



Rockfall hazard and risk assessments along roads at a regional scale: example in Swiss Alps

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Abstract. Unlike fragmental rockfall runout assessments, there are only few robust methods to quantify rock-mass-failure susceptibilities at regional scale. A detailed slope angle analysis of recent Digital Elevation Models (DEM) can be used to detect potential rockfall source areas, thanks to the Slope Angle Distribution procedure. However, this method does not provide any information on block-release frequencies inside identified areas. The present paper adds to the Slope Angle Distribution of cliffs unit its normalized cumulative distribution function. This improvement is assimilated to a quantitative weighting of slope angles, introducing rock-mass-failure susceptibilities inside rockfall source areas previously detected. Then rockfall runout assessment is performed using the GIS- and process-based software Flow-R, providing relative frequencies for runout. Thus, taking into consideration both susceptibility results, this approach can be used to establish, after calibration, hazard and risk maps at regional scale. As an example, a risk analysis of vehicle traffic exposed to rockfalls is performed along the main roads of the Swiss alpine valley of Bagnes.

Cascini, 2008; Jaboyedoff et al., 2012). The field of propagation modeling is under fast development, aiming to compute runout probabilities with empirical, process-based and GIS-based models (Dorren, 2003; Volkwein et al., 2011), such as CONEFALL (Jaboyedoff and Labiouse, 2011), Rockyfor3D (Dorren, 2011), HY-STONE (Crosta et al., 2004) or ILWIS (van Dijke and van Westen, 1990). However, there are not yet robust and objective methods to detect source areas at a regional scale and quantify rock-mass-failure mean susceptibilities. In the present work, the authors intend to provide information about susceptibility indicators on potential rockfall source areas.

Rockfall is very likely to be found in steep slopes (Heim, 1932; Hoek and Bray, 1981; Crosta and Agliardi, 2003; Dorren, 2003). From a basic approach, unstable rock slopes can be delimited through the steepness of the topography. It can be done with a simple method of slope angle threshold, which can be defined from distinctive evidence (i.e. cliffs lying above scree deposits, fieldworks or historical events) when it is not arbitrary defined (Toppe, 1987; Dorren and Seijmonsbergen, 2003; Guzzetti et al., 2003; Jaboyedoff and Labiouse, 2003; Frattini et al., 2008).

Furthermore, several authors showed supplementary conditions influencing rock slope stability (Terzaghi, 1950, 1962; Bieniawski, 1976; Selby, 1982; Willie and Mah, 2004; Jaboyedoff and Derron, 2005), classified in internal parameters (IP, i.e. lithological, geo-mechanical and structural settings) and external factors (EF, e.g. active tectonic, water infiltration, weathering, etc.). Therefore, more complex models have been developed integrating these conditions to enhance the source detection at regional scale. They introduced rating systems following empirical multi-criteria

1 Introduction

Mountain roads are frequently exposed to fragmental rockfalls (Piteau and Peckover, 1978; Budetta, 2004), involving independent blocks of relatively small sizes characterized by high energy and mobility (Whalley, 1984; Willie and Mah, 2004). Recent advances of high resolution Digital Elevation Models (HRDEM) combined with Geographical Information System (GIS) technologies have made rockfall susceptibility mapping possible (Willie and Mah, 2004; Derron et al., 2005;

observations (Pierson et al., 1990; Baillifard et al., 2003), structural settings and kinematics analysis (Wagner et al., 1988; Jaboyedoff et al., 1999; Gokceoglu et al., 2000; Günther, 2003), safety factor computations (Hoek and Bray, 1981), or joining IP and EF conditions (Günther et al., 2004; Oppikofer et al., 2007).

But, all these methods obviously depend on the possibility of collecting a lot of complex and reliable information on the area of interest. For example, the simplified Rockfall Hazard Rating System method (Pierson et al., 1990; Budetta, 2004) requires eleven parameters per outcrop as an input to estimate the rockfall susceptibility along a road. Moreover, these methods usually use very high resolution datasets that are not often available at regional scale. For instance, Günther (2003) applied his model SLOPEMAP to extract structural features of the hard rock terrain using a 5×5 m DEM pixel size for a study area of 2.5 km^2 , which is inappropriate when only 10×10 up to 30×30 m DEM pixel sizes are available at regional scale. These methods require too high resolution information and too many parameters to be practically and rapidly applied on fairly large areas.

However, strong correlations between topography and earth surface processes have been suggested for many years (Powel, 1876 and Gilbert, 1877, cited in Montgomery and Brandon, 2002; Strahler, 1954). The terrain morphology reflects the compounded influence of these internal settings (Locat et al., 2000). Hence, Rouiller et al. (1998) and then Loye et al. (2009) proposed the Slope Angle Distribution (SAD) procedure to use the topography as a proxy to detect potential source locations. The next step is to assess the susceptibility level of rockfall release of the potential source locations previously detected. Therefore, this paper proposes to improve the SAD procedure by linking the cumulative distribution function of the slope angle to quantitative block release susceptibility.

The Flow-R software (Horton et al., 2008; Blahut et al., 2010; Kappes et al., 2011) is used to compute rockfall runout areas. It assesses propagations thanks to an open choice of algorithms and parameters of probabilistic spreading and basic energy balance, such as a multiple flow direction model (Holmgren, 1994) coupled with an inertial factor (Gamma, 2000) and a maximum runout distance based on a Coulomb friction model. Moreover, since Horton et al. (2008), the model has been modified to take into account the susceptibilities of block releases in the resulting spreading.

Finally, this improved methodology allows us to draw rockfall susceptibility maps. Then, after a calibration based on available rockfall inventories, hazard maps can be obtained, taking into consideration both relative frequencies of block release and propagation (Jaboyedoff et al., 2005; Corominas and Moya, 2008). Indeed, the hazard is always a challenging parameter to estimate in a Quantitative Risk Assessment (QRA) (Corominas et al., 2005).

As an example of the applicability of this procedure, the risk of fragmental rockfalls to vehicle traffic along the main



Fig. 1. Photography of a rockfalls event in 2006 that reached twice the road section near Le Plamproz, in the Bagnes Valley.

roads of the Swiss Alpine valley of Bagnes (Fig. 1) is assessed and expressed in terms of number of direct impacts per year of blocks on vehicles.

2 Methodology

2.1 Detection of sources areas

2.1.1 Slope Angle Distribution procedure

Strahler's law of constancy of slopes (Strahler, 1950) tells that the morphology of a slope topography tends to group predominantly around several mean slope angle values that are normally distributed with low dispersion. These particular slope angles of convergence can be often related to the most frequently encountered four major morphological units (Oppikofer et al., 2007; Loye et al., 2009):

- Plains formed by fluvio-glacial deposit; these correspond to the set of low slope angles;
- Bottom parts of the valley flanks comprising alluvial fans related to debris flow deposits and landslides mass. These correspond to the set of foot slopes angles;
- Talus slopes and valley sides (flank) covered by till, screes and debris mantles as well as rocky outcrops lightly covered with soil. These correspond to the set of steep slopes angles;
- Cliffs and rock faces corresponding to the very steep sets of slope angles.

Hence, the morphology of a terrain displays characteristic slope angles that can be directly related to the geomorphic

processes involved in slope stability. Rockfall source areas are commonly found in the steepest morphological units.

