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Modeling extreme wave heights from laboratory experiments with the nonlinear Schrödinger equation

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Spatial variation of nonlinear wave groups with different initial envelope shapes is theoretically studied first, confirming that the simplest nonlinear theoretical model is capable of describing the evolution of propagating wave packets in deep water. Moreover, three groups of laboratory experiments run in the wave basin of CEHIPAR are systematically compared with the numerical simulations of the nonlinear Schrödinger equation. Although a small overestimation is detected, especially in the set of experiments characterized by higher initial wave steepness, the numerical simulations still display a high degree of agreement with the laboratory experiments. Therefore, the nonlinear Schrödinger equation catches the essential characteristics of the extreme waves and provides an important physical insight into their generation. The modulation instability, resulted by the guasi-resonant four wave interaction in a unidirectional sea state, can be indicated by the coefficient of kurtosis, which shows an appreciable correlation with the extreme wave height and hence is used in the modified Edgeworth-Rayleigh distribution. Finally, some statistical properties on the maximum wave heights in different sea states have been related with the initial Benjamin-Feir Index.

Introduction

In the early formulations the free surface elevation in deep water has been assumed to follow a Gaussian structure and has been modeled as the linear superposition of a large number of elementary wavelets with Rayleigh distributed amplitudes and random phases (Longuet-Higgins, 1952). At this linear level of approximation, surface displacements are symmetric with respect to the mean water level and completely described by the autocorrelation function or power spectrum.

However, surface waves are nonlinear in nature and bound waves need to be taken into account (Hasselmann, 1962; Longuet-Higgins, 1963). As reviewed by Guedes Soares (2003), numerous theoretical and empirical models of wave heights have been

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suggested after the proposal of the linear Rayleigh model. The non-Gaussian and phase-coupled bound modes have no significant effect on the crest-to-trough wave heights although they make wave crests shaper and narrower, and troughs shallower and more rounded (Tayfun and Fedele, 2007; Petrova et al., 2008).

In a recent study, third-order nonlinearity represented by the fourth-order cumulants has been successfully applied in the statistics of the so called abnormal, freak or roque waves, of which the probability is described reasonably well by the theoretical approximation based on Gram-Charlier (GC) expansions (Tayfun and Fedele, 2007). The deviation from the Gaussian structure is mainly attributed to modulation instability in the wave train, which can be considered as a quasi-resonant four-wave interaction in unidirectional narrowband waves. The third-order nonlinear interactions between free wave modes, described quantitatively by means of the coefficient of kurtosis λ_{40} , are responsible for the large amplitude events and the increased probability of occurrence of abnormal waves, as shown in a series of studies (e.g., Hagen, 2002; Guedes Soares et al., 2003, 2004a, b; Petrova et al., 2007; Onorato et al., 2006; Mori et al., 2007; Cherneva et al., 2009, 2011; Shemer et al., 2009, 2010).

Due to the potentially severe damage of extreme waves to the vessels and offshore structures at sea (Guedes Soares et al., 2008; Fonseca et al., 2010), a lot of efforts have been devoted to understanding the mechanisms of their generation and a number of reasons why abnormal waves may occur have been put forward. Besides the linear superposition of Fourier components with coherent phases and strong wave-current interaction or wave diffraction, recently it has been strongly argued that nonlinear selfmodulation of a slowly varying wave train can produce abnormal waves. A simple example is the case of a uniform narrowband wave train to sideband perturbations where nonlinear interaction known as the Benjamin-Feir instability will result in focusing of wave energy in space and/or time as illustrated in laboratory experiments (Lake et al., 1977).

To a first approximation, the evolution of the envelope of a narrowband wave train is described by the nonlinear Schrödinger equation which was first derived by

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Zakharov (1968) using a spectral method and by Hasimoto and Ono (1972) and Davey (1972) using multiple-scale methods. The nonlinear Schrödinger equation in one-space dimension may be solved by means of the inverse scattering transform. For vanishing boundary conditions, Zakharov and Shabat (1972) found that for large times the solution consists of a combination of envelope solitons and radiation modes, in analogy with the solution of the Korteweg-de Vries equation. For periodic boundary conditions, the solution is more complex. Linear stability analysis of a uniform wave train shows that close side bands grow exponentially in time in good qualitative agreement with the experimental results of Benjamin and Feir (1967) and Lake et al. (1977). For large times there is a considerable energy transfer from the carrier wave to the side bands.

