

analysis tool to analyze the dynamics of the underlying systems that generated the series (Ghil et al., 2002). It is very popular for principle component analysis (Serita et al., 2005) of different types of atmospheric and geophysical signals and useful for filtering the geophysical fields (Rajesh et al., 2014) and astronomical images (Zotov, 2012) to identify significant dynamical components. In the present work we have adopted SSA algorithm to decompose the annual earthquake number data to identify the principle component. The SSA has been performed following the steps (Golyandina et al., 2001).

Trajectory matrix $\mathbf{T}_{(L \times K)}$ formulation. The time series $\mathbf{X}(\mathbf{t}) = \{x_1, x_2, \dots, x_N\}$ of length N will be projected into phase space of dimensions L called window length ($2 < L \leq N/2$, and $K = N - L + 1$) to get trajectory matrix $\mathbf{T}_{L \times K} = [X_1 : \dots : X_K]$. Where $X_i = \{x_{i+1}, x_{i+2}, \dots, x_{i+L}\}$ is a vector of length L and i takes values from 1 to K .

Singular value decomposition. Eigen vectors (U_i, V_i) and values $(\sqrt{\lambda_i})$ of the trajectory matrix are obtained through the Singular Value Decomposition.

$$\mathbf{T} = \sum_{i=1}^d \sqrt{\lambda_i} U_i V_i^T \quad (1)$$

The group $(\sqrt{\lambda_i}, U_i, V_i)$ is called the i th eigen triplet.

Grouping and reconstruction. From the identified eigen triplets we will reconstruct the trajectory matrix (\mathbf{T}_r) using $\mathbf{T}_r = \sum_i \sqrt{\lambda_i} U_i V_i^T$, where i represent the a group of Eigen triplets.

$$\mathbf{T}_r = \begin{bmatrix} \mathbf{y}_{(1,1)} & \dots & \mathbf{y}_{(1,K)} \\ \vdots & \ddots & \vdots \\ \mathbf{y}_{(L,1)} & \dots & \mathbf{y}_{(L,K)} \end{bmatrix} \quad (2)$$

Diagonal averaging. The reconstructed series $X_r = \{g_1, g_2, \dots, g_k, \dots, g_N\}$ can be obtained through diagonalization or Hankelization of reconstructed trajectory matrix

shown in Eq. (2).

$$g_k = \begin{cases} \frac{1}{k+1} \sum_{m=1}^{k+1} y_{m,k-m+2} & \text{for } 1 \leq k < L \\ \frac{1}{L} \sum_{m=1}^L y_{m,k-m+2} & \text{for } L \leq k < K \\ \frac{1}{N-k} \sum_{m=k-K+2}^{N-K+1} y_{m,k-m+2} & \text{for } K \leq k \leq N \end{cases} \quad (3)$$

4 Result

The consideration of earth as a closed and/or an isolated system for studying its various processes may not be appropriate, since the modern concept of earth system science suggest the coupling of endogenic and exogenic forcing to drive the earth's dynamical processes. Here, we study the occurrences of the global earthquake to understand the dynamics and driving forces by means of the contributions of their principle components and eigenvalues on global scales. As a first step of our analysis, we have filtered the entire data with a cutoff magnitude ($M \geq 4.7$) (Fig. 1) and then the annual earthquake rates are normalized and compared with the normalized surface air temperature data. The trends of earthquake data are clearly matching with the temperature data (Fig. 2). We find a strong correlation with correlation coefficient +0.77 among normalized earthquake numbers and normalized temperature.

The strong correlation between temperature and global earthquake rates infers that the major dynamical processes driving the global temperature and earthquake process are of the same kind. The global surface air temperature contains an increasing trend along with oscillatory pattern during the period of analysis. As a whole the global temperature is the representative of solar activity as well as energy receiving from earth (in the form of radiation). The radiation from the earth is possible, as the earth undergoing cooling from the day one of its origin. As we do not have a blackbody as sensor

to observe all the radiation bands emanating from earth, we are missing some crucial information in the measurements of heat flow. Nevertheless, atmosphere is a strong absorber containing large variety of chemical species, which are sensitive to specific bands of radiation. Therefore, the radiations that are missing in our measurements could also be captured by the atmosphere and thus retaining in the form of trends in the atmospheric parametric measurements. Researchers inferred the centennial to millennial scale solar induce oscillations in the temperature data set (Tiwari et al., 2013). The comparison of solar activity with temperature data also supports the effect of higher order solar cycles (centennial scale) on the seismic activity reported by Shestopalov and Kharin (2006).