Based on these statements, Rouiller et al. (1998) and then Loye et al. (2009) have established a DEM-based geomorphometric approach to detect these morphological units and therefore rockfall source areas, named the Slope Angle Distribution (SAD) procedure. The classification is done by computing the Slope Angle Frequency Distribution (SAFD) of the study area, the frequency being normalized considering their real surface of occurrence. The SAFD is then decomposed into several Normal distributions f :

$$f(s) = w \cdot \frac{1}{\sigma \sqrt{2\pi}} \cdot \exp \left[-\frac{1}{2} \cdot \left(\frac{s - m_c}{\sigma} \right)^2 \right] \quad (1)$$

where f is the normal probability distribution function (PDF) of the slope angle value s included within the interval $[0;90]$, σ its standard deviation, m_c its mean value (Kreyzig, 2006) and w a weighting factor which is linked to the proportions between unit surfaces inside study areas. The sum of these theoretical normal curves has to rebuild the real SAFD (Fig. 2a).

The above-mentioned sets of morphological units do not always exist in the study area; the number of normal curves is therefore given according to the number of morphological units present in the area of interest (as detailed in Loye et al., 2009). Moreover, in some cases (Fig. 3a), the distribution of the slope angles of cliffs units has to be decomposed into two normal functions f_1 and f_2 . This can be caused by the topography itself (potential high dispersion of this unit that possibly exists from 45° to 90°) or by the extent of the support (limits of the study domain). In theory, it could be divided into more than two distributions; but in our experience, two distributions are sufficient. Then, the total distribution f_i of cliffs units is simply defined as the sum of f_1 and f_2 :

$$f_i(s) = f_1(s) + f_2(s) \quad (2)$$

Technically, the input values for the initial normal distributions are defined according to the local maximum and minimum that can be visually identified along the SAFD. The fitting process is performed by minimizing the error between the most-likely sets of normal curves and the target function (namely the SAFD) using a simplex optimization solver. The morphological units are then delimited finally according to the sets of normal Slope Angle Distribution, where a normal curve becomes dominant over the others. An example of classified slope steepness map is shown in Fig. 4. The cliffs morphological unit f_i is then considered as the potential rockfall sources areas.

Finally, considering that the local morphology of an Alpine valley is partly controlled by structural settings and rock-mass properties (Terzaghi, 1962; Selby, 1982; Willie and Mah, 2004), different lithological and tectonic units have to be considered in order to refine the morphological analysis. Therefore, the study area is classified in homogeneous

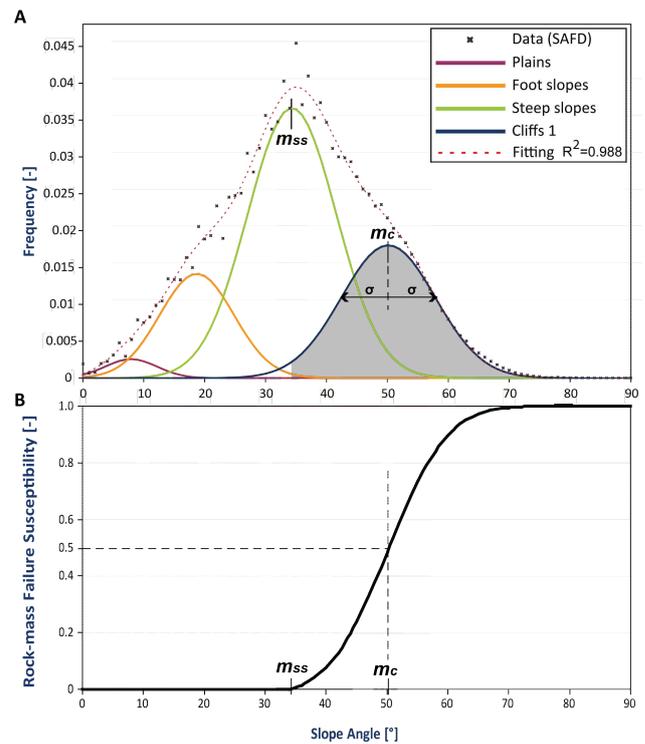


Fig. 2. (A) Normal distributions of the slope angles of the granitoids HMA in the Bagnes Valley, extracted from a 10 m-DEM. Three parameters are used to detect potential rockfall source areas: m_c which is the mean angle of the cliffs distribution and σ its standard deviation; m_{ss} which is the mean angle of the steep slopes distribution. In this case, cliffs units are decomposed in only one normal distribution. (B) Normalized cumulative distribution function (F_n) for the cliffs units, assimilated to a quantitative weighting of potential rockfall source areas, i.e. to a rock-mass-failure susceptibility. The mean angle of the steep slopes distribution m_{ss} is used as a first threshold to exclude lower values as potential rockfall source areas.

morphotectonic areas (HMA), following similar lithological characteristic rock mass structure and geomorphic activity, and one SAD procedure has to be done for each HMA.

To sum up, the SAD is a systematic approach to extract a slope angle lower threshold for each HMA, corresponding to the limit between the steep slopes and cliffs normal distributions. This procedure leads to Boolean results (i.e. in/out cliffs units) and cells included inside these cliffs areas are considered as potential sources of fragmental rockfalls.

2.1.2 Refinement of the Slope Angle Distribution

As stated in the introduction, taking into account all internal parameters and external factors can require too high resolution dataset and too many parameters to be applied on a fairly regional scale in order to precisely detect and rate potential rockfall source areas. But as topographies are strongly correlated with internal rock settings (Locat et al., 2000) and

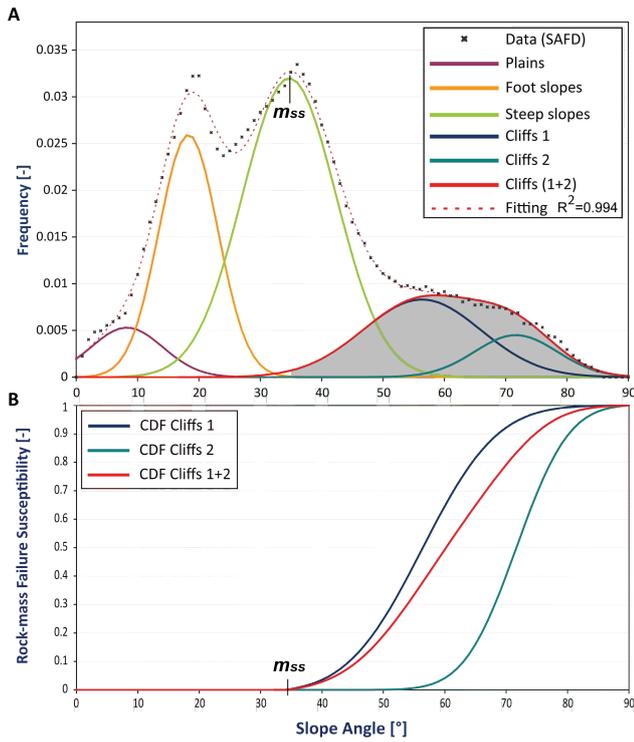


Fig. 3. (A) Normal distributions of the slope angles of the marbles HMA in the Bagnes Valley. Here, cliffs are decomposed in two normal distributions. (B) The normalized cumulative distribution function (F_n) of the sum of the two cliffs distributions (f_i) is shown by the red line. In comparison, the normalized cumulative distribution functions for the two cliffs distributions are shown in blue (f_1) and cyan (f_2).