Numerical modeling performed with a higher-order nonlinear Schrödinger equation can provide more information as shown in the comparison with real data from field experiment collected in the WACSIS JIP has been done in the work of Liu et al. (2005), as well as in other studies that dealt with full-scale data (Slunyaev et al. 2005, 2013).

Although higher-order nonlinear equations such as Dysthe equation are more accurate than NLS model in describing the evolution of groups of strongly nonlinear waves produced in the wave tanks (Shemer et al., 2002), the studies of the properties of nonlinear Schrödinger equation have been vital in understanding the conditions under which abnormal waves may occur (Onorato et al., 2001). One typical example in explanation of extreme waves is the work of Osborne (2000) where the solution of the one-dimensional nonlinear Schrödinger equation with periodic boundary conditions is written as a "linear" superposition of stable modes, unstable modes, and their mutual nonlinear interactions. The stable modes form a Gaussian background wave field from which the unstable modes occasionally rise up and subsequently disappear again, repeating the process quasi-periodically in time.

In this study, the properties of the nonlinear Schrödinger equation will be analyzed in describing the evolution of various envelopes and simulations will be performed of random waves in unidirectional sea states characterized by the JONSWAP power

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This paper is organized as follows: in Sect. 2 a short review of basic theory and analytical formulae applied in this paper are given. Section 3 briefly introduces the facilities in the wave basin and the experimental data, and Sect. 4 devotes to the numerical simulation of spatial evolution of wave envelops of Gaussian and Bichromatic waves. The exceedance distributions of wave height in three typical sea states are compared between laboratory experiments and numerical simulations in the first part of Sect. 5 where the theoretical models including linear and nonlinear are also presented. The second part of Sect. 5 reveals some statistics on the maximum wave heights and some useful conclusions are summarized in the last section.

2 Theory

The simplest weakly nonlinear model that describes the evolution of free waves is the so-called cubic Schrödinger equation, which has been derived from the Zakharov equation under the narrow-band approximation (Zakharov, 1968) and represents a perfect framework in which the basic features of the modulational instability are contained. Working as a balance between dispersion and nonlinearity, the dimensional NLS equation in arbitrary depth, in a frame of reference moving with the group velocity, has the following form:

$$\frac{\partial A}{\partial t} + i\alpha \frac{\omega_0}{8k_0^2} \frac{\partial^2 A}{\partial x^2} + i\beta \frac{\omega_0 k_0^2}{2} |A|^2 A = 0$$
 (1)

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In order to derive the Benjamin-Feir index (*BFI*) in a simple and instructive way, Eq. (1) is nondimensionalized in the following ways: $A = A/a_0$, $x = x\Delta K$ and $t = t(\Delta K/k_0)^2 \alpha \omega_0/8$, where ΔK represents a typical spectral band-width, a_0 a typical wave amplitude and thus reduces to:

$$\frac{\partial A}{\partial t} + i \frac{\partial^2 A}{\partial x^2} + i \left(\frac{2\varepsilon}{\Delta K/k_0} \right)^2 \frac{\beta}{\alpha} |A|^2 A = 0$$
 (2)

where primes have been omitted for brevity. The variable $\varepsilon = a_0 k_0$ is a measure of the wave steepness. The Benjamin-Feir Index is now defined as the square root of the coefficient that multiplies the nonlinear term:

$$BFI = \frac{2\varepsilon}{\Delta K/k_0} \sqrt{\frac{|\beta|}{\alpha}}$$
 (3)

The term $\sqrt{|\beta|/\alpha}$ is close to one as k_0h tends to infinity and decreases as the water becomes increasingly shallow, and β will become negative if the value of k_0h is smaller than 1.36 as shown in Fig.1. In such case the modulational instability disappears and Stokes waves are stable to perturbations (Shemer et al., 1998; Onorato et al., 2001). Considering that time series are normally measured in the laboratory experiments, the term $\Delta K/k_0$ in the BFI is replaced by $2\Delta\omega/\omega_0$ for infinite water depth. Due to a historical reason, a factor $\sqrt{2}$ is also added into Eq. (3), hence a random wave train will become unstable if BFI > 1 (Alber and Saffman, 1978).

