



**The Hurst exponent  
of the magnetic field  
and the seismicity**

F. Masci and  
J. N. Thomas

This discussion paper is/has been under review for the journal Natural Hazards and Earth System Sciences (NHESS). Please refer to the corresponding final paper in NHESS if available.

# **Review “On the relation between the seismic activity and the Hurst exponent of the geomagnetic field at the time of the 2000 Izu swarm”**

**F. Masci<sup>1</sup> and J. N. Thomas<sup>2,3,4</sup>**

<sup>1</sup>Istituto Nazionale di Geofisica e Vulcanologia, L'Aquila, Italy

<sup>2</sup>Northwest Research Associates, Redmond, Washington, USA

<sup>3</sup>Department of Electrical and Computer Engineering, DigiPen Institute of Technology, Redmond, Washington, USA

<sup>4</sup>Department of Earth and Space Sciences, University of Washington, Seattle, Washington, USA

Received: 28 January 2013 – Accepted: 16 March 2013 – Published: 26 March 2013

Correspondence to: F. Masci (fabrizio.masci@ingv.it)

Published by Copernicus Publications on behalf of the European Geosciences Union.

|                          |              |
|--------------------------|--------------|
| Title Page               |              |
| Abstract                 | Introduction |
| Conclusions              | References   |
| Tables                   | Figures      |
| ⏪                        | ⏩            |
| ◀                        | ▶            |
| Back                     | Close        |
| Full Screen / Esc        |              |
| Printer-friendly Version |              |
| Interactive Discussion   |              |







## The Hurst exponent of the magnetic field and the seismicity

F. Masci and  
J. N. Thomas

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

⏪

⏩

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

is a positive correlation between the values of a time-series (persistent behaviour), that is, if the time-series increases in a period of time it is likely that it continues to increase in the following interval. For  $H_u < 0.5$  there is a negative correlation between the values of a time-series (anti-persistent behaviour), that is, if the time-series increases in a period of time it is likely that it decrease in the following interval.  $H_u = 0.5$  indicates a completely uncorrelated time-series. Refer to Hayakawa et al. (2004) for details on the calculation of the Hurst exponent.

According to Hayakawa et al. (2004), the local seismic activity and the Hurst exponent of the geomagnetic field components in the ULF frequency band show a strong correlation from the end of June to the first weeks of July 2000. Figure 1 shows the behaviour from February to December 2000 of the Hurst exponent of the geomagnetic field H component and local seismic activity ( $M^*$ ) as reported by Hayakawa et al. (2004).  $M^*$  is the earthquake magnitude estimated by the Japan Meteorological Agency. Yellow bounded areas highlight the period during which  $H_u$  seems to vary in accord with  $M^*$ . Our first observation concerns the lack of a corresponding correlation after the middle of July 2000 when, as can be seen from Fig. 1, the seismic swarm was still in progress. This fact already casts some doubts on the possible relationship between  $H_u$  and  $M^*$ . Hayakawa et al. (2004) noted that  $M^*$  and  $H_u$  do not vary coherently all the time. The authors justify the lack of correlation after the middle of July invoking “a kind of saturation” which took place during the evolution of the seismic swarm. Unfortunately, they do not explain the true meaning of the supposed “saturation”, nor they specify what saturated.

Figure 2 is a reproduction of Fig. 2 by Hayakawa et al. (2004). The figure shows the local seismic activity  $M^*$  and the Hurst exponent of the geomagnetic field components H, D, and Z during the period from February to August 2000. Enlarged views from 7 June to 18 July shows both daily values and  $\pm 3$ -day running average of the Hurst exponent compared with the  $\pm 3$ -day running average of the earthquake magnitude  $M^*$ . According to Hayakawa et al. (2004) there is a strong correspondence between the increase of  $M^*$  and the variation of the Hurst exponent of the geomagnetic field horizontal

components H and D. Conversely, the Hurst exponent of the vertical component Z of the geomagnetic field does not show a similar pronounced correspondence with the seismic activity.

