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Simulating dam-breach flood scenarios of the Tangjiashan landslide dam induced by the Wenchuan Earthquake

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Abstract. Floods from failures of landslide dams can pose a hazard to people and property downstream, which have to be rapidly assessed and mitigated in order to reduce the potential risk. The Tangjiashan landslide dam induced by the $M_{\rm w} = 7.9$ 2008 Wenchuan earthquake had impounded the largest lake in the earthquake affected area with an estimated volume of $3 \times 10^8 \text{ m}^3$, and the potential catastrophic dam breach posed a serious threat to more than 2.5 million people in downstream towns and Mianyang city, located 85 km downstream. Chinese authorities had to evacuate parts of the city until the Tangjiashan landslide dam was artificially breached by a spillway, and the lake was drained. We propose an integrated approach to simulate the dam-breach floods for a number of possible scenarios, to evaluate the severity of the threat to Mianyang city. Firstly, the physicallybased BREACH model was applied to predict the flood hydrographs at the dam location, which were calibrated with observational data of the flood resulting from the artificial breaching. The output hydrographs from this model were inputted into the 1-D-2-D SOBEK hydrodynamic model to simulate the spatial variations in flood parameters. The simulated flood hydrograph, peak discharge and peak arrival time at the downstream towns fit the observations. Thus this approach is capable of providing reliable predictions for the decision makers to determine the mitigation plans. The sensitivity analysis of the BREACH model input parameters reveals that the average grain size, the unit weight and porosity of the dam materials are the most sensitive parameters. The variability of the dam material properties causes a large uncertainty in the estimation of the peak flood discharge and peak arrival time, but has little influence on the flood inundation area and flood depth downstream. The effect of cascading breaches of smaller dams downstream of the Tangjiashan dam was insignificant, due to their rather small volumes, which were only 2% of the volume of the Tangjiashan lake. The construction of the spillway was proven to have played a crucial role in reducing the dam-breach flood, because all the other natural breach scenarios would have caused the flooding of the downstream towns and parts of Mianyang city. However, in retrospect improvements on the spillway design and the evacuation planning would have been possible. The dam-break flood risk will be better controlled by reducing the spillway channel gradient and the porosity of the coating of the channel bottom. The experience and lessons we learned from the Tangjiashan case will contribute to improving the hazard mitigation and risk management planning of similar events in future.

1 Introduction

Natural damming of rivers by mass movements are very common and potentially dangerous phenomena (Costa and Schuster, 1988; Evans et al., 2011), which have been documented all over the world, e.g. in Japan (Swanson et al., 1986), Canada (Clague and Evans, 1994), China (Chai et al., 1995), the northern Apennines in Italy (Casagli and Ermini, 1999) and New Zealand (Korup, 2005). Hazards and risks resulting from landslide dams have been reported in many historic accounts of catastrophic floods from natural dam failures. The 27 largest floods of the Quaternary period with discharges greater than $100\,000\,\mathrm{m}^3\,\mathrm{s}^{-1}$

were listed by O'Connor and Costa (2004), most of which were caused by breaches of glacier or landslide dams. The largest flood in recorded history was caused by the failure of the earthquake-induced Raikhot landslide dam in 1841 on the Indus River in Pakistan, which has an estimated peak discharge of ~ 540 000 m³ s⁻¹ (Mason, 1929; Shroder Jr., 1998). Schneider (2009) described the largest landslide triggered by the Kashmir earthquake ($M_w = 7.6$, 2005) in Pakistan, which formed a natural dam impounding two lakes in the Karli river. Some other representative cases were studied by Alexander (1988), Hewitt (1998), Cruden and Miller (2002), Dunning et al. (2006), Gupta and Sah (2008) and Duman (2009). On overview of research work on landslide dams was made by Korup (2002) and Evans et al. (2011).

Many records of large landslide dams and catastrophic outburst floods are known in China. On 1 June 1786, a M = 7.8 earthquake in the Kangding-Luding area triggered a large (> 10^6 m^3) landslide dam that blocked the Dadu River. Ten days later, the dam breached resulting in catastrophic downstream flooding and 100 000 fatalities (Dai et al., 2005). Another examples is the sudden breach of three dams (Dahaizi. Xiaohaizi, and Deixi) induced by the Diexi earthquake causing a tragic flood that affected settlements along a downstream distance of 250 km, killing more than 2500 people (Chai et al., 2000). Of all the recorded cases, the largest dam was formed by the Yigong landslide ($\sim 3 \times 10^8 \text{ m}^3$) on 9 April 2000 in Tibet, which breached two months later and caused a flash flood with a peak discharge of \sim $120\,000\,\mathrm{m^3\,s^{-1}}$, resulting in 30 fatalities and over 100 people missing (Shang et al., 2003; Xu et al., 2012).

The Tangjiashan landslide dam induced by the devastating 2008 Wenchuan earthquake ($M_w = 7.9$) in China, highlighted the importance of the dam-breach flooding problem. This dam was the most dangerous one out of the > 800 coseismic landslide dams mapped by Fan et al. (2012a, b), which had impounded the largest barrier lake with an estimated volume of 3×10^8 m³, threatening more than 2.5 million people downstream. Chinese authorities decided to evacuate parts of the city until the Tangjiashan landslide dam was artificially breached by a spillway, and the lake was drained (Liu et al., 2009).

