after a delay of two days. For the two databases, no correlation was detected between rockfalls and the daily 21 22 temperature amplitude or the freezing duration. Another marker of freeze-thaw activity could 23 be the number of freeze-thaw cycle occurrences in one day. This marker is frequently cited in the literature (Douglas, 1980; Matsuoka and Sakai, 1999) and could be used to validate or 24

invalidate our result. Unfortunately, this marker was not available to us for the studied data.

6 Discussion

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6.1 Physical processes involved in each study sites

- 3 The method presented in this paper highlights several statistical correlations between rockfalls
- 4 and meteorological factors, depending on the geology and the climate of the studied sites.
- 5 Below are several physical interpretations of these correlations.
- 6 On La Réunion Island, intense rainfall events, typical of the island's tropical climate, are the
- 7 main triggering factor for rockfalls. Their effect is very short-term, lasting no longer than one
- 8 day. It consists in a leaching of the cliff, during which already unconsolidated blocks of rock
- 9 are swept along by temporary torrents flowing down the steep topography.
- 10 Geologically, the steep slopes in the Bourgogne region are mainly characterized by
- alternating layers of limestone and marl. The marls are capable of absorbing rainwater that
- 12 infiltrates and causes creeping of the clay minerals contained within the substrate (Peck and
- 13 Terzaghi, 1948). This process is relatively slow and is primarily related to low-intensity
- 14 rainfall episodes lasting several days. Repeated water infiltrations cause the rupture of the
- overlying prefractured limestone layers via a fatigue effect (Pariseau and Voight, 1978).
- 16 The Auvergne region differs significantly from the Bourgogne region in that the rupture
- 17 processes leading to block detachments are associated with different geological settings and
- 18 triggering factors. The Auvergne is a region of volcanic and plutonic magmatic rocks, and the
- main meteorological factor observed to correlate well with rockfalls in this region is a strong
- 20 negative temperature gradient occurring two days before the rockfalls. This correlation can be
- 21 explained by the freeze-thaw process, inducing progressive expansion and loosening of rock
- 22 fractures by repeated diurnal freezing and thawing of water-filled cavities (Coutard and
- 23 Francou, 1989; Matsuoka and Sakai, 1999; Matsuoka, 1994, 2008).

6.2 Conditional probabilities used for risk management

- 25 The new approach also allows the <u>estimation</u> of the conditional probability of rockfall given
- 26 the interval of rain ($[P_i, P_{i+1}]$), to be determined as follows:

P (rockfall given the interval) =
$$\frac{\text{Nrd}}{\text{Nd}}$$
, (3)

- where Nrd is the number of days with at least one event within the considered interval and Nd
- is the total number of days within the considered interval.

Table 6 provides the conditional probabilities for (1) the accumulated rain over two days for La Réunion Island, (2) the accumulated rain over three days for the Bourgogne region, and (3) the temperature minimum for D_2 for the Auvergne region. The values of the conditional probabilities (Nrd/Nd) can be compared to the daily rockfall probability in each case (number of events divided by the total number of days in the database). Given the interval for the meteorological factor (e.g., the daily rainfall), the infrastructure manager can then estimate the probability of rockfall and make a risk management decision based on a rainfall forecast (a rainfall prediction provided at least a day in advance). Specifically, for both the La Réunion region and Bourgogne region, when 15 mm of cumulative rain is reached (over two and three days, respectively), the probability of a fall is doubled compared to the daily rockfall probability. For the Auvergne region, this probability is doubled when -5°C is reached. When 120 mm of rain falls in the La Réunion region, the conditional probability of rockfall reaches one, which means that the daily rockfall probability is multiplied almost by eight. In the most unfavorable case, this probability is multiplied by 5.5 for the Bourgogne region and by 3.5 for the Auvergne region.

6.3 Advantages and drawbacks of the proposed approach

The correlation between rockfalls and meteorological factors is a classical observation. However, the correlations are difficult to detect (cf. Part 3) for databases with fewer rockfalls (such as the Bourgogne and Auvergne databases) (Frayssines and Hantz, 2006). By testing the proposed method on a virtual database (cf. Table 4), it was confirmed that with a correlation rate (C_r) of 100%, a correlation could be detected even within databases entailing very few events (x = 3%). By reducing the correlation rate, a correlation can still be detected for only 50% of days with events completely correlated ($C_r = 50\%$). In terms of the size of the intervals used in the correlation analysis, we conducted several tests using either the smallest or largest possible interval size when at least one event and five days were observed. The results, expressed in terms of the p-value, did not change significantly. However, the R^2 values increased slightly in the largest intervals. Our evaluation of the cross-correlation method using the virtual databases (cf. Table 3) demonstrated that no cross-correlation is detected if there are fewer than 3% of days with events. Moreover, the cross-correlation analysis appears unsuitable if only one event occurs per day (given that the cross-correlation is calculated as a function of the daily number of rockfalls).