The earthquake rate data was further subjected to SSA using the appropriate window length 15. The window length was chosen appropriately keeping in view the length of the data size. The first three principle components were found significant with 98 % variance and the remaining principal components contributes only 2 %. The first principle component alone shows 93 % variance with a linear increasing trend starting from 1975 to 2005. The second and third principle components superimposed on the main trend shows apparently 11 years periodic component with variance 5 %. The rest of the components contribute 2 % , which may be attributed to artificial and natural triggering forces (reservoir and tidal triggering etc.). Thus, our analysis quantified the contribution of ~ 11 year solar cycle effect on global seismic activity in terms of Eigen value percentages (5 %). We have reconstructed the data using principle components 2 and 3 to compare with the sunspot number data. The normalized reconstructed data of earthquake rates along with the normalized annual sunspot number data are shown in Fig. 3. One can clearly see that there is peak-to-peak out of phase match between the sunspot numbers and reconstructed annual earthquake rates (Fig. 3). Thus, the normalized global earthquake numbers reconstructed from the periodic components of 11 years periodicity has shown a significant negative correlation (-0.4) with the sunspot number. The earlier researchers (Simpson, 1967; Shestopalov and Kharin,

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2014) have also reported the negative correlation between sunspot number 11 year cycle and earthquake occurrence.

Statistical correlation and/or evidence of matching periodicity among the two or more phenomena cannot guarantee their physical link. Hence, at this stage, we can only surmise a probable physical mechanism among the solar activity, temperature variations and earthquakes occurrences. Keeping in view of only 5 % contribution of 11 year oscillatory component superimposed on the main monotonic earthquake data trend, the link between earthquakes and solar cycle may not be the direct one. Hence, the solar cycle apparently visible in the global earthquake record could be considered as a triggering agent only. We, however, note that the surface activity of the Sun produces variations in its electromagnetic and corpuscular emissions, which consist of both continuous (photospheric) and sporadic (flare) components (Stothers, 1989; Roberts, 2013). Accordingly, the variable part of this solar radiation produces small incremental reversals of heating or cooling of the earth's atmosphere. This is clearly seen in various records of earth's global and regional temperature, pressure, precipitation and zonal wind pattern in the form of 11 year solar cycle (Kelly, 1977; Labitzke, 1987; Labitzke and van Loon, 1989; Stothers, 1989). A direct implication of this perturbation on circulation patterns of the earth's air masses may lead a slight alteration of the earth's angular momentum (Stothers, 1989). For sustainability and stability of earth's dynamics, the solar induced changes in angular momentum attuned through a change in its rotational speed, which are apparently reflected in the length of the day (LOD) variations. In a recent study, Michelis et al. (2013) verified and reconfirmed the periodic variations in LOD (Curries, 1981). According to Lambeck and Cazanev (1976), the change in the length of the day is due to the impact of seasonally changing solar insolation. The observed 11 year solar induced cyclic variation in the LOD is one of the evidences for such periodic forcing (Challinor, 1971; Curries, 1981). The other slower cycles reported by them are also confirmed in a recent work (Michelis et al., 2013) and probably also observed after very large individual solar flare (Danjon, 1962a, b; Gribbin and Plagemann, 1973; Stothers, 1989). It appears, therefore, that atmospheric

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disturbances/perturbations might some way or other is involved in catalyzing the small abrupt/instantaneous changes in the earth's rate of rotation. Associated torques in the solid earth might then trigger a host of minor and major earthquake (Anderson, 1974) depending upon the intensity of nonlinear coupling among these phenomena. Integrating the above results, the change in the earth's angular momentum by the solar activity may drive seismic activities with a common periodicity.