For emergency mitigation planning related to potential dam-break floods, the key issues are (1) assessing the dam stability; (2) evaluating the potential dam breach process and mechanism; and (3) predicting the dam-break flood parameters, including the probable peak discharge, depth, velocity, duration and the affected area.

The stability assessment of landslide dams has been an important research theme for a long time. Recently, a geomorphic approach is widely used to correlate the dam and the impounded lake geomorphic features with the landslide dam's stability (Ermini and Casagli, 2003; Dong et al., 2009). Using this approach Cui et al. (2010) concluded that the Tangjiashan dam was unstable. The limitation of this method is that it ignores the dam structure and geotechnical properties of the dam materials (Dunning et al., 2005).

Concerning the dam breach process, Walder and O'Connor (1997) concluded that it was still poorly understood, since it involves a variety of processes, including sediment entrainment from the breach floor, the gravitational collapse of breach sides and the downstream dam face. In the Tangjiashan case, the availability of detailed field data and laboratory-tested geotechnical parameters allow us to use a physically-based model to simulate the dam breach process, predicting the dam-breach flood hydrograph, the failure time and the ultimate breach geometry.

Regarding the dam-break flood modelling, the peak discharge can be predicted by both empirical and numerical simulation methods. The empirical method relies on regression relations between the peak discharge and other parameters, such as the impounded lake volume, depth, and area (Evans, 1986; Costa and Schuster, 1988; see Peng and Zhang, 2012 for an overview). The numerical method includes both a physically based model, e.g. the US National Weather Service BREACH Model (Fread, 1991) and Chang and Zhang (2010) as well as a GIS-based hydraulic model (Li et al., 2011), which can also predict other flood characteristics (flood routing, depth, velocity, duration and the affected area). The empirical model is simple to apply, compared to the numerical model which requires detailed parameters, but it provides less accurate results.

The previous studies on the Tangjiashan landslide dam are mainly concentrated on describing the emergency mitigation works and on the estimation of the dam-break flood using empirical methods (Liu et al., 2009; Xu et al., 2009; Cui et al., 2010) as well as on the prediction of the outburst flood hydrograph using physical models (Wang et al., 2008; Dai et al., 2010). However, there is little work on 2-D hydraulic modelling of the dam-breach flood with consideration of different scenarios, neither on the calibration of the model and on the cascading breach of several smaller downstream dams. To fill these gaps, the physically-based BREACH model and the GIS-based hydraulic SOBEK 1-D-2-D model are integrated in this study to facilitate the dam-break flood modelling of the Tangjiashan dam. This study aims to model the dam-break floods of possible scenarios up to Mianyang city, based on our best understanding of the dam breach process.

2 Study area

2.1 Hydrologic and geological setting

The Tangjiashan landslide dam is located at 31.84° N, 104.43° E, ~ 5 km upstream of the town of Beichuan, which was completely devastated by the Wenchuan earthquake and the large co-seismic landslides, and has not been reconstructed. The landslide blocked the Tongkou river (also called Jianjiang) with an upstream catchment area of 3, 550 km²

(Fig. 1). The river is 100–130 m wide and 0.5–4 m deep, having an asymmetrical V-shaped cross-section with right and left valley-side slope gradient of $\sim 45^{\circ}$ and 25° , respectively. The Tongkou river is mainly supplied by rainfall, with a mean annual precipitation rate of 1287.5 mm. The recorded maximum daily precipitation is 323.4 mm. According to the record from the Beichuan hydraulic station, the average annual discharge of the Tongkou river is $81 \text{ m}^3 \text{ s}^{-1}$, and increases to $167 \text{ m}^3 \text{ s}^{-1}$ during the monsoon season which lasts from May to October. The discharge before the dam breached was recorded as $90 \text{ m}^3 \text{ s}^{-1}$ (Liu et al., 2009). Historical flood records indicate that most of floods occurred in June to September due to extreme rainstorms, with the highest frequency in July and August. In the past 100 yr, the largest floods happened in 1902 and 1934 with peak discharges of $6720 \text{ m}^3 \text{ s}^{-1}$ and $5750 \text{ m}^3 \text{ s}^{-1}$, respectively. Table 1 shows the peak discharges of floods with different return periods.

The Tangjiashan landslide dam was formed by a rock slide in fragmented bedrock composed of siltstone, siliceous rocks and mudstone of the Qingping Group, from the lower Cambrian (Figs. 2 and 3, modified based on Xu et al., 2009). The bedrock was covered by colluvium (mixed soil and fine rock fragments) with dense vegetation. The landslide is located on the hanging wall of the main fault (Yingxiu-Beichuan fault), only 2 km away from the surface fault rupture. Due to the strong seismic energy, the steep terrain and the fragile geological structure, the landslide slid down into the river along the steep sliding surface (60°) and even ran up to the opposite slope, forming a 550 m high scarp (Fig. 2). The dam volume was estimated to be 2.04×10^7 m³ with a height varying from 82 m to 124 m through preliminary field measures (Liu et al., 2009). The dam crest extended approximately 600 m across the valley and 800 m along the valley. It had impounded a lake with $2.47 \times 10^8 \text{ m}^3$ of water till 7 June 2008, and with an estimated maximum capacity of $3 \times 10^8 \text{ m}^3$ (Liu et al., 2009). We generated the post-earthquake DEM with 5-m spatial resolution from the field-measured 2-m interval contours covering the area from the dam site to the Beichuan town (Fig. 4). The dam volume was calculated to be $1.7 \times 10^7 \text{ m}^3$ by comparing the pre- and post- earthquake DEMs. There are also several smaller landslide dams located at the downstream of the Tangjiashan dam (Fig. 4).