Considering that interaction of the solar wind with the Earth's magnetosphere and ionosphere–magnetosphere coupling are the main sources of ULF disturbances (see McPherron et al., 2005; Saito, 1969) we compared the findings of Hayakawa et al. (2004) with global geomagnetic activity by means of the  $\Sigma Kp$  index time-series. In Fig. 2, the  $\pm 3$ -day running average of the  $\Sigma Kp$  index is superimposed onto the original views by Hayakawa et al. (2004). We found a strong correlation between the  $\pm 3$ -day running averages of the Hurst exponent of the horizontal components of the geomagnetic field and  $\Sigma Kp$  on both short and long time scales. This correlation is particularly evident in the H component. Namely, the Hurst exponent shows a close correlation with  $\Sigma Kp$  during the entire period of time (February–December 2000) reported in the figure and not only during few weeks from 7 June to 18 July. This fact suggests that the variations of the Hurst exponent of the geomagnetic field are closely related to changes in geomagnetic activity. In addition, the greater correspondence with the geomagnetic index of the Hurst exponent of the horizontal components H and D is clearly justified because the Kp index is calculated using these components of the geomagnetic field (Mayaud, 1980).

Figure 3 shows in detail the comparison between  $M^*$ ,  $\Sigma Kp$ , and the Hurst exponent of the geomagnetic field H component ( $Hu\_H$ ), during the period from 7 June to 18 July 2000. The daily values and the  $\pm 3$ -day running averages of  $Hu\_H$  and  $M^*$  were obtained by digitizing the original view of Hayakawa et al. (2004). We can see the strong inverse correlation that exists between the daily values of  $Hu\_H$  and  $\Sigma Kp$ . Figure 3b, c show the linear relationships between the  $\pm 3$ -day running averages of  $Hu\_H$  and  $\Sigma Kp$ , and  $Hu\_H$  and  $M^*$ , respectively. It is clearly evident that the strong correlation that exists between  $Hu\_H$  and  $\Sigma Kp$  (correlation coefficient =  $-0.87$ ) cannot be stated for the pair  $Hu\_H$  and  $M^*$  (correlation coefficient =  $0.36$ ). This finding is confirmed by Fig. 3d that shows the original  $Hu\_H$  time-series and the  $Hu\_H$  time-series reconstructed using the

## The Hurst exponent of the magnetic field and the seismicity

F. Masci and  
J. N. Thomas

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



linear relationships with  $\Sigma Kp$  and  $M^*$ , respectively. We can see that Hu\_H constructed by the linear relationship with  $\Sigma Kp$  is very similar to the original Hu\_H time-series. On the contrary, this cannot be stated for the Hu\_H time-series constructed by the  $M^*$  linear relationship.

### 3 Conclusions

Here we have shown that the variation of the Hurst exponent of the ULF component of the geomagnetic field during the period from February to December 2000 and particularly from the beginning of June to the middle of July is highly-correlated to geomagnetic activity. Moreover, contrary to the claims of Hayakawa et al. (2004), we have found that during the 2000 Izu swarm the behaviour of the Hurst exponent of the ULF geomagnetic field is poorly-correlated with the energy released by the local seismic activity. This paper supports the findings by Masci (2010, 2011a,b), which demonstrated that many presumed magnetic seismogenic signatures claimed to be related to the swarm occurred at Izu during 2000 were actually normal magnetospheric disturbances.

*Acknowledgements.* The authors wish to thank the World Data Center for Geomagnetism, Kyoto University for providing the Kp index. JNT was supported by the USGS Earthquake Hazards Program, external research grant G11AP20177.

### References

- Campbell, W. H.: Natural magnetic disturbance fields, not precursors, preceding the Loma Prieta earthquake, *J. Geophys. Res.*, 114, A05307, doi:10.1029/2008JA013932, 2009.
- Gotoh, K., Hayakawa, M., and Smirnova, N.: Fractal analysis of the ULF geomagnetic data obtained at Izu Peninsula, Japan in relation to the nearby earthquake swarm of June–August 2000, *Nat. Hazards Earth Syst. Sci.*, 3, 229–236, doi:10.5194/nhess-3-229-2003, 2003.
- Gotoh, K., Hayakawa, M., Smirnova, N. A., Hattori, K.: Fractal analysis of seismogenic ULF emissions, *Phys. Chem. Earth*, 29, 419–424, doi:10.1016/j.pce.2003.11.013, 2004.

## The Hurst exponent of the magnetic field and the seismicity

F. Masci and  
J. N. Thomas

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



## The Hurst exponent of the magnetic field and the seismicity

F. Masci and  
J. N. Thomas

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

Hayakawa, M.: On the fluctuation spectra of seismo-electromagnetic phenomena, *Nat. Hazards Earth Syst. Sci.*, 11, 301–308, doi:10.5194/nhess-11-301-2011, 2011.