For the proposed method to be applicable, the database must be as complete as possible and re-established on a daily basis, as is the case when patrolling is performed daily. The study of the correlations between the events of the day (D_0) and the meteorological factors of the days before (D_n) is not possible if these conditions are not met. Furthermore, the studied site should present homogeneous geological conditions to allow the statistical analyses to be relevant to the entire database. Indeed, differences in geological conditions may lead to differences in the failure mechanisms (Douglas, 1980; Fityus et al., 2013; Luckman, 1976); in such an event, it is probable that both the triggering factors and statistical conclusions will differ. To be more precise in the analysis, the Bourgogne and Auvergne databases could be divided into different parts according to the geology. However, the databases are not sufficiently "rich" to allow this

11 partitioning.

Moreover, the assessment of the conditional probability of rockfall given the interval of the meteorological factor allows us to compare each of the conditional probabilities with the daily rockfall hazard, which corresponds to the proportion of days with events in the entire database.

At present, one of our objectives is to investigate other fields by testing this method on databases involving events other than rockfalls. This extension will permit us to examine the scope of this method, particularly in the study of slow phenomena (at least 15 days between the factor and the event).

7 Conclusion

The objective of this study was to identify any possible correlation between meteorological factors and rockfalls, even in the case of databases containing very few events. Preliminary statistical analyses helped to identify several correlations in the case of a "rich" database. However, no correlation was detected in the more typical "poor" databases due to the sparse representation of days with several rockfalls. The proposed method uses the probability of occurrence of the chosen triggering factor to assess the influence of this factor on the rockfalls. This approach serves to highlight the correlation between a small number of events and a meteorological factor. For a database containing only 3% of days with events, the method used to detect a correlation assessed whether approximately 50% of the events were perfectly correlated with the meteorological factor chosen. The use of this method confirms the positive correlation between rainfalls and rockfalls on La Réunion database. It highlights a

correlation between the cumulative rainfalls and rockfalls in the Bourgogne region, and it detects a correlation between the daily minimum temperature and rockfalls in the Auvergne database. The proposed method allowed the probability of events to be estimated given the value of the meteorological factor studied. These probabilities should be helpful in terms of risk management, e.g., for optimizing the patrolling services for each site according to the susceptibility of that site to the meteorological factors.

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Tables

Table 1. Principal characteristics of the three databases

	RN1 on La Réunion Island	Bourgogne region	Auvergne region
Number of events	949	135	142
Number of days with events	529	126	122
Average number of events per day with events	1.79	1.07	1.16
Number of days in the database	4,008	4,739	4,008
Daily rockfall hazard	0.013	0.003	0.003

Table 2. Number of rockfalls for various intervals of daily rainfall

RN1 or	n La Réunior	ı Island	Вс	ourgogne reg	ion	A	uvergne regi	on
Daily		Frequenc	Daily		Frequenc	Daily		Frequenc
rainfall	Frequenc	y of	rainfall	Frequenc	y of	rainfall	Frequenc	y of
interval	y of the	rockfalls	interval	y of the	rockfalls	interval	y of the	rockfalls
(mm/day	interval	in the	(mm/day	interval	in the	(mm/day	interval	in the
)		interval)		interval)		interval
0-20	0.97	0.76	0-5	0.79	0.6	0-5	0.88	0.77
20-40	0.014	0.053	5-10	0.099	0.16	5-10	0.062	0.12
40-60	0.0077	0.072	10-15	0.051	0.13	10-15	0.022	0.049
60-80	0.0032	0.022	15-20	0.029	0.044	15-20	0.014	0.035
80-100	0.0014	0.02	20-25	0.014	0.022	20-25	0.0077	0.014
100-120	0.00075	0.013	25-30	0.0055	0.007	25-35	0.0072	0.007
120-140	0.00075	0.023	30-35	0.0055	0.022	35-60	0.0048	0.007
140-160	0.0005	0.022	35-50	0.0061	0.015			
160-180	0.00075	0.012						
180-220	0.00075	0.003						
220-370	0.00025	2						