The detailed geological survey and boreholes were carried out by Chengdu Hydroelectric Investigation and Design Institute (CHIDI) in China (2008), revealing that the Tangjiashan landslide dam body is complex in its geological structure with four different layers from the top to the bottom (Fig. 3): (1) a 5–15 m thick layer of loose soil (60%) and rock fragments (40%) with grain sizes < 5 cm, which are easily erodible; (2) a 10–30 m thick layer of stronglyweathered rock blocks (6–40 cm in diameter) and boulders (1–2 m); (3) a 50–67 m thick layer consisting of partly intact rock strata retaining the original structure, which is relatively more densely packed and has lower permeability than **Fig. 1.** Location of the Tangjiashan landslide dam and the layout of the field measurements. The measurement location in Beichuan is the same as the Beichuan hydraulic station.



the above two layers; and (4) a 6-15.7 m thick layer of silt, sand and fine gravels mostly from the alluvial deposits on the river bed.

2.2 Mitigation measures

The Tangjiashan landslide dam was formed in the monsoon season, thus the high inflow filled the lake rapidly and made the mitigation more urgent. To reduce this risk, the Chinese government carried out several mitigation measures,



Table 1. Peak Discharge of floods with different return periods calculated from measurements at the Beichuan Hydraulic Station.

Return period (years)	2	5	10	20	50	100	200
Peak discharge ($m^3 s^{-1}$)	1180	2190	3040	3920	5120	6040	6970



Fig. 3. (A) Geological profile (A-A' in Fig. 2) of the Tangjiashan landslide; (B) Longitudinal cross-section of the dam body along the valley showing four-layered structure, modified based on Chengdu Hydroelectric Investigation and Design Institute (CHIDI) in China (2008) and Xu et al. (2009).

including 24-h monitoring of the lake level and the dam stability situation, construction of a large emergency spillway and evacuation of the people in the possible flooded area. The spillway was designed as a trapezoid cross-section with a slope of 1:1.5 on both sides of the channel (Fig. 5a). It was 13 m wide, up to 9 m deep, 695 m long, and designed to be capable to accommodate $1,160 \text{ m}^3 \text{ s}^{-1}$. The longitudinal channel gradient of the spillway varies from 0.6% to 24% from the upper reaches to the lower reaches (Liu et al., 2009). The construction work started on 26 May and was completed on 1 June 2008, lowering the lowest point on the dam crest from 750 m to 740.7 m. On 7 June when the impounded water level rose to the lowest point on the dam crest, the spillway started to drain the lake. The peak discharge of 6, $500 \text{ m}^3 \text{ s}^{-1}$ appeared at 12:30 h (LT) on 10 June and declined quickly to $79 \text{ m}^3 \text{ s}^{-1}$ at 8:45 h (LT) on 11 June (Fig. 5b). During this period, $1.6 \times 10^8 \text{ m}^3$ water was released and the water level of the lake dropped $\sim 27 \text{ m}$ (Cui et al., 2010). Due to the strong incision and erosion of the two top layers of the dam body, the spillway rapidly enlarged to a width of 100-130 m and eventually a depth of 40–60 m, and about 5×10^6 m³ of material was eroded (Liu et al., 2009). Currently, the remaining part of the dam body is enhanced by concrete, still impounding about $8 \times 10^7 \text{ m}^3$ of water (Fig. 5c and d).

3 Data and methods

To simulate the dam-breach flood, we integrated the BREACH model (Fread, 1991) and the SOBEK 1-D–2-D model developed by Deltares (Dhondia and Stelling, 2002). The BREACH model can simulate the outflow hydrograph emanating from a dam and quantify the dam breach process. To calibrate the model, we reconstructed the 2008 event by setting up the spillway as a base scenario. The outputs of the BREACH model for different scenarios were subsequently used in the SOBEK model. The integrated simulation approach is depicted in the flowchart in Fig. 6.

Four scenarios were considered in this study:

Scenarios 1: assuming that the dam would breach naturally without the spillway under the same hydrological condition as the base (calibrated) scenario for the purpose of evaluating the effects of the spillway.

Scenarios 2: the same as *Scenario 1*, but also considering that the breach of the Tangjiashan dam would cause the cascading breach of the four smaller downstream dams as shown in Figs. 1 and 4.

Scenarios 3: assuming that the dam would breach naturally given a 5-yr return period flood discharge of $2190 \text{ m}^3 \text{ s}^{-1}$ (see Table 1) as inflow to lake, under a heavy rainstorm situation. The 5-yr return period was selected as it is likely to occur and can provide largely different outputs from other scenarios.