Hayakawa, M., Hattori, K., Nickolaenko, A. P., Rabinowicz, L. M.: Relation between the energy of earthquake swarm and the Hurst exponent of random variations of the geomagnetic field, *Phys. Chem. Earth*, 29, 379–387, doi:10.1016/j.pce.2003.07.001, 2004.

Ismaguilov, V. S., Kopytenko, Yu. A., Hattori, K., and Hayakawa, M.: Variations of phase velocity and gradient values of ULF geomagnetic disturbances connected with the Izu strong earthquakes, *Nat. Hazards Earth Syst. Sci.*, 3, 211–215, doi:10.5194/nhess-3-211-2003, 2003.

Masci, F.: On claimed ULF seismogenic fractal signatures in the geomagnetic field, *J. Geophys. Res.*, A10236, 115, doi:10.1029/2010JA015311, 2010.

Masci, F.: On the seismogenic increase of the ratio of the ULF geomagnetic field components, *Phys. Earth Planet. In.*, 187, 19–32, doi:10.1016/j.pepi.2011.05.001, 2011a.

Masci, F.: Brief communication “On the recent reaffirmation of ULF magnetic earthquakes precursors”, *Nat. Hazards Earth Syst. Sci.*, 11, 2193–2198, doi:10.5194/nhess-11-2193-2011, 2011b.

Masci, F.: Comment on “Ultra Low Frequency (ULF) European multi station magnetic field analysis before and during the 2009 earthquake at L’Aquila regarding regional geotechnical information” by Prattes et al. (2011), *Nat. Hazards Earth Syst. Sci.*, 12, 17717–1719, doi:10.5194/nhess-12-1717-2012, 2012a.

Masci, F.: Comment on “Possible association between anomalous geomagnetic variations and the Molise Earthquakes at Central Italy during 2002” by Takla et al. (2011), *Phys. Earth Planet. In.*, 202–203, 92–94, doi:10.1016/j.pepi.2012.02.006, 2012b.

Masci, F.: On the ULF magnetic ratio increase before the 2008 Iwate-Miyagi Nairiku earthquake by Hirano and Hattori (2011), *J. Asian Earth Sci.*, 56, 258–262, doi:10.1016/j.jseaes.2012.05.020, 2012c.

Masci, F.: The study of ionospheric anomalies in Japan area during 1998–2010 by Kon et al.: an inaccurate claim of earthquake-related signatures?, *J. Asian Earth Sci.*, 57, 1–5, doi:10.1016/j.jseaes.2012.06.009, 2012d.

Masci, F.: On the multi-fractal characteristics of the ULF geomagnetic field before the 1993 Guam earthquake, *Nat. Hazards Earth Syst. Sci.*, 13, 187–191, doi:10.5194/nhess-13-187-2013, 2013a.

## The Hurst exponent of the magnetic field and the seismicity

F. Masci and  
J. N. Thomas

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

⏪

⏩

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Masci, F.: Brief communication “Further comments on the ionospheric precursor of the 1999 Hector Mine earthquake”, *Nat. Hazards Earth Syst. Sci.*, 13, 193–196, doi:10.5194/nhess-13-193-2013, 2013b.

Mayaud, P. N.: Derivation, Meaning, and Use of Geomagnetic Indices, *Geophys. Mon. Ser.*, 22, American Geophysical Union, Washington, D. C., 1980.

McPherron, R. L.: Magnetic pulsations: their sources and relation to solar wind and geomagnetic activity, *Surv. Geophys.*, 26, 545–592, doi:10.1007/s10712-005-1758-7, 2005.