For the purpose of better understanding the capability of the NLS equation in describing the evolution of propagating wave packet with a narrow spectrum, two simple

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$$\eta(t) = a_0 \exp\left[-\left(\frac{t}{mT_0}\right)^2\right] \cos(\omega_0 t), \quad -16T_0 < t < 16T_0$$
(4)

where the carrier wave period $T_0 = 2\pi/\omega_0$. The energy spectrum of Eq. (4) presents a Gaussian shape as well and its relative width at half maximum is given by $\Delta\omega/\omega_0 = \sqrt{2\ln 2}/(2m\pi)$. The value of the parameter m is set to be 4.0 in this paper, so that all cases considered meet the condition: $\Delta\omega/\omega_0 = 0.047 < \varepsilon$, thus satisfying the narrow spectrum assumption of NLS equation.

In the second series of numerical simulations the bichromatic wave has been studied with the initial surface elevation in the following form:

$$\eta(t) = a_0 \cos(\omega_0/20t) \cos(\omega_0 t), \quad -15T_0 < t < 15T_0$$
 (5)

The carrier wave frequency and the maximum amplitude in the simulation are identical to those with the shape given by Eq. (4). The spectrum of this kind of surface elevation is bi-modal, with two equal-height peaks at $\omega = \omega_0 \pm \Delta \omega$, where $\Delta \omega = \omega_0/20$, satisfying the requirement of narrow spectrum approximation again (Shemer et al., 2002).

For the more realistic ocean environment, the initial condition for the numerical simulations is typical of sea states described by the JONSWAP power spectrum.

$$S(\omega) = \alpha_1 g^2 \omega^{-5} \exp\left[-\frac{5}{4} \left(\frac{\omega_0}{\omega}\right)^4\right] \gamma^{\exp\left[-(\omega-\omega_0)^2/\left(2\sigma_0^2\omega_0^2\right)\right]}$$
 (6)

where $\sigma_0 = 0.07$ if $\omega \le \omega_0$ and $\sigma_0 = 0.09$ if $\omega > \omega_0$. Here ω_0 is the peak frequency, γ is the peak enhancement parameter, and α_1 is the Phillips' constant related with the 5267

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significant wave height H_s . As γ increases, the spectrum becomes higher and narrower around the peak frequency. In the present simulations, $\gamma=3$ and $\Delta\omega$ is estimated with half-width at half maximum of the computed wave spectrum and $\varepsilon=k_0H_s/2$ (Onorato et al., 2006). The initial JONSWAP random surface elevation has been synthesized as sums of independent harmonic components, by means of the inverse Fast Fourier Transform of complex random Fourier amplitudes which are prepared according to the "random realization approach" by using random spectral amplitudes as well as random phases (Onorato and Proment, 2011).

Some previous investigations (Hagen, 2002; Onorato et al., 2006; Cherneva et al., 2009; Toffoli et al., 2008a, b, 2010a, b, 2011) suggest that the noticeably increase of frequency of occurrence of unusually large waves is accompanied by an increment on the coefficient of kurtosis λ_{40} , which has been related with Benjamin-Feir Index for narrowband long-crested waves at large times (Janssen, 2003).

$$\lambda_{40} = \frac{\pi}{\sqrt{3}} BFI^2 \tag{7}$$

where BFI is stationary. Larger BFI means that nonlinearity dominates dispersion and apparently leads to a higher value of coefficient of kurtosis λ_{40} in accordance with Eq. (7). Considering that BFI has a larger variability in its computation (Serio et al., 2005), it makes sense to use BFI as an initial parameter to indicate the chance of observing the freak waves and to take λ_{40} as a critical parameter to describe the extreme wave height in the produced series. The statistics of the unusually large wave heights generated by modulation instability can be explained reasonably well by the theoretical approximations based on Gram-Charlier (GC) expansions (Bitner, 1980; Tayfun and Fedele, 2007; Mori and Janssen, 2006). Such approximation represents Hermite series expansions of distributions describing non-Gaussian random functions which are related to the stochastic structure of waves only through certain key statistic such as the coefficient of kurtosis of surface displacements. For narrowband long-crested waves,

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$$E(h) = \exp\left(-\frac{h^2}{8}\right) \left[1 + \frac{\lambda_{40}}{384}h^2\left(h^2 - 16\right)\right]$$
 (8)

A more general form of third-order nonlinear model (GC) is given by Tayfun and Fedele