Table 3. Values of the cross-correlation between rainfalls and rockfalls for three virtual databases, with a time delay of zero days. This value is compared to the significance threshold, which is equal to 0.031 in all cases. The results presented in bold identify the non-significant correlations (values equal to the threshold value were also considered insignificant).

	x = 43%	x = 13%	x = 3%
$C_r = 100\%$	Maximum value of cross-	Maximum value of cross-	Maximum value of cross-
	correlation = 0.65	correlation = 0.42	correlation = 0.23
$C_r = 75\%$	Maximum value of cross-	Maximum value of cross-	Maximum value of cross-
	correlation = 0.45	correlation = 0.18	correlation = 0.031
$C_r = 50\%$	Maximum value of cross-	Maximum value of cross-	Maximum value of cross-
	correlation = 0.23	correlation = 0.031	correlation = 0.031
$C_r = 25\%$	Maximum value of cross-	Maximum value of cross-	Maximum value of cross-
	correlation = 0.031	correlation = 0.030	correlation = 0.026

Table 4. R^2 and p-values of the linear regression line obtained by the proposed method for three virtual databases. C_r corresponds to the "correlation rate" between the rainfalls and number of events, and x corresponds to the proportion of days with events. The results shown in bold identify non-significant correlations

	x = 43%	x = 13%	x = 3%
$C_r = 100\%$	$R^2 = 0.98$;	$R^2 = 0.93;$	$R^2 = 0.73$;
$C_r = 100\%$	p-value~10 ⁻³⁶	p-value~10 ⁻¹⁸	p-value~10 ⁻⁶
$C_r = 75\%$	$R^2 = 0.88$;	$R^2 = 0.81;$	$R^2 = 0.57$;
$C_r = 7370$	p-value~10 ⁻²⁰	p-value~10 ⁻¹²	p-value~10 ⁻⁴
$C_r = 50\%$	$R^2 = 0.72$;	$R^2 = 0.71;$	$R^2 = 0.50;$
$C_r = 30\%$	p-value~10 ⁻¹¹	p-value~10 ⁻⁷	p-value~10 ⁻³
$C_r = 25\%$	$R^2 = 0.54;$	$R^2 = 0.41;$	$R^2 = 0.47$; p-value > 0.05
$C_r = 23\%$	p-value~10 ⁻⁶	p-value~10 ⁻⁴	p-value = 0.06
$C_r = 10\%$	$R^2 = 0.25$;	$R^2 = 0.18$; p-value > 0.05	_
$C_r = 10\%$	p-value~10 ⁻³	p-value = 0.13	-

- 1 Table 5. Correlations between the chosen meteorological factors and the daily number of
- 2 rockfalls; results obtained with the proposed method on the real databases. Only the
- 3 maximum correlations are presented here.

	La Réunion Island	Bourgogne region	Auvergne region
Daily precipitation (P)	For D_1 - R^2 = 0.70 p-value = 10^{-9} Correlation coefficient = 0.12	No correlation	No correlation
Cumulative Daily precipitation (P_c)	For D_1 - R^2 = 0.74 p-value = 10^{-13} Correlation coefficient = 0.10	For D_2 - R^2 = 0.54 p-value = 10^{-5} Correlation coefficient = 0.012	No correlation
Daily minimum temperature (T_{min})	For D_1 - R^2 = 0.69 p-value = 10^{-6} Correlation coefficient = 0.5	No correlation	For D_2 - R^2 = 0.34 p-value = 10^{-5} Correlation coefficient = 0.05
Daily maximum temperature (T_{max})	For D_1 - R^2 = 0.60 p-value = 10^{-5} Correlation coefficient = 0.8	No correlation	No correlation
Daily temperature amplitude (T_{amp})	No correlation	No correlation	No correlation
Daily freezing duration	No correlation	No correlation	No correlation

- 4 D_0 is the day of the event(s) studied, and (D_n) identifies the n days before, with n varying from one to 10.
- Table 6. Probability of having at least one event on a day falling within a given interval of daily rainfall (La Réunion Island and Bourgogne region) and different intervals of daily
- 8 minimum temperatures (Auvergne)