Scenarios 4: assuming the geotechnical parameters of dam material would be the most unfavourable (worst combination), leading to the whole breach of the dam and the completely releasing all the water in the barrier lake, which is the most catastrophic scenario compared to others.

3.1 The BREACH model and data requirements

The BREACH model is a physically based mathematical model capable of predicting the breach characteristics and the discharge hydrograph from the breach of a man-made dam or a naturally-formed landslide dam, developed by Fread (1991) at the US National Weather Service. This model is created by coupling the conservation of mass of



Fig. 4. Post-earthquake 5-m DEM of the Tangjiashan dam and three of the four downstream dams (the fourth one is at the further downstream).



Fig. 5. (**A**) Helicopter view of the artificial spillway; inset shows the spillway cross-section; (**B**) releasing impounded water through the spillway, taken on 10 June 2008 when the discharge reached its peak (provided by Liu, N. from Ministry of Water Resources of the People's Republic of China); (**C**) remaining dam; (**D**) Remaining lake, (**C**) and (**D**) were field photo taken in September 2011.

the reservoir inflow, spillway outflow, and breach outflow with the sediment transport capacity of the unsteady uniform flow along a breach channel formed by erosion. Cencetti et al. (2006) modified the bed-load transport formula (the Meyer-Peter and Muller formula, modified by Smart, 1984) used in the BREACH model to better suit the simulation of channel erosion on landslide dams. The model can deal with breach caused by overtopping and piping, and has been applied to landslide dam breach modelling (Dai et al., 2010; Li et al., 2011). Previous studies (Liu et al., 2009; Cui et al., 2010) have a good agreement that the most probable failure mode of the Tangjiashan dam will be overtopping rather than piping and complete collapse, due to the its geological structure.



Fig. 6. Flowchart of the integrated simulation approach.

The required input parameters of the BREACH model include the relationship between the water level and the coverage area of the barrier lake, the upstream inflow rate to the barrier lake and the spillway geometry, the dam geometry and material geotechnical properties (Table 2). To obtain a range of material properties of the Tangjiashan dam, 15 samples from dam surface and boreholes were collected and tested in laboratory using various methods (e.g. the quick direct shear test, density test, permeability test and triaxial compression test etc.) by Chengdu Hydroelectric Investigation and Design Institute (CHIDI) in China (2008). Within this range, the most critical combination of the values was determined by the calibrated model (base scenario), which was also used in Scenarios 1-3. For Scenario 4, we have selected the most unfavourable geotechnical properties from the range. A detailed explanation of the physical meaning of the parameters and the model theory can be found in Fread (1991) and Cencetti et al. (2006).

We used the pre-earthquake Digital Elevation Model with a spatial resolution of 25 m to calculate the lake volume and coverage area for a given lake water level using the Open-Source GIS software ILWIS, which has a specific volume

Table 2. Input parameters for the BREACH model. A range of the dam material geotechnical properties was measured using laborate	ory tests
shown in the brackets in the base scenario column.	

Parameters	Base scenario	Scenarios 1 and 2	Scenario 3	Scenario 4
	Lake parameters	8		
Inflow to lake $(m^3 s^{-1})$	90.0	90.0	2190.0	90.0
Lake water level, H (m)	740.7	750.0	750.0	750.0
Lake volume, $V (m^3)$	2.3×10^{8}	3.1×10^{8}	3.1×10^{8}	3.1×10^{8}
Average depth of lake, D (m)	30.6	33.7	33.7	33.7
Lake covered area, S_a (m ²)	7.4×10^6	9.0×10^6	$9.0 imes 10^6$	$9.0 imes 10^6$
Dam and spillway geometry				
Dam crest elevation, H_u (m)	750.0	750.0	750.0	750.0
Dam downstream face gradient, S	0.10	0.18	0.18	0.18
Initial breach bottom elevation, H_c (m)	740.7	-	_	_
Initial width of breach bottom, B_0 (m)	13.0	-	_	_
Spillway length, L (m)	695.0	_	-	-
Geotechnical properties of dam material				
Unit weight, ρ (kg m ⁻³)	2400 (1900–2500)	2400	2400	1900
Internal friction angle ϕ , (°)	30 (24–36)	30	30	24
Cohesion, C (kPa)	13 (10–15)	13	13	10
<i>D</i> ₅₀ (m)	1.1 (0.4–2.0)	1.1	1.1	0.4
Porosity, Por	0.32 (0.28-0.45)	0.32	0.32	0.45

Note: D_{50} is defined as the grain diameter at which 50% of dam sediments are finer; porosity, P_{or} is the ratio of voids to the total volume of a specimen.



Fig. 7. Variation of the barrier lake depth (the background is the shaded relief map of the pre-earthquake 25-m DEM).

calculation function (Fig. 7). The result is consistent with previous estimations (Liu et al., 2009; Cui et al., 2010), showing that the maximum capacity of the barrier lake is $3.1 \times 10^8 \text{ m}^3$ with the lake water level at 750 m, and about $1.5 \times 10^8 \text{ m}^3$ water was drained by the spillway as the lake water level was lowered from 740.7 m to 714.0 m. (Fig. 8).