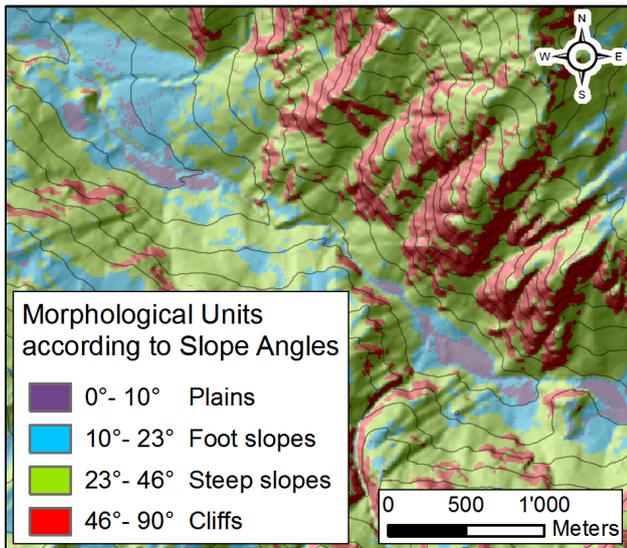


Fig. 4. Example of main morphological units in a region of the Bagnes valley according to slope angle thresholds got thanks to the SAD procedure. (Hillshade and 10 m isohypses: ©2008 swisstopo).

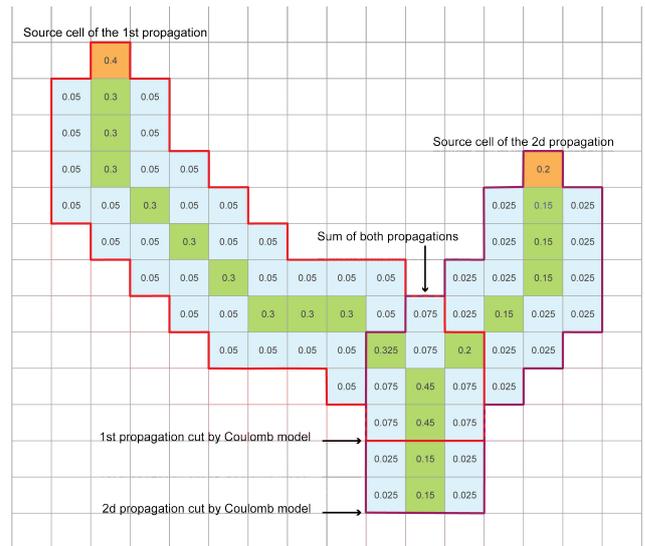


Fig. 5. Theoretical computation of rockfall runouts from two source areas on a DEM grid. These relative frequencies (numbers in the green and blue cells) of rockfall propagations take into account (1) the initial rock-mass-failure susceptibilities (numbers in the orange cells) and (2) the integration of all computed propagations with probabilistic spreading algorithms. The maximum runout distance is reached when the simple Coulomb friction model becomes zero.

Earth surface processes (Montgomery and Brandon, 2002), we assume that for large areas, the block release susceptibility is a function of slope angles. Thus, improving the SAD approach, this paper aims to link the cumulative distribution functions of slope angles of cliffs units to rock-mass-failure susceptibility inside rockfall source areas previously identified.

The explanations below will illustrate only the situation where cliffs units are decomposed in two distributions (Eq. 2). When it is not the case, f_i is equal to f_1 . The associated cumulative distribution function F of cliffs distribution is defined by:

$$F(\beta) = \int_0^\beta f_i(s) \cdot ds \quad (3)$$

where s and β are two slope angle values included within the interval $[0;90]$. By definition, Eq. (3) gives the probability that a slope angle s is lower than β (Kreyzig, 2006). Therefore, it is by extension assimilated to a quantitative block release susceptibility. Moreover, the mean value of the steep slopes distribution m_{ss} , extracted from the SAD procedure (Figs. 2a and 3a), relates to an apparent equilibrium slope angle of scree deposits (usually around 35° , that mainly compose steep slopes units). Thus, for higher slope angle values than m_{ss} , blocks can be mobilized; on the contrary, for lower slope angle values, blocks are not considered. As a consequence, m_{ss} is used as a lower threshold to exclude areas

not steep enough to be potential source of rockfalls. Thus, Eq. (3) has to be cutoff by m_{ss} and then normalized for slope angle values higher than m_{ss} ; the final cumulative function F_n is shown in Figs. 2b and 3b and defined by:

$$\begin{cases} \forall \beta \in [0 ; m_{ss}[\Rightarrow F_n(\beta) = 0 \\ \forall \beta \in [m_{ss} ; 90] \Rightarrow F_n(\beta) = \frac{F(\beta) - F(m_{ss})}{F(90) - F(m_{ss})} \end{cases} \quad (4)$$

The normalized cumulative distribution function F_n can be assimilated to a quantitative weighting of potential rockfall source areas, i.e. a rock-mass-failure susceptibility indicator (Fig. 7), identified according to the slope angles and the SAD procedures.

2.2 Runout assessment

Many tools have been developed to calculate runout areas of rolling, bouncing or falling blocks (Ritchie, 1963) and have been reviewed by Dorren (2003). In this study, the runout simulation is computed by the Flow-R software (Horton et al., 2008). The propagation is assessed by means of a probabilistic spreading and a basic energy balance, controlling respectively the lateral extent and the runout distance, merging several models and approaches. Everything is processed at the cell level and iterated on the DEM grid according to the propagation direction. This study is the first to use the Flow-R software for rockfall runout assessment. Thanks to the open choice of algorithms and parameters, it has been possible to parameterize the model according to our needs at regional scale. The model has also been modified to take into account the susceptibilities of the sources (calibrated on the base of F_n) in the resulting spreading, which is a step further in the frequency analysis. It allows us to approach the hazard frequency of a location more consistently than before by relating it to the source susceptibilities.

2.2.1 Probabilistic spreading

Probabilistic spreading is based on flow direction algorithms that process the probability of a cell to flow to its neighbors (Horton et al., 2008). The probability is integrated in a continuous way, meaning every neighboring cell having a non-null probability will be propagated further. Flow direction algorithms, that are the basis of the spreading, portion the probabilities according to the slope of the surrounding cells.

Fairfield and Leymarie (1991) have introduced the multiple flow direction algorithm as a stochastic method which gives a probability to every cell with a descending slope. Then Holmgren (1994) has suggested a variation of this method by introducing the exponent α on the slope gradient:

$$\forall \begin{cases} \tan \beta_i > 0 \\ \alpha \in [1; +\infty[\end{cases} \Rightarrow P_f(x) = \frac{(\tan \beta_i)^\alpha}{\sum_{j=1}^8 (\tan \beta_j)^\alpha} \quad (5)$$

where i, j are the flow directions, P_f is the probability proportion in direction i , $\tan \beta_i$ is the slope gradient between the

central cell and cell in direction i , and α is the exponent to calibrate.

The exponent α allows us to better control the spreading extent from the multiple flow direction algorithm. When $\alpha = 1$, Eq. (5) is equivalent to the multiple flow direction algorithm (Fairfield and Leymarie, 1991), and when $\alpha \rightarrow \infty$ to the D8 algorithm (propagation following only the steepest slope: O'Callaghan and Mark, 1984; Jensen and Domingue, 1988).

In addition to the flow direction algorithm, a persistence factor was introduced as in Gamma (2000), which is a weighting of the probability according to a direction change. The chosen values are the same as Gamma (2000), i.e. 1 when there is no change in direction and 2/3 in any other case. The role of this persistence factor is to take into consideration the inertia according to the previous directions of the moving blocks which can therefore deviate from the steepest paths.