La Réunion Island		Bourgogne	region	egion Auvergne region	
Interval of cumulative daily rainfall over two days $(D_0 + D_1)$ (mm/day)	Probability of at least one event	Interval of cumulative daily rainfall over three days $(D_0 + D_1 + D_2)$ (mm/day)	Probability of at least one event	Interval of daily minimum of temperature (D ₂) (°C/day)	Probability of at least one event
Daily rockfall probability: 0.13 Dail		Daily rockfall prob	bability: 0.02	Daily rockfall 0.0 2	
0-5	0.09	0-5	0.013	-20; -10	0.1
5-10	0.16	5-10	0.026	-10; -5	0.052
10-15	0.25	10-15	0.036	-5; 0	0.039
15-20	0.32	15-20	0.041	0-5	0.024
20-30	0.39	20-30	0.032	5-10	0.023
30-40	0.45	30-40	0.03	10-15	0.029
40-50	0.55	40-50	0.043	15-22	0.027
50-70	0.54	50-70	0.053		•
70-90	0.64	70-136	0.111		

90-120	0.64
120-150	1
150-200	1
200-516	0.73

1	
2	
3	
1	



Figure 1. Location of the three sites, corresponding to (a) the Auvergne region, (b) the Bourgogne region, and (c) Highway RN1 on La Réunion Island.

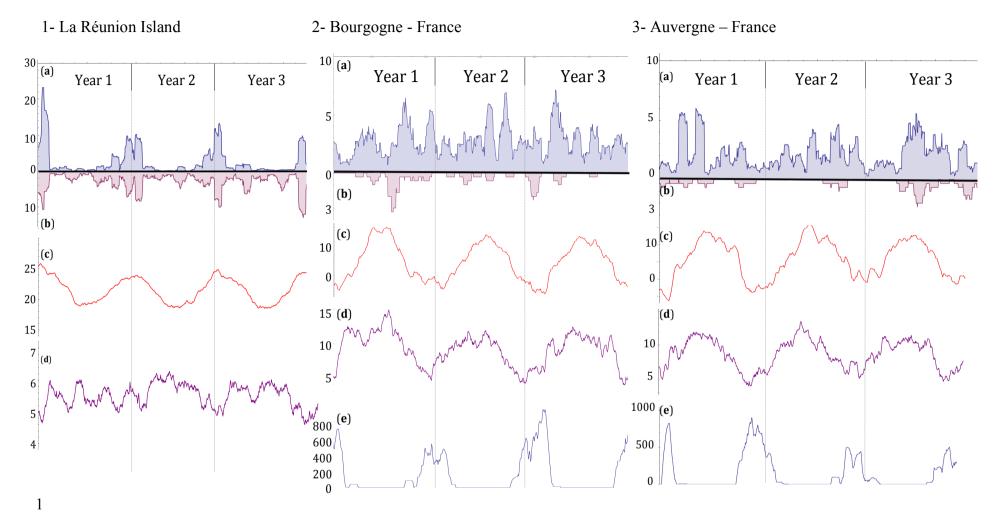


Figure 2. Temperature, rainfall, and rockfall for a three-year period for the three studied sites (30-day moving average). (a) Precipitation (mm

of rain). (b) Rockfall. (c) Minimum of temperature (°C). (d) Daily temperature amplitude (°C). (e) Duration of the freezing period (min).

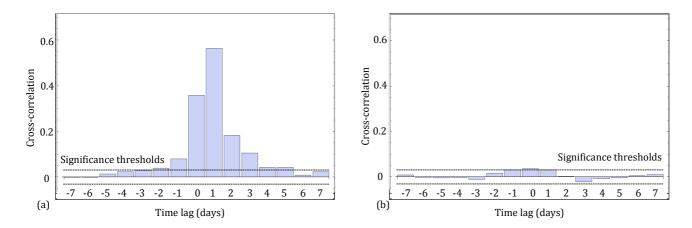


Figure 3. Cross-correlation of rockfall and rainfalls for (a) La Réunion Island and (b) the Bourgogne region. The significance threshold, equal to 0.031, is represented by the dashed lines.