Fig. 8. Relationship between the volume and the water level of the barrier lake.

3.2 The SOBEK 1-D-2-D model and data acquisition

The SOBEK 1-D–2-D model was used to calculate the spatial and temporal variation in flood parameters (e.g. the flood area, depth, velocity, arrival time etc.), which is a graphically orientated model. This model combines the one-dimensional river flow and two-dimensional overland flow, switching from 1-D simulation of the flow in the river in the normal condition to 2-D when water overflows the channel and



Fig. 9. Outflow hydrographs from the BREACH model and the observational data.

inundates areas along the river (see Dhondia and Stelling, 2002 for the background principles and the detailed hydrodynamic equations). It has been used for reconstructing a large-magnitude outburst flood from a glacial lake by Carrivick (2006).

To set up the model for the Tangjiashan dam-break flood simulation following data were collected:

- Field surveyed cross-sections and embankments of the Tongkou river channel: 35 cross-sections and 40 embankments were measured in the field by a handheld GPS and a laser distance meter (Fig. 1).
- The pre-earthquake Digital Elevation Model (DEM) with 25 m spatial resolution was generated from 1:50000 scale digital topographic maps by interpolating contour lines with intervals of 10 m and 20 m for low- and high-relief terrain, respectively (Fig. 1). The DEM was pre-processed before input into the model by filling the sinks and adding the embankments present at the time of the earthquake.
- The discharge and historical flood records of the Tongkou river were obtained from the Beichuan hydraulic stations and by reconstructing flood heights through field interviews (Table 1 and Fig. 1).
- The channel and floodplain roughness coefficients were estimated based on field observations and available land cover maps.

4 Results

4.1 The BREACH model calibration and parameter sensitivity analysis

The BREACH model was calibrated through reconstructing the 2008 event, by adjusting the geotechnical material

Table 3. The BREACH model calibration results. The peak duration represents the lasted time for the discharge being over $1000 \text{ m}^3 \text{ s}^{-1}$; the peak appearing time is referred to the time from the first flow released through the spillway till the peak arrived; and the total released volume includes not only the lake volume but also the inflow volume during the breach.

Output parameters	Simulation	Observation
Peak discharge ($m^3 s^{-1}$)	6678	6540
Total released-volume (m ³)	1.94×10^8	1.86×10^8
Peak duration (h)	12	9
Peak appearing time at the dam site (h)	77.9	77.5
Ultimate breach depth (m)	33.6	30.0
Ultimate breach width (m)	77.6	100
Ultimate breach bottom elevation (m)	706.4	710.0

properties of the dam within the range of measured values, until the results were in correspondence with the observed hydrograph, showing a peak of $\sim 6500 \text{ m}^3 \text{ s}^{-1}$ appearing around 77 h after the first flow out of the spillway on 7 June 2008 (Fig. 9 and Table 3). The breach channel predicted by the model was a bit deeper and narrower than the observations (Table 3).

A sensitivity analysis of dam material properties (Table 2) was carried out based on the *Scenario 1*. We found that the outflow hydrograph is more sensitive to the grain size, the unit weight and the porosity (Fig. 10a–c), while less sensitive to the internal friction angle and cohesion (see the supplementary material for the results). Larger grain size has little effect on the peak discharge, but postpones the peak arrival time obviously, as it controls the sediment transport rate (Fig. 10a). Lower values for the unit weight of the dam material lead to larger and faster outflow hydrograph peaks (Fig. 10b). The same effect is obtained by increasing the porosity (Fig. 10c).

4.2 The BREACH model output uncertainty and results

The uncertainties of the model outputs were analysed by using the extreme values from the range of the dam material properties of the dam, and using the *Scenario 1*. The peak discharge and time of the flood generated from the weakest combination were $\sim 10\,000 \text{ m}^3 \text{ s}^{-1}$ higher and near 27 h earlier than those from the strongest case (Fig. 10d). The resulting variations of the flood 2-D simulation will be discussed in Sect. 4.3.

The BREACH model results demonstrate that the most catastrophic scenario (*Scenario 4*) produces the highest flood peak discharge of ~ 75 500 m³ s⁻¹, but the shortest peak duration that lasted until the time the discharge reached > 1000 m³ s⁻¹ (Fig. 11). The peak arrival time of the flood is the shortest for *Scenario 3*, due to the higher inflow rate, the lake would be filled up faster and the dam breach process would be accelerated. Compared to *Scenario 1*, in the base (calibrated) scenario the peak discharge decreases



Fig. 10. Sensitivity analysis of the BREACH model outflow hydrograph to dam material properties (A: D_{50} grain size; B: dam material unit weight; and C: porosity) and uncertainty analysis of the BREACH model outputs (D).



Fig. 11. Output hydrographs of the BREACH model.

significantly and the peak arrival time is delayed by nearly 32 h, which proves that the spillway played a crucial role in reducing the dam-break outburst flood hazard. The difference of the *Scenarios 1 and 2* is due to the cascading breach of the downstream dams, which can only be analysed in the SOBEK model.