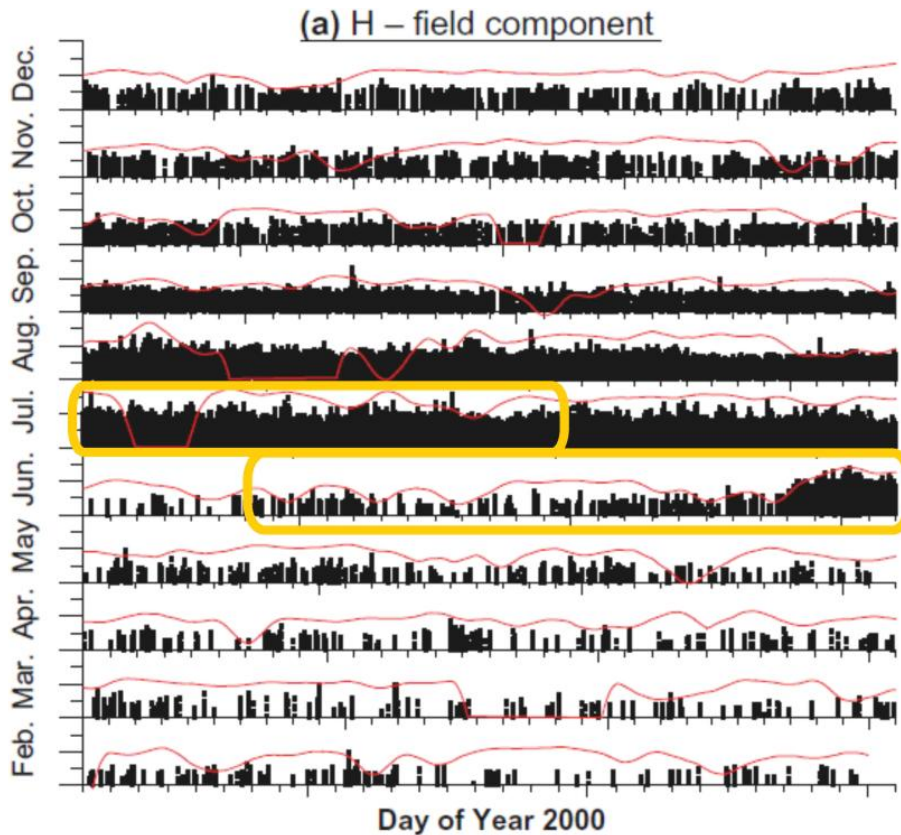
Saito, T.: Geomagnetic pulsations, *Space Sci. Rev.*, 10, 319–342, 1969.

Thomas, J. N., Love, J. J., Johnston, M. J. S.: On the reported magnetic precursor of the 1989 Loma Prieta earthquakes, *Phys. Earth Planet. In.*, 173, 207–215, doi:10.1016/j.pepi.2008.11.014, 2009a.

Thomas, J. N., Love, J. J., Johnston, M. J. S., Yumoto, K.: On the reported magnetic precursor of the 1993 Guam earthquake, *Geophys. Res. Lett.*, 36, L16301, doi:10.1029/2009GL039020, 2009b.

Thomas, J. N., Love, J. J., Komjathy, A., Verkhoglyadova, O. P., Butala, M., Rivera, N.: On the reported ionospheric precursor of the 1999 Hector Mine, California earthquake, *Geophys. Res. Lett.*, 39, L06302, doi:10.1029/2012GL051022, 2012.





**Fig. 1.** A reproduction of Fig. 1 by Hayakawa et al. (2004). The vertical black bars represent the local seismic activity  $M^*$  estimated by the Japan Meteorological Agency, whereas the solid red line represents the behaviour of the Hurst exponent of the geomagnetic field H component during 2000. Yellow rounded rectangles highlight the period in which the Hurst exponent is claimed to change coherently with  $M^*$  by Hayakawa et al. (2004).