2.2.2 Runout distance

The runout distance is assessed thanks to a basic energy balance including the potential and kinetic energy components and an energy loss function. As the source mass is unknown, the energy balance is processed on a unit mass. For the energy loss function, a simple Coulomb friction model (with a single friction coefficient) was used:

$$\Delta E_{\text{loss}} = g \times \Delta x \times \mu \quad (6)$$

where Δx is the increment of horizontal displacement, g the gravity acceleration and μ is the tangent of the friction angle. To this algorithm, we can add an upper threshold to limit the velocity of blocks or an equivalent kinetic energy (Horton et al., 2008). Then, the maximum runout distance is reached when the energy becomes zero, i.e. when the initial potential energy has been completely lost by friction.

2.2.3 Results in Flow-R

Flow-R can be used now to draw maps of relative frequencies of rockfall using: (1) the spreading probability based on a multiple flow algorithm including an inertial factor, and (2) the maximum runout distance based on a Coulomb friction model. Finally, Flow-R provides for each cell of the DEM the integration of relative frequencies, function of (1) the initial rock-mass-failure susceptibilities F_n of onset cells and (2) of all computed rockfall propagations P_f which can be superimposed (Fig. 5).

2.3 Rockfall quantitative hazard mapping along roads

The hazard H is the mean frequency of occurrence at a punctual location x of a defined phenomenon of magnitude equal or greater than E per year, i.e. the multiplication of a rock-mass-failure mean frequency and a probability (P_f) of

Table 1. Parameters used to assess rockfall hazard and risks along roads. Bold typo: input parameters needed to solve equations; normal typo: intermediary or final results solved during the assessment; italic typo: useless parameters because deleted during the equations' simplifications.

Acronym	Complete appellation
α	Exponent in the Holmgren's (1994) expression
d	Diameter of blocks considered
l	Mean length of the car
m_c	Mean values of cliffs distributions
m_{ss}	Mean values of steep slopes distributions
μ	Friction angle of the runout energy calculation
N_b	Number of rockfall events inventoried along road section
s and β	Slope angle values
σ	Standard deviations of cliffs distributions
T	Traffic per time period t_c
t_i	Time period of the inventory
v	Mean velocity
w	Weighting factor of normal distribution function
x_{rs}	Road section's cells locations
f, f_1, f_2 and f_t	Normal distribution function
F	Cumulative distribution function
F_n	Normalized F: rock-mass-failure susceptibility
H	Hazard
k	Calibration factor of hazard
R	Risk
E	<i>Magnitude of the rockfall event (function of d)</i>
Exp	<i>Exposure</i>
g	<i>Terrestrial acceleration</i>
i and j	<i>Flow directions in the Holmgren's (1994) expression</i>
L	<i>Mean length of the road within a pixel</i>
N_c	<i>Total number of vehicles during t_c</i>
P_{cell}	<i>Probability of a car to be hit inside a pixel</i>
P_f	<i>Relative frequency of propagation (in the Flow-R's results)</i>
t_c	<i>Considered period of time in the Risk equation</i>
x	<i>Punctual location</i>
x_p	<i>Pixel location</i>
Δx	<i>Increment of horizontal displacements in the friction model</i>

propagation (Leroi, 1996; Fell et al., 2005, 2008; Jaboyedoff et al., 2005; Volkwein et al., 2011).

However, the rock-mass-release susceptibilities F_n extracted from the improved SAD approach are relative to the slope angles and are not absolute numbers. Moreover, the frequencies of propagations P_f are assessed by Flow-R based on a unit mass and no different magnitudes of events (i.e. blocks volumes) can be considered. As a consequence, Flow-R results (namely F_n multiplied by P_f) have to be calibrated to adjust the hazard by a factor k which is a calibration term that links these results with observed events per year for a given magnitude:

$$H(E, x_p) = k(E) \times F_n \times P_f(x_p) \quad (7)$$

In Eq. (7), the rockfall hazard H (number of event per year) for a magnitude E is defined for a period of reference t_i at

a cell x_p and is equal to the product of rock-mass failure susceptibilities F_n times frequencies of propagation P_f up to a cell x_p and times a calibrating factor k , that depends on E .

This coefficient k depends on a known number of rockfall events with a given magnitude E in a cell x_p . However, in a context of rockfall studies along corridors, exact positions of impacts are unknown. For practical issues, inventories are frequently made along road sections. On a DEM, a road section is composed of a group of cells x_{rs} . So the inventoried number of events N_b along the section is the sum of all the rockfalls that occurred within the cells of this section during the time period t_i of the inventory. Thus, N_b has to be distributed in all the cells assessed following:

$$k(E) = N_b(E, t_r, x_{rs}) \times \frac{1}{\sum [F_n \times P_f(x_{rs})]} \times \frac{1}{t_i} \quad (8)$$

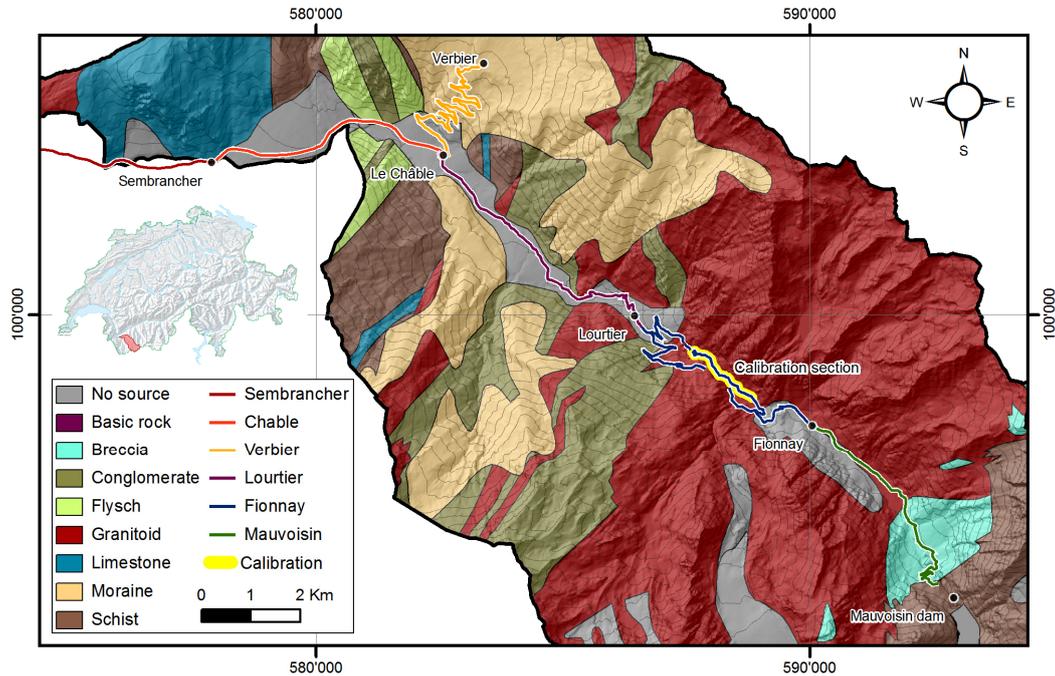


Fig. 6. Studied road sections and homogenous morphometric areas of the Bagnes Valley, located in the Swiss Alps, classified according to the swiss national geological atlas and the Vector25 (©swisstopo). They were identified differentiating daily traffic and mean velocities along the roads. The road section used to calibrate the rockfall hazard assessment is located between the second gallery after Lourtier and Le Plamproz (section underlined in yellow), where the rockfall activity is high, as shown in Fig. 1. (Hillshade and 10 m isohypses: ©2008 swisstopo).