4.3 The SOBEK 1-D–2-D model results

The SOBEK 1-D–2-D modelling was done with a special focus on the following issues:

4.3.1 Cascading breach of four dams at the downstream of the Tangjiashan dam

The *Scenario* 2 (cascading breach of downstream dams) (Figs. 1 and 4) is based on the assumption that these dams would fail by overtopping, which is supported by the previous conclusion that the majority of the landslide dams worldwide were documented to fail by overtopping (Costa and Schuster, 1988). The overtopping time of the downstream dams can be estimated by their geometry, the terrain and the outflow hydrograph of the Tangjiashan dam. Table 4 shows that their overtopping time is all a bit earlier than the peak arrival time at the Tangjiashan dam (45.9 h, Fig. 11). They were estimated to be breaching during 44.2 to 45.3 h after the Tangjiashan dam was overtopped. Figure 12 demonstrates the cascading breach process of these dams.

4.3.2 Simulation of flood hydrodynamics at the downstream towns

We selected four measurement locations in the major towns and Mianyang city located downstream of the Tangjiashan



Fig. 12. Cascading breach of dam 1–4 (**A–D**) at the downstream part of the Tangjiashan dam.

dam to check the flood hydraulic parameters (Fig. 1). The result of the base scenario agrees well with the observational data (Table 5), which further verified that the BREACH model provided robust results and the SOBEK 1-D–2-D model results resemble reality. Figure 13 depicts the variation of the peak discharge and peak arrival time at these towns for different scenarios. In general, the peak discharge attenuates with an increase of the distance from the dam site. Flood control structures in Mianyang city were designed for a maximum discharge of $13\ 000\ m^3\ s^{-1}$, therefore all scenarios except the base scenario would cause flooding in the city (Fig. 13). Hence, the construction of the spillway did avoid serious flooding in Mianyang city. The *Scenario* 4 would generate a peak discharge which is almost five times larger

Table 4. Estimated failure time (by overtopping) of the downstream dams. The dam height and lake volume were reported by Xu et al. (2009), and are consistent with the calculation results by comparing the pre- and post- earthquake DEMs.

Number	Dam height (m)	Lake volume (m ³)	Overtopping time (h)	Breach duration (h)
1	60	2.0×10^6	44.2	1.3
2	20	0.6×10^6	44.4	0.5
3	20	0.8×10^6	44.7	0.5
4	30	4.0×10^6	45.3	0.8

and an arrival time that is 1.3 h earlier than the base scenario. The comparison of the Scenarios 1 and 2 indicates that the cascading breach of the downstream dams did not significantly increase the peak discharge and delay of the peak arrival time. This is because these dams were estimated to impound rather small amounts of water (in total, $7.4 \times 10^6 \text{ m}^3$), which is only 2% of the volume of the Tangjiashan lake (Fig. 13). The Tongkou town located nearest to the Tangjiashan dam downstream would be most influenced.

Figure 14 presents the flooded area, which occurs mainly on the floodplain, as the surrounding areas are substantial higher in elevation. The flooded area of *Scenarios 1 and 2* are almost identical ($\sim 62 \text{ km}^2$) due to the limited effect of the cascading breaches of the downstream dams. *Scenarios 3* and 4 may cause flooded areas of 70.5 and 78.7 km², respectively, including most parts of Mianyang city. The spatial variation in flood parameters in different scenarios is presented in the Supplement.

4.3.3 Variations of the 2-D flood simulation related to the SOBEK model input

The variations of the 2-D flood simulation are highly related to the range of dam material properties. To assess these variations (uncertainties), we used as input in the SOBEK model the variations of BREACH model output hydrographs of both the weakest and strongest combinations of dam material properties shown in Fig. 10d. For Scenario 1 as an example, the resulting flooded area varies between 61 km² (using the strongest dam properties) to $66 \,\mathrm{km^2}$ (using the weakest ones). The maximum flood depth generated from the strongest combination is generally smaller than that from the weakest case (Fig. 15a and b). The difference between them at the downstream towns is less than 1 m. In Mianyang city, the estimated variation of the flood depth is 3.09-3.65 m. Figure 15c and d depict that the flood peak appearing time in the weakest case is about 27 h earlier than that in the strongest case, which is determined by the BREACH model output (Fig. 10d). The variability of the dam material properties causes a large uncertainty in the estimation of the peak arrival time, as it controls the dam breach speed and process. However, it has little influence on the flood inundation area 3040



Fig. 13. Flood peak discharge (A) and peak arrival (B) passing through the towns located downstream of the Tangjiashan dam.

Table 5. The SOBEK simulation results of base scenario compared with observational data. The peak arrival time is referred to as the time lag between the peak appearing time at the Tangjiashan dam site and the time when it reaches the downstream towns.

Towns	Distance from dam (km)	SOBEK simulation results			Observations		
	uum (kini)	Maximum depth (m)	Peak discharge (m ³ s ⁻¹)	Peak arrival time (h)	Peak discharge $(m^3 s^{-1})$	Peak arrival time (h)	
Beichuan	5.3	6.4	6665.3	0.18	6500	0.20	
Dengjia	12.3	11.7	6622.0	0.55	_	_	
Tongkou	27.3	18.3	6589.1	1.18	6300	1.25	
Qinglian	46.7	5.6	6481.0	2.25	_	_	
Mianyang	74.9	4.1	6281.4	4.48	6100	4.33	

and flood depth downstream, which are more determined by the lake volume. The time referred to here is from when the Tangjiashan dam was overtopped till the peak appeared at different locations. It can be converted to the relative time lag as shown in Table 5 and Fig. 13 by subtracting the peak appearing time at the Tangjiashan dam site (52.7 and 25.4 h for the strongest and weakest combinations, respectively; Fig. 10d). Thus, the time when it reaches Mianyang city after the peak appears at the dam site varies from 3.6 to 3.9 h.