(2007). Under a certain condition, i.e., $\Lambda \to \Lambda_{\rm app} \equiv 8\lambda_{40}/3$ where $\Lambda = \lambda_{40} + 2\lambda_{22} + \lambda_{04}$, the GC model converges to MER model. The cumulant coefficients are expressed in the same way as Tayfun and Lo (1990): $\lambda_{40} = \left\langle \eta_1^4 \right\rangle/\sigma^4 - 3$, $\lambda_{22} = \left\langle \eta_1^2 \hat{\eta}_1^2 \right\rangle/\sigma^4 - 1$, $\lambda_{04} = \left\langle \hat{\eta}_1^4 \right\rangle/\sigma^4 - 3$ where σ is the standard deviation of the free wave profile η_1 that is derived via inversion of the observational time series η (Fedele et al., 2010). The bound waves could also be removed by band-pass filter (Onorato et al., 2005) or other procedures (Shemer et al., 2007). Evidently, η_1 is non-Gaussian, but its crest and trough amplitudes have the same distribution. The symmetric amplification imposed on them is due to quasi-resonant interactions and reflected on Λ . If the third-order nonlinearity is negligible, i.e., $\lambda_{40} \cong 0$, Eq. (8) reduces to the Rayleigh exceedance distribution given by

$$_{15} \quad E(h) = \exp\left(-\frac{h^2}{8}\right) \tag{9}$$

3 Facilities and experimental data

The wave basin in CEHIPAR, Spain is 152 m long, 30 m wide and 5 m deep as sketched in Fig. 2. The wave maker is located at one of the 30 m sides. The waves are produced by 60 flaps with independent motion. On the opposite side to the wave maker there is a wave beach which serves to absorb the incident wave energy. The wave maker can produce long and short crested sea states with up to 0.4 m significant wave heights and

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spectra of standard or arbitrary shape. The length scale of the laboratory experiments examined here is 1:40. The waves generated for this study are long-crested and are registered by 6 capacitance wave gauges situated in the mid-line of the basin. Each experiment with the same initial conditions is carried out for two times. For the second ₅ experiment, the gauges are moved 10 m downstream and repeat the same realization. The detailed gauge locations are listed in Table 1.

In this study the spectrum generated at the wave maker is unidirectional. Each experiment uses different sets of random phases but the variance of amplitudes is such that the spectrum of waves generated at the wave-maker represents at full scale a JON-SWAP spectrum characterized with peak-enhancement factor y and Philips parameter α_1 in dependence of the produced significant wave heights.

There are 23 sea states in the experiments with different initial wave parameters listed in full scale in Table 2. According to the initial wave steepness ε , they can be categorized into three groups: the smooth, moderate and severe sea states, and represented by different symbols in the later analysis.

It needs to be pointed out that the numerical simulation results will be labeled by the same type of but open symbols in the later comparisons. The parameters used in the envelope analysis are also from Table 2, that is, the forcing amplitude $a = H_s/2$ and the carrier frequency $\omega_0 = 2\pi/T_0$. One thing has to be kept in mind is that BFI and ε reflect the same initial condition in the study due to the same peak enhancement parameter γ in all sea states.

Wave envelopes

In this section, the transformation of deterministic wave groups is investigated in deep water by the numerical solution of the simplest nonlinear model, i.e., the NLS equation which can reproduce the Benjamin-Feir instability. The initial wave envelopes are derived by Hilbert transform of the surface elevations expressed in Eqs. (4) and (5), and depicted on the two columns in Fig. 3, respectively. The generated surface elevations

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tions. For economy of space, only three results from Cases 4, 13 and 23 in Table 2

are presented from top to bottom in Fig. 3, where the spatial evolution tendencies of

envelopes are typical since they are from different sea state groups.

In the low sea state, e.g., Fig. 3a and d, no significant variation of the wave envelope

along the tank is observed either in the Gaussian wave or in the bichromatic wave for

are normalized by their corresponding maximum wave amplitudes in the initial condi-

the reason that the modulation instability is weak as the initial steepness is small. In the moderate sea state, e.g., Fig. 3b and e, they show the similar evolution speed but different tendency. For the envelope pulse, the initial Gaussian wave group adjusts

its shape and width to become a fundamental soliton with oscillatory tails and attains a "sech" profile. The related theoretical predictions (Zakharov and Shabat, 1972) were

tested experimentally by Yuen and Lake (1975). For the case of the evolution of a nonlinear continuous wave train, the amplitude does not grow exponentially for all time, but instead grows to a maximum value and then decreases in amplitude for later times

and most of them repeat this oscillation periodically over time (Fermi-Pasta-Ulam recurrence). This modulation and demodulation process has been verified in the exper-

iments (Lake et al., 1977) and the oscillatory unstable modes of this type are often referred to as breathers. In the present simulation, this is demonstrated by a periodi-

cally repeated pulse trains for the specified bichromatic wave envelope.