Further to the above mechanism, one could also hypothesize the global atmospheric perturbation, which might influence earthquake activities through changes in annual/seasonal precipitation. It has been suggested (Stothers, 1989; Tiwari and Rao, 2001) that increase in rain fall around the year of solar minima must lead to temporally larger reservoir's of ground water in and near rift and shear zones, volcanic magmas, (earthquakes prone regions). The increase in the precipitation near the earthquake prone site (epicenter) at the times of "earthquake criticality" has been reported from Indian earthquakes (Goswami et al., 2014). There is well known relation between the Indian precipitation records and solar activities (Reddy et al., 1989). Tiwari and Rao (2001) analyzed the power law distribution of earthquake occurrence from Northeast, India and inferred a possible seasonal and solar cyclic pattern in earthquake record. Hence, there is possible explanation for the indirect link between seismicity and temperature/solar activity.

5 Conclusions

We have applied SSA to separate the dynamical principal components from the global earthquake record spanning over the period of 1975 to 2005, which are involved in generating the earthquake activities. Based on SSA of a complete earthquake data set, we have quantified the 11 year solar cyclic pattern, with 5% variance in terms of eigen value, which is superimposed on a linear monotonic trend. The observed monotonic trend in the earthquake data alone contributing to 93% variance, which appears to be linked with the earth's internal dynamical processes. The negative correlation

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(correlation coefficient -0.4) between the SSA reconstructed data of the 11 year periodic components and Sunspot numbers agree well with the earlier results carried out by other researchers on regional and global scale. Even though the possible evidence of periodicities in the earthquake process is a somewhat debated issue in earth science community, the 11 year cyclic variation in the earthquake occurrence was verified and reconfirmed through the comparison of the reconstructed earthquake rates with sunspot data. Evidence of periodicities implies predictably and therefore, if such cycles indeed exist they would add a significant dimension to improve predictions of the future earthquakes.

The correlation analysis between the annual global earthquake rates and global temperature revealed that there is a good correlation (coefficient $+0.77$) between the two phenomena, rendering an impression that both dynamical processes are coupled some way or other. The present study provide an interesting example of coupled multiple physical processes, which require more rigorous data analyses using the longer earthquake record for quantifying and confirming the contribution of such cyclic forcing.

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References

- Anderson, D. L.: Earthquakes and the rotation of the Earth, *Science*, 186, 4158, doi:10.1126/science.186.4158.49, 1974.
- Broomhead, D. S. and King, G. P.: Extracting qualitative dynamics from experimental data, *Physica D*, 20, 217–236, 1986a.
- Broomhead, D. S. and King, G. P.: On the qualitative analysis of experimental dynamical systems, in: *Nonlinear Phenomena and Chaos*, edited by: Sarkar, S., Adam Hilger, Bristol, 113, 1986b.

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- Cadicheanu, N., van Ruymbeke, M., and Zhu, P.: Tidal triggering evidence of intermediate depth earthquakes in the Vrancea zone (Romania), *Nat. Hazards Earth Syst. Sci.*, 7, 733–740, doi:10.5194/nhess-7-733-2007, 2007.
- Carder, D. S.: Influence of reservoir-loading on earthquake-activity in the Boulder dam area, *Trans. AGU*, 26, p. 203, doi:10.1029/TR026i002p00203, 1945.
- 5 Challinor, R. A.: Variations in the rate of rotation of the Earth, *Science*, 172, 1022–1025, 1971.
- Chao-Di, X., Xiao-Ping, W., Xing-Lin, L., Wei, M., and Nan, S.: Long-period tides and global earthquake energy release, *Chinese J. Geophys.-Ch.*, 56, 823–832, doi:10.1002/cjg2.20074, 2013.
- 10 Cochran, E. S., Vidale, J. E., and Tanaka, S.: Earth tides can trigger shallow thrust fault earthquakes, *Science*, 306, 1164–1166, doi:10.1126/science.1103961, 2004.
- Currie, R. G.: Solar cycle signal in Earth rotation: nonstationary behavior, *Science*, 211, 386–389, doi:10.1126/science.211.4480.386, 1981.
- Danjon, A.: Sur la variation continue de la rotation de la Terre, *C. R. Hebd. Seances Acad. Sci.*, 254, 2479–2482, 1962a.
- 15 Danjon, A.: La rotation de la Terre et le Soleil calme, *C. R. Hebd. Seances Acad. Sci.*, 254, 3058–3061, 1962b.
- De Michelis, P., Tozzi, R., and Consolini, G.: On the nonstationarity of the decadal periodicities of the length of day, *Nonlin. Processes Geophys.*, 20, 1127–1135, doi:10.5194/npg-20-1127-2013, 2013.
- 20 Fourel, L., Milelli, L., Jaupart, C., and Limare, A.: Generation of continental rifts, basins, and swells by lithosphere instabilities, *J. Geophys. Res.-Sol. Ea.*, 118, 3080, doi:10.1002/jgrb.50218, 2013.
- Fraedrich, K.: Estimating dimensions of weather and climate attractors, *J. Atmos. Sci.*, 43, 419–432, 1986.
- 25 Ghil, M., Allen, M. R., Dettinger, M. D., Ide, K., Kondrashov, D., Mann, M. E., Robertson, A. W., Saunders, A., Tian, Y., Varadi, F., and Yiou, P.: Advanced spectral methods for climatic time series, *Rev. Geophys.*, 40, 1003, doi:10.1029/2000RG000092, 2002.
- Golyandina, N., Nekrutkin, V., and Zhigljavsky, A.: *Analysis of Time Series Structure: SSA and Related Techniques*, Chapman & Hall/CRC Monographs on Statistics & Applied Probability, Taylor & Francis, 2001.
- 30