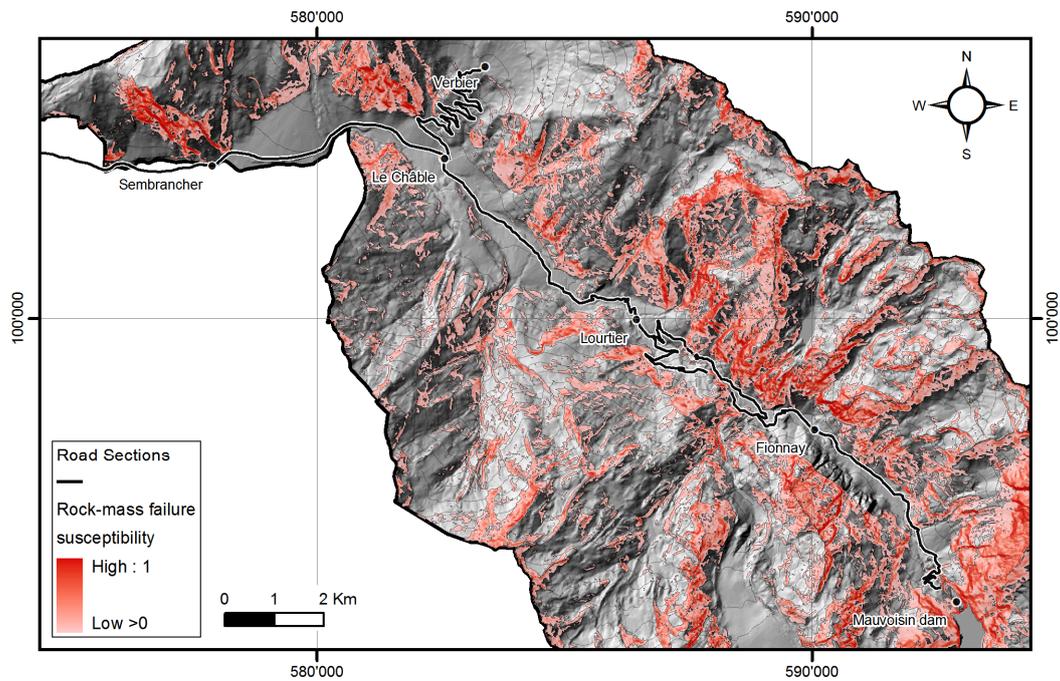


Fig. 7. Rock-mass failure susceptibility in the Bagnes Valley, identified thanks to the improved Slope Angle Distribution approach. (Hillshade and 10 m isohypses: © 2008 swisstopo).

where k is calibration factor with a frequency unit, function of a number of rockfall events N_b of magnitude E during a period of time t_i inventoried along a road section of cell x_{rs} divided by the sum of the Flow-R results within the whole road section.

2.4 Rockfall quantitative risk assessment along roads

Blocks frequently hit cars along Swiss mountain roads and occupants of vehicles are not necessarily killed or injured. Therefore, this paper is focused on the risk R of rockfalls to vehicle traffic; no considerations about vulnerabilities and elements at risk are provided, even if it would give proportional results. Adapting the risk equation of Fell et al. (2005) to this specific case, the annual risk can be defined by:

$$R(E, x_p) = H(E, x_p) \times \text{Exp}(x_p) \times N_c(x_p) \quad (9)$$

where R is the risk expressed in terms of number of direct impacts of blocks on cars per year, according to the hazard H and the exposure Exp , i.e. the probability that cars is hit in the hazardous area, and N_c the number of threatened vehicles. Modified after Fell et al. (2005), the exposure is presented as:

$$\text{Exp}(x_p) = \frac{L}{v(x_p)} \times \frac{1}{t_c} \times P_{\text{cell}}(x_p) \quad (10)$$

Exp depending on the mean length of the road inside cells L and the mean velocity v for a considered time period t_c (one year in this case) and the conditional probability P_{cell} :

$$P_{\text{cell}}(x_p) = \frac{d+l}{L} \quad (11)$$

where P_{cell} is the probability that a car of length l is hit by a block of diameter d on average inside a cell of length L , knowing that a block falls into a cell where a car is present. Indeed, in this study hazard and exposure are defined on a cell's scale x_p , not on a punctual location x . It is assumed that d is the minimum size block that will significantly affect the car and the magnitude E is equivalent to the block size. The diameter of blocks d has to tally with the inventoried events N_b considered to calibrate the hazard in Eq. (8). Then, the total number of vehicles attended on a road section is equal to Eq. (12):

$$N_c(x_p) = T(x_p) \times t_c \quad (12)$$

where T correspond to the daily traffic. Finally, the annual risk induced by rockfalls to vehicle traffic for an event with defined magnitude at a pixel x_p can be rewritten as follows:

$$R(E, x_p) = H(E, x_p) \times \frac{d+l}{v(x_p)} \times T(x_p) \quad (13)$$

R being a number of direct impacts of blocks of diameter d on cars of length l per year for a defined magnitude E at a cell x_p , function of the hazard H , the daily road traffic T ,

the mean velocity v , the mean car length l and the minimum block diameter d . Finally, the total risk along corridors is defined as the integration of all calculated $R(E, x_p)$ within the considered road sections.

3 Case study: the Val de Bagnes

3.1 Settings

The Val de Bagnes is located in the Canton of Valais in Switzerland. With a surface area of 300 km² and an elevation ranging from 677 m to 4313 m a.s.l., this municipality is under rapid development, in particular because of the fast growth of the Verbier ski resort. Moreover, an important power dam is located in the upper part of the valley. It means that the daily traffic is rather heavy, up to 5800 cars and 32 buses per day according to open-access databases (SRCE, 2009; CarPostal, 2010). Rockfall susceptibility maps at 1:25 000 were already performed (Michoud et al., 2010; Jaboyedoff et al., 2012). In this paper, a QRA of rockfalls to vehicle traffic is performed along the main roads (40 km) of the valley.

To achieve this goal, the authors used a 10 m cell size DEM derived from national maps at 1:25 000 (CN25, © swisstopo) to extract slope angles, the geological and tectonic vector atlas at 1:500 000 (© swisstopo) to classify the valley by HMA and the vectorized landscape model of Switzerland (Vector25, © swisstopo) to extract the location of the 40 km of roads.

3.2 Rockfall hazard assessments

3.2.1 Detection of block release areas

The rock type present is very large, from Cambrian polycyclic basements to Mesozoic and Cenozoic sedimentary covers (Sartori et al., 2006) of the Helvetic, Penninic and Austro-Alpine domains (Trümpy, 1980). Furthermore, large areas are covered by quaternary deposits that are fluvio-glacial deposits, colluvial fans or moraines. As the material diversity is wide, it justifies the importance of the HMA separation before further steps. Thus, each HMA was determined according to similar lithologies extracted from the 1:500 000 vectorised geological Atlas of Switzerland. Height classes were identified (Fig. 6): basic rocks, conglomerates, flyschs, granitoids, limestones, moraines, marble plus breccias and schists. In addition, some areas, such as lakes or alluvial deposits, were directly mapped as areas without any rockfall sources, due to absence of relief and/or material.

Then SAD analysis was performed from the 10 m DEM (©2008 swisstopo) and the useful slope angles (m_{ss} , m_c and σ for each HMA) were extracted to identify and weight potential rockfall source areas within the height HMAs. Results are presented in Table 2. This procedure was done thanks to the freeware Histofit (Loye et al., 2009) which decomposes

Table 2. Slope angles extracted from SAD analysis of each HMA. According to Fig. 2a and 3a, mean values and standard deviations of cliffs distributions correspond respectively to letters m_c and σ , and mean values of the steep slopes to letters m_{ss} .