In the severe sea state, e.g., Fig. 3c and f, the same variation could be observed but with a higher evolution speed and a steeper envelope due to the stronger modulation instability. It needs to be stressed that for long distances the Gaussian envelope displays a periodic variation more or less like the continued series in the presence of stronger nonlinearity. Moreover, the symmetry of the initial condition is conserved in all cases, which obviously contradicts with the reality, but the envelope modulation is quantitatively correct which has been confirmed many years ago. Thus the NLS equation can be applied in the analysis of extreme wave height distribution considering that it is capable of describing the evolution of wave packet.

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5.1 Exceedance distribution

In general, Λ is smaller than Λ_{app} and, as pointed out by Cherneva et al. (2013), the difference will grow slightly as the wave steepness increases. However, in Fig. 4 Λ is almost equal to Λ_{app} in all sea states not only in the simulation but also in the experiment after the bound waves have been removed. Thus it can be concluded that the small discrepancy between Λ and Λ_{app} is mainly due to the Stokes contribution, which supports the fact that the strong deviation of coefficient of kurtosis from Gaussian behavior is in principle the result of modulation instability, i.e., a quasi-resonant four-wave interaction process that takes place near the peak of the spectrum (Onorato et al., 2005). Furthermore, it is obvious that a large Λ appears in the case of larger initial *BFI* and the numerical simulations overestimate the experiments, especially in the third group of severe sea states.

With reference to the above discussion and considering that $\Lambda \approx \Lambda_{app}$, the MER model will make no difference from the GC model in the prediction of extreme wave heights and the MER model is adopted for the study in this paper. To have sufficiently good statistics, the exceedance probability of wave heights presented in Fig. 5 is based on both zero up-crossing and down-crossing waves. Due to the limitation in space, the comparison will only focus on three locations along the tank, which could represent the initial, intermediate and end stages of wave evolution and correspond to the three columns in Fig. 5, respectively. From top to bottom, the sea states become more and more sever and come from three typical cases listed in Table 2. Meanwhile, for clarity in graphics, the empirical exceedance distributions are compared with the theoretical predictions of the linear Rayleigh distribution in Eq. (9) and the third-order MER model in Eq. (8) as well.

Under the low sea state, e.g., Fig. 5a-c, the numerical simulation agrees almost perfectly with the experiment. Since the initial wave steepness is so small in the first group that the nonlinearity is negligible the wave surface elevation approximates the

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Gaussian distribution. As a result, the third-order nonlinear MER model reduces to Rayleigh statistics along the wave tank as anticipated.

As for the moderate sea state, e.g., Fig. 5d to f, the NLS equation also simulates the experiment reasonably well except for the initial stage where the wave height in the experiment is still Rayleigh distributed but the numerical result has achieved fully developed condition earlier due to no energy dissipation in the simulation. As the wave propagates downstream in the basin, modulation instability will significantly work on the evolution process, as reflected by the perfect fit of third-order MER model to the larger wave heights distribution. What needs to be reminded of is that the number of waves in the time series also plays a significant role on the prediction of extreme wave height, in particular in long-term evaluation (Mori and Janssen, 2006; Cherneva et al., 2011; Zhang et al., 2013). Further comparison of MER model with a large amount of data achieved from a higher-order nonlinear Schrödinger equation can be found in the work of Gramstad and Trulsen (2007).

It should be also mentioned that real ocean waves are not long crested and directional spread may play an important role in determination of the statistical properties of the surface elevation as described in Onorato et al. (2009), Mori et al. (2011) and Toffoli et al. (2010a).

In the most severe sea state, e.g., Fig. 5g-i, the same conclusion can be drawn that the NLS equation still captures the main characteristics of extreme wave heights, particularly in the intermediate and end stages of the evolution process, and the pronounced deviation at the beginning stage can be explained in the same manner as before. It is also detected that the numerical simulation presents larger wave heights than the experiments which definitely attribute to the energy dissipation such as wave breaking in reality (Bitner-Gregersen and Toffoli, 2012). In other words, to give an exact description of the tail of the exceedance probability, the influence of wave breaking must be considered.