5 Discussion

After the sudden formation of a landslide dam, it is important to assess the dam stability and possible failure mode rapidly, to predict the dam-break flood magnitude, and to estimate the dam failure time and flood arrival time.

5.1 Dam stability assessment

The Tangjiashan landslide dam was considered unstable and might fail by overtopping (Cui et al., 2010; Fan et al., 2012a). The BREACH model was able to reconstruct the Tangjiashan event well. However, it cannot account for the heterogeneity of the dam composition materials. The existence of a thick layer of partly intact rock strata in the middle and bottom part of the dam were the main factors that prevented the dam to breach or collapse totally, except in extreme situations (e.g. heavy rainstorm, strong aftershocks). A sensitivity analysis of these parameters can help to quantify the uncertainty and diminish the effect of this limitation. Further improvement of the model is needed especially for inhomogeneous landslide dams, but this is beyond the scope of this study.

5.2 Dam-break flood magnitude estimation

The physically based and numerical models can provide more accurate results compared to the empirical method, but rely on more detailed dam and lake geometry data and geotechnical parameters of the dam materials. The predictions of peak discharge of the Tangjiashan dam from empirical equations proposed by previous studies in Table 6 are compared with those from the Scenario 4 of the BREACH model, as both of them consider the whole breach of the dam. These equations are based on either the lake volume (V_L) or on the potential energy (P_E), which is the product of dam height, lake volume, and specific weight of water.



Fig. 14. Modelled flooded area for different scenarios. The yellow and red areas represent the increase in flooded area for Scenario 4 and 5, respectively.

Table 6. Comparison of predictions of the peak discharge of the Tangjiashan landslide dam from empirical equations and the BREACH model.

Empirical equations	Reference	Peak discharge $(m^3 s^{-1})$
$Q_{\rm p} = 0.72 V_{\rm L}^{0.53}$	Evans (1986)	2.28×10^4
$Q_{\rm p} = 1.6 V_{\rm L}^{0.46}$	Walder and O'Connor (1997)	1.29×10^4
$Q_{\rm p} = 3.4 V_{\rm L}^{0.46}$	Cenderelli (2000)	2.74×10^4
$Q_{\rm p} = 0.0158 P_E^{0.41}$	Costa and Schuster (1988)	1.28×10^4
$Q_{\rm p} = 0.063 P_{\rm E}^{0.42}$	Clague and Evans (2000)	7.08×10^4
BREACH model	Fread (1991)	7.55×10^4

Note: V_L equals to 3.1×10^8 m³ for the Tangjiashan dam; and P_E is 2.55×10^{14} joules, given the dam height of 84 m and the specific weight of water of 9800 N m⁻³.

The predicted peak discharge (Q_p) varies from 1.28×10^4 to 7.55×10^4 m³ s⁻¹, with an average of 3.7×10^4 m³ s⁻¹. The deviations of different empirical equations might result from site-specific characteristics of the original sample lakes in different study areas. The empirical equations underestimate the peak discharge compared to the results of the BREACH model. We consider the prediction from the BREACH model to be more reliable, as the model was calibrated by observational data (Fig. 9). In the Tangjiashan case, the equation proposed by Clague and Evans (2000) provides the closest prediction compared to the results of the BREACH model.



Fig. 15. Variation related to the inputs in the SOBEK model expressed as: the maximum flood depth generated from the strongest and weakest combinations of dam material properties (**A** and **B**), and the peak appearing time in the strongest and weakest cases (**C** and **D**) based on the Scenario 1.



Fig. 16. Time needed for the barrier lake rising to a certain level and the lake volume (V_L) .

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Locations (towns)	Distance from	SOBEK sim results <i>Scen</i>	ulation ario 1	Results from empirical equations	
		Peak discharge (m ³ s ⁻¹)	Peak arrival time (h)	Peak discharge (m ³ s ⁻¹)	Peak arrival time (h)
Beichuan	5.3	19752.3 ± 6512.7	0.15 ± 0.04	25028.3 ± 974.0	0.05 ± 0.02
Dengjia	12.3	19430.0 ± 6280.5	0.45 ± 0.02	22096.7 ± 1732.0	0.20 ± 0.06
Tongkou	27.3	19164.4 ± 6193.3	0.85 ± 0.05	17956.5 ± 2505.9	0.57 ± 0.16
Qinglian	46.7	17610.0 ± 5082.8	1.98 ± 0.04	14453.9 ± 2766.3	1.39 ± 0.40
Mianyang	74.9	16157.1 ± 4226.9	3.85 ± 0.03	11260.9 ± 2698.0	2.95 ± 0.85

Note: the values in the table are mean \pm standard deviation. The range of the SOBEK simulation results is generated from the strongest and weakest combinations of dam material properties.