Homogenous Morphometrical Areas	m_{ss}	1st normal distribution		2nd normal distribution (when necessary)	
		m_c	σ	m_c	σ
Basic rocks	33°	53°	8.3°	–	–
Conglomerates	31°	46°	8.7°	–	–
Flyschs	35°	48°	7.5°	60°	7.7°
Granitoids	34°	51°	7.7°	–	–
Limestones	35°	45°	8°	60°	8.0°
Marble and Breccias	33°	50°	6.4°	62°	7.4°
Moraines	33°	44°	6.1°	–	–
Schists	30°	47°	8.3°	61°	8.9°

the SAFD extracted from the software ArcGIS of Esri[©] and fits it with a predefined number of normal distributions. With the normal curves defined in Histofit and a slope angles map of the region, a MATLAB script allows to calculate directly rock-mass-failure susceptibilities F_n (Eq. 4) in each potential rockfall source cell of the map. Finally, the potential onset areas within each HMA were merged in one map (Fig. 7) before computing one propagation assessment.

3.2.2 Runout assessment

Taking into account local observations (Jaboyedoff et al., 2012) and detailed studies including computations of 2-D and 3-D rockfall modeling made for specific local cliffs into the valley, parameters of the runout assessment by Flow-R were calibrated as following: $\alpha = 1$ (Eq. 5) and $\mu = \tan 33^\circ$ (Eq. 6). Then, only one computation was done for the whole valley using the 10 m DEM (Fig. 8) to ensure continuous and homogenous results. Finally, these results were compared with a test simulation performed by the freeware CONEFALL (Jaboyedoff and Labiouse, 2011) based on an energy line angle equal to $\tan 33^\circ$ too. Both lateral and longitudinal extensions of computed runout areas are quite similar inside the Bagnes valley, which guarantee the coherence of the Flow-R runout assessment.

3.2.3 Rockfall hazard assessments

In order to achieve the normalized quantitative hazard assessment along the road sections, it is necessary to calibrate the Flow-R results with the factor k (Eq. 8 in Sect. 2.3). The road section used to calibrate the model is located on the NW side of the Dranse river, between the second gallery after Lourtier and Le Plamproz (Fig. 6), where the strong activity of cliffs has been well known for many years (Fig. 1). Along this section, covered by 237 cells with a sum of Flow-R results equal to 9453, it was assumed that 3 blocks with diameters d equal or greater than 25 cm reach the road every year ($t_i = 1$)

Table 3. Parameters for risk calculation along the different studied road sections (according to CarPostal, 2010, SRCE, 2009 and local road regulations). These road sections are mapped in Fig. 6.

Road Sections	T [daily traffic]	v [km h ⁻¹]	d [m]	l [m]
Sembrancher	10 600 cars	80	0.25	4
Chable	5800 cars	80	0.25	4
Verbier	5000 cars – 32 bus	60	0.25	4
Lourtier	2200 cars – 22 bus	70	0.25	4
Fionnay	800 cars – 8 bus	50	0.25	4
Mauvoisin	600 cars – 6 bus	40	0.25	4

according to our knowledge of past events. Then according to Eq. (8):

$$k(d \geq 25 \text{ cm}) = 3 \times \frac{1}{9453} [\text{events per year}] \quad (14)$$

An extract of the hazard map is presented in Fig. 9.

3.3 Rockfall risk assessment along the main roads of the valley

3.3.1 Inputs

The main important roads of the Val de Bagnes were extracted from the Vector25 (© swisstopo). The daily traffic along the valley roads considered T were obtained from open-access databases (SRCE, 2010 and CarPostal, 2010). Mean vehicles velocities v were estimated according to the local regulation and the state of the roads (roadwidth and ageing). Thus, six distinct road sections were distinguished and presented in Fig. 6 and Table 3, differentiating daily traffic and velocities along them. Moreover, the mean car length was set at 4 m, which corresponds to normal European compact car length. All parameters used in Eq. (13) are summarized in Table 3.

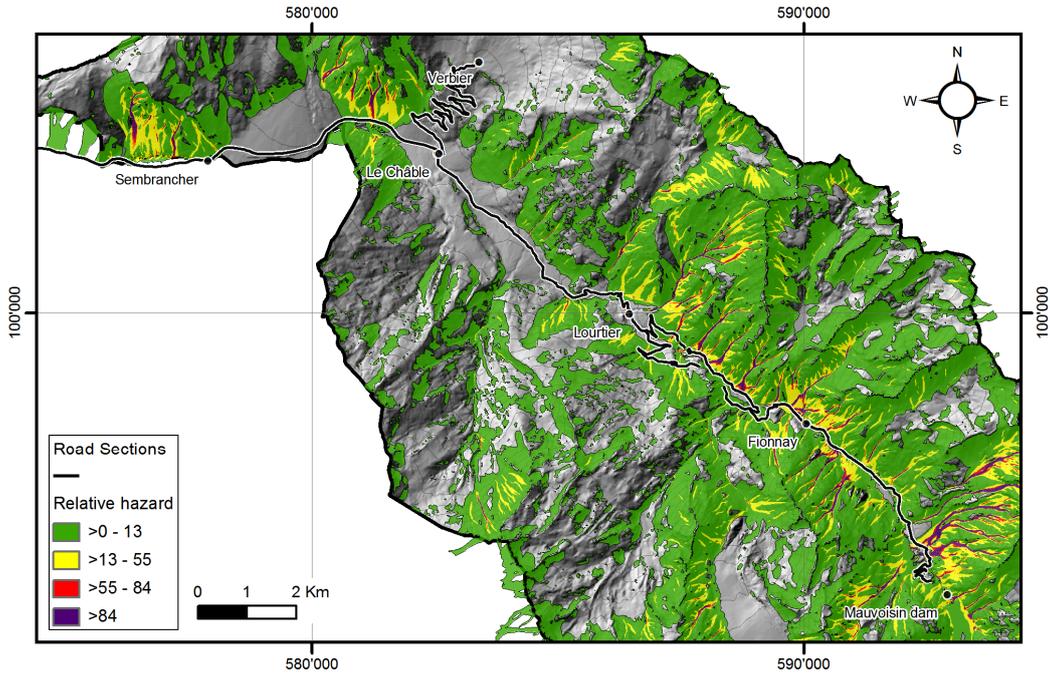


Fig. 8. Rockfalls relative hazard assessment in a part of the Bagnes Valley, performed by the software Flow-R. In the lower part of the valley (Sembrancher, Chable, Verbier), the daily traffic is rather heavy but the exposition is low. On the contrary, in the upper part of the valley (Fionnay and Mauvoisin), the daily traffic is lower but the hazard is pretty much higher. (Hillshade and 10 m isohypsés: ©2008 swisstopo).