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The relationship between coefficient of kurtosis and BFI is depicted in Fig. 6. As expected, the theoretical function (solid line) represented by Eq. (7) overestimates the results both in experiments and in simulations for the reason that the analytical expression is derived for the nonlinear steady state at the infinity while the data points are from all wave gauges, for most of which the nonlinearity is not fully developed. Moreover, in laboratory experiments, the coefficient of kurtosis is sensitive to wave breaking in high sea states, which definitely leads to a further deviation from the theoretical prediction as can be seen (the full symbols) in Fig. 6. These conclusions are in conformity with those derived by Zhang et al. (2013) with wave data from the Marintek wave basin.

Based on a large number of abnormal waves registered in Japan Sea, Tomita and Kawamura (2000) obtained an appreciable correlation between the scaled maximum wave height and the coefficient of kurtosis. After analyzing all sea state records during the storm of November 1997 in North Alwyn and Draupner's storm in the beginning of 1995, a linear regression model was derived by Guedes Soares et al. (2003). As shown in Fig. 7, the same conclusion can be seen clearly in the present experiments and simulations. Now it is confirmed again that the behavior of some statistical quantities such as λ_{40} could work as an indicator on the presence of extreme events in the time series (Guedes Soares et al., 2004). In this sense, the coefficient of kurtosis is thought to be the representative statistical measure with respect to the probability of occurrence of abnormal waves (Hagen, 2002). Meanwhile, it is observed again that the simulated results are larger than those in the experiments, particularly in the case with larger initial BFI. As explained before, this discrepancy is due to the non-breaking phenomenon which leads to no energy dissipation and thus allows the formation of extremely large waves.

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As a result of the interest in understanding the rogue wave generation, the maximum achievable wave height during the evolution of an unstable wave train has been investigated in the past. The first experimental study was made by Su and Green (1984) Conclusions

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who tried to describe the steepness of the maximum wave as a function of the initial steepness of the wave train. Moreover, their results were further compared with the cubic NLS solution by Tanaka (1990) who had shown that the simulation generated much higher maximum wave steepness than the tank experiment, and were also compared with another tank experiment carried out in Tokyo by Waseda (2005) who showed a systematic deviation from Su's result and gave a higher value due to the controlled perturbations. In the analysis of the present experiments, the maximum wave heights are computed from zero up-crossing and down-crossing waves respectively. Thus four scaled maximum wave heights could be derived from the two series for each sea state, and their mean value is displayed in Fig. 8. It is very interesting that the maximum scaled wave height appears in the moderate sea state where the initial steepness $\varepsilon \approx 0.14$ rather than in the severe sea state. This variation is consistent with that observed in Su and Green's experiment (1984). The numerical simulation also presents the same tendency although a little overestimation is observed in moderate and severe sea states. Considering that there is no energy dissipation in the numerical simulation, this change should be attributed in part to the complicated nonlinear effect. This kind of limitation, which also the Higher Order Spectral Method (HOSM) has, was observed in other studies as well (Bitner-Gregersen and Toffoli, 2012).

The same procedure of processing wave data is adopted in Fig. 9 where the relationship between steepness of maximum wave height and initial Benjamin-Feir Index is exhibited. The experiment shows a similar variation to Su and Green's (1984) as well as to Waseda's results (2005) despite the difference in the wave system (continuous spectrum vs. 3 waves system). The present numerical results are also consistent with those derived from simulation of higher order nonlinear equations, i.e., Dysthe and Zakharov equations (Waseda, 2005). Apparently in Fig. 9, a good agreement between simulation and experiment can be detected except for the severe sea state and this discrepancy is mainly due to energy dissipation in the form of wave breaking. Moreover, many observations have proved that the maximum wave steepness (Michell, 1893), known as Miche-Stokes limit which is close to 0.1429 in deep water and depicted by dash line in

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Fig. 9, could be exceeded (Toffoli et al., 2010b), but the mean steepness of maximum wave height in the present laboratory experiment does not exceed the Stokes' limit. Thus it reveals that the change of wave shape is more related to the reduction of the wave period rather than to the increase of wave height (Toffoli et al., 2010b).

Conclusions

This paper considers the capability of the NLS equation in describing the evolution of propagating wave packets that have a narrow spectrum. The influence of nonlinearity on the prediction of extreme wave heights in different random sea state is also investigated. The high-level agreement between numerical simulations, governed by the dynamics of the NLS equation, and the laboratory experiments carried out in the wave basin of CEHIPAR, provides another validation for the nonlinear Schrödinger equation in describing the formation of extreme waves.

The numerical simulations overestimate the experimental results particularly in the group of severe sea states because the NLS equation cannot model wave breaking. Nevertheless, it still catches the main characteristics of the extreme waves and provides an important physical insight into their formation.