5.3 Dam failure time and flood arrival time prediction

The estimation of the dam failure time and flood arrival time is normally a race against the clock in an emergency situation. The prediction of dam overtopping (failure starting) time and peak arrival time at the downstream towns is crucial to determine the appropriate mitigation measures and available time for the engineering works or evacuation planning. The relation between the barrier lake volume and water level in Fig. 8 can be employed to predict the dam overtopping time for a given inflow rate. Using this method, we calculated the time needed for the lake to reach a certain level, given the measured-inflow in May 2008 (90 $\text{m}^3 \text{s}^{-1}$) and the average discharge of the Tongkou river in the monsoon season $(167 \text{ m}^3 \text{ s}^{-1})$ in Fig. 16. The time is referred to the number of days after the dam was formed, e.g. "0" represents 12 May 2008. The spillway was constructed when the lake level was \sim 720 m and designed to be overtopped when the lake level reached \sim 740 m, so the maximum available time for construction was 15 days with a $90 \text{ m}^3 \text{ s}^{-1}$ inflow rate, and would be shortened to 8 days with the inflow increasing to $167 \text{ m}^3 \text{ s}^{-1}$. Our calculation was consistent with the reality that the spillway was overtopped on 7 June, 14 days after its construction on 26 May 2008.

The peak arrival time at the downstream towns was predicted by the SOBEK 1-D–2-D hydraulic model with the consideration of the terrain, channel and embankment features. Previous studies (Liu et al., 2009; Cui et al., 2010) have applied empirical equations to predict the flood peak discharge (Q_{PL} in Eq. 1) and the peak arrival time (*t* in the unit of second in Eq. 2) downstream from a landslide dam.

$$Q_{\rm PL} = \frac{W}{\frac{w}{Q_{\rm P}} + \frac{L}{VK}} \tag{1}$$

where *L* is the distance from the dam (m); *W* is the capacity of the lake (m³); Q_P is the peak discharge at the dam (m³ s⁻¹); and *VK* is an empirical coefficient, equaling to 3.13 for rivers on plains, 7.15 for mountain rivers, and 4.76 for

rivers flowing through the terrain with intermediate relief (Li, 1980).

$$t = k \frac{L^{1.4}}{W^{0.2} H_0^{0.5} h_{\rm m}^{0.25}} \tag{2}$$

where k is a coefficient, ranging from 0.8 to 1.2; H_0 is the lake water level before dam failure (m); and h_m is the water level (m) at a control section when the peak discharge reaches (Hydrological manual of Sichuan Province, 1979).

We compared our SOBEK simulation results of *Scenario 1* with the results of 50 % dam failure scenario from the empirical Eqs. (1) and (2) obtained by Cui et al. (2010) in Table 7, as in *Scenario 1* near half of dam material was estimated to be eroded. The empirical equations overestimated the peak discharge in the Beichuan and Dengjia towns, but underestimated it for the downstream towns and Mianyang city. The peak arrival time in the downstream towns was all overestimated, although they still can give a preliminary estimation, especially in the data scarcity and emergent situation.

5.4 Discuss the design of the spillway

The construction of the spillway played a significant role in preventing catastrophic flooding to the downstream towns and Mianyang city. However, in retrospect, there are lessons that can be learned for optimizing the design of the spillway and the excavation planning. For instance, the breach process was quite slow initially, with low discharge in the first three days after the breach (from 7 to 9 June), but suddenly accelerated on 10 June, reaching the peak of \sim $6500 \text{ m}^3 \text{ s}^{-1}$ just within 3 h (Fig. 9). This was faster than expected and increased the risk of catastrophic failure. Through the BREACH model parameter sensitivity analysis, we found that decreasing the channel gradient and material porosity of the coating of the channel bottom would have reduced the peak flood discharge and delayed the arrival time effectively. In addition, Cui et al. (2010) recommended that a compound cross-section combining a triangular configuration with that of a small trapezoid would have increased the low initial discharge.

6 Conclusions

The Tangjiashan landslide dam was the most dangerous one of the approximately 800 coseismic landslide dams induced by the Wenchuan earthquake, and impounded the largest lake whose catastrophic outburst flooding threatened ~ 2.5 million people downstream. This research provided insights in the dam-breach process and the resulting flood propagation in possible scenarios. The integration of the BREACH model and the SOBEK model can provide predictions that agreed well with the observations. The uncertainty analysis revealed that the variability of the dam material properties will not significantly affect the flood inundation area and the maximum flood depth in the downstream area. However, it will cause large variation in the flood peak discharge and peak arrival time. We found that the cascading breach of the downstream dams did not have a major influence on the modelled flood parameters, because they had lake volumes much smaller than that of the Tangjiashan Lake. Based on the experience and lessons we learned from the simulations of the Tangjiashan event, we recommend making the mitigation measures on the basis of predictions from physically and hydraulically based models whenever possible. In data scarce situation, and in emergency situations with limited time to take decisions, the empirical method can also provide relatively good first-hand estimations.

Supplementary material related to this article is available online at: http://www.nat-hazards-earth-syst-sci.net/12/3031/2012/

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