2861

- Goswami, H., Devi, M., Rambabu, S., Barbara, A. K., and Prakash, K.: An analysis of the relationship between precipitation and earthquakes in the Indian region, *Indian J. Radio Space*, 43, 41–47, 2014.
- Gribbin, J. and Plagemann, S.: Discontinuous change in Earth's spin rate following great solar storm of August 1972, *Nature*, 243, 26–27, 1973.
- 5 Gupta, H. K.: Induced seismicity hazard mitigation through water level manipulation at Koyna, India: a suggestion, *B. Seismol. Soc. Am.*, 73, 679–682, 1983.
- Gupta, H. K.: A review of recent studies of triggered earthquakes by artificial water reservoirs with special emphasis on earthquakes in Koyna, India, *Earth-Sci. Rev.*, 58, 279–310, 2002.
- 10 Heaton, T. H.: Tidal triggering of earthquakes, *B. Seismol. Soc. Am.*, 72, 2181–2200, 1982.
- Jusoh, M. H. and Yumonto, K.: Possible Correlation between Solar Activity and Global Seismicity, *Proceeding of the IEEE International Conference on Space Science and Communication (Icon Space)*, Penang, Malaysia, 2011.
- Kasahara, J.: Tides, earthquakes, and volcanoes, *Science*, 297, 348–349, 2002.
- 15 Kelly, P. M.: Solar influence on North Atlantic mean sea level pressure, *Nature*, 269, 320–322, 1977.
- Knopoff, L.: Earth tides as a triggering mechanism for earthquakes, *B. Seismol. Soc. Am.*, 54, 1865–1870, 1964.
- Labitzke, K.: Sunspots, the QBO, and the stratospheric temperature in the north polar region, *Geophys. Res. Lett.*, 14, 535–537, 1987.
- 20 Labitzke, K. and Van Loon, H.: Recent work correlating the 11 year solar cycle with atmospheric elements grouped according to the phase of the quasi-biennial oscillation, *Space Sci. Rev.*, 49, 239–258, 1989.
- Lambeck, K. and Cazenave, A.: Long term variations in the length of day and climatic change, *Geophys. J. R. Astron. Soc.*, 46, 555–573, 1976.
- 25 Métivier, L., de Viron, O., Clinton, P. C., Renault, S., Diament, M., and Patau, G.: Evidence of earthquake triggering by the solid earth tides, *Earth Planet. Sc. Lett.*, 278, 370–375, 2009.
- Odintsov, S. D., Ivanov-Kholodnyi, G. S., and Georgieva, K.: Solar activity and global seismicity of the Earth, *B. Russ. Acad. Sci.-Phys.*, 71, 593–595, 2007.
- 30 Rajesh, R., Tiwari, R. K., Dhanam, K., and Seshunarayana, T.: T-x frequency filtering of high resolution seismic reflection data using singular spectral analysis, *J. Appl. Geophys.*, 105, 180–184, doi:10.1016/j.jappgeo.2014.03.017, 2014.