The speed and type of the evolution of the wave packet strongly depends on the initial conditions. The envelope pulse will eventually disintegrate into a definite number of envelope pulses or solitons which are stable to collisions. In the absence of dissipative effects, the end state of the evolution of a nonlinear wave train in deep water is neither random nor steady, but is a series of periodically recurring states (FPU recurrence).

Without the influence of bound waves, the third-order GC and MER models make no difference in prediction of extreme wave heights in that Λ is almost equal to Λ_{app} in all sea states not only for laboratory experiments but also for the numerical simulations. To be more precise, the MER model tends to the linear Rayleigh distribution in the low sea state due to the insignificant nonlinearity; with higher waves, in the moderate sea state, the third-order MER model can describe the larger wave heights reasonably well; in

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the most severe sea state MER model still works but is strongly affected by the serious wave breaking in the experiment.

As expected, the relationship between the coefficient of kurtosis and BFI is overestimated by Eq. (7) considering that the analytical expression is derived for the nonlinear steady state at the infinity while the data points are from all wave gauges. The scaled maximum wave height presents a highly correlated relationship with the coefficient of kurtosis. Thus to a certain degree, λ_{40} can give an indication of the presence of extreme events in the time series.

It is noted that the maximum scaled wave height appears in the moderate sea state where the initial steepness is $\varepsilon \approx 0.14$ rather than in the severe sea state, and the numerical simulation also presents the same tendency. Considering that there is no energy dissipation in the numerical simulation, this phenomenon should be attributed in part to the complicated nonlinear effect. For the severe sea state represented by larger initial BFI, the steepness of maximum wave height is normally large.

Acknowledgements. The present work has been performed within the project EXTREME SEAS (www.mar.ist.utl.pt/extremeseas/), "Design for Ship Safety in Extreme Seas", which has been partially financed by the European Union through its 7th Framework program under contract SCP8-GA-2009-24175. The experiments in CEHIPAR that have been used in this study have been conducted by Adolfo Maron. M. Onorato thanks B. Giulinico for interesting discussions.

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Table 1. Locations of wave gauges.

Gauge	1	2	3	4	5	6
I Pos. (m) II Pos. (m)						

Table 2. Parameters in different sea states.

Case	H_{s} (m)	T_{p} (s)	arepsilon	Symbol	
1	5	14	0.051		
2	6	14	0.062		
3	6	13	0.071		
4	8	14	0.082	Square	
5	12	16	0.094		
6	5	10	0.101		
7	12	15	0.107		
8	3	7	0.123	Circle	
9	9	12	0.126		
10	8	11	0.133		
11	7	10	0.141		
12	3.5	7	0.144	Circle	
13	6	9	0.149		
14	11	12	0.154		
15	8	10	0.161		
16	4	7	0.164		
17	12	12	0.168		
18	7	9	0.174		
19	9	10	0.181	Triangle	
20	11	11	0.183	Triangle	
21	6	8	0.188		
22	12	11	0.199		
23	5	7	0.205		

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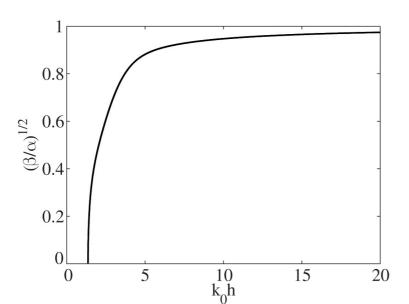


Fig. 1. Effect of finite water depth on the BFI.

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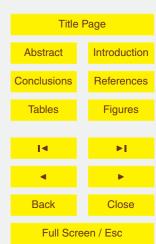


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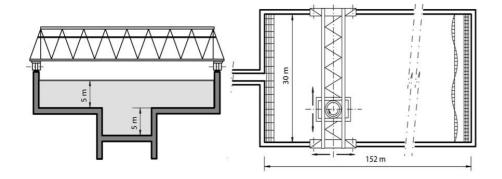


Fig. 2. Layout of the CEHIPAR wave basin.