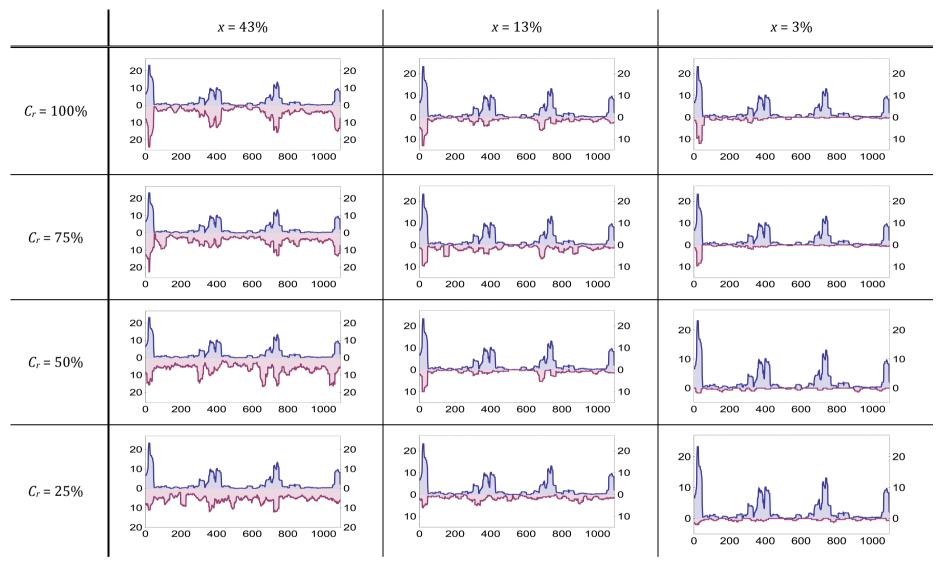
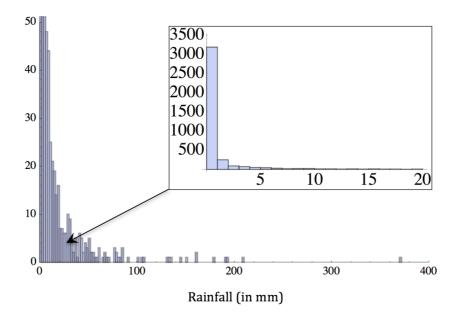


Figure 4. Qualitative correlation between rockfalls and rainfalls (30-day moving average) for the 12 virtual databases. C_r corresponds to the "correlation rate" between the rainfall and number of events, and x corresponds to the proportion of days with events. The x-axis corresponds to the days. The y-axis corresponds to the daily rainfall in mm (above zero) versus the number of rockfalls (below zero).



2 Figure 5. Histogram of the rainfall for the La Réunion region.

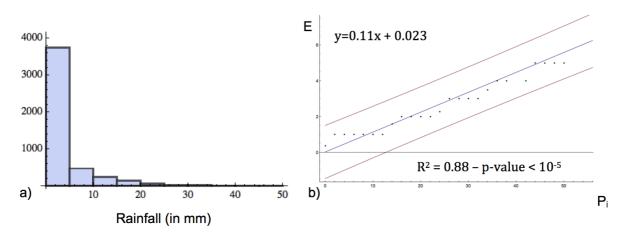


Figure 6. a) Histogram of the rainfall for the Bourgogne region; b) Application of the method to a virtual database with 56% of days with events and rain that fits the empirical distribution of the Bourgogne rainfall. For these days, the rockfall and rainfall magnitudes are 100% correlated.

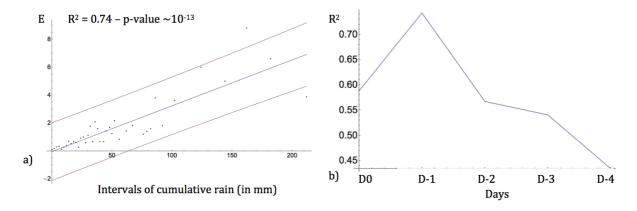


Figure 7. La Réunion Island; a) Application of the method to the cumulative rain over two days $(D_0 + D_1)$; b) \mathbb{R}^2 of rockfall vs. rain accumulated over several days.

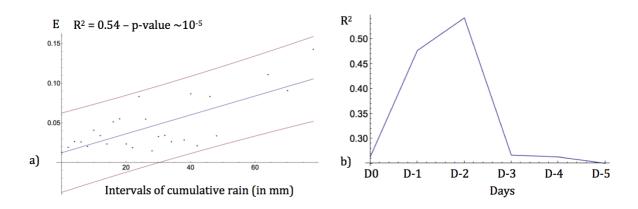


Figure 8. Same as Figure 7 for the Bourgogne region. a) Cumulative rain over three days (D_0 + D_1 + D_2).

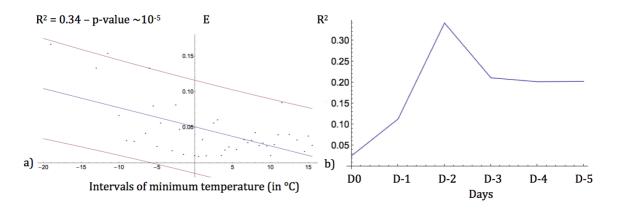


Figure 9. Same as Figure 7 for the Auvergne region. a) Minimum temperature on D_2 .