2862

- Reddy, R. S., Neralla, V. R., and Godson, W. L.: The solar cycle and Indian rainfall, *Theor. Appl. Climatol.*, 39, 194–198, 1989.
- Roberts, W. O.: Solar-Terrestrial Relationship, in: *Geophysics and the IGY: Proceedings of the Symposium at the Opening of the International Geophysical Year*, edited by: Odishaw, H. and Ruttenberg, S., American Geophysical Union, Washington DC, doi:10.1029/GM002p0001, 2013.
- 5 Schuster, A.: On lunar and solar periodicities of earthquakes, *P. R. Soc. London*, 61, 455–465, 1897.
- Serita, A., Hattori, K., Yoshino, C., Hayakawa, M., and Isezaki, N.: Principal component analysis and singular spectrum analysis of ULF geomagnetic data associated with earthquakes, *Nat. Hazards Earth Syst. Sci.*, 5, 685–689, doi:10.5194/nhess-5-685-2005, 2005.
- 10 Shestopalov, I. P. and Kharin, E. P.: Time variations in the relations between seismicity of the earth and solar activity cycles of different duration, *Geofiz. Zh.*, 28, 59–70, 2006.
- Shestopalov, I. P. and Kharin, E. P.: Relationship between solar activity and global seismicity and neutrons of terrestrial origin, *Russ. J. Earth Sci.*, 14, ES1002, doi:10.2205/2014ES000536, 2014.
- 15 Simpson, J. H.: Solar activity as a triggering mechanism for earthquakes, *Earth Planet. Sc. Lett.*, 3, 417–425, 1967.
- Souriau, M., Souriau, A., and Gagnepain, J.: Modeling and detecting interactions between Earth tides and earthquakes with application to an aftershock sequence in the Pyrenees, *B. Seismol. Soc. Am.*, 72, 165–180, 1982.
- 20 Stothers, R. B.: Volcanic eruptions and solar activity, *J. Geophys. Res.*, 94, 17371–17381, 1989.
- Tanaka, S.: Tidal triggering of earthquakes precursory to the recent Sumatra megathrust earthquakes, *Geophys. Res. Lett.*, 37, L02301, doi:10.1029/2009GL041581, 2010.
- 25 Tanaka, S., Ohtake, M., and Sato, H.: Evidence for tidal triggering of earthquakes as revealed from statistical analysis of global data, *J. Geophys. Res.*, 107, 2211, doi:10.1029/2001JB001577, 2002.
- Tavares, M. and Azevedo, A.: Influences of solar cycles on earthquakes, *Natur. Sci.*, 3, 436, doi:10.4236/ns.2011.36060, 2011.
- 30 Tiwari, R. K. and Rao, K. N. N.: Power law random behavior and deterministic earthquake seasonality of Northeast India, *J. Geol. Soc. India*, 57, 369–376, 2001.

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- Tiwari, R. K. and Sri Lakshmi, S.: Some common and contrasting features of earthquake dynamics in major tectonic zones of Himalayas using nonlinear forecasting approach, *Curr. Sci. India*, 88, 640–647, 2005.
- Tiwari, R. K., Sri Lakshmi, S., and Rao, K. N. N.: Nature of earthquake dynamics in the central Himalayan region: a nonlinear forecasting analysis, *J. Geodyn.*, 35, 273–287, 2003.
- 5 Tiwari, R. K., Yadav, R. R., and Kaladhar Rao, K. P. C.: Empirical orthogonal function spectra of extreme temperature variability decoded from tree rings of the western Himalayas, *Geoph. Monog. Series*, 196, 169–176, 2013.
- Vidale, J. E., Agnew, D. C., Johnston, M. J. S., and Oppenheimer, D. H.: Absence of earthquake correlation with Earth tides: an indication of high preseismic fault stress rate, *J. Geophys. Res.*, 103, 24567–24572, 1998.
- 10 Wilcock, W. S. D.: Tidal triggering of microearthquakes on the Juan de Fuca Ridge, *Geophys. Res. Lett.*, 28, 3999, doi:10.1029/2001GL013370, 2001.
- Zhang, G.-Q.: Relationship between global seismicity and solar activity, *Acta Seismol. Sin.*, 11, 495–500, 1998.
- 15 Zotov, L. V.: Application of multichannel singular spectrum analysis to geophysical fields and astronomical images, *Adv. Astronom. Space Phys.*, 2, 82–84, 2012.