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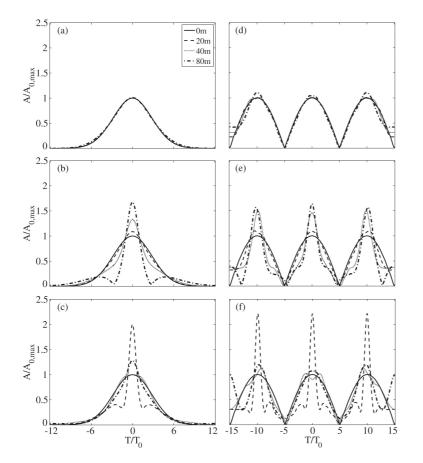


Fig. 3. Spatial variations of wave envelopes in three typical sea states. (a-c) Are from Gaussian waves and (d-f) are from bichromatic waves. The three rows correspond to the smooth, moderate and sever sea states, respectively.



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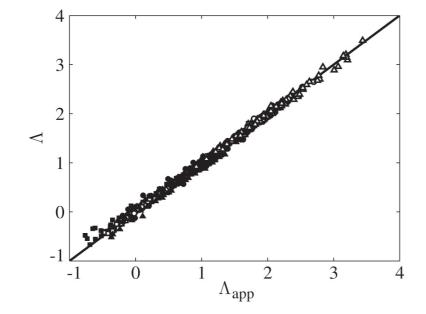


Fig. 4. Relationship between Λ and Λ_{app} .

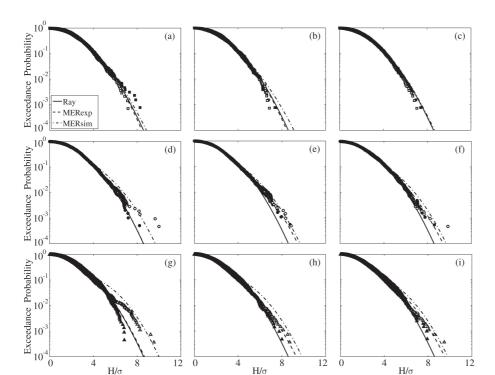


Fig. 5. Exceedance distributions of scaled wave heights. The three rows correspond to three typical sea states listed in Table 2, i.e., Case 4, Case 13 and Case 23. The three columns present the results obtained from Gauges set at 20 m, 80 m and 120 m away from the wave maker respectively. The solid line, dash line and dot-dash line mean Rayleigh distribution, MER models in experiment and in simulation in sequence. The full and empty marks still have the same meaning as before.

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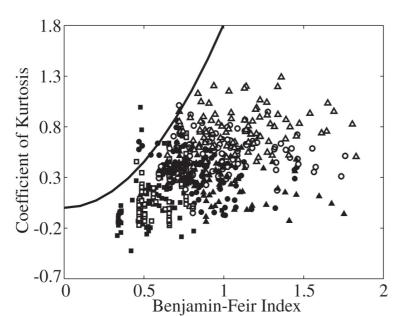


Fig. 6. Coefficient of kurtosis versus BFI.

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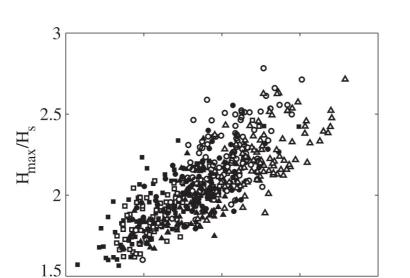
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1.5



0.5

Coefficient of Kurtosis

Fig. 7. Scaled maximum wave height versus coefficient of kurtosis.

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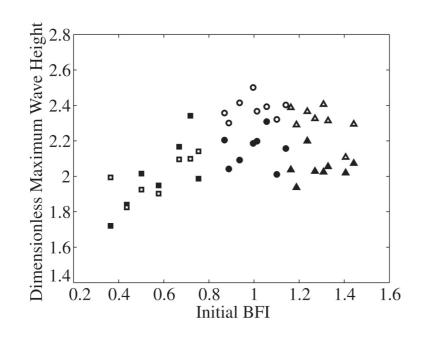


Fig. 8. Dimensionless maximum wave height versus initial BFI.

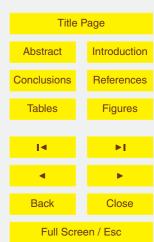


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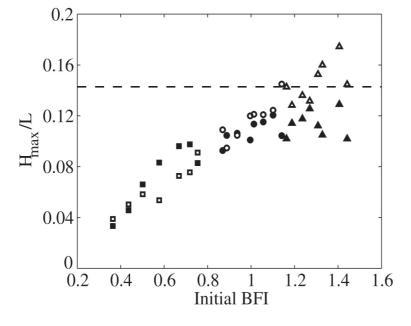


Fig. 9. Steepness of maximum wave height vs. initial BFI.