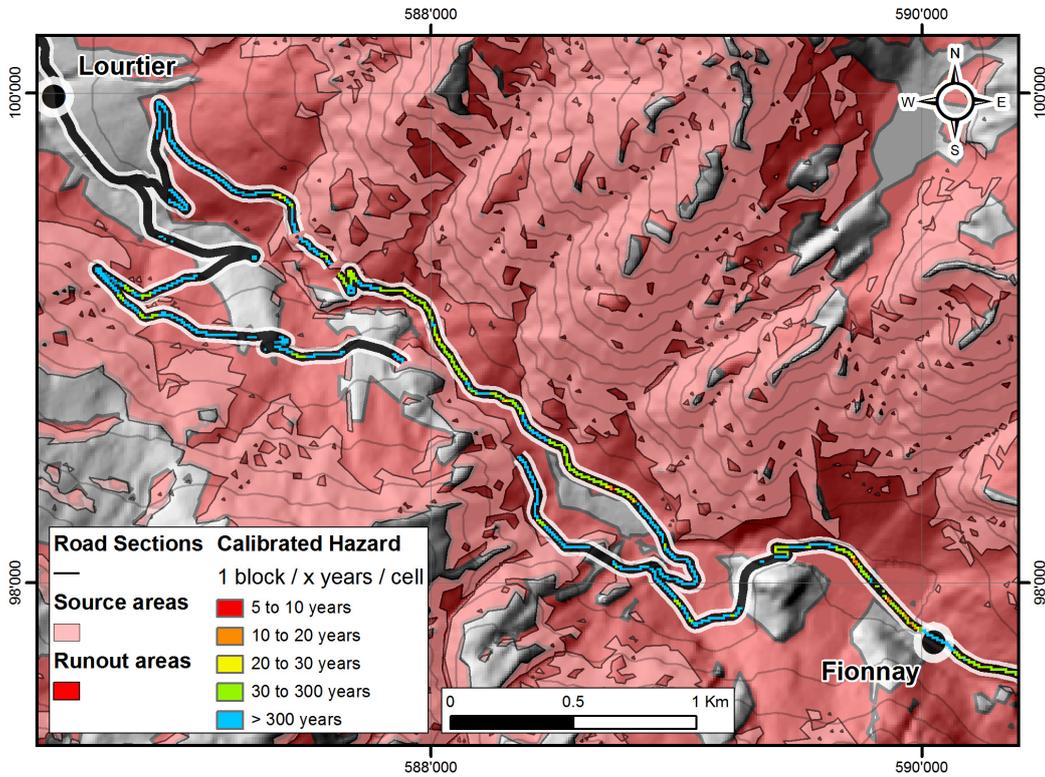


Fig. 9. Inverse hazard once the calibration has been performed, focused along the road section of Fionnay. Gaps along the section correspond to tunnels. (Hillshade and 10 m isohypsés: ©2008 swisstopo).

Table 4. Results of the quantitative risk assessment induced by rockfalls (mean diameter: 25 cm) to vehicle traffic along road sections of the Val de Bagnes. Finally, the whole risk is defined as the sum of all calculated pixel.

Road Sections	Total number of cells	Number of reached cells	Risk [x cars every year]	Inverse risk [1 car every x years]
Sembrancher	559	197(35%)	2.955×10^{-3}	~ 340
Chable	664	178 (27%)	4.626×10^{-3}	~ 220
Verbier	1031	98 (10%)	1.668×10^{-4}	~ 6000
Lourtier	851	63 (7%)	8.369×10^{-4}	~ 1200
Fionnay	1288	976 (76%)	1.676×10^{-2}	~ 60
Mauvoisin	742	591 (80%)	8.787×10^{-3}	~ 110
All roads	5135	2103 (41%)	3.414×10^{-2}	~ 30

3.3.2 Results

Finally, the annual risk induced by fragmental rockfalls greater or equal to a diameter of 25 cm to vehicle traffic was assessed along each road section of the Val de Bagnes. Results are summarized in Table 4. Along these sections, they vary a lot. In the lower part of the valley (Sembrancher, Chable and Verbier sections), where the daily traffic is important, there are only a few rockfall propagations that reach the road. This is why the risk is evaluated at one hit car every two hundreds to six thousands years. On the opposite, in the upper part of the valley (Lourtier, Fionnay and Barrage sections), the daily traffic is lower but there are a lot of blocks that reach the road; the risk is significantly higher, namely to one hit car every sixty years (Table 4). The integrated risk along all the road sections of the Val de Bagnes is evaluated to 0.03414 hit cars per year, i.e. approximately one incident every thirty years.

4 Discussions

4.1 Results within the study area

According to the authors' experience and testimonies from local security services and geologists, the results (i.e. the localization of potential rockfall onset areas, the runout computation and the risk assessment) are in agreement with observations. Nevertheless, the hazard calibration (Eq. 14) could be significantly improved with more complete inventories along these roads (detailed discussion in Sect. 4.5). In addition, the calculated risk is approximated and simplified, because it does not take into account some factors. First, the time lapse for the driver to react and the braking distance in front of blocks already on the road are ignored, considering that the velocity is low enough to avoid a collision along the most exposed sections. Moreover, all surveys and remediation measures already done (such as anchors, nets, removal of unstable blocks, monitoring systems, etc.) are ignored, except for tunnels and galleries which are mapped from orthophotos. Finally, the potential inhomogeneous repartitions of rockfall events and traffic during the day are ignored; for

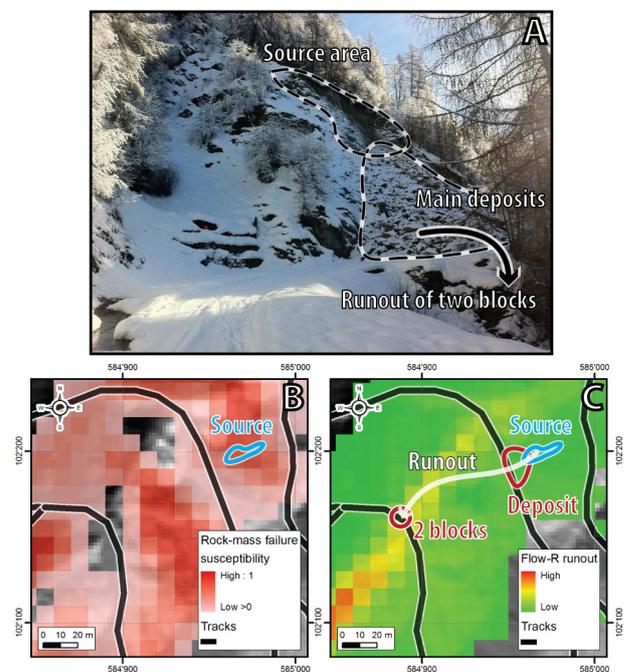


Fig. 10. (A) A recent rockfall event (2 January 2012) cut a mountain road with a deposit of approx. 1000 m^3 . The height difference between the fresh scarp and the road is about 30 m. (B) The rock-mass failure susceptibility map indicates that the onset is clearly defined as a potential rockfall source area with a high rock-mass failure susceptibility of about 0.8. (C) The trajectory of two blocks that reached a second road 80 m lower fit well with the predicted runout and confirms Flow-R results. (Hillshade: ©2008 swisstopo).

example, during winter periods, workers drive early in the morning and late in the afternoon, when the cliffs are frozen.

4.2 Recent rockfall event

A recent rockfall occurred on 2 January 2012, during the review process of this paper. The deposit of approx. 1000 m^3

cut a small road (Fig. 10a) and mostly stopped on it. The source area was localized in a zone clearly defined as a potential rockfall source area with a high rock-mass failure susceptibility of about 0.8 (scale: no susceptibility = 0 – highest susceptibility = 1; see Fig. 10b). The trajectories of two blocks that reached a second road 80 m lower fit well with the predicted runout using Flow-R (Fig. 10c). Thus, this event is in agreement with the improved SAD approach and the Flow-R results, showing its potential ability to predict hazard and risk zones.