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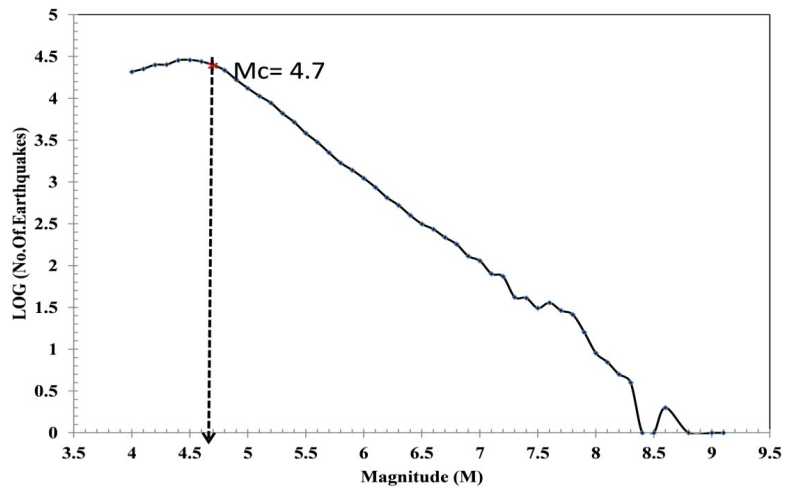


Fig. 1. Gutenberg–Richter plot of Global earthquake data from 1975 to 2005.

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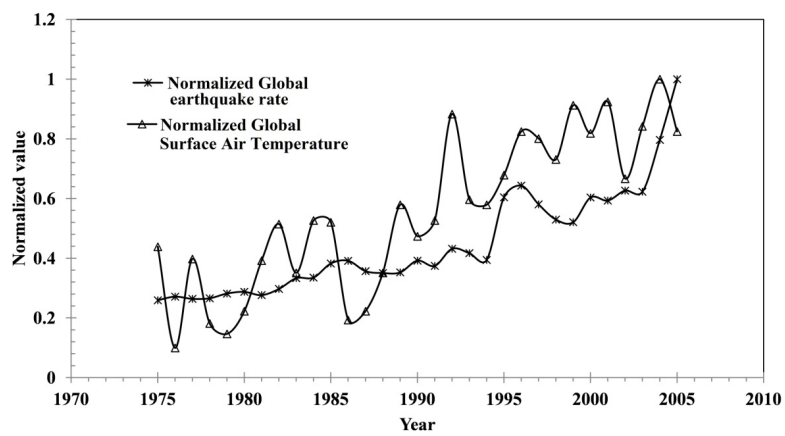


Fig. 2. Normalized yearly global earthquake rates and normalized global surface air temperature from 1975 to 2005.

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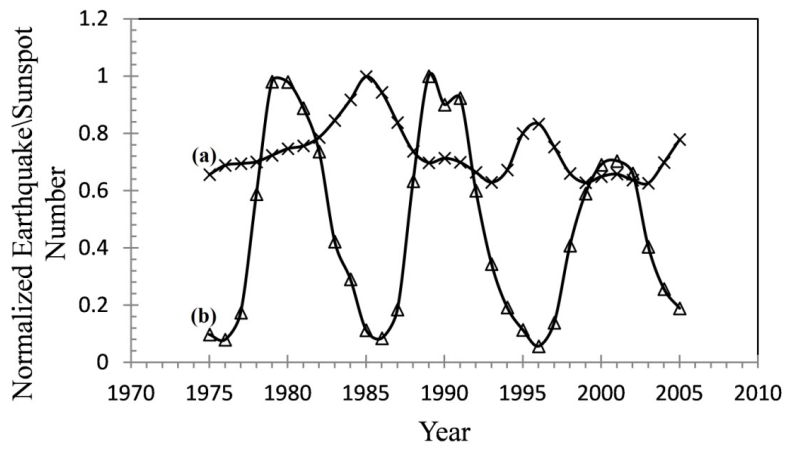


Fig. 3. SSA reconstructed normalized yearly global earthquake rates from principle components 2 and 3 **(a)** and normalized Sunspot numbers from 1975 to 2005 **(b)**.