**The Hurst exponent of the magnetic field and the seismicity**

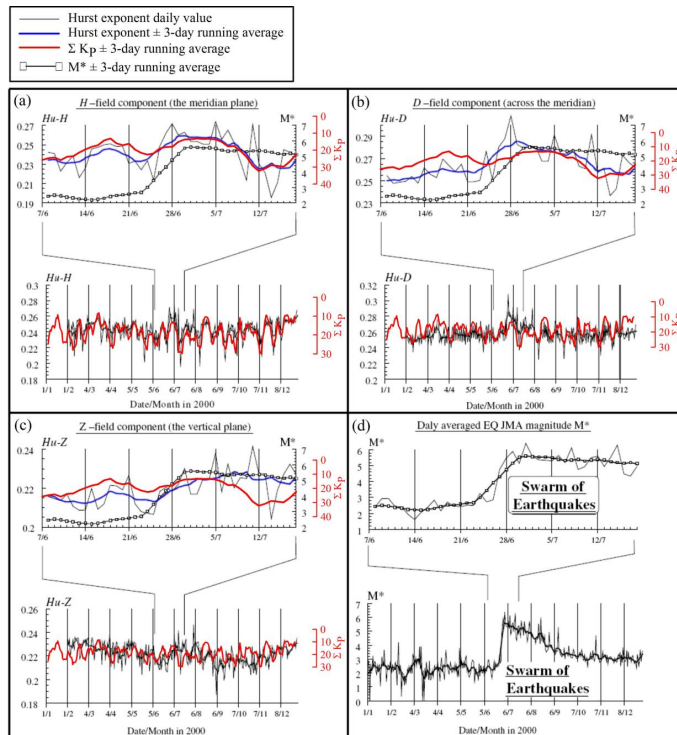
F. Masci and  
J. N. Thomas

|                          |              |
|--------------------------|--------------|
| Title Page               |              |
| Abstract                 | Introduction |
| Conclusions              | References   |
| Tables                   | Figures      |
| ⏪                        | ⏩            |
| ◀                        | ▶            |
| Back                     | Close        |
| Full Screen / Esc        |              |
| Printer-friendly Version |              |
| Interactive Discussion   |              |



The Hurst exponent of the magnetic field and the seismicity

F. Masci and  
J. N. Thomas



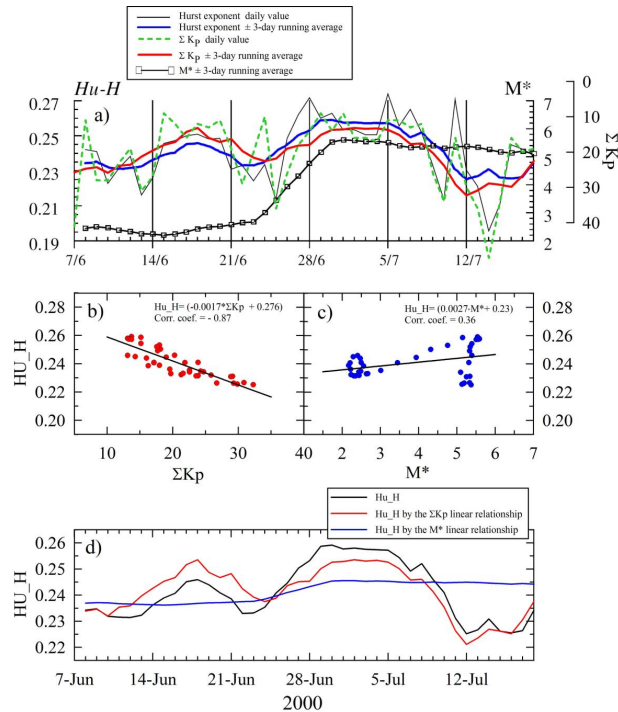
**Fig. 2.** A reproduction of Fig. 2 by Hayakawa et al. (2004). **(a)**, **(b)**, and **(c)**: the variation of the Hurst exponent (daily values and  $\pm 3$ -day running average) of the geomagnetic field components H, D, and Z during 2000. The enlarged views of each panel refer to the rise of the seismic activity at Izu. **(d)**: daily values and  $\pm 3$ -day running average of the local seismic activity  $M^*$ . The  $\pm 3$ -day running average of  $M^*$  (solid line with open squares) is also reported in panels **(a)**, **(b)**, and **(c)**. The  $\pm 3$ -day running average of the global geomagnetic index  $\Sigma Kp$  is superimposed on the original views. See text for details.

|                          |              |
|--------------------------|--------------|
| Title Page               |              |
| Abstract                 | Introduction |
| Conclusions              | References   |
| Tables                   | Figures      |
| ◀                        | ▶            |
| ◀                        | ▶            |
| Back                     | Close        |
| Full Screen / Esc        |              |
| Printer-friendly Version |              |
| Interactive Discussion   |              |



The Hurst exponent of the magnetic field and the seismicity

F. Masci and J. N. Thomas



**Fig. 3.** (a) A reproduction of Fig. 2 by Hayakawa et al. (2004). Variation of the Hurst exponent (daily values and  $\pm 3$ -day running average) of the geomagnetic field H component at the time of the Izu swarm. The  $\pm 3$ -day running average of the local seismic activity  $M^*$  (solid line with open squares) is also shown.  $\Sigma Kp$  time-series (daily values and  $\pm 3$ -day running average) have been superimposed onto the original view. (b) and (c) linear relationships between the  $\pm 3$ -day running average of the Hurst exponent and  $\Sigma Kp$  and  $M^*$ , respectively. (d) The Hurst exponent calculated by Hayakawa et al. (2004) compared with reconstructed Hurst exponents using the linear relationships shown in panels (b) and (c). See text for details.

Title Page

Abstract Introduction

Conclusions References

Tables Figures

◀ ▶

◀ ▶

Back Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