4.3 Advantages and limitations of the presented approach

The combination of the improved SAD approach and the Flow-R software allows us to establish rockfall susceptibility, and when inventories are available, to obtain scaled hazard to assess risk along roads. This methodology has been optimized for studies at regional scale with only a little information available. Indeed, this procedure requires at least topography DEM and, if possible, a geological map in order to improve the rock-mass failures susceptibilities and spreading probabilities.

The refinement of the SAD approach is based on the assumption that the release susceptibility is related to the geomorphology, i.e. steepness of the topography, even if it is a simple rockfall activity factor. But, using geological information aims to indirectly take into account rock mass quality that influences the stability conditions, too. Nevertheless, it is also true that other very important local factors (such as weathering and/or deburstressing) cannot be taken into consideration for large areas, using documents available at regional scale. Then, regarding propagations, Flow-R assesses runout areas using only a DEM, since the parameters of the Holmgren's and the Coulomb's expressions (Eqs. 5 and 6) can be based on literature and/or past event records. This software is particularly optimized for regional studies and computation times are still acceptable with a normal workstation (five days for the study in Bagnes). Moreover, the approach can be even better calibrated according to other potential documents available for the study area (such as landuse maps, aerial images or information about mechanical rock parameters) in order to improve detection and runout settings. However, this procedure oversimplifies the laws governing rock-mass failures and block propagations, which are suitable at regional scale but become hazy for small studies' areas. Finally, this approach should be used as a preliminary quantitative assessment for large regions, highlighting hotspots requiring more detailed studies.

At local scales, robust empirical and physically-based methods have been developed for many years, allowing fine and realistic rock-mass failure detections & block propagations. For instance, the RSS-GIS method (Günther et al., 2004) allows us to deal with internal parameters and external factors of rockfalls. But, it requires a lot of data on topog-

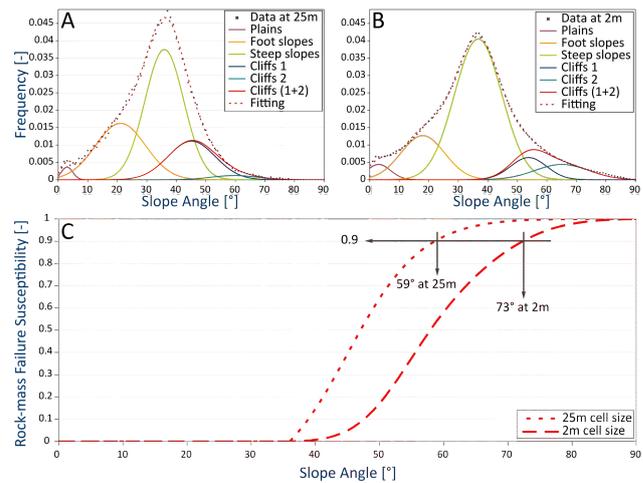


Fig. 11. (A) Normal distributions of the slope angles of the limestones HMA in the Bagnes Valley extracted from a 25 m resolution DEM. (B) Normal distributions of the slope angles of the same limestones HMA in the Bagnes Valley extracted now from a 2 m resolution DEM. (C) Cumulative distribution functions are shown for the same limestone HMA, once with a 25 m resolution DEM and once with a 2 m resolution.

raphy, structural geology, geotechnical settings and climatic conditions. The RHRS method (Pierson et al., 1990) is based on eleven parameters that have to be checked on the field. These two approaches are therefore indicated for studies at local scales to reliably and accurately detect and rate potential rockfall source areas; however, they would be too time-consuming for regional works if prioritized locations have not been defined before in-situ investigations. Then, regarding rockfall propagations, software like HY-STONE (Crosta et al., 2004; Frattini et al., 2008; Agliardi et al., 2009) is able to deal with both local and regional scales; moreover, it assesses probabilistic runout areas based on physical processes and computations of trajectographies. Furthermore, such software is able to consider countermeasures; fence design and location efficiencies can be estimated before their setup (Agliardi et al., 2009) to optimize them. However, it requires many inputs (such as rolling frictional angles, normal and tangential restitution coefficients) that have to be estimated and spatially distributed for all surface types of the study area, depending on landuses as well as superficial and bedrock geologies. Therefore, for studies at regional scale, it involves more time to acquire differentiated input parameters and compute runout than the Flow-R model.

4.4 Influences of the cell size DEM

The DEM resolution influences rockfall source detections: a coarse DEM tends to smooth high slope angle values. As stated in Loye et al. (2009), it implies that the higher resolution of the DEM, the smaller the potential source areas detected are. Furthermore, the coarser the DEM, the lower

the apparent slope angle of a vertical cliff is. For example, a 10 m vertical cliff has an apparent slope angle of 83° on a 2 m DEM instead of 55° on a 10 m DEM (Loye et al., 2009). As threshold angles which are used to identify block release susceptibilities (namely m_{ss} , m_c and σ) are extracted from slope maps, their values directly depend on the DEM cell size. Thus, for the same detected cliff, the coarser the DEM, the lower these threshold angles of cliff detection are (Fig. 11a, b). It means that the influence of the DEM cell size is implicitly taken into account during the SAD approach and no corrections have to be added. Fig. 11c illustrates a limestone cliff with an apparent slope angle of 59° on a 25 m DEM and 73° on a 2 m DEM having the same susceptibility of 0.9, regardless of the DEM cell size used during the SAD approach.

4.5 Hazard calibration

When it comes to converting rockfall susceptibilities into hazard (i.e. number of blocks per year per cell), the location of the calibration section associated to an inventory has a strong importance. Ideally, the section should be located along a non-forested slope without remediation systems. Therefore, if the calibration section is located along forested slopes, the final hazard would be underestimated along a non-forested adjacent slope because of a biased number of events due to blocks deviated or stopped by trees or anthropogenic countermeasures.

However, due to practical issues, the calibration step has to be achieved with inventories that are available (when they are), even if they are not always performed along optimum road sections. Nevertheless, a preliminary method to calibrate hazard is proposed and is still in progress; enhanced approaches will have to be developed in future work. Up to now, at least one section is needed to perform this calibration, but multiple road sections could also be used. Moreover, introducing two adjustment factors to take into account during the calibration step (i.e. Eq. 8) – (1) classical censoring effects inside inventories (Hungry et al., 1999) and (2) rockfall-forest interactions along forested slopes based on statistical studies (Dorren et al., 2005) – would be the first example of future evolution that could improve the reliability of the hazard calibration.

5 Conclusions

The improved approach of the Slope Angle Distribution and the Flow-R software were introduced and carried out along roads of the Val de Bagnes to assess the risk induced by fragmental rockfall to vehicle traffic. Linking the normal distributions of cliffs units with normalized cumulative functions, rockfall onset areas can be identified with rock-mass-failure susceptibility. Indeed, these indexes can be achieved at regional scale according to slope angle values inside homo-

geneous morphometric areas thanks to the enhanced SAD procedure. Then Flow-R software provides the relative frequencies of block propagations, using several approaches and susceptibilities of source areas. Thanks to these results, i.e. rock-mass-failure susceptibilities and relative frequencies of propagations, hazard maps can be achieved and calibrated with an inventoried number of events along a road section.

Even if the obtained quantitative risk assessment is an approximation, this improved approach allows us to deal at low cost with real hazard maps at a regional scale, requiring only few documents, namely a DEM and a geological map (if available). So this approach is indicated for regions which cannot afford systematic detailed assessments of the risk due to rockfalls; thus hotspots can be identified in order to prioritize sections on which detailed investigation and mitigation measures will be the most efficient.

Histofit and Flow-R software packages are available on request at www.flow-r.org.

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